

Arrays and Structures

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Definition of Array

- “a set of consecutive memory locations”
- “a collection of data of the same type”
- “a set of pairs, $\langle \text{index}, \text{value} \rangle$, such that each index that is defined has a value associated with it”

Array as an Abstract Data Type

ADT Array is

objects: A set of pairs $\langle index, value \rangle$ where for each value of *index* there is a value from the set *item*.

index is a finite ordered set of one or more dimensions

functions: for all $A \in Array$, $i \in index$, $x \in item$, j , $size \in integer$

Array Create($j, list$) ::= return ...

item Retrieve(A, i) ::= if () return ... else return ...

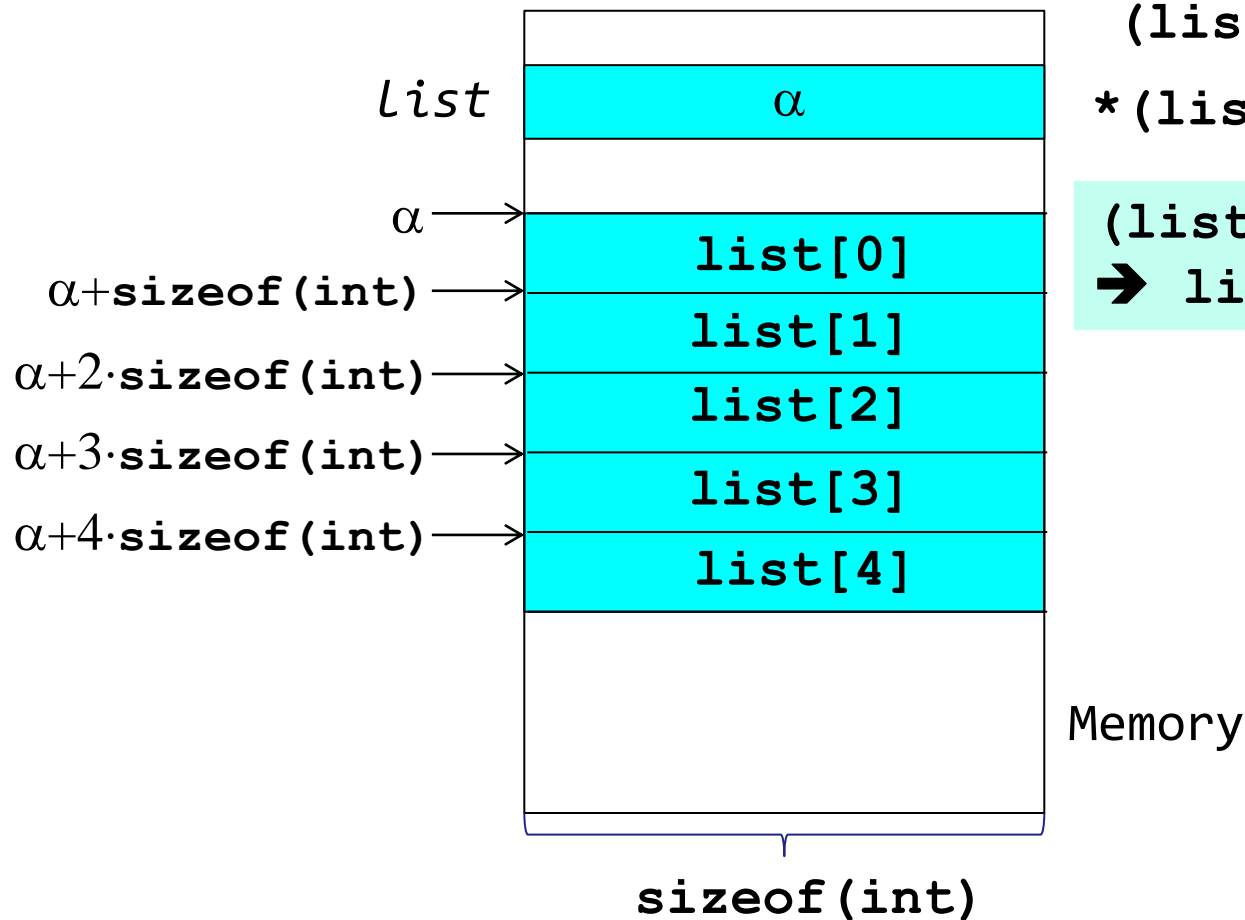
Array Store(A, i, x) ::= if () return ... else return ...

