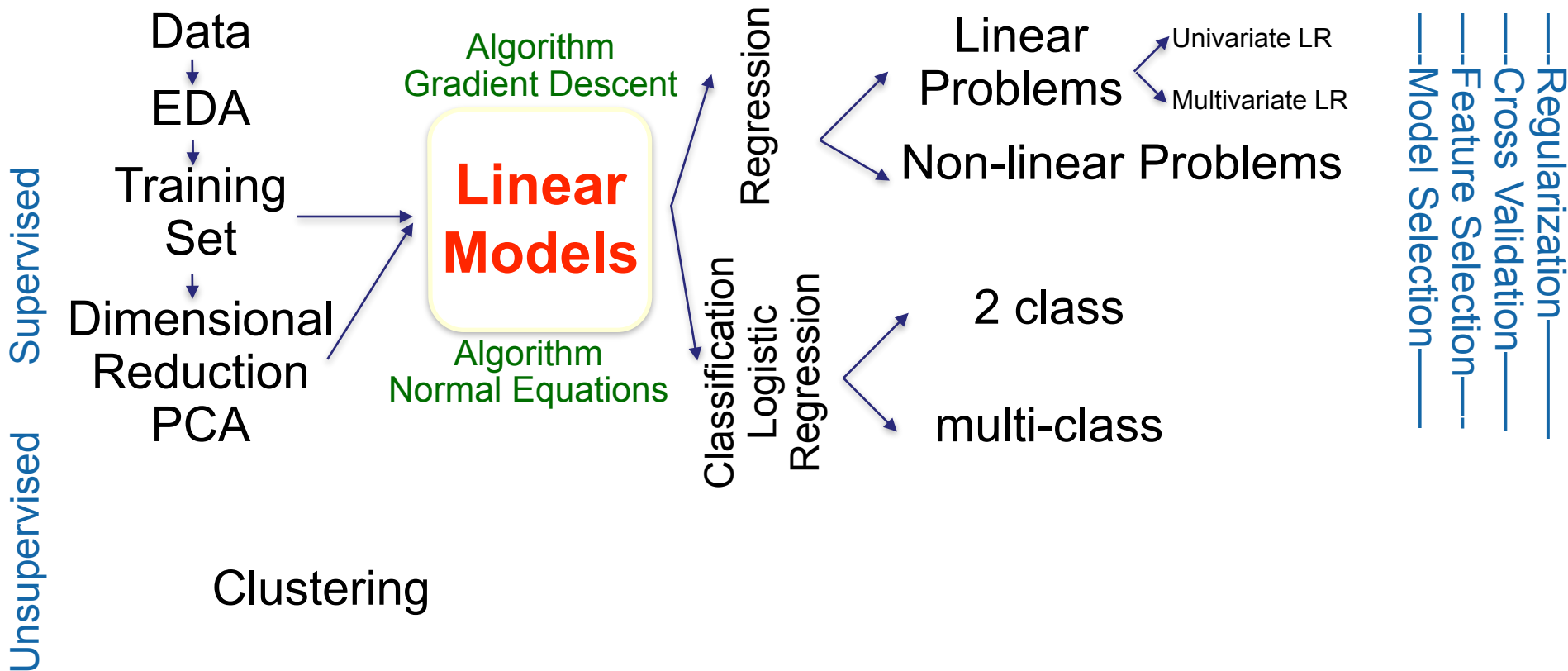


# INTRO TO DATA SCIENCE

## LECTURE 10: UNSUPERVISED LEARNING

## WHERE ARE WE ON THE DATA SCIENCE ROAD-MAP?



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## KEY CONCEPTS - UNSUPERVISED LEARNING

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- Unsupervised learning
  - No requirement for labelled data or known outcomes
  - No  $y$
- Is there some underlying structure in the data?
  - Do any sub-populations exist in the data?
  - If so, how many are there?
  - If so, how big are they?
  - What are their common properties?
  - Are there outliers?

