1

Inference for SRL Report

Capita Selecta AI (Probabilistic Programming) 2016-2017

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I. Probabilistic Inference Using Weighted Model Counting

A. PGM to CNF

Not sure if the 6th clause of the network variable A in IV is correctly substituted due to the property describe in the paper "Consider again Figure 1 and imagine that the parameter $\theta c1|a1$ were 0. Given that this parameter is known to be 0, all models that set this parameter variable to true will have weight 0."

For VII, should we also chance the closure that contains a probability of 0, like we did in the ENC1 encoding? Look comment above

Tables I and II show the logical variables used for encoded the Bayesian Network in [1].

Tables III and IV represent the encoded Bayesian Network using ENC1 and table V contains the corresponding weights.

Likewise, tables VI and VII represent the encoded Bayesian Network using ENC2 and table VIII contains the corresponding weights.

REFERENCES

[1] Bayesian networks.

Table I. LOGICAL VARIABLES USING ENC1

Network variables	Indicator Variable	CTP
В	$\lambda_{b1}, \lambda_{b2}$	θ_{b1},θ_{b2}
Е	$\lambda_{e1}, \lambda_{e2}, \lambda_3$	$\theta_{e1},\theta_{e2},\theta_3$
A	$\lambda_{a1},\lambda_{a2}$	$\begin{array}{l} \theta_{a1 b1,e1}, \theta_{a1 b1,e2}, \theta_{a1 b1,e3}, \\ \theta_{a1 b2,e1}, \theta_{a1 b2,e2}, \theta_{a1 b2,e3}, \\ \theta_{a2 b1,e1}, \theta_{a2 b1,e2}, \theta_{a2 b1,e3}, \\ \theta_{a2 b2,e1}, \theta_{a2 b2,e2}, \theta_{a2 b2,e3} \end{array}$
J	$\lambda_{j1}, \lambda_{j2}$	$\theta_{j1 a1}, \theta_{j2 a1}, \theta_{j1 a2}, \theta_{j2 a2}$
M	$\lambda_{m1}, \lambda_{m2}$	$\theta_{m1 a1}, \theta_{m2 a1}, \theta_{m1 a2}, \theta_{m2 a2}$

Table II. INDICATOR VARIABLES USING ENC2

Variables	Indicator Variable	CTP
В	$\lambda_{b1}, \lambda_{b2}$	ρ_{b1}
Е	$\lambda_{e1}, \lambda_{e2}, \lambda_3$	$ ho_{e1}, ho_{e2}$
A	$\lambda_{a1}, \lambda_{a2}$	$\rho_{a1 b1,c1}, \rho_{a1 b1,c2}, \rho_{a1 b1,c3}, \\ \rho_{a1 b2,c1}, \rho_{a1 b2,c2}, \rho_{a1 b2,c3}$
J	$\lambda_{j1}, \lambda_{j2}$	$ ho_{j1 a1}, ho_{j1 a2}$
M	$\lambda_{m1}, \lambda_{m2}$	$\rho_{m1 a1}, \rho_{m1 a2}$

