team 10

2022-12-05

```
library(ggplot2)
library(moderndive)
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
      filter, lag
## The following objects are masked from 'package:base':
##
##
      intersect, setdiff, setequal, union
library(readr)
library(faraway)
library(tidyverse)
## -- Attaching packages -----
                                           ----- tidyverse 1.3.2 --
## v tibble 3.1.8
                    v stringr 1.4.1
                     v forcats 0.5.2
## v tidyr 1.2.1
## v purrr
           0.3.5
## -- Conflicts ------ tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
library(olsrr)
##
## Attaching package: 'olsrr'
## The following object is masked from 'package:faraway':
##
##
      hsb
##
## The following object is masked from 'package:datasets':
##
##
      rivers
library(glmnet)
## Loading required package: Matrix
## Attaching package: 'Matrix'
## The following objects are masked from 'package:tidyr':
##
```

```
##
       expand, pack, unpack
##
## Loaded glmnet 4.1-6
Cleaning Data set:
lifeExpectancyData1 <- read_csv("Life Expectancy Data.csv")</pre>
## Rows: 2938 Columns: 22
## -- Column specification -----
## Delimiter: ","
## chr (2): Country, Status
## dbl (20): Year, Life expectancy, Adult Mortality, infant deaths, Alcohol, pe...
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.
lifeExpectancyData <- lifeExpectancyData1 %>%
  rename(Life.expectancy = "Life expectancy") %>%
  rename(Adult.Mortality = "Adult Mortality") %>%
  rename(infant.deaths = "infant deaths") %>%
  rename(percentage.expenditure = "percentage expenditure") %>%
  rename(Measles = "Measles") %>%
  rename(under.five.deaths = "under-five deaths" ) %>%
  rename(Polio = "Polio")%>%
  rename(Diphtheria = "Diphtheria" )%>%
  rename(HIV.AIDS = "HIV/AIDS")
lifeExpectancyDataUpdated <- lifeExpectancyData[which(grepl(pattern="2015", lifeExpectancyData$Year)),]
After looking at the dataset, only 8 of the variables had values for all the countries (some of the columns had
NA entries):
lmod <- lm(Life.expectancy~Adult.Mortality+infant.deaths+percentage.expenditure+ Measles+under.five.dea</pre>
summary(lmod)
##
## lm(formula = Life.expectancy ~ Adult.Mortality + infant.deaths +
       percentage.expenditure + Measles + under.five.deaths + Polio +
##
##
       Diphtheria + HIV.AIDS, data = lifeExpectancyDataUpdated)
##
## Residuals:
##
       Min
                  1Q
                     Median
                                    3Q
                                            Max
## -17.8445 -2.5420 0.3501 3.3574 10.8480
## Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
                          7.120e+01 1.809e+00 39.356 < 2e-16 ***
## (Intercept)
## Adult.Mortality
                          -4.881e-02 4.517e-03 -10.806 < 2e-16 ***
## infant.deaths
                          6.752e-02 4.644e-02 1.454 0.14780
## percentage.expenditure 2.410e-03 1.220e-02
                                                 0.198 0.84358
## Measles
                          4.743e-06 8.175e-05
                                                 0.058 0.95380
## under.five.deaths
                         -5.958e-02 3.380e-02 -1.763 0.07972 .
## Polio
                          4.352e-02 1.892e-02
                                                2.300 0.02261 *
```

-5.543e-01 3.381e-01 -1.639 0.10296

2.762 0.00636 **

5.775e-02 2.091e-02

Diphtheria

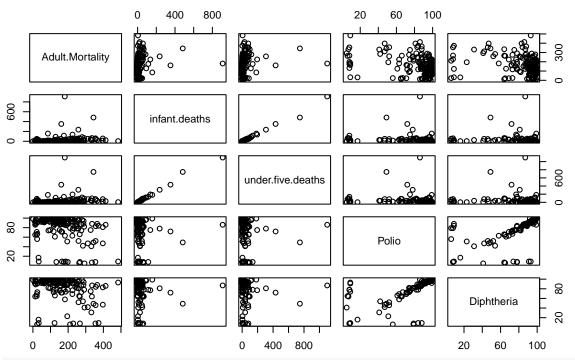
HIV.AIDS

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.509 on 174 degrees of freedom
## Multiple R-squared: 0.7054, Adjusted R-squared: 0.6919
## F-statistic: 52.08 on 8 and 174 DF, p-value: < 2.2e-16
anova(lmod)
## Analysis of Variance Table
## Response: Life.expectancy
##
                          Df Sum Sq Mean Sq F value
                                                        Pr(>F)
## Adult.Mortality
                           1 7291.0 7291.0 358.5390 < 2.2e-16 ***
## infant.deaths
                                              5.4863 0.020297 *
                             111.6
                                      111.6
## percentage.expenditure
                                              0.0581
                                                      0.809784
                                1.2
                                        1.2
## Measles
                               63.7
                                       63.7
                                              3.1338
                                                     0.078436
                           1
## under.five.deaths
                              128.2
                                      128.2
                                              6.3030
                                                     0.012966 *
## Polio
                              612.0
                                      612.0
                                             30.0950 1.432e-07 ***
## Diphtheria
                              210.4
                                      210.4
                                             10.3448
                                                     0.001548 **
## HIV.AIDS
                               54.6
                                       54.6
                                              2.6873 0.102956
                           1
                         174 3538.3
## Residuals
                                       20.3
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Based on the ANOVA table, we see that Adult Mortality, infant deaths, under-five deaths, polio, diphtheria have significant p values

pairs(~ Adult.Mortality + infant.deaths + under.five.deaths + Polio + Diphtheria, data=lifeExpectancyDa

