# Politics Are Afoot!

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# The Setup

There is a lot of money that is spent in politics in Presidential election years. So far, estimates have the number at about \$11,000,000,000 (11 billion USD). For context, in 2019 Twitter's annual revenue was about \$3,500,000,000 (3.5 billion USD).

### The work

Install the package, fec16.

```
## install.packages('fec16')
```

This package is a compendium of spending and results from the 2016 election cycle. In this dataset are 9 different datasets that cover:

- candidates: candidate attributes, like their name, a unique id of the candidate, the election year under consideration, the office they're running for, etc.
- results\_house: race attributes, like the name of the candidates running in the election, a unique id of the candidate, the number of general\_votes garnered by each candidate, and other information.
- campaigns: financial information for each house & senate campaign. This includes a unique candidate id, the total receipts (how much came in the doors), and total disbursements (the total spent by the campaign), the total contributed by party central committees, and other information.

# Your task

Describe the relationship between spending on a candidate's behalf and the votes they receive.

## Your work

- We want to keep this work relatively constrained, which is why we're providing you with data through
  the fec16 package. It is possible to gather all the information from current FEC reports, but it would
  require you to make a series of API calls that would pull us away from the core modeling tasks that
  we want you to focus on instead.
- Throughout this assignment, limit yourself to functions that are within the tidyverse family of packages: dplyr, ggplot, patchwork, and magrittr for wrangling and exploration and base, stats, sandwich and lmtest for modeling and testing. You do not have to use these packages; but try to limit yourself to using only these.

## 1. What does the distribution of votes and of spending look like?

1. (3 points) In separate histograms, show both the distribution of votes (measured in results\_house\$general\_percent for now) and spending (measured in ttl\_disb). Use a log transform if appropriate for each visualization. How would you describe what you see in these two plots?

### **ANSWER:**

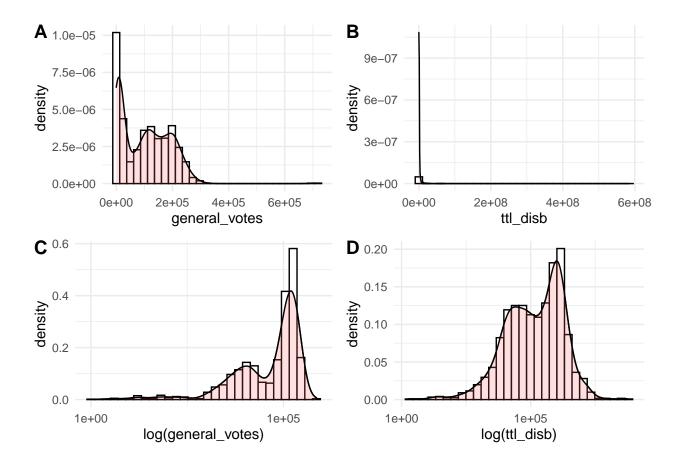
From my observation, the data general\_percent and ttl\_disb have the following problems:

- The original data of the 2 variables are not on the same scale (Fig. A-B) .
- Has skewness problems because the curve appears distorted and skewed to the left in a statistical distribution.
- The data are not centered.

At this stage, based on my finding, we need to perform data transforming including scaling, centering and skewness corrections.

I will perform Log transformation first, because log transform makes the data as "normal" as possible so that the statistical analysis results from this data become more valid, the log transformation reduces or removes the skewness of our original data. In detail I choose natural logarithm here for the purposes of linear modeling, i.e., using Log transformation replaces each variable x with a log(x). The results are shown in Fig. C-D, repectivelay. In C and D, after the transfermation, the vurves approximately follows normal distribution, the graph appears symmetry, there are about as many data values on the left side of the median as on the right side.

I will do other data transformations later in the following questions. Data transformation can make our model working efficiently: distance based models perform well when data is pre-processed and transformed; having all features scaled it speeds up the model; better accuracy and more generalized model.



# 2. Exploring the relationship between spending and votes.

2. (3 points) Create a new dataframe by joining results\_house and campaigns using the inner\_join function from dplyr. (We use the format package::function - so dplyr::inner\_join.)

#### ANSWER:

##

##

##

##

##

## ##

##

##

##

Max.

