# Inference for SRL Report

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Capita Selecta AI (Probabilistic Programming) 2016-2017

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Daniel: Not sure if the 6th clause of the network variable A in ?? is correctly substituted due to the property describe in the paper "Consider again Figure 1 and imagine that the parameter  $\theta c1|a1$  were 0. Given that this parameter is known to be 0, all models that set this parameter variable to true will have weight 0."

Daniel: For ??, should we also chance the closure that contains a probability of 0, like we did in the ENC1 encoding? Look comment above

### I. PROBABILISTIC INFERENCE USING WEIGHTED MODEL COUNTING

#### A. PGM to CNF

Table I shows the semantics of the domain variables used for those tasks.

Tables II and III show the logical variables used for encoding the Bayesian Network in [1].

Table ?? represents the encoded Bayesian Network using ENC1 and table V contains the corresponding weights.

Likewise, table ?? represents the encoded Bayesian Network using ENC2 and table VII contains the corresponding weights.

#### REFERENCES

[1] Bayesian networks.

Table I. VARIABLES AND DOMAIN SEMANTICS

Variable	Domain	
B = Burglary	b1 = theres is a burglary	
	b2 = theres is no burglary	
	e1 = there is a heavy earthquake	
E = Earthquake	e2 = there is a mild earthquake	
	e3 = there is no earthquake	
A = Alarm	a1 = alarm rings	
	a2 = alarm does not ring	
J = John	j1 = John calls	
	j2 = John does not call	
M = Mary	m1 = Mary calls	
	m2 = Mary does not call	

Table II. LOGICAL VARIABLES USING ENC1

Network variables	Indicator Variable	СТР
В	$\lambda_{b1}, \lambda_{b2}$	$\theta_{b1},\theta_{b2}$
Е	$\lambda_{e1}, \lambda_{e2}, \lambda_3$	$\theta_{e1},\theta_{e2},\theta_3$
A	$\lambda_{a1},\lambda_{a2}$	$\begin{array}{c} \theta_{a1 b1,e1},  \theta_{a1 b1,e2}, \theta_{a1 b1,e3}, \\ \theta_{a1 b2,e1},  \theta_{a1 b2,e2},  \theta_{a1 b2,e3}, \\ \theta_{a2 b1,e1},  \theta_{a2 b1,e2}, \theta_{a2 b1,e3}, \\ \theta_{a2 b2,e1},  \theta_{a2 b2,e2},  \theta_{a2 b2,e3} \end{array}$
J	$\lambda_{j1}, \lambda_{j2}$	$\theta_{j1 a1},  \theta_{j2 a1},  \theta_{j1 a2},  \theta_{j2 a2}$
M	$\lambda_{m1}, \lambda_{m2}$	$\theta_{m1 a1}, \theta_{m2 a1}, \theta_{m1 a2}, \theta_{m2 a2}$

Table III. LOGICAL VARIABLES USING ENC2

Variables	Indicator Variable	СТР
В	$\lambda_{b1}, \lambda_{b2}$	$ ho_{b1}$
Е	$\lambda_{e1}, \lambda_{e2}, \lambda_3$	$ ho_{e1}, ho_{e2}$
A	$\lambda_{a1}, \lambda_{a2}$	$\rho_{a1 b1,e1}, \rho_{a1 b1,e2}, \rho_{a1 b1,e3}, \\ \rho_{a1 b2,e1}, \rho_{a1 b2,c2}, \rho_{a1 b2,e3}$
J	$\lambda_{j1}, \lambda_{j2}$	$ ho_{j1 a1}, ho_{j1 a2}$
M	$\lambda_{m1}, \lambda_{m2}$	$\rho_{m1 a1}, \rho_{m1 a2}$