Scatterplot Matrix



lifeExpectancyDataUpdated2 <- lifeExpectancyDataUpdated[c(-1,-2,-3,-7,-8,-9, -10, -11, -14, -16, -17, -print(cor(lifeExpectancyDataUpdated2[,2:5]),digits=4)

```
##
                    Adult.Mortality infant.deaths under.five.deaths Polio
## Adult.Mortality
                             1.0000
                                         0.1882
                                                           0.2120 -0.3724
## infant.deaths
                             0.1882
                                          1.0000
                                                           0.9942 -0.1297
## under.five.deaths
                             0.2120
                                          0.9942
                                                            1.0000 -0.1475
                            -0.3724
## Polio
                                         -0.1297
                                                           -0.1475 1.0000
Performing all possible, forward, and backward regressions
ourmodel <- lm(Life.expectancy~Adult.Mortality+infant.deaths+under.five.deaths+Polio+Diphtheria, data =
anova(ourmodel)
## Analysis of Variance Table
## Response: Life.expectancy
                     Df Sum Sq Mean Sq F value
                      1 7291.0 7291.0 359.0728 < 2.2e-16 ***
## Adult.Mortality
## infant.deaths
                      1 111.6
                                111.6
                                        5.4945 0.020187 *
## under.five.deaths 1 188.5
                               188.5 9.2836 0.002666 **
## Polio
                      1 613.1
                                 613.1 30.1957 1.344e-07 ***
## Diphtheria
                     1 212.8
                                212.8 10.4802 0.001441 **
## Residuals
                  177 3594.0
                                 20.3
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(ourmodel)
##
## Call:
## lm(formula = Life.expectancy ~ Adult.Mortality + infant.deaths +
##
      under.five.deaths + Polio + Diphtheria, data = lifeExpectancyDataUpdated2)
##
## Residuals:
                 10 Median
       Min
                                   30
## -18.3307 -2.5620 0.5472 3.1795 10.7421
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    70.656344 1.775388 39.798 < 2e-16 ***
## Adult.Mortality -0.052790 0.003815 -13.837 < 2e-16 ***
## infant.deaths
                                          1.986 0.04856 *
                     0.076029
                              0.038280
## under.five.deaths -0.065702   0.029900   -2.197   0.02929 *
## Polio
                    0.044868
                                0.018868
                                         2.378 0.01847 *
                    0.065743
                                0.020308
                                         3.237 0.00144 **
## Diphtheria
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.506 on 177 degrees of freedom
## Multiple R-squared: 0.7008, Adjusted R-squared: 0.6923
## F-statistic: 82.91 on 5 and 177 DF, p-value: < 2.2e-16
k <- ols_step_all_possible(ourmodel)</pre>
##
     Index N
                                                                  Predictors
## 1
```