NA's

3rd Qu.:0.5376

footnotes

Length: 1342

:0.6573

:1330

Class :character

Mode :character

Done the creation of new dataframe by joining results\_house and campaigns using the inner\_join function from dplyr. The new data frame is named "d1". A discription of "d1" is as the follows:

```
d1 <- dplyr::inner_join(results_house, campaigns, by = NULL)</pre>
## Joining, by = "cand_id"
nrow(d1)
## [1] 1342
summary(d1)
##
                        district_id
                                              {\tt cand\_id}
                                                                 incumbent
       state
##
    Length: 1342
                        Length: 1342
                                            Length: 1342
                                                                 Mode :logical
##
    Class : character
                        Class : character
                                            Class : character
                                                                 FALSE:895
                        Mode :character
                                            Mode :character
                                                                 TRUE: 447
##
    Mode :character
##
##
##
##
##
                        primary_votes
                                          primary_percent
                                                              runoff_votes
       party
    Length: 1342
                                          Min.
                                                  :0.00015
                                                                     : 1096
##
                        Min.
                              :
                                                             Min.
##
    Class :character
                        1st Qu.: 8650
                                          1st Qu.:0.19158
                                                             1st Qu.: 1464
    Mode :character
                        Median : 21299
                                          Median :0.42257
                                                             Median: 8206
##
                               : 32227
                                                  :0.48844
                                                                     :11274
                        Mean
                                          Mean
                                                             Mean
##
                        3rd Qu.: 45638
                                          3rd Qu.:0.78382
                                                             3rd Qu.:20082
##
                        Max.
                               :326988
                                          Max.
                                                  :1.00000
                                                                     :25322
                                                             Max.
##
                        NA's
                               :291
                                          NA's
                                                  :292
                                                             NA's
                                                                     :1330
##
    runoff_percent
                      general_votes
                                        general_percent
                                                             won
##
    Min.
           :0.3427
                      Min.
                                   55
                                        Min.
                                                :0.0000
                                                          Mode :logical
##
    1st Qu.:0.4624
                      1st Qu.: 88229
                                        1st Qu.:0.3087
                                                          FALSE:850
##
   Median :0.5000
                      Median :142597
                                        Median :0.4773
                                                          TRUE: 492
##
    Mean
           :0.5000
                      Mean
                             :136932
                                        Mean
                                                :0.4597
```

3rd Qu.:0.6406

:1.0000

:463

 $cand_ici$ 

Class : character

Mode :character

Length: 1342

pty\_cd :1.000

1st Qu.:1.000

Median :2.000

3rd Qu.:2.000

:1.607

:3.000

Min.

Mean

Max.

Max.

NA's

3rd Qu.:198290

cand\_name

Length: 1342

:718591

Class :character

Mode :character

:462

Max.