end Array

Array Representation in C

Data structure for one dimensional array

• `int list[5] → int* list;`



`(list+2)` vs. `&list[2]`

`*(list+2)` vs. `list[2]`

`(list+2)`
→ `list + 2 * sizeof(int)`

Example Array Program

```
#define MAX_SIZE 100
float sum(float [], int);
float input[MAX_SIZE], answer;
int i;

void main(void)
{
    for (i = 0; i < MAX_SIZE; i++)
        input[i] = i;
    answer = sum(input, MAX_SIZE);
    printf("The sum is: %f\n", answer);
}

float sum(float list[], int n)
{
    int i;
    float tempsum = 0;
    for (i = 0; i < n; i++)
        tempsum += list[i];
    return tempsum;
}
```

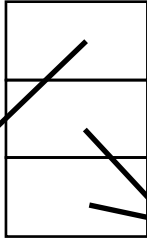
2D Array Representation In C

```
int x[3][4];
```

```
x = x[0]
```

```
x[1]
```

```
x[2]
```



| | | | | | | | | | | | |
|---|---|---|---|----|----|----|----|----|----|----|----|
| 3 | 5 | 6 | 7 | 10 | 21 | 32 | 52 | 32 | 25 | 73 | 54 |
|---|---|---|---|----|----|----|----|----|----|----|----|

Array-of-arrays representation

- Requires contiguous memory of size 3, 4, 4, and 4 for the 4 1D arrays
- One memory block of size number of rows and number of rows blocks of size number of columns

Dynamically Allocated Arrays

– One Dimension (1)

```
#include <math.h>
#include <stdio.h>
#define MAX_SIZE 101

main()
{
    int i, n, list[MAX_SIZE];

    printf("Enter the number of number to generate: ");
    scanf("%d", &n);

    for (i=0;i<n;i++)
    {
        list[i]=rand()%1000;
        printf ("%d\n", list[i]);
    }
}
```

What if we change MAX_SIZE to a very large number to avoid run time error??

→ We increase the likelihood that program may fail to compile due to lack of memory

Dynamically Allocated Arrays

– One Dimension (2)

```
int i, n, *list;

printf("Enter the number of number to generate: ");
scanf("%d", &n);

if (n < 1) {
    fprintf(stderr, "Improper value of n \n");
    exit (EXIT_FAILURE);
}

list=malloc(n * sizeof(int));
if (list==NULL) {
    fprintf(stderr, "lack of memory\n");
    exit (EXIT_FAILURE);
}
```

It fails only when $n < 1$ or we do not have sufficient memory to hold the list of numbers

Dynamically Allocated Arrays

- Two Dimension

```
int** make2dArray(int rows, int cols)
{
    /* create a two dimensional rows × cols array */

    int** x, i;

    /* get memory for row pointers */
    MALLOC(x, rows * sizeof (*x));

    /* get memory for each row */
    for (i = 0; i < rows; i++)
        MALLOC(x[i], cols * sizeof (**x));

    return x;
}

void main()
{
    int** myArray;
    myArray=make2dArray(5,10);
    myArray[2][4]=6;
}
```

x

x[0]

x[0][0]

rows

cols

Quiz 4

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Let `length[i]` be the desired length of row `i` of a two dimensional array.
Write a function similar to `make2dArray()` to create a two dimensional array such that row `i` has `length[i]` elements.