**Clustering**, or **cluster analysis**, is the task of grouping observations such that members of the same group, or **cluster**, are more similar to each other by some metric than they are to the members of the other clusters



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## KEY CONCEPTS - CLUSTERING

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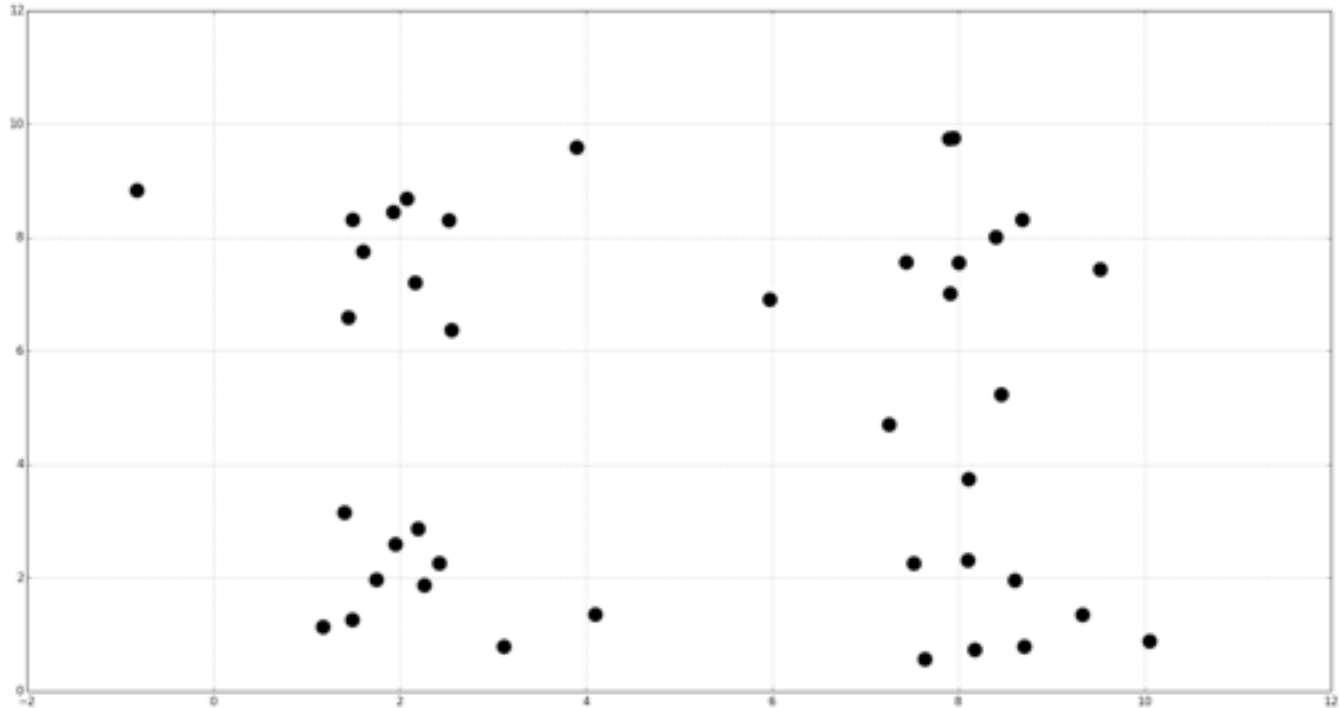
- What is a cluster?
- A cluster comprises a group of data points whose inter-point distances are 'small' compared with the distances to points outside the cluster
- We need an algorithmic solution to finding these clusters

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## KEY CONCEPTS - CLUSTERING

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How many clusters are there?