Table III. CNF representation of Δ using ENC1

Variables		CNF
В	$\begin{array}{c} \lambda_{b1} \vee \lambda_{b2} \\ \neg \lambda_{b1} \vee \neg \lambda_{b2} \end{array}$	$ \lambda_{b1} \Leftrightarrow \theta_{b1} \\ \lambda_{b2} \Leftrightarrow \theta_{b2} $
Е	$\lambda_{e1} \lor \lambda_{e2} \lor \lambda_{e3}$ $\neg \lambda_{e1} \lor \neg \lambda_{e2}$ $\neg \lambda_{e1} \lor \neg \lambda_{e3}$ $\neg \lambda_{e2} \lor \neg \lambda_{e3}$	$\lambda_{e1} \Leftrightarrow \theta_{e1}$ $\lambda_{e2} \Leftrightarrow \theta_{e2}$ $\lambda_{e3} \Leftrightarrow \theta_{e3}$
A	$\lambda_{a1} \vee \lambda_{a2}$ $\neg \lambda_{a1} \vee \neg \lambda_{a2}$	$\begin{array}{c} \lambda_{a1} \wedge \lambda_{b1} \wedge \lambda_{e1} \Leftrightarrow \theta_{a1 b1,e1} \\ \lambda_{a1} \wedge \lambda_{b1} \wedge \lambda_{e2} \Leftrightarrow \theta_{a1 b1,e2} \\ \lambda_{a1} \wedge \lambda_{b1} \wedge \lambda_{e3} \Leftrightarrow \theta_{a1 b1,e3} \\ \lambda_{a1} \wedge \lambda_{b2} \wedge \lambda_{e1} \Leftrightarrow \theta_{a1 b2,e1} \\ \lambda_{a1} \wedge \lambda_{b2} \wedge \lambda_{e2} \Leftrightarrow \theta_{a1 b2,e2} \\ \lambda_{a1} \wedge \lambda_{b2} \wedge \lambda_{e3} \Leftrightarrow \theta_{a1 b2,e3} \\ \lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e1} \Leftrightarrow \theta_{a1 b1,e1} \\ \lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e2} \Leftrightarrow \theta_{a1 b1,e2} \\ \lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e3} \Leftrightarrow \theta_{a1 b1,e2} \\ \lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e3} \Leftrightarrow \theta_{a1 b1,e3} \\ \lambda_{a2} \wedge \lambda_{b2} \wedge \lambda_{e1} \Leftrightarrow \theta_{a1 b2,e1} \\ \lambda_{a2} \wedge \lambda_{b2} \wedge \lambda_{e2} \Leftrightarrow \theta_{a1 b2,e2} \\ \lambda_{a2} \wedge \lambda_{b2} \wedge \lambda_{e3} \Leftrightarrow \theta_{a1 b2,e2} \\ \lambda_{a2} \wedge \lambda_{b2} \wedge \lambda_{e3} \Leftrightarrow \theta_{a1 b2,e3} \end{array}$
J	$\lambda_{j1} \vee \lambda_{j2} \\ \neg \lambda_{j1} \vee \neg \lambda_{j2}$	$\lambda_{j1} \wedge \lambda_{a1} \Leftrightarrow \theta_{j1 a1}$ $\lambda_{j1} \wedge \lambda_{a2} \Leftrightarrow \theta_{j1 a2}$ $\lambda_{j2} \wedge \lambda_{a1} \Leftrightarrow \theta_{j2 a1}$ $\lambda_{j2} \wedge \lambda_{a2} \Leftrightarrow \theta_{j2 a2}$
М	$\lambda_{m1} \vee \lambda_{m2}$ $\neg \lambda_{m1} \vee \neg \lambda_{m2}$	$\lambda_{m1} \wedge \lambda_{a1} \Leftrightarrow \theta_{m1 a1}$ $\lambda_{m1} \wedge \lambda_{a2} \Leftrightarrow \theta_{m1 a2}$ $\lambda_{m2} \wedge \lambda_{a1} \Leftrightarrow \theta_{m2 a1}$ $\lambda_{m2} \wedge \lambda_{a2} \Leftrightarrow \theta_{m2 a2}$