Adult.Mortality

1 1

```
## 4
          2 1
                                                                            Polio
          3 1
                                                                       Diphtheria
## 3
          4 1
                                                               under.five.deaths
## 2
          5 1
                                                                    infant.deaths
          6 2
## 9
                                                      Adult.Mortality Diphtheria
## 8
          7 2
                                                           Adult.Mortality Polio
## 7
          8 2
                                               Adult.Mortality under.five.deaths
          9 2
                                                   Adult.Mortality infant.deaths
## 6
## 15
         10 2
                                                                 Polio Diphtheria
## 13
         11 2
                                                         under.five.deaths Polio
## 11
         12 2
                                                              infant.deaths Polio
         13 2
## 14
                                                    under.five.deaths Diphtheria
## 12
         14 2
                                                        infant.deaths Diphtheria
         15 2
## 10
                                                 infant.deaths under.five.deaths
## 21
         16 3
                                                Adult.Mortality Polio Diphtheria
## 20
         17 3
                                   Adult.Mortality under.five.deaths Diphtheria
## 18
         18 3
                                        Adult.Mortality infant.deaths Diphtheria
         19 3
                                         Adult.Mortality under.five.deaths Polio
## 19
## 17
         20 3
                                             Adult.Mortality infant.deaths Polio
         21 3
## 16
                                Adult.Mortality infant.deaths under.five.deaths
## 25
         22.3
                                              under.five.deaths Polio Diphtheria
## 22
         23 3
                                           infant.deaths under.five.deaths Polio
## 24
         24 3
                                                  infant.deaths Polio Diphtheria
## 23
         25 3
                                     infant.deaths under.five.deaths Diphtheria
         26 4
## 29
                             Adult.Mortality under.five.deaths Polio Diphtheria
## 28
         27 4
                                 Adult.Mortality infant.deaths Polio Diphtheria
                     Adult.Mortality infant.deaths under.five.deaths Diphtheria
## 27
         28 4
## 26
         29 4
                          Adult.Mortality infant.deaths under.five.deaths Polio
         30 4
                               infant.deaths under.five.deaths Polio Diphtheria
## 30
         31 5 Adult.Mortality infant.deaths under.five.deaths Polio Diphtheria
   31
##
        R-Square Adj. R-Square Mallow's Cp
## 1
      0.60702715
                     0.60485603
                                  53.453978
##
      0.26584521
                                 255.272250
                     0.26178911
## 5
      0.25030006
                     0.24615807
                                 264.467625
## 3
      0.07394106
                     0.06882471
                                 368.788705
## 2
      0.05822064
                     0.05301744
                                 378.087750
## 9
      0.67617183
                     0.67257374
                                  14.553047
## 8
      0.66604570
                     0.66233510
                                  20.542926
## 7
      0.61895787
                     0.61472407
                                  48.396640
                                  49.959505
## 6
     0.61631578
                     0.61205263
## 15 0.31090042
                     0.30324376
                                 230.620886
## 13 0.30507170
                     0.29735027
                                 234.068730
## 11 0.29678159
                     0.28896805
                                 238.972552
## 14 0.29228605
                     0.28442256
                                 241.631787
## 12 0.28398757
                     0.27603188
                                 246.540558
## 10 0.14686529
                     0.13738602
                                 327.652061
## 21 0.68671445
                     0.68146386
                                  10.316804
## 20 0.68422466
                     0.67893234
                                  11.789582
## 18 0.68262532
                     0.67730619
                                  12.735638
## 19 0.67435180
                     0.66889401
                                  17.629646
## 17 0.67255075
                     0.66706278
                                  18.695013
## 16 0.63201008
                     0.62584265
                                  42.675907
## 25 0.34579411
                     0.33482977
                                 211.980329
## 22 0.34360456
                     0.33260352
                                 213.275508
```

```
## 29 0.69410563 0.68723160 7.944727
## 27 0.69121458 0.68427558
                      9.654857
## 30 0.37707642 0.36307813 195.476008
forward
f <- ols_step_forward_p(ourmodel, penter= 0.3, details = TRUE)</pre>
## Forward Selection Method
## Candidate Terms:
##
## 1. Adult.Mortality
## 2. infant.deaths
## 3. under.five.deaths
## 4. Polio
## 5. Diphtheria
## We are selecting variables based on p value...
##
##
## Forward Selection: Step 1
## - Adult.Mortality
##
##
                  Model Summary
                  0.779 RMSE
0.607 Coef. Var
0.605 MSE
## R
                                         5.107
## R-Squared
                                        7.130
## Adj. R-Squared
                 0.605
                                        26.077
## Pred R-Squared
                  0.596
                         MAE
                                        3.581
## RMSE: Root Mean Square Error
## MSE: Mean Square Error
## MAE: Mean Absolute Error
##
##
                         ANOVA
##
             Sum of
           Squares
                   DF Mean Square F Sig.
## -----
                      1 7291.014
## Regression 7291.014
                                       279.592 0.0000
## Residual
           4720.004
                       181
                               26.077
                       182
## Total
           12011.017
##
##
                           Parameter Estimates
        model Beta Std. Error Std. Beta t Sig lower upper
```