Structures (1)

A collection of data items, where each item is identified as to its type and name

```
struct {  
    char name[10];  
    int age;  
    float salary;  
} person;
```

```
strcpy(person.name, "korykang");  
person.age=34;  
person.salary=35000;
```

Structures (2)

To create own structure data type

```
typedef struct humanBeing {  
    char name[10];  
    int age;  
    float salary;  
};
```

or

```
typedef struct {  
    char name[10];  
    int age;  
    float salary;  
} humanBeing;
```

humanBeing person1, person2;

Assignments

person1=person2;

Or

```
strcpy(person1.name, person2.name);  
person1.age=person2.age;  
person1.salary=person2.salary;
```

```
if (person1 == person2) {  
    ...  
}
```

????

(Chapter 2 p.61)

Structures (3)

To embed a structure within a structure

```
typedef struct {  
    int month;  
    int day;  
    int year;  
} date;
```

```
typedef struct humanBeing{  
    char name[10];  
    int age;  
    float salary;  
    date dob;  
} humanBeing;
```

```
person1.dob.month=12; person1.dob.day=3;  
person1.dob.year=1969;
```

Quiz 5

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Develop a structure to represent each of the following geometric objects: rectangle, triangle, and circle.

Applications of Array

Ordered list

- One dimensional array
- Polynomial: components will be numeric
- String: components can be non-numeric

Matrix

- Standard: multi-dimensional array
- Sparse matrix: one dimensional array
- Components may be numeric

Ordered List (1)

Example

- Days of a week

(Sunday, Monday, Tuesday, Wednesday, Thursday, Friday, Saturday)

- Values in a deck of cards

(Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, King)

- Years Switzerland fought in World War II: ()

Ordered List (2)

Operations

- Finding the length, n , of a list
- Reading the items in a list from left to right (or reversely)
- Retrieving the i -th item from a list, $0 \leq i \leq n$
- Replacing the item in the i -th position of a list, $0 \leq i \leq n$
- Inserting a new item in the i -th position of a list, $0 \leq i \leq n$
- Deleting an item from the i -th position of a list, $0 \leq i \leq n$

Polynomial Abstract Data Type (1)

Example of polynomials

$$A(x) = 3x^6 + 2x^5 + 4, \quad B(x) = x^4 + 10x^3 + 3x^2 + 1$$

$$\rightarrow A(x) + B(x) = 3x^6 + 2x^5 + x^4 + 10x^3 + 3x^2 + 5$$

Manipulation of symbolic polynomials

$$A(x) = \sum_{i=0}^n a_i x^i \quad B(x) = \sum_{j=0}^m b_j x^j$$

$$A(x) + B(x) = \sum_{i=0}^{\max(n,m)} (a_i + b_i) \cdot x^i$$

$$A(x) \cdot B(x) = \sum_{i=0}^n (a_i x^i \sum_{j=0}^m (b_j \cdot x^j))$$

Polynomial Abstract Data Type (2)

ADT *Polynomial* is

objects : $p(x) = a_1x^{e_1} + \dots + a_nx^{e_n}$: a set of ordered pairs of $\langle e_i, a_i \rangle$, where a_i in *Coefficients* and e_i in *Exponents*, e_i are integers ≥ 0 .

functions : for all *poly*, *poly1*, *poly2* \in *Polynomial*,
coef \in *Coefficients*, *expon* \in *Exponents*

Polynomial Zero() ::= ...

Boolean IsZero(*poly*) ::= ...

Coefficient Coef(*poly*, *expon*) ::= ...

Exponent LeadExp(*poly*) ::= ...

Polynomial Attach(*poly*, *coef*, *expon*) ::= ...

Polynomial Remove(*poly*, *expon*) ::= ...

Polynomial SingleMult(*poly*, *coef*, *expon*) ::= ...

Polynomial Add(*poly1*, *poly2*) ::= ...