NA's

```
cand_pty_affiliation ttl_receipts
                                         trans from auth
                                                              ttl disb
                                                            Min. :
##
   Length: 1342
                       Min. :
                                         Min. :
                                                        0
                                      0
                                                                          0
   Class : character
                       1st Qu.:
                                          1st Qu.:
##
                                  46612
                                                        0
                                                            1st Qu.:
                                                                      46147
  Mode :character
                       Median : 398962
                                         Median :
                                                            Median: 379570
##
                                                        0
                       Mean : 883177
##
                                         Mean :
                                                    26408
                                                            Mean : 814754
                                          3rd Qu.:
##
                       3rd Qu.: 1290266
                                                        0
                                                            3rd Qu.: 1154148
##
                       Max. :19852221
                                         Max. :12374657
                                                            Max. :13433669
##
##
   trans to auth
                       coh_bop
                                        coh_cop
                                                       cand contrib
##
   Min. :
                    Min. : -18681
                                     Min. : -32074
                                                      Min. :
                                                                    0
                0
   1st Qu.:
                    1st Qu.:
                                     1st Qu.:
                                                      1st Qu.:
                                                                    0
   Median :
                    Median :
                                     Median :
                                               3881
                                                      Median :
                                                                    0
##
                0
                                 0
   Mean : 7577
                    Mean : 150271
                                          : 218929
##
                                     Mean
                                                      Mean
                                                                 21879
   3rd Qu.:
                    3rd Qu.: 85884
                                     3rd Qu.: 170548
                                                      3rd Qu.:
                                                                 1000
##
                0
##
   Max. :766500
                    Max. :3750024
                                     Max.
                                           :9098873
                                                      Max.
                                                             :13414225
##
##
     cand_loans
                     other_loans
                                     cand_loan_repay
                                                      other_loan_repay
                                     Min. :
                                                      Min. :
##
   Min. :
                 0
                    Min. :
                                 0
                                                  0
##
   1st Qu.:
                 0
                    1st Qu.:
                                     1st Qu.:
                                                  0
                                                      1st Qu.:
                                                                   0.0
                                 0
                    Median :
                                     Median :
   Median :
                                                      Median :
##
                 0
                                 0
                                                  0
                                                                   0.0
##
   Mean
         : 56809
                    Mean : 1049
                                     Mean : 12579
                                                      Mean
                                                                 638.7
   3rd Qu.:
              9000
                     3rd Qu.:
                                 0
                                     3rd Qu.:
                                                  0
                                                      3rd Qu.:
                                                                   0.0
   Max. :8050000
                    Max. :350000
                                     Max. :1655854
                                                      Max. :350000.0
##
##
                    ttl_indiv_contrib cand_office_st
##
                                                        cand office district
   debts owed by
   Min. : -1786
                    Min. :
                                 0
                                      Length: 1342
                                                        Length: 1342
##
   1st Qu.:
                 0
                    1st Qu.: 21310
                                      Class :character
                                                        Class : character
   Median :
                 0
                    Median : 207337
                                      Mode :character
                                                        Mode :character
##
   Mean : 42528
                    Mean
                          : 464597
   3rd Qu.: 12903
                     3rd Qu.: 638629
   Max. :2795000
                    Max. :5975190
##
##
##
   other_pol_cmte_contrib pol_pty_contrib
                                           cvg_end_dt
                                                             indiv_refunds
   Min. :
                 0
                         Min. :
                                    0
                                         Min. :2015-08-10
                                                             Min. : -1150
##
   1st Qu.:
                         1st Qu.:
                                                             1st Qu.:
##
                 0
                                     0
                                         1st Qu.:2016-12-31
                                                                         0
##
   Median : 13700
                         Median:
                                     0
                                         Median :2016-12-31
                                                             Median :
                                                                       200
   Mean : 305670
                         Mean : 1230
                                         Mean :2016-11-30
                                                             Mean : 6617
##
   3rd Qu.: 506471
                         3rd Qu.: 150
                                         3rd Qu.:2016-12-31
                                                             3rd Qu.: 5400
   Max. :3279747
##
                         Max. :25400
                                         Max. :2017-01-31
                                                             Max. :227497
##
##
    cmte refunds
##
   Min. :
                0
##
   1st Qu.:
                0
##
   Median :
                0
   Mean : 1093
##
   3rd Qu.:
              250
##
   Max. :104758
##
```

3. (3 points) Produce a scatter plot of general\_votes on the y-axis and ttl\_disb on the x-axis. What do you observe about the shape of the joint distribution?

### ANSWER:

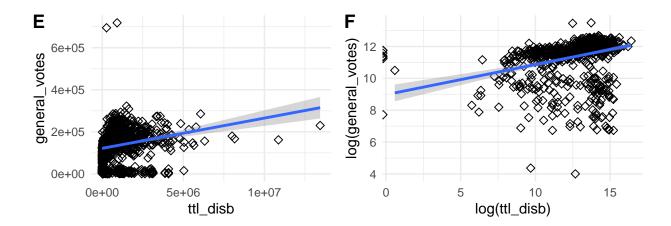
The scatter plot of general\_votes on the y-axis and  $ttl_disb$  on the x-axis is shown below Fig.E. I also made a scatter plot using  $y = \log(\text{general\_votes})$  and  $x = \log(\text{ttl\_disb})$ , as shown in Fig.F.

In general, a x-y scatter graph displays and compares values to show the numerical distribution of variables in a rectangular coordinate system. A two-dimensional scatter chart can show the data analysis of two variables to provide the relationship and correlation between the two. Scatter plots can provide three types of key information:

- Whether there is a quantitative correlation trend between variables;
- If there is a correlation trend, is it linear or non-linear;
- Observe whether there are outliers and analyze The influence of these outliers on the modeling analysis.

However, I couldn't find obvious correlation between variables since most of them look randomly distributed on the scatter plot. If there is a certain correlation, then most of the data points will be relatively dense and present in a certain trend, however I cannot figure it out it by simple observation.