(Intercept							0.000		
Adult.Mortalit					-0.779 	-16.721 	0.000	-0.073 	-0.05
Forward Select	tion: Step	2							
- Diphtheria									
		Model	Summa	ary					
R		0.822		RMSE		4.648			
R-Squared				Coef.	Var	6.491			
Adj. R-Squared						21.608			
Pred R-Squared						3.473			
RMSE: Root Me	-								
MSE: Mean Squ MAE: Mean Abs									
HAL. Heall Abs	SOLUCE LIIV	OI.							
				AVOV					
	Sum of								
	Squares		DF	Mea	n Square	F	Sig.		
Regression			2		4060.756	187.925	0.0000		
Regiduel									
	3889.506				21.608				
Total	12011.017		180 182		21.608				
Total	12011.017		182	 Para	meter Estima	 ates			
Total	12011.017		182	Para	meter Estima		 Sig	 lower	 uppe
Total mode	12011.017	 ta S	182 Std. E	Para Error	meter Estima	t			
Total mode	12011.017 	 ta S 	182 Std. E	Para Error 	meter Estima	t 42.236	0.000	68.421	75.12
Total mode (Intercept Adult.Mortalit	12011.017 el Be c) 71.7 cy -0.09	 ta S 74 57	182 Std. E	Para Error 1.699 0.004	meter Estima 	t 42.236 -15.386	0.000	68.421 -0.065	75.12 -0.05
Total mode (Intercept Adult.Mortalit	2011.017 21 Be 71.7 Ty -0.09 1a 0.10	 ta \$ 74 57	182 Std. E 1	Para Error 1.699 0.004 0.016	meter Estima 	t 42.236 -15.386 6.200	0.000 0.000 0.000	68.421 -0.065 0.069	75.12 -0.05 0.13
Total mode (Intercept Adult.Mortalit Diphtheri	2011.017 21 Be 71.7 Ty -0.09 1a 0.10	 ta \$ 74 57	182 Std. E 1	Para Error 1.699 0.004 0.016	meter Estima 	t 42.236 -15.386 6.200	0.000 0.000 0.000	68.421 -0.065 0.069	75.12 -0.05 0.13
Total mode (Intercept Adult.Mortalit Diphtheri	2011.017 21 Be 71.7 Ty -0.09 1a 0.10	 ta \$ 74 57	182 Std. E 1	Para Error 1.699 0.004 0.016	meter Estima 	t 42.236 -15.386 6.200	0.000 0.000 0.000	68.421 -0.065 0.069	75.12 -0.05 0.13
Total mode (Intercept Adult.Mortalit Diphtheri	12011.017 el Be c) 71.7 ty -0.09 ia 0.16	 ta S 74 57 02	182 Std. E 1	Para Error 1.699 0.004 0.016	meter Estima 	t 42.236 -15.386 6.200	0.000 0.000 0.000	68.421 -0.065 0.069	75.12 -0.05 0.13
Total mode (Intercept Adult.Mortalit Diphtheri	12011.017 el Be c) 71.7 ty -0.09 ia 0.16	 ta S 74 57 02	182 Std. E 1	Para Error 1.699 0.004 0.016	meter Estima 	t 42.236 -15.386 6.200	0.000 0.000 0.000	68.421 -0.065 0.069	75.12 -0.05 0.13
Total mode (Intercept Adult.Mortalit Diphtheri Forward Select	12011.017 el Be c) 71.7 ty -0.09 ia 0.16	ta S	182	Para Error 1.699 0.004 0.016	meter Estima 	t 42.236 -15.386 6.200	0.000 0.000 0.000	68.421 -0.065 0.069	75.12 -0.05 0.13
Total mode (Intercept Adult.Mortalit Diphtheri Forward Select	12011.017	ta S 74 57 02 3	182	Para Error 1.699 0.004 0.016	meter Estima Std. Beta -0.689 0.278	t 42.236 -15.386 6.200	0.000 0.000 0.000	68.421 -0.065 0.069	75.12 -0.05 0.13
Total mode (Intercept Adult.Mortalit Diphtheri Forward Select	12011.017	ta S 74 57 02 3	182 Std. E	Para: Error 1.699 0.004 0.016	meter Estima Std. Beta -0.689 0.278	t 42.236 -15.386 6.200	0.000 0.000 0.000	68.421 -0.065 0.069	75.12 -0.05 0.13
Total mode (Intercept Adult.Mortalit Diphtheri Forward Select - Polio R R-Squared	12011.017 el Be c) 71.7 ty -0.09 tia 0.10	ta S 74 57 02 3 Model 0.829	182 Std. F	Para Error 1.699 0.004 0.016 	meter Estima Std. Beta -0.689 0.278	t 42.236 -15.386 6.200	0.000 0.000 0.000	68.421 -0.065 0.069	75.12 -0.05 0.13
Total mode (Intercept Adult.Mortalit Diphtheri Forward Select	12011.017	ta S 74 57 02 3 Model 0.829	182 Std. E	Para Error 1.699 0.004 0.016	meter Estima Std. Beta -0.689 0.278	t 42.236 -15.386 6.200	0.000 0.000 0.000	68.421 -0.065 0.069	0.13