Polynomial Mult(*poly1*, *poly2*) ::= ...

end *Polynomial*

Polynomial Abstract Data Type (3)

```
/* d = a + b, where a, b, and d are polynomials */
d = Zero();
while (! IsZero(a) && ! IsZero(b)) do {
    switch COMPARE(LeadExp(a), LeadExp(b)) {
        case -1: /* if LeadExp(a) < LeadExp(b) */
            d = Attach(d, Coef(b, LeadExp(b)), LeadExp(b));
            b = Remove(b, LeadExp(b));
            break;
        case 0: /* if LeadExp(a) == LeadExp(b) */
            sum = Coef(a, LeadExp(a)) + Coef(b, LeadExp(b));
            if (sum) {
                d = Attach(d, sum, LeadExp(a));
                a = Remove(a, LeadExp(a));
                b = Remove(b, LeadExp(b));
            }
            break;
        case 1: /* if LeadExp(a) > LeadExp(b) */
            d = Attach(d, Coef(a, LeadExp(a)), LeadExp(a));
            a = Remove(a, LeadExp(a));
    }
}
Insert any remaining terms of a or b into d
```

$$A(x) = 3x^6 + 2x^5 + 4, \quad B(x) = x^4 + 10x^3 + 3x^2 + 1$$

Polynomial Representation (1)

```
#define MAX_DEGREE 101
```

```
typedef struct {
```

```
    int degree;
```

```
    float coef[MAX_DEGREE];
```

```
} polynomial;
```

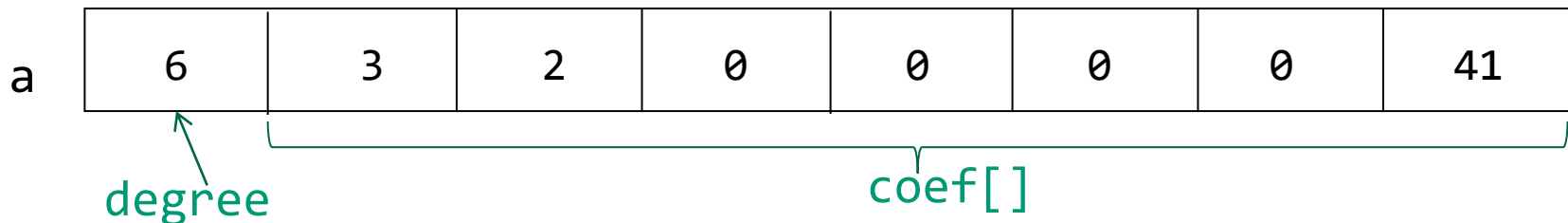
$$n < \text{MAX_DEGREE} \quad A(x) = \sum_{i=0}^n a_i x^i$$

```
polynomial a;
```

```
a.degree = n,    a.coef[i] = an-i, 0 ≤ i ≤ n
```

$$A(x) = 3x^6 + 2x^5 + 41$$

How about $2x^{1000} + 1$?



Polynomial Representation (2)

```
#define MAX_TERMS 100
```

```
typedef struct {
    float coef;
    int expon;
} polynomial;
```

```
polynomial terms[MAX_TERMS];
```

```
int starta, finisha, startb, finishb, avail;
```

```
starta=0; finisha=1; startb=2; finishb=5; avail=6;
```

~~#define MAX_DEGREE 101~~

$$A(x) = 2x^{1000} + 1,$$

$$B(x) = x^4 + 10x^3 + 3x^2 + 1$$

| | | | | | | | | | | | | |
|---------|--------|-----|---------|-----|--------|-----|---------|-----|-------|-----|-------|------|
| | starta | | finisha | | startb | | finishb | | avail | | avail | |
| terms[] | ↓ | ↓ | ↓ | | ↓ | ↓ | | | | | ↓ | |
| coef | 2 | 1 | 1 | 10 | 3 | 1 | 2 | 1 | 10 | 3 | 2 | |
| expon | 1000 | 0 | 4 | 3 | 2 | 0 | 1000 | 4 | 3 | 2 | 0 | |
| | [0] | [1] | [2] | [3] | [4] | [5] | [6] | [7] | [8] | [9] | [10] | [11] |

Quiz 6

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Implement Remove() and Attach() in slide 21 using polynomial representation in slide 22.