Table IV. CNF REPRESENTATION OF BAYESIAN NETWORK USING ENC1

Variables		CNF
В	$\begin{array}{c} \lambda_{b1} \vee \lambda_{b2} \\ \neg \lambda_{b1} \vee \neg \lambda_{b2} \end{array}$	$ \lambda_{b1} \Leftrightarrow \theta_{b1} \\ \lambda_{b2} \Leftrightarrow \theta_{b2} $
Е	$\lambda_{e1} \lor \lambda_{e2} \lor \lambda_{e3}$ $\neg \lambda_{e1} \lor \neg \lambda_{e2}$ $\neg \lambda_{e1} \lor \neg \lambda_{e3}$ $\neg \lambda_{e2} \lor \neg \lambda_{e3}$	$\lambda_{e1} \Leftrightarrow \theta_{e1}$ $\lambda_{e2} \Leftrightarrow \theta_{e2}$ $\lambda_{e3} \Leftrightarrow \theta_{e3}$
A	$\lambda_{a1} \vee \lambda_{a2}$ $\neg \lambda_{a1} \vee \neg \lambda_{a2}$	$\begin{array}{c} \lambda_{a1} \wedge \lambda_{b1} \wedge \lambda_{e1} \Leftrightarrow \theta_{a1 b1,e1} \\ \lambda_{a1} \wedge \lambda_{b1} \wedge \lambda_{e2} \Leftrightarrow \theta_{a1 b1,e2} \\ \lambda_{a1} \wedge \lambda_{b1} \wedge \lambda_{e3} \Leftrightarrow \theta_{a1 b1,e3} \\ \lambda_{a1} \wedge \lambda_{b2} \wedge \lambda_{e1} \Leftrightarrow \theta_{a1 b2,e1} \\ \lambda_{a1} \wedge \lambda_{b2} \wedge \lambda_{e2} \Leftrightarrow \theta_{a1 b2,e2} \\ \lambda_{a1} \wedge \lambda_{b2} \wedge \lambda_{e3} \Leftrightarrow \theta_{a1 b2,e3} \\ \lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e1} \Leftrightarrow \theta_{a2 b1,e1} \\ \lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e2} \Leftrightarrow \theta_{a2 b1,e2} \\ \lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e3} \Leftrightarrow \theta_{a2 b1,e2} \\ \lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e3} \Leftrightarrow \theta_{a2 b1,e2} \\ \lambda_{a2} \wedge \lambda_{b2} \wedge \lambda_{e1} \Leftrightarrow \theta_{a2 b2,e2} \\ \lambda_{a2} \wedge \lambda_{b2} \wedge \lambda_{e2} \Leftrightarrow \theta_{a2 b2,e2} \\ \lambda_{a2} \wedge \lambda_{b2} \wedge \lambda_{e3} \Leftrightarrow \theta_{a2 b2,e3} \\ \end{array}$
J	$\lambda_{j1} \vee \lambda_{j2} \\ \neg \lambda_{j1} \vee \neg \lambda_{j2}$	$\lambda_{j1} \wedge \lambda_{a1} \Leftrightarrow \theta_{j1 a1}$ $\lambda_{j1} \wedge \lambda_{a2} \Leftrightarrow \theta_{j1 a2}$ $\lambda_{j2} \wedge \lambda_{a1} \Leftrightarrow \theta_{j2 a1}$ $\lambda_{j2} \wedge \lambda_{a2} \Leftrightarrow \theta_{j2 a2}$
М	$\lambda_{m1} \vee \lambda_{m2}$ $\neg \lambda_{m1} \vee \neg \lambda_{m2}$	$\lambda_{m1} \wedge \lambda_{a1} \Leftrightarrow \theta_{m1 a1}$ $\lambda_{m1} \wedge \lambda_{a2} \Leftrightarrow \theta_{m1 a2}$ $\lambda_{m2} \wedge \lambda_{a1} \Leftrightarrow \theta_{m2 a1}$ $\lambda_{m2} \wedge \lambda_{a2} \Leftrightarrow \theta_{m2 a2}$

Table V. WEIGHTS ASSOCIATION USING ENC1

Weights	Value
$W(\theta_{b1})$	0.7
$W(\theta_{b2})$	0.3
$W(\theta_{e1})$	0.01
$W(\theta_{e2})$	0.19
$W(\theta_{e3})$	0.80
$W(\theta_{a1 b1,e1})$	0.90
$W(\theta_{a1 b1,e2})$	0.85
$W(\theta_{a1 b1,e3})$	0.80
$\mathrm{W}(\theta_{a1 b2,e1})$	0.30
$\mathrm{W}(\theta_{a1 b2,e2})$	0.10
$W(\theta_{a1 b2,e3})$	0.00
$\mathrm{W}(\theta_{a2 b1,e1})$	0.10
$\mathrm{W}(\theta_{a2 b1,e2})$	0.15
$W(\theta_{a2 b1,e3})$	0.20
$W(\theta_{a2 b2,e1})$	0.70
$W(\theta_{a2 b2,e2})$	0.90
$\mathrm{W}(\theta_{a2 b2,e3})$	1.00
$W(\theta_{i1 a1})$	0.80
$W(\theta_{j1 a2})$	0.10
$W(\theta_{j2 a1})$	0.20
$W(\theta_{j2 a2})$	0.90
$W(\theta_{m1 a1})$	0.80
$W(\theta_{m1 a2})$	0.10
$W(\theta_{m2 a1})$	0.20
$W(\theta_{m2 a2})$	0.90
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Table VI. CNF REPRESENTATION OF BAYESIAN NETWORK USING ENC2

