Fibonacci Numbers: A Deep Dive

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Abstract

TODO check CI

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Listings

$$\mathcal{O}(1)$$
 = $\mathcal{O}(\text{yeah})$
 $\mathcal{O}(\log n)$ = $\mathcal{O}(\text{nice})$
 $\mathcal{O}(n)$ = $\mathcal{O}(k)$
 $\mathcal{O}(n^2)$ = $\mathcal{O}(\text{my})$
 $\mathcal{O}(2^n)$ = $\mathcal{O}(\text{no})$
 $\mathcal{O}(n!)$ = $\mathcal{O}(\text{mg})$
 $\mathcal{O}(n^n)$ = $\mathcal{O}(\text{sh*t!})$

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