MAE: Mean A	Absolute Er	ror							
			AN	OVA					
	Sum o Sauare		DF	Meai	n Square	F	Sig.		
						- 			
Regression	8248.13	9	3		2749.380	130.788	0.0000		
Residual Total			179 182		21.022				
	12011.01 	<i>.</i>	162						
					meter Estima	ates			
	odel B	eta S	td. E	rror	Std. Beta		 Sig	lower	upper
	ept) 70.						0.000		73.723
Adult.Mortal	lity -0.	055	0	.004	-0.665	-14.654	0.000	-0.063	-0.048
Diphthe	eria 0.	071	0	.021	0.193	3.436	0.001	0.030	0.111
Pc	olio 0.	047	0	.019	0.141	2.454	0.015	0.009	0.085
- under.five		-							
Forward Sele	e.deaths	Model							
- under.five	e.deaths	Model 		RMSE		4.543			
- under.five	e.deaths	Model 0.833 0.694		RMSE Coef.		4.543 6.344			
- under.five	e.deaths red red	Model 0.833 0.694		RMSE		4.543			
- under.five	e.deaths red red	Model 0.833 0.694 0.687 0.662		RMSE Coef. MSE		4.543 6.344 20.641			
- under.five	red red Mean Squar	Model 0.833 0.694 0.687 0.662 e Error		RMSE Coef. MSE		4.543 6.344 20.641			
- under.five	red red Mean Squar	Model 0.833 0.694 0.687 0.662 e Error		RMSE Coef. MSE		4.543 6.344 20.641			
- under.five	red red Mean Squar Square Erro	Model 0.833 0.694 0.687 0.662 e Error r	AN	RMSE Coef. MSE MAE	Var	4.543 6.344 20.641 3.412			
- under.five	red red Mean Squar Square Erro Absolute Er Sum o	Model 0.833 0.694 0.687 0.662 e Error r ror	AN	RMSE Coef. MSE MAE	Var	4.543 6.344 20.641 3.412	 Sig.		
- under.five	red red Mean Squar Square Erro Absolute Er	Model 0.833 0.694 0.687 0.662 e Error r ror	AN	RMSE Coef. MSE MAE	Var	4.543 6.344 20.641 3.412 			
- under.five	red red Mean Squar Square Erro Absolute Er Sum o Square	Model 0.833 0.694 0.687 0.662 e Error r ror	AN	RMSE Coef. MSE MAE	Var n Square 	4.543 6.344 20.641 3.412 			
- under.five	red red Mean Squar Square Erro Absolute Er Sum o Square 8336.91 3674.10	Model 0.833 0.694 0.687 0.662 e Error r ror f s 5 3 7	AN DF 4 178 182	RMSE Coef. MSE MAE	Var n Square 	4.543 6.344 20.641 3.412 			
- under.five	red red Mean Squar Square Erro Absolute Er Sum o Square 8336.91 3674.10	Model 0.833 0.694 0.687 0.662 e Error r ror f s 5 3 7	AN DF 4 178 182	RMSE Coef. MSE MAE	Var n Square 	4.543 6.344 20.641 3.412 			