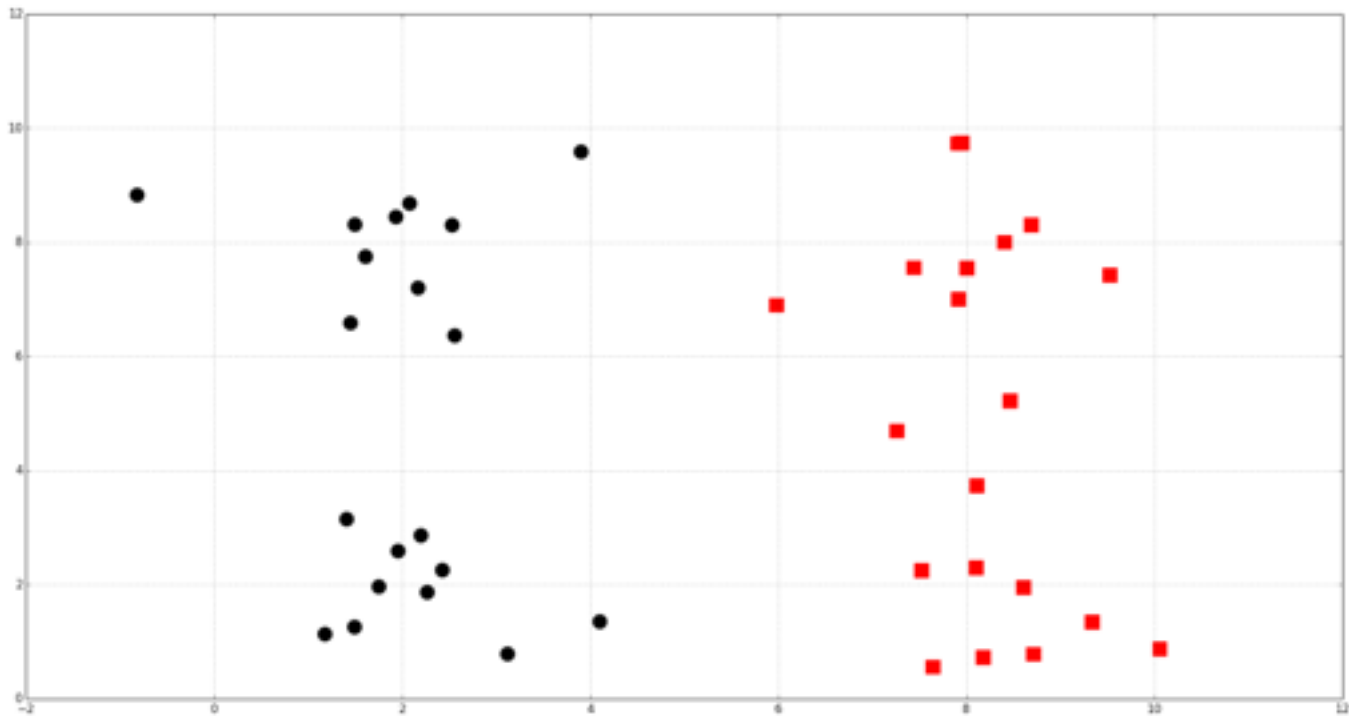


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## KEY CONCEPTS - CLUSTERING

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Three?

