

--approx x : An infinite list of approximations which converge on the square

--root of a negative float 'x'

approx :: Float -> [Float]

approx x = 1.0 : [(prev + x / prev) / 2.0 | prev <- approx x]

--squareRoot x : An estimate of the square root of non negative float 'x'

squareRoot :: Float -> Float

squareRoot x = converge (approx x) 0.0001

--converge xs diff : The first item in infinite list 'xs' which differs to

-- the previous item by less than 'diff'

converge :: [Float] -> Float -> Float

converge (x:y:xs) diff

| (abs (x - y)) >= diff = converge (y:xs) diff

| otherwise = y

--iSquareRoot x : An integer estimate of the square root of integer 'x'

iSquareRoot :: Integer -> Integer

iSquareRoot x = floor (squareRoot (fromIntegral x))

--primes : The infinite list of prime numbers

primes :: [Integer]

primes = 2:[p | p <- [3,5..], null (primeFactors p)]

--primeFactors : The prime factors of an integer

primeFactors :: Integer -> [Integer]

primeFactors x = [f | f <- takeWhile (<= iSquareRoot x) primes, mod x f == 0]