(Intercept)			1.787		;	39.426	0.000	66.912	73.96
Adult.Mortality									
Diphtheria				0.18					
	0.046								
under.five.deaths				-0.08	38 -	-2.074	0.040	-0.013	0.0
Forward Selection:	Step 5								
- infant.deaths									
		~							
	Model		-						
R	0.837		RMSE		4.50)6			
R-Squared	0.701		Coef.	Var	6.29	92			
Adj. R-Squared					20.30)5			
Pred R-Squared					3.38	34			
RMSE: Root Mean Sq	•								
MSE: Mean Square E MAE: Mean Absolute									
MAE: Mean Absolute	Error								
		ANOV	7 Δ						
		11110							
	 m of								
Su Squ	m of ares	DF	Mean	Square	F	s	 ig.		
Su Squ	m of ares	DF	Mean						
Su Squ Regression 8417	m of ares 	DF 5	Mean 1	683.403					
Su Squ 	m of lares 	DF 5 177	Mean 1						
Su Squ 	m of lares 	DF 5 177 182	Mean	683.403 20.305					
Su Squ 	m of lares 	DF 5 177 182	Mean	683.403 20.305					
Su Squ 	m of lares 	DF 5 177 182	Mean 1	683.403 20.305	82.905				
Su Squ 	m of lares	DF 5 177 182	Mean 1	683.403 20.305	82.905				
Su Squ 	m of lares	DF 5 177 182	Mean 1	683.403 20.305	82.905			lower	 upp
Su Squ Squ Squ Regression 8417 Residual 3594 Total 12011	m of lares	DF 5 177 182	Mean 1 Para Error	683.403 20.305	82.905	0.0	 0000 Sig		
Su Squ Squ Squ Squ Regression 8417 Residual 3594 Total 12011	m of lares	DF 5 177 182	Mean 1 Para Error 1.775	683.403 20.305 meter Estim	82.905	0.00 t	Sig 	67.153	74.1
Su Squ Squ Squ Squ Squ Squ Squ Squ Squ S	m of lares 7.013 8.005 8.017 8eta 70.656 -0.053	DF 5 177 182	Para Error 1.775	683.403 20.305 meter Estim Std. Bet	82.905 nates a 34	0.00 t 39.798	Sig 0.000	67.153 -0.060	74.1 -0.0
Su Squ Squ Squ Squ Regression 8417 Residual 3594 Total 12011	m of lares 7.013 7.005 7.017 8eta 70.656 70.053 70.066	DF 5 177 182	Para Error 1.775 0.004 0.020	683.403 20.305 meter Estim Std. Bet	82.905 nates a 34 -:	0.00 t 39.798 13.837 3.237	0.000 Sig 0.000 0.000 0.000	67.153	74.1 -0.0 0.1
Su Squ Squ Squ Squ Squ Squ Squ Squ Squ S	m of lares 7.013 8.005 8.017 8eta 70.656 -0.053	DF 5 177 182	Para Error 1.775	683.403 20.305 meter Estim Std. Bet	82.905 nates a 34 -1	0.00 t 39.798	Sig 0.000	67.153 -0.060 0.026	74.1 -0.0 0.1 0.0
Regression 8417 Residual 3594 Total 12011	m of lares 7.013 7.005 7.017 8eta 70.656 70.053 7.066 7.045	DF 5 177 182	Para Error 1.775 0.004 0.020 0.019	683.403 20.305 meter Estim Std. Bet	82.905	t	Sig 0.000 0.000 0.000 0.001 0.018	67.153 -0.060 0.026 0.008	74.1 -0.0 0.1 0.0 -0.0
Regression 8417 Residual 3594 Total 12011	Beta 70.656 -0.053 0.066 0.045 -0.066	DF 5 177 182	Para Error 1.775 0.004 0.020 0.019 0.030	683.403 20.305 meter Estim Std. Bet -0.63 0.17 0.13 -0.87	82.905	t 39.798 13.837 3.237 2.378 -2.197	Sig 0.000 0.000 0.000 0.001 0.018 0.029	67.153 -0.060 0.026 0.008 -0.125	74.1 -0.0 0.1 0.0 -0.0
Regression 8417 Residual 3594 Total 12011	Beta 70.656 -0.053 0.066 0.045 -0.066	DF 5 177 182	Para Error 1.775 0.004 0.020 0.019 0.030	683.403 20.305 meter Estim Std. Bet -0.63 0.17 0.13 -0.87	82.905	t 39.798 13.837 3.237 2.378 -2.197	Sig 0.000 0.000 0.000 0.001 0.018 0.029	67.153 -0.060 0.026 0.008 -0.125	74.1 -0.0 0.1 0.0 -0.0
Regression 8417 Residual 3594 Total 12011	Beta 70.656 -0.053 0.066 0.045 -0.066	DF 5 177 182	Para Error 1.775 0.004 0.020 0.019 0.030	683.403 20.305 meter Estim Std. Bet -0.63 0.17 0.13 -0.87	82.905	t 39.798 13.837 3.237 2.378 -2.197	Sig 0.000 0.000 0.000 0.001 0.018 0.029	67.153 -0.060 0.026 0.008 -0.125	74.1 -0.0 0.1 0.0 -0.0
Regression 8417 Residual 3594 Total 12011	Beta 70.656 -0.053 0.066 0.045 -0.066	DF 5 177 182	Para Error 1.775 0.004 0.020 0.019 0.030	683.403 20.305 meter Estim Std. Bet -0.63 0.17 0.13 -0.87	82.905	t 39.798 13.837 3.237 2.378 -2.197	Sig 0.000 0.000 0.000 0.001 0.018 0.029	67.153 -0.060 0.026 0.008 -0.125	74.1 -0.0 0.1 0.0 -0.0
Regression 8417 Residual 3594 Total 12011	Beta 70.656 -0.053 0.066 0.045 -0.066	DF 5 177 182	Para Error 1.775 0.004 0.020 0.019 0.030	683.403 20.305 meter Estim Std. Bet -0.63 0.17 0.13 -0.87	82.905	t 39.798 13.837 3.237 2.378 -2.197	Sig 0.000 0.000 0.000 0.001 0.018 0.029	67.153 -0.060 0.026 0.008 -0.125	74.1 -0.0 0.1 0.0 -0.0
Regression 8417 Residual 3594 Total 12011	Beta 70.656 -0.053 0.066 0.045 -0.066	DF 5 177 182	Para Error 1.775 0.004 0.020 0.019 0.030	683.403 20.305 meter Estim Std. Bet -0.63 0.17 0.13 -0.87	82.905	t 39.798 13.837 3.237 2.378 -2.197	Sig 0.000 0.000 0.000 0.001 0.018 0.029	67.153 -0.060 0.026 0.008 -0.125	74.1 -0.0 0.1 0.0 -0.0
Regression 8417 Residual 3594 Total 12011	Beta 70.656 -0.053 0.066 0.045 -0.066	DF 5 177 182	Para Error 1.775 0.004 0.020 0.019 0.030	683.403 20.305 meter Estim Std. Bet -0.63 0.17 0.13 -0.87	82.905	t 39.798 13.837 3.237 2.378 -2.197	Sig 0.000 0.000 0.000 0.001 0.018 0.029	67.153 -0.060 0.026 0.008 -0.125	74.1 -0.0 0.1 0.0 -0.0 0.1

```
## + Polio
## + under.five.deaths
## + infant.deaths
##
## Final Model Output
                     Model Summary
## -----
                     0.837
                            RMSE
## R
                                             4.506
                    0.701 Coef. Var
0.692 MSE
0.374 MAE
## R-Squared
                                              6.292
## Adj. R-Squared
                                             20.305
## Pred R-Squared
                                             3.384
## -----
## RMSE: Root Mean Square Error
## MSE: Mean Square Error
## MAE: Mean Absolute Error
##
##
                           ANOVA
## -----
              Sum of
                      DF Mean Square F Sig.
##
             Squares
## -----
## Regression 8417.013 5 1683.403 82.905 0.0000
## Residual 3594.005
                         177
                                  20.305
           12011.017
## Total
                         182
##
                                Parameter Estimates
          model
                   Beta Std. Error Std. Beta
                                                  t Sig
                                                                lower upper
## ------
##
     (Intercept) 70.656
                              1.775
                                                39.798 0.000 67.153
                                                                       74.160
   Adult.Mortality -0.053 0.004 -0.634 -13.837 0.000 -0.060
Diphtheria 0.066 0.020 0.179 3.237 0.001 0.026
Polio 0.045 0.019 0.134 2.378 0.018 0.008
Diphtheria -0.066 0.030 -0.872 -2.197 0.029 -0.125
Diphtheria 0.076 0.038 0.783 1.986 0.049 0.000
  Adult.Mortality -0.053
                                                                      -0.045
##
                                                                       0.106
##
                                                                       0.082
## under.five.deaths -0.066
                                                                       -0.007
## infant.deaths 0.076
                                                                       0.152
```

