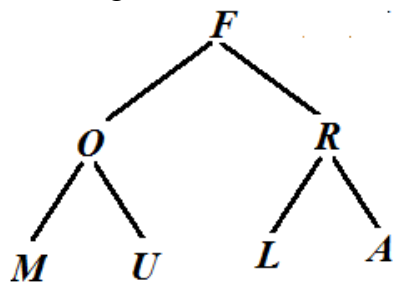


1. [4 points] Given a sequence of characters: <F, O, R, M, U, L, A>, build a heap using each of the following approaches:

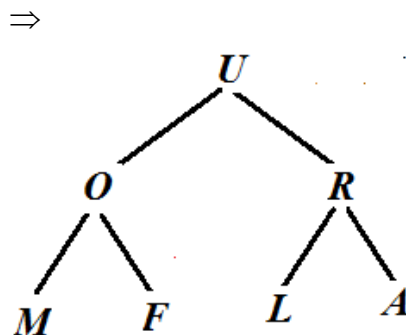
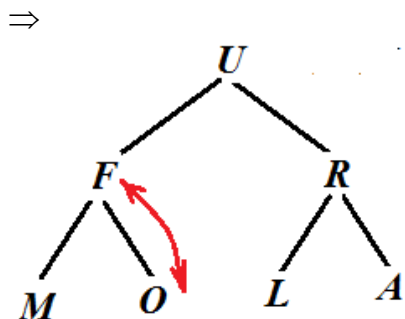
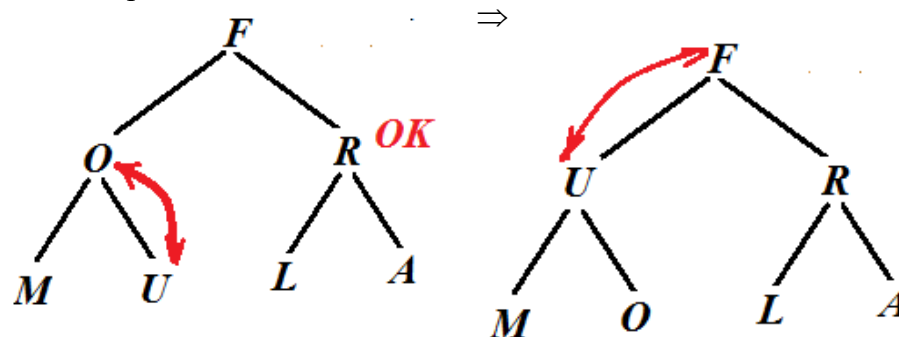
(a) Bottom-up approach.

Solution.

First, we build a nearly complete binary tree from incoming characters:

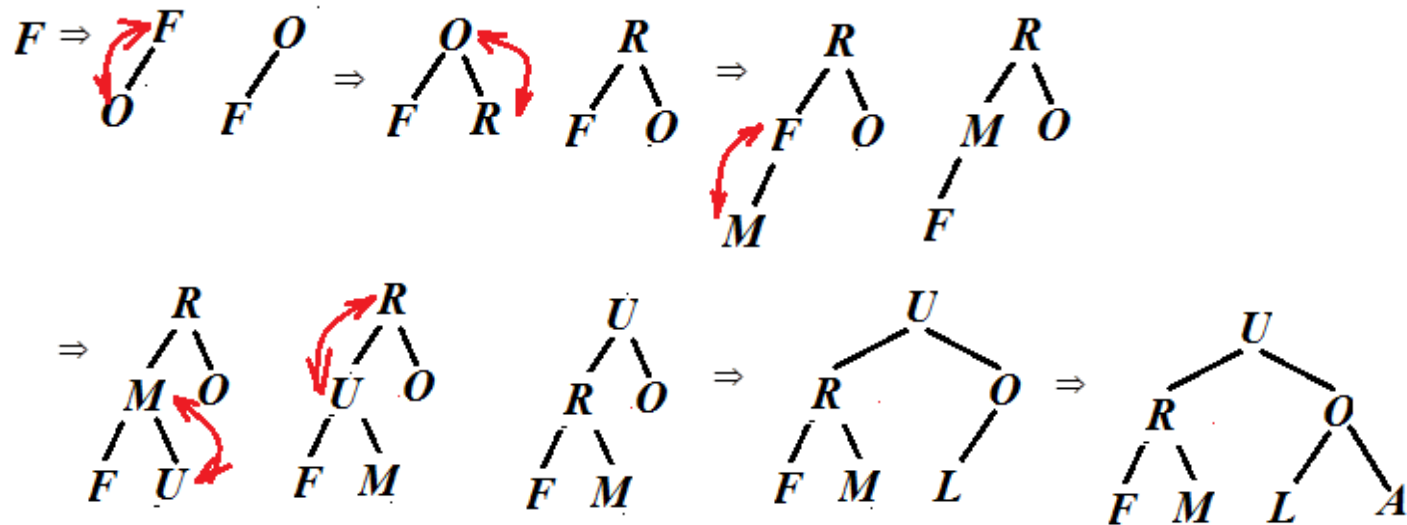


Now, we fix violations of parental-dominance requirement when going through all parental nodes, starting from the last one, from right to left, bottom – up:



(b) Top-down approach.

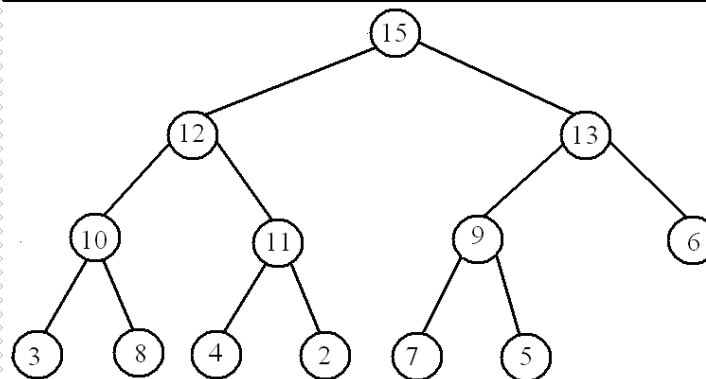
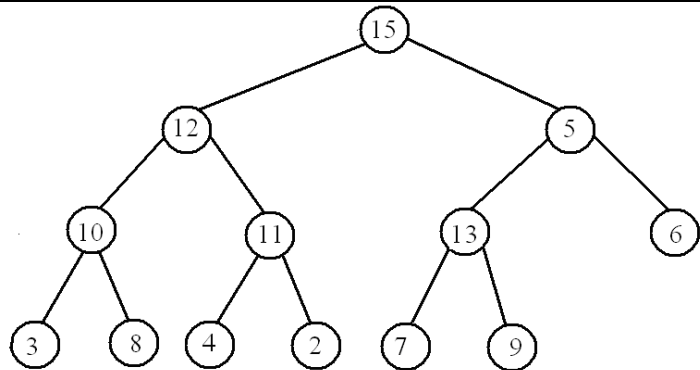
Solution.



2. [2 points] (a) Build an essentially complete binary tree from the items:

$A = \langle 15, 12, 5, 10, 11, 13, 6, 3, 8, 4, 2, 7, 9 \rangle$

- (b) Show the heap that is a result of a function call MAX-HEAPIFY($A, 3$), where the array A comes from part (a) of this problem.



3. [3 points] Show all the heaps that may be built from the items: **a**, **b**, **c**, **d**, **e** that may come in an arbitrary order.