Table IV. BAYESIAN NETWORK ENCODED USING ENC1

Network variable	Indicator Clauses	ENC1 Parameter Clauses
В	$\lambda_{b1} \vee \lambda_{b2}$,	$\lambda_{b1} \Rightarrow \theta_{b1}, \theta_{b1} \Rightarrow \lambda_{b1}$
	$\neg \lambda_{b1} \lor \neg \lambda_{b2}$	$\lambda_{b2} \Rightarrow \theta_{b2}, \theta_{b2} \Rightarrow \lambda_{b2}$
	$\lambda_{e1} \vee \lambda_{e2} \vee \lambda_{e3}$,	$\lambda_{e1}\Rightarrow heta_{e1}, heta_{e1}\Rightarrow\lambda_{e1}$
E	$\neg \lambda_{e1} \lor \neg \lambda_{e2}$,	$\lambda_{e2} \Rightarrow \theta_{e2}, \theta_{e2} \Rightarrow \lambda_{e2}$
	$\neg \lambda_{e1} \lor \neg \lambda_{e3},$	$\lambda_{e3} \Rightarrow \theta_{e3}, \theta_{e3} \Rightarrow \lambda_{e3}$
	$\neg \lambda_{e2} \lor \neg \lambda_{e3}$	
		$\lambda_{a1} \wedge \lambda_{b1} \wedge \lambda_{e1} \Rightarrow \theta_{a1 b1,e1}, \theta_{a1 b1,e1} \Rightarrow \lambda_{a1}, \theta_{a1 b1,e1} \Rightarrow \lambda_{b1}, \theta_{a1 b1,e1} \Rightarrow \lambda_{e1}$
		$\lambda_{a1} \wedge \lambda_{b1} \wedge \lambda_{e2} \Rightarrow \theta_{a1 b1,e2}, \theta_{a1 b1,e2} \Rightarrow \lambda_{a1}, \theta_{a1 b1,e2} \Rightarrow \lambda_{b1}, \theta_{a1 b1,e2} \Rightarrow \lambda_{e2}$
	$\lambda_{a1} \vee \lambda_{a2}, \\ \neg \lambda_{a1} \vee \neg \lambda_{a2}$	$\lambda_{a1} \wedge \lambda_{b1} \wedge \lambda_{e3} \Rightarrow \theta_{a1 b1,e3}, \theta_{a1 b1,e3} \Rightarrow \lambda_{a1}, \theta_{a1 b1,e3} \Rightarrow \lambda_{b1}, \theta_{a1 b1,e3} \Rightarrow \lambda_{e3}$
		$\lambda_{a1} \wedge \lambda_{b2} \wedge \lambda_{e1}, \Rightarrow \theta_{a1 b2,e1}, \theta_{a1 b2,e1} \Rightarrow \lambda_{a1}, \theta_{a1 b2,e1} \Rightarrow \lambda_{b2}, \theta_{a1 b2,e1} \Rightarrow \lambda_{e1}$
		$\lambda_{a1} \wedge \lambda_{b2} \wedge \lambda_{e2}, \Rightarrow \theta_{a1 b2,e2}, \theta_{a1 b2,e2} \Rightarrow \lambda_{a1}, \theta_{a1 b2,e2} \Rightarrow \lambda_{b2}, \theta_{a1 b2,e2} \Rightarrow \lambda_{e2}$ $\neg \lambda_{a1} \vee \neg \lambda_{b2} \vee \neg \lambda_{c3}$
A		$\lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e1}, \Rightarrow \theta_{a2 b1,e1}, \theta_{a2 b1,e1} \Rightarrow \lambda_{a2}, \theta_{a2 b1,e1} \Rightarrow \lambda_{b1}, \theta_{a2 b1,e1} \Rightarrow \lambda_{e1}$
		$\lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e2}, \Rightarrow \theta_{a2 b1,e1}, \lambda_{a2 b1,e1} \rightarrow \lambda_{a2}, \lambda_{a2 b1,e1} \rightarrow \lambda_{b1}, \lambda_{a2 b1,e1} \rightarrow \lambda_{e1}$ $\lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e2}, \Rightarrow \theta_{a2 b1,e2}, \theta_{a2 b1,e2} \Rightarrow \lambda_{a2}, \theta_{a2 b1,e2} \Rightarrow \lambda_{b1}, \theta_{a2 b1,e2} \Rightarrow \lambda_{e2}$
		$\lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e2}, \Rightarrow \lambda_{a2 b1,e2}, \lambda_{a2 b1,e2} \rightarrow \lambda_{a2}, \lambda_{a2 b1,e2} \rightarrow \lambda_{b1}, \lambda_{a2 b1,e2} \rightarrow \lambda_{e2}$ $\lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e3}, \Rightarrow \theta_{a2 b1,e3}, \theta_{a2 b1,e3} \Rightarrow \lambda_{a2}, \theta_{a2 b1,e3} \Rightarrow \lambda_{b1}, \theta_{a2 b1,e3} \Rightarrow \lambda_{e3}$