By observing the distribution of data points on the scatter plot, I found there are some outliers.



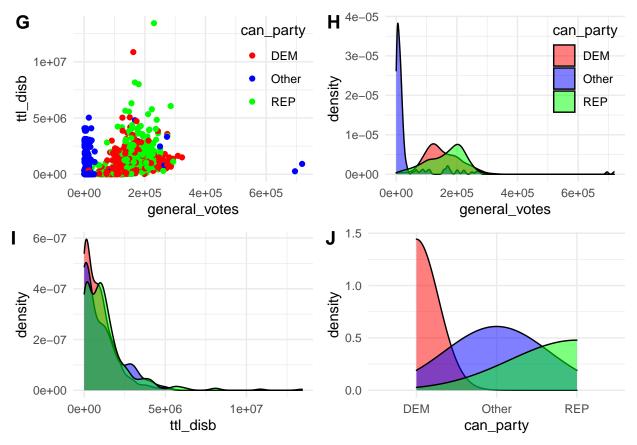
- 4. (3 points) Create a new variable to indicate whether each individual is a "Democrat", "Republican" or "Other Party".
- Here's an example of how you might use mutate and case\_when together to create a variable.

Once you've produced the new variable, plot your scatter plot again, but this time adding an argument into the aes() function that colors the points by party membership. What do you observe about the distribution of all three variables?

#### ANSWER:

The new variable has been produced, the new data frame is named "d2", a discription is as the follows:

```
##
     can_party
                       general_votes
                                           ttl_disb
##
   Length:880
                       Min.
                                   55
                             :
                                        Min.
                       1st Qu.: 88229
                                        1st Qu.: 102276
##
   Class : character
   Mode :character
                       Median :142597
                                        Median: 830659
##
                       Mean
                              :136932
                                              : 1084565
                                        Mean
                                        3rd Qu.: 1527533
                       3rd Qu.:198290
##
##
                       Max.
                              :718591
                                               :13433669
                                        Max.
```



From my observation in Fig H-J, the variable general\_percent,ttl\_disb and can\_party have the following properties:

- The distribution of each of the three variables (i.e. can\_party, ttl\_disp, general\_vote) are a combination of 3 different curves that are approximately following normal distributions.
- For each variable, the 3 curves in different color clustered by the 3 (i.e. DEM, REP, and Other) parties.
- Among the total 9 curves, each of the curves appears symmetry, there are about as many data values on the left side of the median as on the right side.
- Each of the curves has skewness problems because the curve appears distorted or skewed to the left or right in a statistical distribution.
- The data in each curve are not centered.

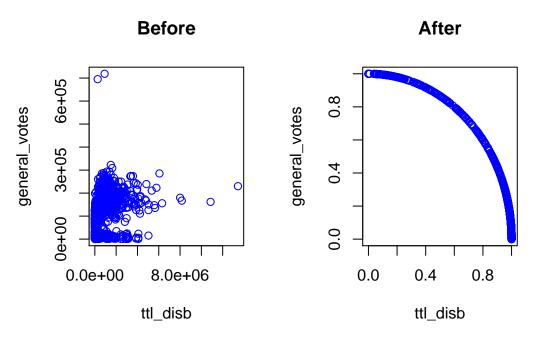
At this stage, based on my finding, the following decisions are made:

- A linear model can be created and fit the relationship between the general\_votes and ttl\_disb and can party.
- Detailed analysis and pre-processing need to be done to the data using maths.
- further data transformations have to be performed.

Next, I will do the data pre-processing and model creation.

