

# Trees

- [branches]

- tree recursion

- ↳ multiple calls per large

- your best friends are:

- base cases

- ↳ is-leaf(t): →

- ↳ if label(t) == "berry":

- recursive calls

- ↳ for b in branches(t):

- ↳ [ \_\_\_\_\_ for b in branches(t)]

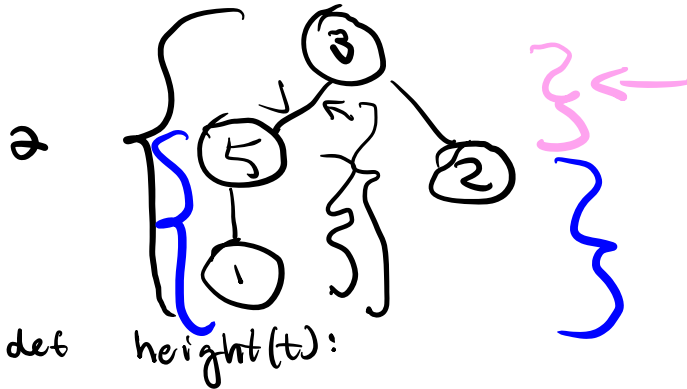
- ↳ max min sum  
any all

[ [ ] ]

for b in branches(t):

Height: (6)

$t = \text{tree}(3, [\text{tree}(5, [\text{tree}(1)])], \text{tree}(2))$



$\left\{ \begin{array}{l} \text{if is-leaf}(t): \\ \quad \text{return } 0 \\ \text{return } 1 + \max([\text{height}(b) \text{ for } b \text{ in branches}(t)]) \end{array} \right.$

[1, 2]    □

1 + 1

↖

return 1 + max([height(b) for b in branches(t)] + [-1])

↖

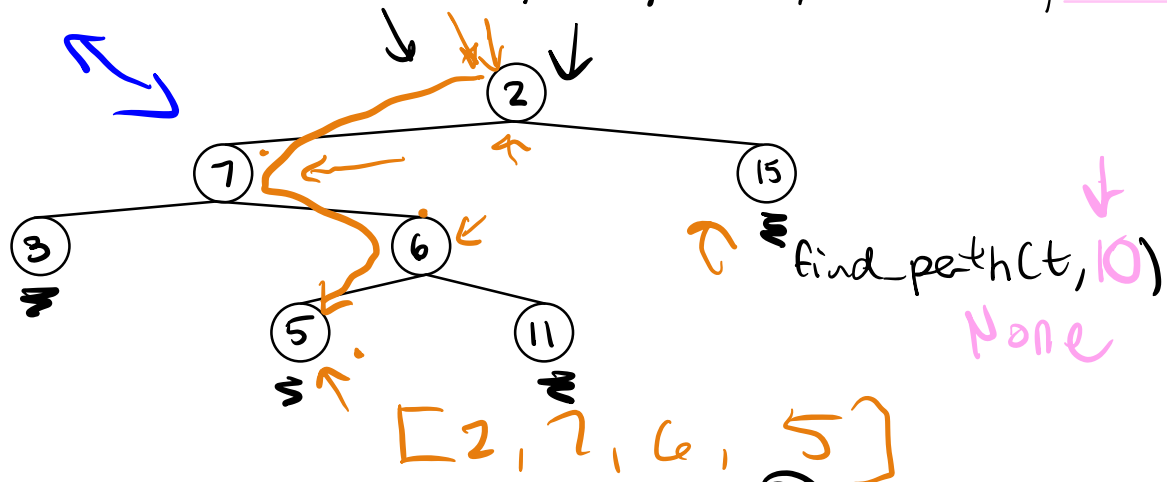
↗ ↗

max([-1]) → -1

$\begin{array}{ll} x & \text{if } a == b \\ \quad \uparrow & \text{else } y \end{array}$

$1 \neq (-1) \rightarrow \emptyset$

Find Path: (8)

$$t = \text{tree}(2, [\text{tree}(7, [\text{tree}(3), \text{tree}(6, [\text{tree}(5), \text{tree}(11)])]), \text{tree}(15)])$$


```
def find_path(tree, x):
```

if label(tree) = x:

```
return list(label(tree))
```

~~result: None~~

for  $b$  in branches(tree):

```
if find_path(b) != None:
```

```
return result + [label(tree)] + find_path(b)
```

~~return result~~

## Lists:

- Objects

- env dir: box & pointer!

$x = [1, 2, 3, 4] \leftarrow x \text{ points to}$

$y = [x, 5, 6] \leftarrow y \text{ points to}$

- indexing:  $x[i]$

- 0 indexed

↳ first item is @ index 0

↳ last item is @ index  $n-1$  (can say  $x[-1]$ )

↳ this is  $n$  items total

$n = \text{len}(x)$

$x[\text{beg}:\text{end}]$

slicing

→ MAKES A COPY ( $x[i:]$  for complete copy)

→ beginning is inclusive, ending exclusive

→  $[1:]$  = "second item to the end"

→  $[:-1]$  = "everything except last item"

• Mutation

→  $x.append(\text{arg})$

→ makes a new box, shoves stuff in

→ arg can be anything

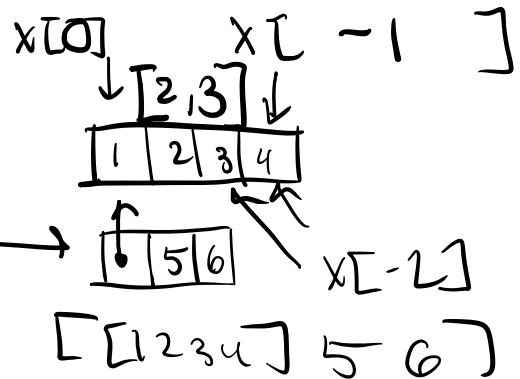
→  $x.extend(\text{arg})$

→ arg must be a list

→ is probably what your intuition gets

→ MODIFIES ORIGINAL

$[]$  is false-y



$x \leftarrow [1, 2, 3, 4, 5, 6]$

$y \leftarrow [5, 6]$

$x.extend(y)$

Max Product:

[10, 3, 1, 9, 2]

[5, 10, 5, 10, 5]

[7]

def max-product(s):

## Add This Many:

$s = [1, 2, 4, 2, 1]$       $s \rightarrow [1|2|4|2|1]$

$\text{add\_this\_many}(1, 5, s)$

$\text{add\_this\_many}(2, 2, s)$

def  $\text{add\_this\_many}(x, el, s)$ :

for  $i$  in  $s$

if  $i == x$ :

$\text{counter} += 1$

$s += [el] * \text{counter}$

$s = \downarrow s + \underline{\hspace{2cm}}$

$s.\text{extend}([el] * \text{counter})$

$s \rightarrow [ \hspace{10cm} ]$

aa

$s \rightarrow [ \hspace{10cm} ]$