		$\lambda_{a2} \wedge \lambda_{b1} \wedge \lambda_{e3}, \Rightarrow \lambda_{a2 b1,e3}, \forall_{a2 b1,e3}, \forall_{a2 b1,e3}, \Rightarrow \lambda_{a2}, \forall_{a2 b1,e3}, \Rightarrow \lambda_{e3}, \forall_{a2 b1,e3}, \Rightarrow \lambda_{e3}, \forall_{a2 b1,e3}, \Rightarrow \lambda_{e3}, \forall_{a2 b1,e3}, \Rightarrow \lambda_{e3}, \forall_{a3 b1,e3}, \Rightarrow \lambda_{e3 b1,e3 b1,e3}, \Rightarrow \lambda_{e3 b1,e3 b1,e$
		$\lambda_{a2} \wedge \lambda_{b2} \wedge \lambda_{e1}, \Rightarrow \lambda_{a2 b2,e1}, \lambda_{a2 b2,e1} \rightarrow \lambda_{a2}, \lambda_{a2 b2,e1} \rightarrow \lambda_{b2}, \lambda_{a2 b2,e1} \rightarrow \lambda_{e1}, \lambda_{a2 b2,e2} \rightarrow \lambda_{a2 b2,e2} $
		$\begin{array}{c} \lambda_{a2} \wedge \lambda_{b2} \wedge \lambda_{e2}, \Rightarrow \lambda_{a2 b2,e2}, \forall_{a2 b2,e2}, \forall_{a2 b2,e2} \rightarrow \lambda_{a2}, \forall_{a2 b2,e2} \rightarrow \lambda_{e2}, \forall_{a2 b2,e2} \rightarrow \lambda_{e2} \\ \lambda_{a2} \wedge \lambda_{b2} \wedge \lambda_{e3}, \Rightarrow \theta_{a2 b2,e3}, \theta_{a2 b2,e3} \Rightarrow \lambda_{a2}, \theta_{a2 b2,e3} \Rightarrow \lambda_{b2}, \theta_{a2 b2,e3} \Rightarrow \lambda_{e3} \end{array}$
		$\lambda_{j1} \wedge \lambda_{a1} \Rightarrow \theta_{j1 a1}, \theta_{j1 a1} \Rightarrow \lambda_{j1}, \theta_{j1 a1} \Rightarrow \lambda_{a1}$
J	$\lambda \cdot 1 \vee \lambda \cdot 0$	$\lambda_{j1} \wedge \lambda_{a2} \Rightarrow \theta_{j1 a2}, \theta_{j1 a2} \Rightarrow \lambda_{j1}, \theta_{j1 a2} \Rightarrow \lambda_{a2}$
	$\lambda_{j1} \vee \lambda_{j2}, \\ \neg \lambda_{j1} \vee \neg \lambda_{j2}$	$\lambda_{j1} \wedge \lambda_{a1} \Rightarrow \theta_{j2 a1}, \theta_{j2 a1} \Rightarrow \lambda_{j2}, \theta_{j2 a1} \Rightarrow \lambda_{a1}$ $\lambda_{j2} \wedge \lambda_{a1} \Rightarrow \theta_{j2 a1}, \theta_{j2 a1} \Rightarrow \lambda_{j2}, \theta_{j2 a1} \Rightarrow \lambda_{a1}$
		$\lambda_{j2} \wedge \lambda_{a2} \Rightarrow \theta_{j2 a2}, \theta_{j2 a2} \Rightarrow \lambda_{j2}, \theta_{j2 a2} \Rightarrow \lambda_{a2}$
М	$\lambda_{m1} \vee \lambda_{m2}, \\ \neg \lambda_{m1} \vee \neg \lambda_{m2}$	$\lambda_{m1} \wedge \lambda_{a1} \Rightarrow \theta_{m1 a1}, \theta_{m1 a1} \Rightarrow \lambda_{m1}, \theta_{m1 a1} \Rightarrow \lambda_{a1}$
		$\lambda_{m1} \wedge \lambda_{a2} \Rightarrow \theta_{m1 a2}, \theta_{m1 a2} \Rightarrow \lambda_{m1}, \theta_{m1 a2} \Rightarrow \lambda_{a2}$
		$\lambda_{m2} \wedge \lambda_{a1} \Rightarrow \theta_{m2 a1}, \theta_{m2 a1} \Rightarrow \lambda_{m2}, \theta_{m2 a1} \Rightarrow \lambda_{a1}$
		$\lambda_{m2} \wedge \lambda_{a2} \Rightarrow \theta_{m2 a2}, \theta_{m2 a2} \Rightarrow \lambda_{m2}, \theta_{m2 a2} \Rightarrow \lambda_{a2}$
	I .	$m_2 = m_2 + m_2 $