# Produce a Descriptive Model

5. (5 Points) Given your observations, produce a linear model that you think does a good job at describing the relationship between candidate spending and votes they receive. You should decide what transformation to apply to spending (if any), what transformation to apply to votes (if any) and also how to include the party affiliation.



```
##
## Call:
## lm(formula = d2$general_votes ~ d2$ttl_disb + d2$can_party)
##
## Residuals:
##
       Min
                1Q
                    Median
                                3Q
                                       Max
##
  -162812
            -50839
                      -463
                             37128
                                    645725
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 1.634e+05
                            4.080e+03
                                       40.061 < 2e-16 ***
## d2$ttl disb
                 1.163e-02
                            1.864e-03
                                        6.238 6.88e-10 ***
## d2$can_party -5.062e+04
                            3.213e+03 -15.756
                                              < 2e-16 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 69240 on 877 degrees of freedom
## Multiple R-squared: 0.2602, Adjusted R-squared: 0.2585
## F-statistic: 154.2 on 2 and 877 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = d2$csvotes ~ d2$csdisb + d2$csparty)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
```

```
## -2.0249 -0.6323 -0.0058 0.4618 8.0309
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5.857e-16 2.903e-02
                                     0.000
                                      6.238 6.88e-10 ***
## d2$csdisb
              1.820e-01 2.917e-02
## d2$csparty -4.597e-01 2.917e-02 -15.756 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8611 on 877 degrees of freedom
## Multiple R-squared: 0.2602, Adjusted R-squared: 0.2585
## F-statistic: 154.2 on 2 and 877 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = d2$novotes ~ d2$nodisb + d2$noparty)
## Residuals:
##
       Min
                 1Q Median
                                   3Q
                                           Max
## -0.25036 -0.09079 -0.01375 0.08107 0.24505
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                1.25036
                           0.01271
                                     98.38
## (Intercept)
                                            <2e-16 ***
## d2$nodisb
               -1.09452
                           0.01426 - 76.76
                                             <2e-16 ***
## d2$noparty -80.80898
                          79.99695
                                    -1.01
                                              0.313
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.117 on 877 degrees of freedom
## Multiple R-squared: 0.8777, Adjusted R-squared: 0.8774
## F-statistic: 3146 on 2 and 877 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = d2$logvotes ~ d2$logdisb + d2$logparty)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -5.3555 -0.1927 0.0741 0.2940 4.1067
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 10.60108
                          0.16135 65.704 < 2e-16 ***
## d2$logdisb
              0.09767
                          0.01226
                                   7.968 5.01e-15 ***
## d2$logparty -3.57205
                          0.10352 -34.507 < 2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.809 on 877 degrees of freedom
## Multiple R-squared: 0.6044, Adjusted R-squared: 0.6035
## F-statistic: 669.9 on 2 and 877 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = d2$general_votes ~ d2$logdisb + d2$can_party)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -164084 -42521
                     2037
                            33117 627966
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                20183.4
                           13565.1
                                     1.488
## d2$logdisb
                11935.7
                             999.7 11.939
                                             <2e-16 ***
## d2$can_party -46716.3
                            3070.3 -15.215
                                             <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 65620 on 877 degrees of freedom
## Multiple R-squared: 0.3354, Adjusted R-squared: 0.3339
## F-statistic: 221.3 on 2 and 877 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = logvotes ~ logdisb + logparty)
## Residuals:
##
                               3Q
      Min
               1Q Median
                                      Max
## -5.3555 -0.1927 0.0741 0.2940 4.1067
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 10.60108
                          0.16135 65.704 < 2e-16 ***
                                    7.968 5.01e-15 ***
## logdisb
               0.09767
                          0.01226
                          0.10352 -34.507 < 2e-16 ***
## logparty
              -3.57205
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.809 on 877 degrees of freedom
## Multiple R-squared: 0.6044, Adjusted R-squared: 0.6035
## F-statistic: 669.9 on 2 and 877 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = logvotes ~ logdisb + logparty, weights = 1/abs(e))
##
## Weighted Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -2.3152 -0.4577 0.2486 0.5280 2.0255
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 10.597863
                          0.035366 299.67
                                             <2e-16 ***
## logdisb
               0.098488
                          0.002631
                                    37.44
                                             <2e-16 ***
## logparty
              -3.579191
                          0.023330 -153.42
                                             <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6811 on 877 degrees of freedom
## Multiple R-squared: 0.9644, Adjusted R-squared: 0.9643
## F-statistic: 1.188e+04 on 2 and 877 DF, p-value: < 2.2e-16
```

- 6. (3 points) Interpret the model coefficients you estimate.
- Tasks to keep in mind as you're writing about your model:
  - At the time that you're writing and interpreting your regression coefficients you'll be deep in the analysis. Nobody will know more about the data than you do, at that point. So, although it will feel tedious, be descriptive and thorough in describing your observations.
  - It can be hard to strike the balance between: on the one hand, writing enough of the technical underpinnings to know that your model meets the assumptions that it must; and, on the other hand, writing little enough about the model assumptions that the implications of the model can still be clear. We're starting this practice now, so that by the end of Lab 2 you will have had several chances to strike this balance.