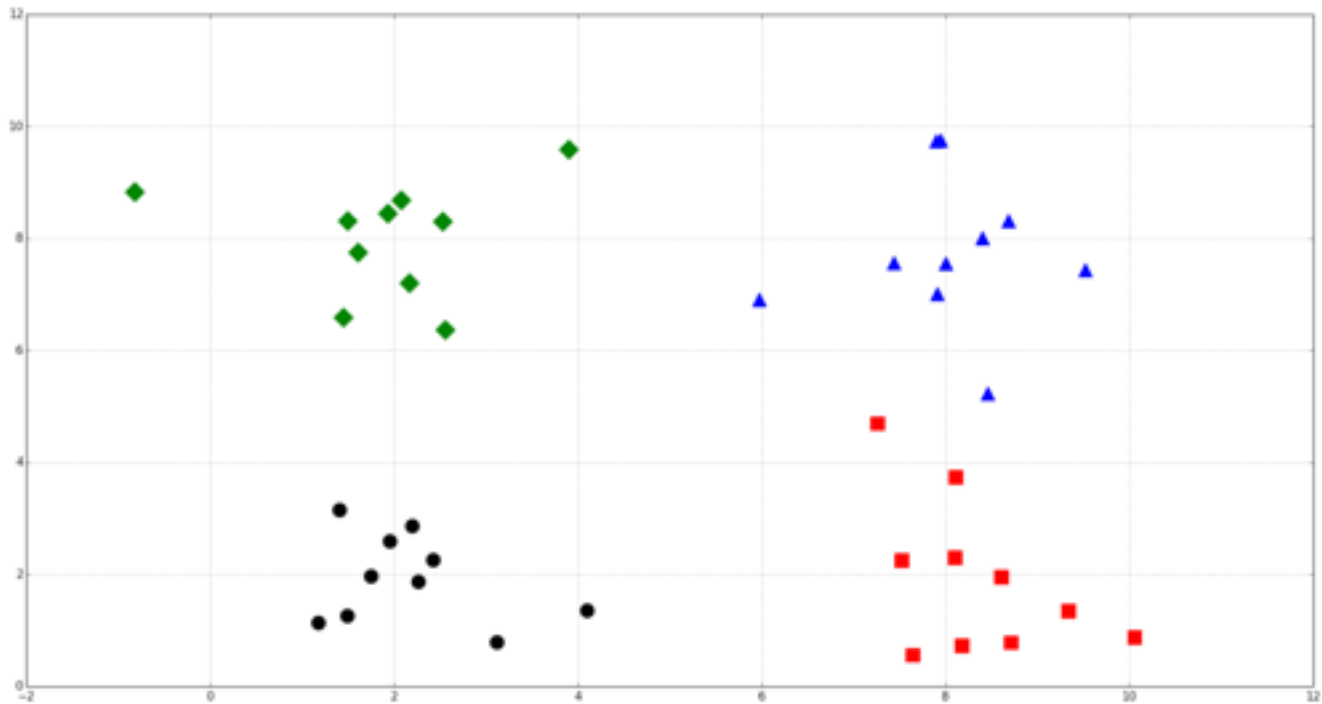


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## KEY CONCEPTS - CLUSTERING

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Four?





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## KEY CONCEPTS - CLUSTERING

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- Data exploration
- Identify communities, connections in social networks
- Customer segmentation
- Find groups of genes with similar expression patterns
- Recommendation systems
- Image compression

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## KEY CONCEPTS - K-MEANS CLUSTERING

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The aim of K-means is to partition your dataset, consisting of  $m$  observations, each of which has  $N$  dimensions, into  $k$  clusters.

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## KEY CONCEPTS - K-MEANS CLUSTERING

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- Possibly the most popular clustering algorithm
- It's simple, and quick – but needs to be used correctly
- It is an iterative algorithm
- If used inappropriately can give poor results
- K-means is affected by starting conditions, and therefore, as a result of 'unlucky' starting conditions it can get 'stuck' in local minima

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## KEY CONCEPTS - K-MEANS CLUSTERING ALGORITHM

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Step 1: Choose the number of clusters

- user provided input to the algorithm

Step 2: Initialize the cluster centroids

- the centroids are found locations within the dataset

Step 3: Assign the data points to their “closest” cluster centroid

Step 4: Using the data points associated with each cluster  
recalculate the cluster centroids

Step 5: Repeat Step 3, 4 & 5 until convergence

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## KEY CONCEPTS - K-MEANS ALGORITHM CHOOSING THE LOCATIONS FOR THE CENTROIDS

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- Initialization is best done by selecting some data points from your dataset, at random, and using the location of those points for the initial positions of the cluster centroid

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## KEY CONCEPTS - K-MEANS ALGORITHM ASSIGNING TO CENTROIDS

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- Having set the initial positions for the centroids, each data point is 'assigned' to a centroid based upon a 'distance' measure
- Euclidean Distance is the most commonly used measure of distance

$$\text{Euclidean\_Distance } (c, x) = \sqrt{\sum_{i=1}^N (c_i - x_i)^2}$$

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## KEY CONCEPTS - K-MEANS ALGORITHM SIMILARITY SCORES

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- Be aware of the Jaccard Similarity Score
- A popular metric in text mining problems or any problems with sparse binary data. E.g. vector may contain a 0 or 1 depending on the absence or presence of a word within a document

$$Jaccard(A, B) = \frac{|A \cap B|}{|A \cup B|}$$

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## KEY CONCEPTS - K-MEANS ALGORITHM RE-LOCATING THE CENTROIDS

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- Each centroid now has a portion of the data set assigned to it
- Using the cluster of points each centroid now finds the mean of the cluster.
- This implies finding the mean position in every dimension
- Once the mean is found the algorithm iterates by re-assigning the dataset to the newly located centroids