Table V. Weights association using ENC1 where missing weights are set to one

Weights	Value
$W(\theta_{b1})$	0.7
$W(\theta_{b2})$	0.3
$W(\theta_{e1})$	0.01
$W(\theta_{e2})$	0.19
$W(\theta_{e3})$	0.80
$\mathrm{W}(\theta_{a1 b1,e1})$	0.90
$W(\theta_{a1 b1,e2})$	0.85
$W(\theta_{a1 b1,e3})$	0.80
$W(\theta_{a1 b2,e1})$	0.30
$W(\theta_{a1 b2,e2})$	0.10
$\mathrm{W}(\theta_{a1 b2,e3})$	0
$W(\theta_{a2 b1,e1})$	0.10
$\mathrm{W}(\theta_{a2 b1,e2})$	0.15
$\mathrm{W}(\theta_{a2 b1,e3})$	0.20
$\mathrm{W}(\theta_{a2 b2,e1})$	0.70
$\mathrm{W}(\theta_{a2 b2,e2})$	0.90
$W(\theta_{j1 a1})$	0.80
$W(\theta_{j1 a2}^{j1 a2})$	0.10
$W(\theta_{j2 a1})$	0.20
$W(\theta_{j2 a2})$	0.90
$W(\theta_{m1 a1})$	0.80
$W(\theta_{m1 a2})$	0.10
$W(\theta_{m2 a1})$	0.20
$W(\theta_{m2 a2})$	0.90
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Table VI. CNF representation of Δ using ENC2

