## Homework 1 Report

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## Linear regression model

1.

### • Iterations: 10

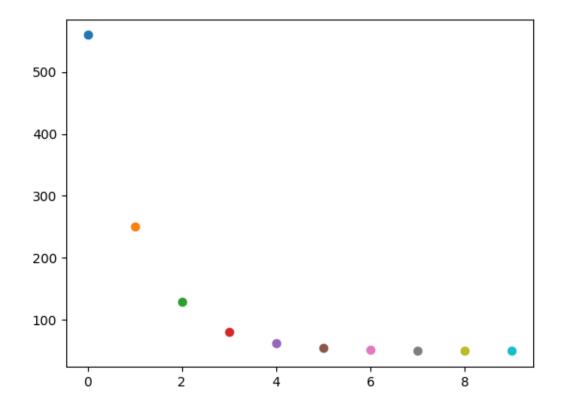
PS C:\Users\danzel\Hsu\課程\大三上\機器學習>

機器學習/HW1/linear\_regression.py

weights: 52.241568680275485

intercepts: -0.38341961689421783

Mean\_square\_error: 54.58001915343924



#### • Iteratons: 30

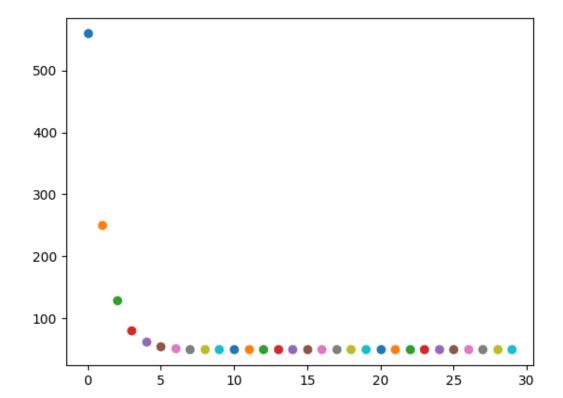
PS C:\Users\danzel\Hsu\課程\大三上\機器學習>

機器學習/HW1/linear\_regression.py

weights: 52.74349369253078

intercepts: -0.3337684770833136

Mean\_square\_error: 55.21902353217067



#### • Iterations: 100

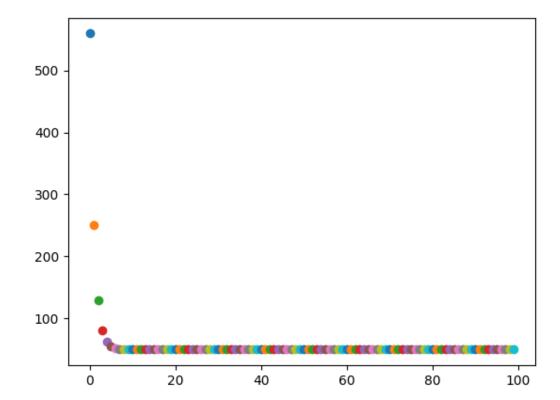
PS C:\Users\danzel\Hsu\課程\大三上\機器學習>

機器學習/HW1/linear\_regression.py

weights: 52.74354046182485

intercepts: -0.33375889502567535

Mean\_square\_error: 55.21909628062007



## **Logistic regression model**

1.