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## KEY CONCEPTS - K-MEANS ALGORITHM THE COST FUNCTION

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- K-means has a cost function, which is the optimization objective
- The K-means cost function is known as the K-means Distortion Function
- The K-means cost function is the sum of squared distances of each point to its assigned cluster

$$\sum_k^K \sum_{i=1, x_i \in C_i}^m e\_dist(C_k, x_i)^2$$

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## KEY CONCEPTS - K-MEANS ALGORITHM CONVERGENCE

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- After each iteration the cost function is evaluated
- The algorithm has converged when there is no further reduction in the cost function
- Convergence is assured!!, each iteration will lower the value of  $J$
- But there is no guaranteed global minimum

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## KEY CONCEPTS - K-MEANS ADVANTAGES

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- K-Means is relatively fast
- Can be scaled to large data sets when using mini-batches
- Excellent for general-purpose clustering

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## KEY CONCEPTS - K-MEANS ADVANTAGES

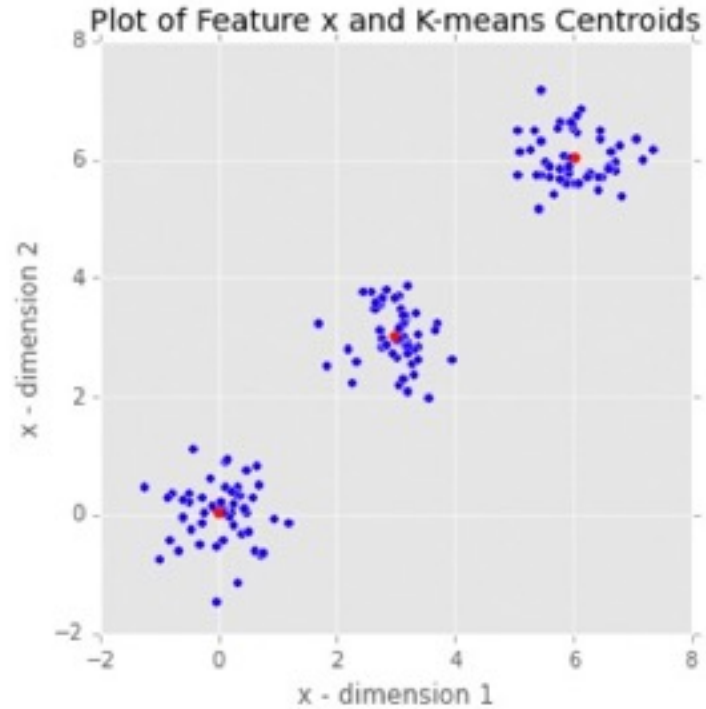
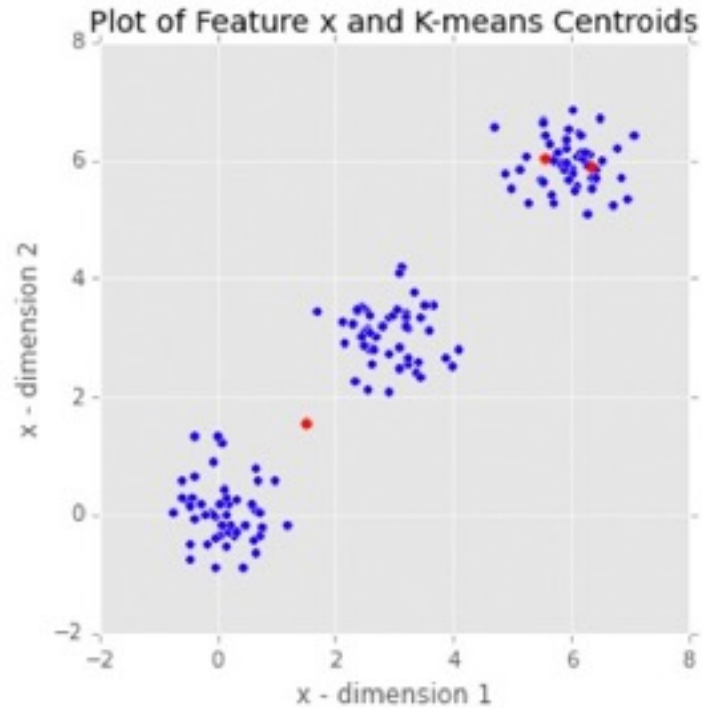
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- The use of euclidean distance makes the algorithm susceptible to outliers
- You have to find a good value for  $k$
- K-means is subject to the local minima problem.
  - An un-lucky initial randomization of centroids may yield a poor clustering result