backward

b <- ols_step_backward_p(ourmodel, penter = 0.3, details = TRUE)

```
## Backward Elimination Method
## -----
##
## Candidate Terms:
##
## 1 . Adult.Mortality
## 2 . infant.deaths
## 3 . under.five.deaths
## 4 . Polio
```

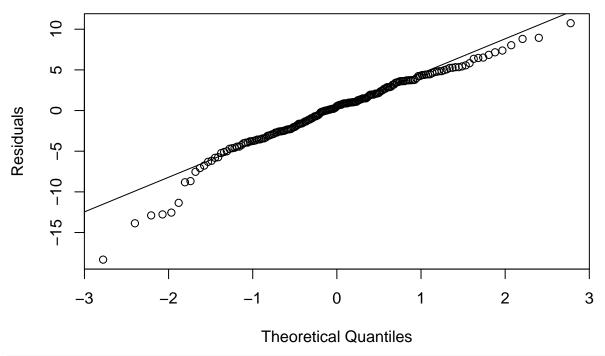
5 . Diphtheria

```
##
## We are eliminating variables based on p value...
##
##
## No more variables satisfy the condition of p value = 0.3
## Variables Removed:
##
##
##
## Final Model Output
## -----
##
                    Model Summary
## -----
                  0.837 RMSE
0.701 Coef. Var
0.692 MSE
## R
                                           4.506
## R-Squared
                                           6.292
## Adj. R-Squared
                                          20.305
                             MAE
## Pred R-Squared
                   0.374
                                           3.384
## RMSE: Root Mean Square Error
## MSE: Mean Square Error
## MAE: Mean Absolute Error
##
                         ANOVA
## -----
              Sum of
             Squares DF Mean Square
                       5 1683.403
177 20.305
                                         82.905 0.0000
## Regression
             8417.013
## Residual
            3594.005
## Total
           12011.017
                        182
##
##
                             Parameter Estimates
## -----
          model Beta Std. Error Std. Beta
##
      (Intercept) 70.656
                                             39.798 0.000 67.153
                            1.775
                                                                  74.160
  Adult.Mortality -0.053
                           0.004
                                    -0.634 -13.837 0.000 -0.060
                                                                  -0.045
                           0.038
    infant.deaths 0.076
                                     0.783
                                              1.986 0.049 0.000
                                                                    0.152
## under.five.deaths -0.066
                                     -0.872 -2.197 0.029 -0.125
                           0.030
                                                                    -0.007
##
    Polio 0.045
                           0.019
                                     0.134
                                             2.378 0.018 0.008
                                                                   0.082
                                     0.179 3.237 0.001 0.026
     Diphtheria 0.066
                           0.020
                                                                   0.106
```

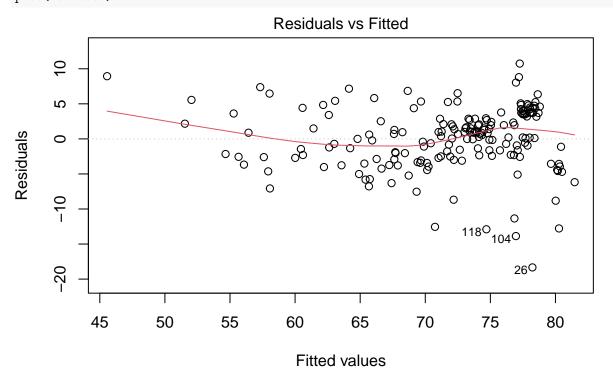
Check model assumptions

```
qqnorm(residuals(ourmodel),ylab="Residuals",main="Q-Q plot")
qqline(residuals(ourmodel))
```