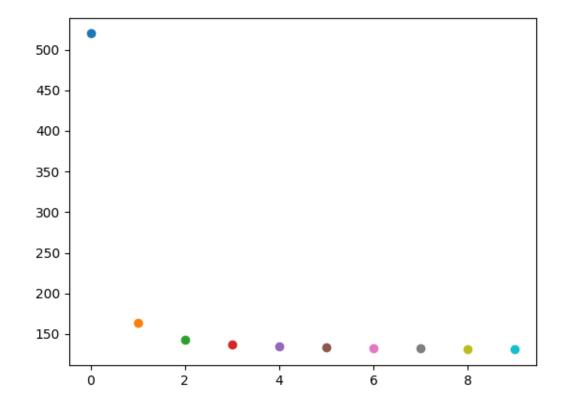
### • Iterations: 10

PS C:\Users\danzel\Hsu\課程\大三上\機器學習> 機器學習/HW1/classification.py

weights: 5.525894194737832

intercepts: 2.108792369594169

Cross Entropy Error: 49.81141865717864



#### • Iterations: 30

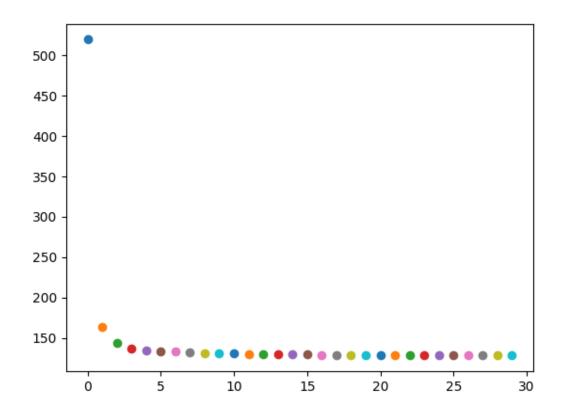
PS C:\Users\danzel\Hsu\課程\大三上\機器學習>

機器學習/HW1/classification.py

weights: 5.002169900946224

intercepts: 1.788060301989326

Cross Entropy Error: 47.69360685469468



#### • Iterations: 100

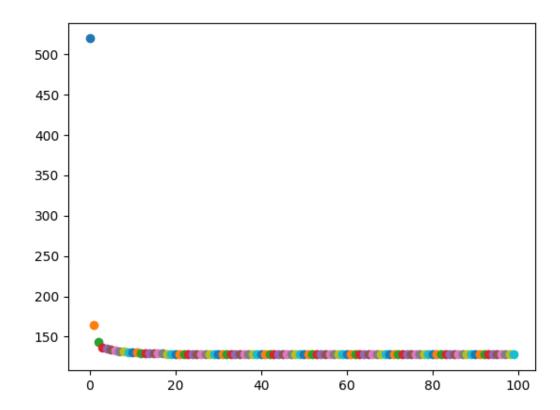
PS C:\Users\danzel\Hsu\課程\大三上\機器學習>

機器學習/HW1/classification.py

weights: 4.877128620284377

intercepts: 1.711767920212915

Cross Entropy Error: 47.248435018985404



## **Part. 2, Questions (40%):**

1. What's the difference between Gradient Descent, Mini-Batch Gradient Descent, and Stochastic Gradient Descent?

Ans: difference between Gradient Descent, Mini-Batch Gradient Descent, and Stochastic Gradient Descent is the amount of data been chosen. Stochastic Gradient Descent do training every piece of data and Mini-Batch Gradient Descentdo training every n pieces of data, while Gradient Descent do training for all data in once.

2. Will different values of learning rate affect the convergence of optimization? Please explain in detail.

Ans: Different values of learning rate do affect the convergence of optimization. Learning rate controls how we adjust weights with respect to loss error. The smaller the value, the slower we travel through the descent slope. It may be good if we slowly walk through the gradient but we might stuck if rate is too small. So it is difficult to choose the right learning rate at first.

3. Show that the logistic sigmoid function (eq. 1) satisfies the property  $\sigma(-a) = 1 - \sigma(a)$  and that its inverse is given by  $\sigma^{-1}(y) = \ln \{y/(1-y)\}$ .

$$\sigma(a) = \frac{1}{1 + \exp(-a)}$$

$$3. \quad 6(a) = \frac{1}{1 + e^{-a}}$$

$$6(-a) = \frac{1}{1 + e^{-a}}$$

$$1 - 6(a) = 1 - \frac{1}{1 + e^{-a}} = \frac{e^{-a}}{1 + e^{-a}}$$

$$1 - \frac{1}{e^{-a}} + \frac{e^{-a}}{e^{-a}} = \frac{1}{e^{a+1}} = 6(-a)$$

4. Show that the gradients of the cross-entropy error (eq. 2) are given by (eq. 3).

$$E(\mathbf{w}_1, \dots, \mathbf{w}_K) = -\ln p(\mathbf{T}|\mathbf{w}_1, \dots, \mathbf{w}_K) = -\sum_{n=1}^N \sum_{k=1}^K t_{nk} \ln y_{nk}$$

$$\nabla_{\mathbf{w}_j} E(\mathbf{w}_1, \dots, \mathbf{w}_K) = \sum_{n=1}^N (y_{nj} - t_{nj}) \phi_n$$
(eq. 2)

Hints:

$$a_{k} = \mathbf{w}_{k}^{T} \phi. \qquad (eq. 4)$$

$$\frac{\partial y_{k}}{\partial a_{j}} = y_{k} (I_{kj} - y_{j}) \qquad (eq. 5)$$

$$4. \quad E(u_{1}, ..., v_{k}) = -\ln_{p} (I[w_{1}, ..., w_{k}]) = -\sum_{n=1}^{N} \sum_{k=1}^{k} t_{n_{k}} \ln y_{n_{k}}$$

$$\nabla_{u_{j}} E(u_{1}, ..., w_{k}) = \sum_{n=1}^{N} (y_{n_{j}} - t_{n_{j}}) \phi_{n}$$

$$= \rangle \qquad \frac{\partial E}{\partial y_{n_{k}}} = -\frac{t_{n_{k}}}{y_{n_{k}}}$$

$$\leq \ln ce \qquad \text{We have} \qquad \hat{u}_{k} = w_{k}^{T} \phi$$

$$\Rightarrow \qquad \frac{\partial E}{\partial u_{n_{j}}} = \sum_{k=1}^{k} \frac{\partial E}{\partial y_{n_{k}}} \frac{\partial y_{n_{k}}}{\partial u_{n_{j}}}$$

$$= -\sum_{k=1}^{k} \frac{t_{n_{k}}}{y_{n_{k}}} \frac{\partial y_{n_{k}}}{\partial u_{n_{j}}} - t_{n_{j}} + \sum_{k=1}^{k} t_{n_{k}} y_{n_{j}} - t_{n_{j}} = y_{n_{j}$$