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## KEY CONCEPTS - K-MEANS - LOCAL OPTIMA

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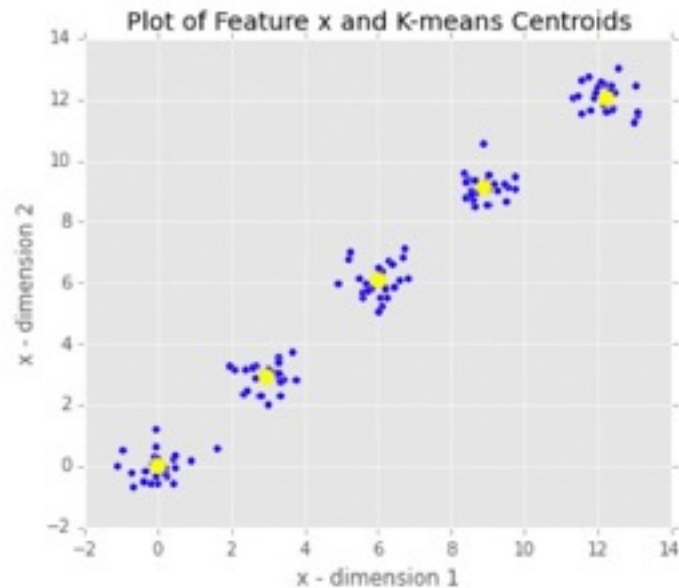
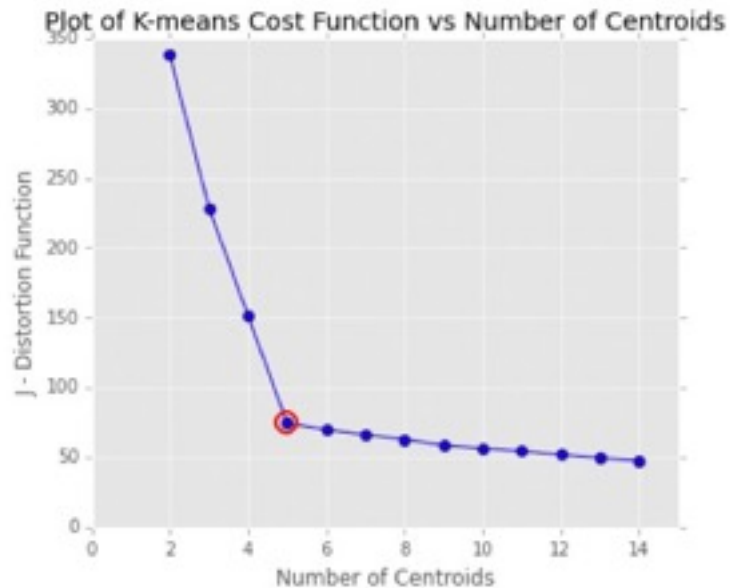
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## KEY CONCEPTS - K-MEANS ALGORITHM OPTIMIZING - FINDING A GOOD VALUE FOR K

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- The elbow (or knee-of-the-curve) method plots the value of the cost function produced by different values of  $k$
- As  $k$  increases, the average distances (and hence  $J$ ) will decrease; each cluster will have fewer constituent instances, and the instances will be closer to their respective centroids
- However, the improvement to  $J$  will decline as  $k$  increases. The value of  $k$  at which the improvement to  $J$  declines the most is called the elbow

## KEY CONCEPTS - K-MEANS ALGORITHM OPTIMIZING - FINDING A GOOD VALUE FOR K



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## KEY CONCEPTS - K-MEANS ALGORITHM OPTIMIZING - AVOIDING LOCAL MINIMA

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- Because K-means is a relatively fast algorithm you can usually run 50, 100, or even 200 runs, each with a different random initialization, so as to avoid poor solutions
- For each choice of K, you would run the algorithm 50, 100 or even 200 times with a different random starting configuration
- This, in general, 'solves' the local minima problem



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## OTHER CLUSTERING ALGORITHMS

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- Connectivity models - e.g. Hierarchical
- Distribution models - e.g. Gaussian Mixture Model
- Density models - e.g. DBSCAN
- Graph-based models - e.g. HCS clustering algorithm