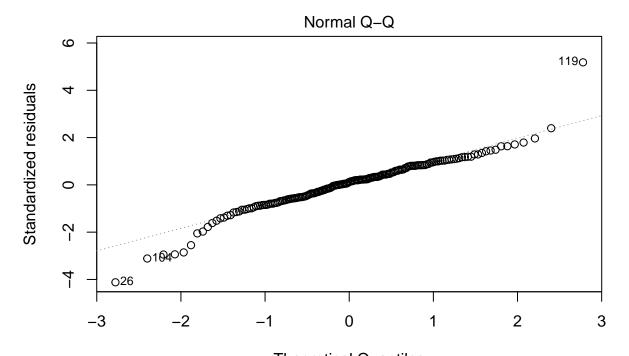




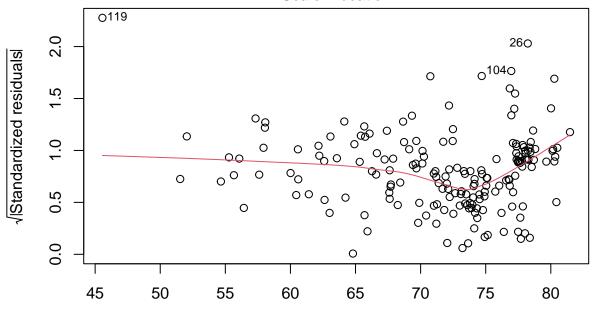
plot(ourmodel)



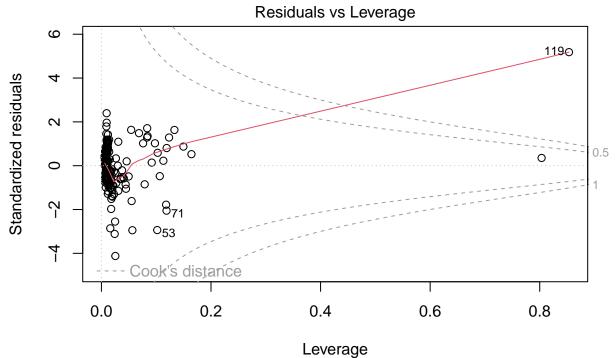
Im(Life.expectancy ~ Adult.Mortality + infant.deaths + under.five.deaths + ...



Theoretical Quantiles
Im(Life.expectancy ~ Adult.Mortality + infant.deaths + under.five.deaths + ...
Scale-Location



Fitted values
Im(Life.expectancy ~ Adult.Mortality + infant.deaths + under.five.deaths + ...



Im(Life.expectancy ~ Adult.Mortality + infant.deaths + under.five.deaths + ...

Check for multicollinearity

```
vif(ourmodel)
```

```
## Adult.Mortality infant.deaths under.five.deaths Polio
## 1.241665 91.979835 93.084879 1.875786
## Diphtheria
## 1.815719
```

Removed infant.deaths to remove multicollinearity? And to obtain final model, also this had higher r squared adj value and minimized Cp (error)

finalmod <- lm(Life.expectancy~Adult.Mortality+under.five.deaths+Polio+Diphtheria, data = lifeExpectancy
summary(finalmod)</pre>

```
##
## Call:
  lm(formula = Life.expectancy ~ Adult.Mortality + under.five.deaths +
       Polio + Diphtheria, data = lifeExpectancyDataUpdated)
##
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
                                 3.2032 10.6572
  -19.1710 -2.6531
                        0.5757
##
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     70.437108
                                  1.786550
                                            39.426
                                                    < 2e-16 ***
## Adult.Mortality
                     -0.054026
                                  0.003795 -14.237
                                                    < 2e-16 ***
## under.five.deaths -0.006654
                                            -2.074
                                  0.003209
                                                    0.03953 *
## Polio
                      0.045606
                                  0.019020
                                             2.398
                                                    0.01753 *
## Diphtheria
                      0.069168
                                  0.020401
                                             3.390
                                                    0.00086 ***
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.543 on 178 degrees of freedom
## Multiple R-squared: 0.6941, Adjusted R-squared: 0.6872
                  101 on 4 and 178 DF, p-value: < 2.2e-16
## F-statistic:
anova(finalmod)
## Analysis of Variance Table
##
## Response: Life.expectancy
                      Df Sum Sq Mean Sq F value
                       1 7291.0 7291.0 353.2292 < 2.2e-16 ***
## Adult.Mortality
## under.five.deaths
                         143.3
                                  143.3
                                          6.9425 0.0091594 **
## Polio
                         665.3
                                  665.3 32.2337 5.467e-08 ***
## Diphtheria
                         237.3
                                  237.3 11.4948 0.0008597 ***
## Residuals
                     178 3674.1
                                   20.6
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
LASSO method
x<-(apply(lifeExpectancyDataUpdated2[,-1],2,as.numeric))</pre>
y<-(apply(lifeExpectancyDataUpdated2[,1],2,as.numeric))</pre>
set.seed(43215)
lasso_cv = cv.glmnet(x, y,family=c("gaussian"),standardize=TRUE,nfolds=10,lambda=seq(0,1,0.001,alpha =
## Warning: In seq.default(0, 1, 0.001, alpha = 1) :
## extra argument 'alpha' will be disregarded
plot(lasso_cv)
             5
                             5 5 5 5 5 5 4 4 4 4
      9
Mean-Squared Error
      50
      4
      30
```

 $Log(\lambda)$

-3

-2

-1

0

20

-7

-6

-5

[1] 0.6929939