Variables		CNF
В	$\begin{array}{c} \lambda_{b1} \vee \lambda_{b2} \\ \neg \lambda_{b1} \vee \neg \lambda_{b2} \end{array}$	$ \rho_{b1} \Rightarrow \lambda_{b1} \neg \rho_{b1} \Rightarrow \lambda_{b2} $
E	$\lambda_{e1} \lor \lambda_{e2} \lor \lambda_{e3}$ $\neg \lambda_{e1} \lor \neg \lambda_{e2}$ $\neg \lambda_{e1} \lor \neg \lambda_{e3}$ $\neg \lambda_{e2} \lor \neg \lambda_{e3}$	$ \rho_{e1} \Rightarrow \lambda_{e1} \neg \rho_{e1} \land \rho_{e2} \Rightarrow \lambda_{e2} \neg \rho_{e1} \land \neg \rho_{e2} \Rightarrow \lambda_{e3} $
A	$\lambda_{a1} \lor \lambda_{a2}$ $\neg \lambda_{a1} \lor \neg \lambda_{a2}$	$\begin{array}{c} \lambda_{b1} \wedge \lambda_{c1} \wedge \rho_{a1 b1,c1} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{c2} \wedge \rho_{a1 b1,c2} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{c3} \wedge \rho_{a1 b1,c3} \Rightarrow \lambda_{a1} \\ \lambda_{b2} \wedge \lambda_{c1} \wedge \rho_{a1 b2,c1} \Rightarrow \lambda_{a1} \\ \lambda_{b2} \wedge \lambda_{c2} \wedge \rho_{a1 b2,c2} \Rightarrow \lambda_{a1} \\ \lambda_{b2} \wedge \lambda_{c3} \wedge \rho_{a1 b2,c3} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{c3} \wedge \rho_{a1 b2,c3} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{c1} \wedge \neg \rho_{a1 b1,c1} \Rightarrow \lambda_{a2} \\ \lambda_{b1} \wedge \lambda_{c2} \wedge \neg \rho_{a1 b1,c2} \Rightarrow \lambda_{a2} \\ \lambda_{b1} \wedge \lambda_{c3} \wedge \neg \rho_{a1 b1,c3} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{c1} \wedge \neg \rho_{a1 b2,c1} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{c3} \wedge \neg \rho_{a1 b2,c2} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{c3} \wedge \neg \rho_{a1 b2,c3} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{c3} \wedge \neg \rho_{a1 b2,c3} \Rightarrow \lambda_{a2} \\ \end{array}$
J	$\begin{array}{c} \lambda_{j1} \vee \lambda_{j2} \\ \neg \lambda_{j1} \vee \neg \lambda_{j2} \end{array}$	$\lambda_{a1} \wedge \rho_{j1 a1} \Rightarrow \lambda_{j1}$ $\lambda_{a2} \wedge \rho_{j1 a2} \Rightarrow \lambda_{j1}$ $\lambda_{a1} \wedge \neg \rho_{j1 a1} \Rightarrow \lambda_{j2}$ $\lambda_{a2} \wedge \neg \rho_{j1 a2} \Rightarrow \lambda_{j2}$
М	$\lambda_{m1} \vee \lambda_{m2} \\ \neg \lambda_{m1} \vee \neg \lambda_{m2}$	$\lambda_{a1} \wedge \rho_{m1 a1} \Rightarrow \lambda_{m1}$ $\lambda_{a2} \wedge \rho_{m1 a2} \Rightarrow \lambda_{m1}$ $\lambda_{a1} \wedge \neg \rho_{m1 a1} \Rightarrow \lambda_{m2}$ $\lambda_{a2} \wedge \neg \rho_{m1 a2} \Rightarrow \lambda_{m2}$