Variables	CNF	
В	$ \begin{array}{c} \lambda_{b1} \vee \lambda_{b2} \\ \neg \lambda_{b1} \vee \neg \lambda_{b2} \end{array} $	$ \begin{array}{c} \rho_{b1} \Rightarrow \lambda_{b1} \\ \neg \rho_{b1} \Rightarrow \lambda_{b2} \end{array} $
Е	$\lambda_{e1} \lor \lambda_{e2} \lor \lambda_{e3}$ $\neg \lambda_{e1} \lor \neg \lambda_{e2}$ $\neg \lambda_{e1} \lor \neg \lambda_{e3}$ $\neg \lambda_{e2} \lor \neg \lambda_{e3}$	$ \rho_{e1} \Rightarrow \lambda_{e1}  \neg \rho_{e1} \wedge \rho_{e2} \Rightarrow \lambda_{e2}  \neg \rho_{e1} \wedge \neg \rho_{e2} \Rightarrow \lambda_{e3} $
A	$\lambda_{a1} \vee \lambda_{a2}$ $\neg \lambda_{a1} \vee \neg \lambda_{a2}$	$\begin{array}{c} \lambda_{b1} \wedge \lambda_{e1} \wedge \rho_{a1 b1,e1} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{e2} \wedge \rho_{a1 b1,e2} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{e3} \wedge \rho_{a1 b1,e3} \Rightarrow \lambda_{a1} \\ \lambda_{b2} \wedge \lambda_{e1} \wedge \rho_{a1 b2,e1} \Rightarrow \lambda_{a1} \\ \lambda_{b2} \wedge \lambda_{e2} \wedge \rho_{a1 b2,e2} \Rightarrow \lambda_{a1} \\ \lambda_{b2} \wedge \lambda_{e3} \wedge \rho_{a1 b2,e3} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{e3} \wedge \rho_{a1 b2,e3} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{e1} \wedge \neg \rho_{a1 b1,e1} \Rightarrow \lambda_{a2} \\ \lambda_{b1} \wedge \lambda_{e2} \wedge \neg \rho_{a1 b1,e2} \Rightarrow \lambda_{a2} \\ \lambda_{b1} \wedge \lambda_{e3} \wedge \neg \rho_{a1 b1,e3} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{e1} \wedge \neg \rho_{a1 b2,e1} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{e2} \wedge \neg \rho_{a1 b2,e2} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{e3} \wedge \neg \rho_{a1 b2,e3} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{e3} \wedge \neg \rho_{a1 b2,e3} \Rightarrow \lambda_{a2} \\ \end{array}$
J	$\lambda_{j1} \vee \lambda_{j2} \\ \neg \lambda_{j1} \vee \neg \lambda_{j2}$	$\lambda_{a1} \wedge \rho_{j1 a1} \Rightarrow \lambda_{j1}$ $\lambda_{a2} \wedge \rho_{j1 a2} \Rightarrow \lambda_{j1}$ $\lambda_{a1} \wedge \neg \rho_{j1 a1} \Rightarrow \lambda_{j2}$ $\lambda_{a2} \wedge \neg \rho_{j1 a2} \Rightarrow \lambda_{j2}$
М	$\lambda_{m1} \vee \lambda_{m2} \\ \neg \lambda_{m1} \vee \neg \lambda_{m2}$	$\lambda_{a1} \wedge \rho_{m1 a1} \Rightarrow \lambda_{m1}$ $\lambda_{a2} \wedge \rho_{m1 a2} \Rightarrow \lambda_{m1}$ $\lambda_{a1} \wedge \neg \rho_{m1 a1} \Rightarrow \lambda_{m2}$ $\lambda_{a2} \wedge \neg \rho_{m1 a2} \Rightarrow \lambda_{m2}$

Table VII. WEIGHTS ASSOCIATION USING ENC2

Weights	Value
$W(\rho_{b1})$	0.7
$W(\neg \rho_{b1})$	0.3
$W(\rho_{e1})$	0.01
$W(\rho_{e2})$	0.19
$W(\neg \rho_{e1})$	1-0.01 = 0.99
$W(\neg \rho_{e2})$	1-0.19 = 0.81
$W(\rho_{a1 b1,e1})$	0.90
$\mathrm{W}(\neg \rho_{a1 b1,e1})$	1-0.90=0.10
$W(\rho_{a1 b1,e2})$	0.85
$W(\neg \rho_{a1 b1,e2})$	1-0.85=0.15
$W(\rho_{a1 b1,e3})$	0.80
$W(\neg \rho_{a1 b1,e3})$	1-0.80=0.20
$W(\rho_{a1 b2,e1})$	0.30
$W(\neg \rho_{a1 b2,e1})$	1-0.30=0.70
$W(\rho_{a1 b2,e2})$	0.10
$\mathrm{W}(\neg \rho_{a1 b2,e2})$	1-0-10=0.90
$W(\rho_{a1 b2,e3})$	0
$W(\neg \rho_{a1 b2,e3})$	1-0=1
$W(\rho_{j1 a1})$	0.80
$W(\neg \rho_{j1 a1})$	1-0.80=0.20
$W(\rho_{j1 a2})$	0.10
$W(\neg \rho_{j1 a2})$	1-0.10=0.90
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