#### ANSWER

Interpreting a Coefficient as a Rate of Change in Y Instead of as a Rate of Change in the Conditional Mean of Y.

As pointed out in the discussion of overfitting, the computed regression equation estimates the true conditional mean function. How well it estimates the behavior of actual values of the random variable depends on the variability of the response variable Y. Thus, interpreting the computed coefficients in terms of the response variable is often misleading.

Illustration: In the graph shown below, the data are marked in green, the true line of conditional means is in violet, and the fitted (computed) regression line is in blue. Note that the fitted regression line is close to the true line of conditional means. The equation of the fitted regression line is (with coefficients rounded to a reasonable degree)  $\hat{y} = 0.56 + 2.18x.1$  Thus it is accurate to say, "For each change of one unit in x, the average change in the mean of Y is about 2.18 units." It is not accurate to say, "For each change of one unit in x, Y changes about 2.18 units." For example, we can see from the graph that when x is 2, Y might be anywhere between a little below 4 to a little above 5.5; when x is 3, Y might be anywhere from a little more than 5.5 to a little more than 9. So when going from x = 2 to x = 3, the change in Y might be almost zero, or it might be as large as 5.5 units.

Interpreting a coefficient as a rate of change in Y instead of as a rate of change in the conditional mean of Y.

2. Not taking confidence intervals for coefficients into account.

Even when a regression coefficient is (correctly) interpreted as a rate of change of a conditional mean (rather than a rate of change of the response variable), it is important to take into account the uncertainty in the estimation of the regression coefficient. To illustrate, in the example used in item 1 above, the computed regression line has equation  $\hat{y} = 0.56 + 2.18x$ . However, a 95% confidence interval for the slope is (1.80, 2.56). So saying, "The rate of change of the conditional mean of Y with respect to x is estimated to be between 1.80 and 2.56" is usually 1 preferable to saying, "The rate of change of the conditional mean Y with respect to x is about 2.18."

3. Interpreting a coefficient that is not statistically significant.2

Interpretations of results that are not statistically significant are made surprisingly often. If the t-test for a regression coefficient is not statistically significant, it is not appropriate to interpret the coefficient. A better alternative might be to say, "No statistically significant linear dependence of the mean of Y on x was detected.

4. Interpreting coefficients in multiple regression with the same language used for a slope in simple linear regression.

Even when there is an exact linear dependence of one variable on two others, the interpretation of coefficients is not as simple as for a slope with one dependent variable.

Example: If y = 1 + 2x1 + 3x2, it is not accurate to say "For each change of 1 unit in x1, y changes 2 units". What is correct is to say, "If x2 is fixed, then for each change of 1 unit in x1, y changes 2 units."

Similarly, if the computed regression line is  $\hat{y} = 1 + 2x1 + 3x2$ , with confidence interval (1.5, 2.5), then a correct interpretation would be, "The estimated rate of change of the conditional mean of Y with respect to x1, when x2 is fixed, is between 1.5 and 2.5 units."

For more on interpreting coefficients in multiple regression, see Section 4.3 (pp 161-175) of Ryan3.

### 5. Multiple inference on coefficients.

## Chapter 1: Sources & Types of Regression Output

Regression analysis can be performed on a variety of software today. The ubiquitous Microsoft Excel is still by far the most popular tool. A variety of other free and paid tools are available to run regression analysis. Some of these include SPSS, SAS, R, Python and JMP, etc.

Each of these tools presents the regression analysis output data in different ways. However, all of these tools provide essentially the same data. We present below the regression output from some of the tools mentioned above.

The raw data is available on the book's webpage here. Please feel free to play with it live and see the impact it has on the regression equation and the corresponding chart. 1.1 Microsoft Excel Output Regression Analysis Output in Microsoft Excel 1.2 R Programming Output Regression Analysis Output in R

Note that in all these cases, the regression analysis output provides essentially the same information although it is presented in different formats or designs.

Every number in the regression output indicates something. We will address only the most frequently used numbers in this book.

======== Chapter 2: The Big Picture Understanding the Model

The first set of numbers my eyes wander to are at the top of the regression output in Microsoft Excel under the heading Regression Statistics.