Table VII. BAYESIAN NETWORK ENCODED USING ENC2

Network variable	Indicator Clauses	ENC1 Parameter Clauses
	$\lambda_{b1} \vee \lambda_{b2}$,	$\rho_{b1} \Rightarrow \lambda_{b1}$
В	$\neg \lambda_{b1} \lor \neg \lambda_{b2}$	$\neg \rho_{b1} \Rightarrow \lambda_{b2}$
E	$\lambda_{e1} \lor \lambda_{e2} \lor \lambda_{e3},$ $\neg \lambda_{e1} \lor \neg \lambda_{e2},$ $\neg \lambda_{e1} \lor \neg \lambda_{e3},$ $\neg \lambda_{e2} \lor \neg \lambda_{e3}$	$\rho_{e1} \Rightarrow \lambda_{e1}$ $\neg \rho_{e1} \wedge \rho_{e2} \Rightarrow \lambda_{e2}$ $\neg \rho_{e1} \wedge \neg \rho_{e2} \Rightarrow \lambda_{e3}$
A	$\lambda_{a1} \vee \lambda_{a2}, \\ \neg \lambda_{a1} \vee \neg \lambda_{a2}$	$\begin{array}{c} \lambda_{b1} \wedge \lambda_{e1} \wedge \rho_{a1 b1,e1} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{e2} \wedge \rho_{a1 b1,e2} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{e3} \wedge \rho_{a1 b1,e3} \Rightarrow \lambda_{a1} \\ \lambda_{b2} \wedge \lambda_{e1} \wedge \rho_{a1 b2,e1} \Rightarrow \lambda_{a1} \\ \lambda_{b2} \wedge \lambda_{e2} \wedge \rho_{a1 b2,e2} \Rightarrow \lambda_{a1} \\ \lambda_{b2} \wedge \lambda_{e3} \wedge \rho_{a1 b2,e3} \Rightarrow \lambda_{a1} \\ \lambda_{b1} \wedge \lambda_{e1} \wedge \neg \rho_{a1 b1,e1} \Rightarrow \lambda_{a2} \\ \lambda_{b1} \wedge \lambda_{e2} \wedge \neg \rho_{a1 b1,e2} \Rightarrow \lambda_{a2} \\ \lambda_{b1} \wedge \lambda_{e3} \wedge \neg \rho_{a1 b1,e3} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{e1} \wedge \neg \rho_{a1 b2,e1} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{e1} \wedge \neg \rho_{a1 b2,e1} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{e2} \wedge \neg \rho_{a1 b2,e2} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{e3} \wedge \neg \rho_{a1 b2,e2} \Rightarrow \lambda_{a2} \\ \lambda_{b2} \wedge \lambda_{e3} \wedge \neg \rho_{a1 b2,e3} \Rightarrow \lambda_{a2} \end{array}$
J	$\lambda_{j1} \vee \lambda_{j2}, \\ \neg \lambda_{j1} \vee \neg \lambda_{j2}$	$\lambda_{a1} \wedge \rho_{j1 a1} \Rightarrow \lambda_{j1}$ $\lambda_{a2} \wedge \rho_{j1 a2} \Rightarrow \lambda_{j1}$ $\lambda_{a1} \wedge \neg \rho_{j1 a1} \Rightarrow \lambda_{j2}$ $\lambda_{a2} \wedge \neg \rho_{j1 a2} \Rightarrow \lambda_{j2}$
М	$\lambda_{m1} \vee \lambda_{m2}, \\ \neg \lambda_{m1} \vee \neg \lambda_{m2}$	$\lambda_{a1} \wedge \rho_{m1 a1} \Rightarrow \lambda_{m1}$ $\lambda_{a2} \wedge \rho_{m1 a2} \Rightarrow \lambda_{m1}$ $\lambda_{a1} \wedge \neg \rho_{m1 a1} \Rightarrow \lambda_{m2}$ $\lambda_{a2} \wedge \neg \rho_{m1 a2} \Rightarrow \lambda_{m2}$

Table VIII. Weights association using ENC2 where missing weights are set to one

Weights	Value
$W(\rho_{b1})$	0.7
$W(\neg \rho_{b1})$	0.3
$W(\rho_{e1})$	0.01
$W(\rho_{e2})$	0.19/(1-0.01) = 0.19
$W(\neg \rho_{e1})$	1-0.01 = 0.99
$W(\neg \rho_{e2})$	1-0.01 = 0.81
$W(\rho_{a1 b1,e1})$	0.90
$W(\neg \rho_{a1 b1,e1})$	1-0.90=0.10
$W(\rho_{a1 b1,e2})$	0.85
$W(\neg \rho_{a1 b1,e2})$	1-0.85=0.15
$W(\rho_{a1 b1,e3})$	0.80
$W(\neg \rho_{a1 b1,e3})$	1-0.80=0.20
$W(\rho_{a1 b2,e1})$	0.30
$W(\neg \rho_{a1 b2,e1})$	1-0.30=0.70
$W(\rho_{a1 b2,e2})$	0.10
$W(\neg \rho_{a1 b2,e2})$	1-0-10=0.90
$W(\rho_{a1 b2,e3})$	0
$W(\neg \rho_{a1 b2,e3})$	1-0=1
$W(\rho_{j1 a1})$	0.80
$W(\neg \rho_{j1 a1})$	1-0.80=0.20
$W(\rho_{j1 a2})$	0.10
$W(\neg \rho_{j1 a2})$	1-0.10=0.90
$P_{j1 a2}$	1 0.10 0.90