### Regression Statistics

This data is presented in the last few rows of the regression output in R. This set of data gives you the big picture about your regression output. It allows you to answer questions such as: How good is your model? What percentage of the variation is explained by the variables included?

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### 2.1 The Multiple R

The multiple R is the absolute value of the correlation coefficient of the two variables (X and Y) being evaluated. The correlation coefficient indicates how closely two variables move in tandem with each other. It assumes that the relationship is linear and so measures the linear relationship between the two variables X and Y.

The correlation coefficient has a value between and . A correlation coefficient of indicates that the variables move in perfect tandem and in the same direction. A correlation coefficient of 0 indicates that there is no relationship between the variables. A correlation coefficient of indicates that the variables move in perfect tandem but in the OPPOSITE direction.

However, since the multiple R is the absolute value of the correlation coefficient, we do not get to know if the correlation is positive or negative! This means that we do not see the direction of the relationship and only know the strength of the relationship.

The correlation coefficient is also referred to as the Pearson correlation coefficient or the Pearson's r.

The Multiple R in our example indicates that there is a strong correlation between the amount spent on TV ads and sales. As indicated above, the Multiple R will not tell us if the correlation is positive or negative.

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#### 2.2 R-Squared or Multiple R-Squared

The R-Squared (in Microsoft Excel) or Multiple R-Squared (in R) indicates how well the model or regression line "fits" the data. It indicates the proportion of variance in the dependent variable (Y) that is explained by the independent variable (X).

We know a variable could be impacted by one or more factors. The R-Squared indicates the percentage of variation in the dependent variable that is explained by the independent variables.

In our example, we know that the unit sales of a product will be influenced by a variety of factors such as price, competitors' actions, economy, etc. and not just by the advertisement expenditure. When we run a regression with sales as the dependent Y variable and only advertisement expenditure as the independent X variable, the R-square indicates the percentage of variation in unit sales that is explained by the advertisement expenditure. It tells you the percentage of change in sales that is caused by varying the advertisement expenditure. This also means that we can compute the percentage of variation that is explained by factors other than advertisement expenditure such as the economy, competition, price, etc. The percentage of variation that is explained by factors other than advertisement expenditure will be 100%-R-square.

Our regression output indicates that 81.48% of variation in unit sales is explained by the advertisement budget. And 18.52% (100%-81.48%) of the variation is caused by factors other than advertisement expenditure.

(Also note that as the name suggests, the R-square is equal to the square of the multiple R!) 2.3 Adjusted R-Squared

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Adjusted R-Squared is used only when analyzing multiple regression output and ignored when analyzing simple linear regression output. When we have more than one independent variable in our analysis, the computation process inflates the R-squared. As the name indicates, the Adjusted R-Squared is the R-Square adjusted for this inflation when performing multiple regression.

The interpretation of the Adjusted R-Squared is similar to the R-square and used only when analyzing multiple regression output. 2.4 The Standard Error

The standard error in the regression output is a very important number to understand when interpreting regression data. The standard error is a measure of the precision of the model. It reflects the average error of the regression model. In other words, if we were using the regression model to predict or estimate the dependent variable or variable of interest, the standard error shows you how wrong you could be if you used the regression model to make predictions. As the standard error reflects how wrong you could be, we want the standard error to be as small as possible.

The standard error is used to help you get a confidence interval for your predicted values. 2.5 Significance F

The simplest way to understand the significance F is to think of it as the probability that our regression model is wrong and needs to be discarded!! The significance F gives you the probability that the model is wrong. We want the significance F or the probability of being wrong to be as small as possible.

Significance F: Smaller is better.... Significance F in Regression Output

We can see that the Significance F is very small in our example. We usually establish a significance level and use it as the cutoff point in evaluating the model. Commonly used significance levels are 1%, 5% or 10%.

Statistically speaking, the significance F is the probability that the null hypothesis in our regression model cannot be rejected. In other words, it indicates the probability that all the coefficients in our regression output are actually zero! The significance F is computed from the F value (found to the left of the significance F in Microsoft Excel's output). The F value is a value similar to the z value, t value, etc. It is a ratio computed

by dividing the mean regression sum of squares by the mean error sum of squares. The F value ranges from zero to a very large number.

Note that the significance F is similar in interpretation to the P value discussed later a later section. The key difference is that the significance F applies to the entire model as a whole whereas the P value will be applied only to each corresponding coefficient.