

# Lab2

2023-04-16

## R Markdown

```
## Item_Identifier    Item_Weight    Item_Fat_Content    Item_Visibility
## Length:14204      Min.      : 4.555    Length:14204      Min.      :0.00000
## Class :character   1st Qu.: 8.710    Class :character   1st Qu.:0.02704
## Mode  :character   Median :12.600    Mode  :character   Median :0.05402
##                      Mean      :12.793                Mean      :0.06595
##                      3rd Qu.:16.750                3rd Qu.:0.09404
##                      Max.      :21.350                Max.      :0.32839
##                      NA's      :2439
## Item_Type          Item_MRP      Outlet_Identifier
## Length:14204      Min.      : 31.29    Length:14204
## Class :character   1st Qu.: 94.01      Class :character
## Mode  :character   Median :142.25      Mode  :character
##                      Mean      :141.00
##                      3rd Qu.:185.86
##                      Max.      :266.89
##
## Outlet_Establishment_Year Outlet_Size      Outlet_Location_Type
## Min.      :1985          Length:14204      Length:14204
## 1st Qu.:1987          Class :character   Class :character
## Median :1999          Mode  :character   Mode  :character
## Mean      :1998
## 3rd Qu.:2004
## Max.      :2009
##
## Outlet_Type        Item_Outlet_Sales
## Length:14204      Min.      : 33.29
## Class :character   1st Qu.: 878.86
## Mode  :character   Median : 1828.27
##                      Mean      : 2099.33
##                      3rd Qu.: 2949.30
##                      Max.      :13086.97
##
## Item_Identifier    Item_Weight    Item_Fat_Content    Item_Visibility
## Length:13325      Min.      : 4.555    Length:13325      Min.      :0.003575
## Class :character   1st Qu.: 8.710    Class :character   1st Qu.:0.031396
## Mode  :character   Median :12.600    Mode  :character   Median :0.057851
##                      Mean      :12.807                Mean      :0.070303
##                      3rd Qu.:16.750                3rd Qu.:0.097618
##                      Max.      :21.350                Max.      :0.328391
## Item_Type          Item_MRP      Outlet_Identifier
## Length:13325      Min.      : 31.29    Length:13325
```

```

## Class :character 1st Qu.: 94.14 Class :character
## Mode :character Median :142.28 Mode :character
## Mean :141.11
## 3rd Qu.:185.86
## Max. :266.89
## Outlet_Establishment_Year Outlet_Size Outlet_Location_Type
## Min. :1985 Length:13325 Length:13325
## 1st Qu.:1987 Class :character Class :character
## Median :1999 Mode :character Mode :character
## Mean :1998
## 3rd Qu.:2004
## Max. :2009
## Outlet_Type Item_Outlet_Sales
## Length:13325 Min. : 33.29
## Class :character 1st Qu.: 875.53
## Mode :character Median : 1821.63
## Mean : 2096.48
## 3rd Qu.: 2942.84
## Max. :13086.97

## Group.1 x
## 1 Grocery Store 154.7059
## 2 Supermarket Type1 147.3417
## 3 Supermarket Type2 146.5251
## 4 Supermarket Type3 148.8826

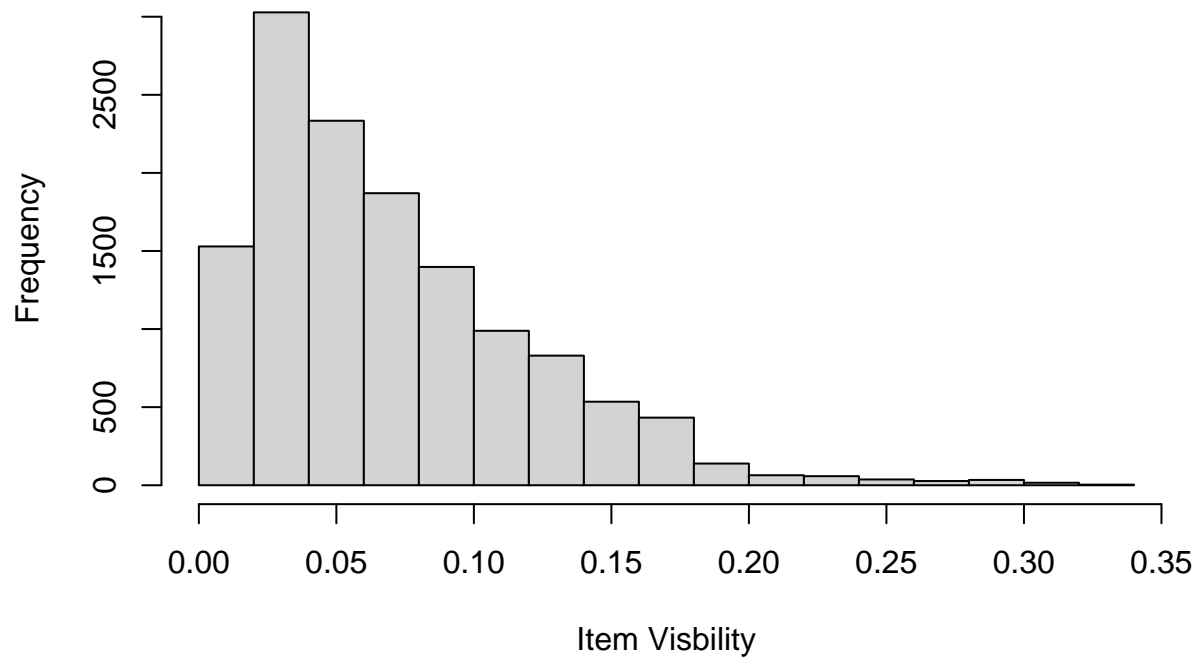
## Group.1 x
## 1 Grocery Store 141.2198
## 2 Supermarket Type1 144.1325
## 3 Supermarket Type2 144.4011
## 4 Supermarket Type3 143.4028

## Group.1 x
## 1 Grocery Store 140.2424
## 2 Supermarket Type1 137.9834
## 3 Supermarket Type2 136.9866
## 4 Supermarket Type3 138.5223

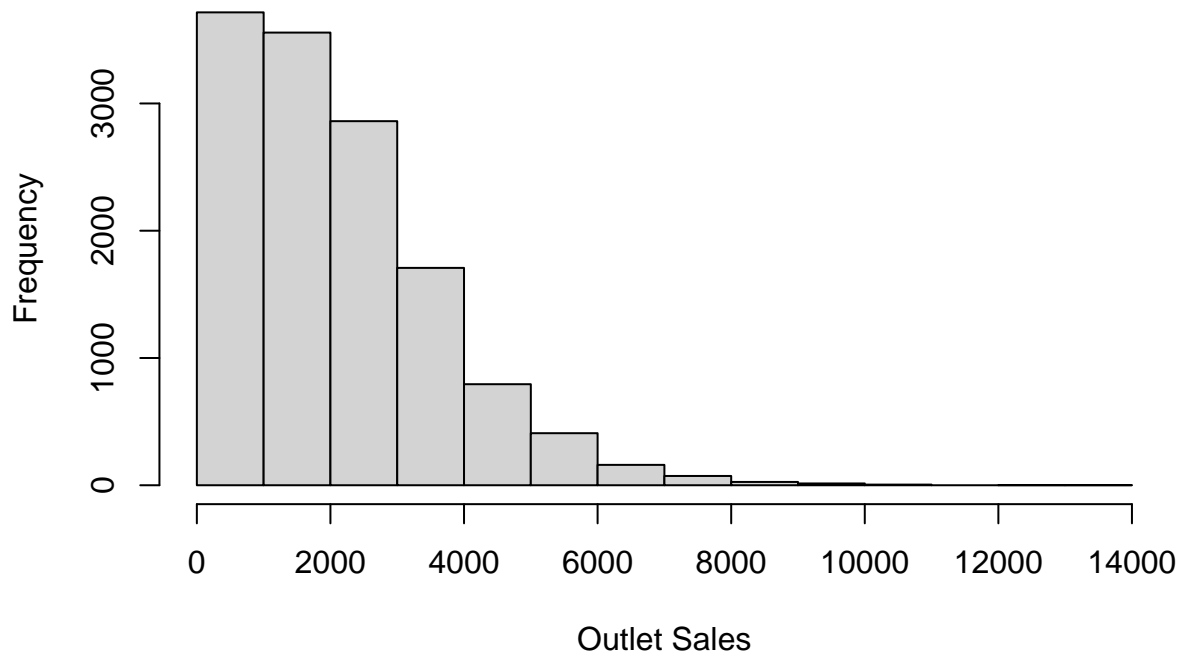
## Group.1 x
## 1 Grocery Store 148.0403
## 2 Supermarket Type1 146.6913
## 3 Supermarket Type2 145.8619
## 4 Supermarket Type3 145.7730

```

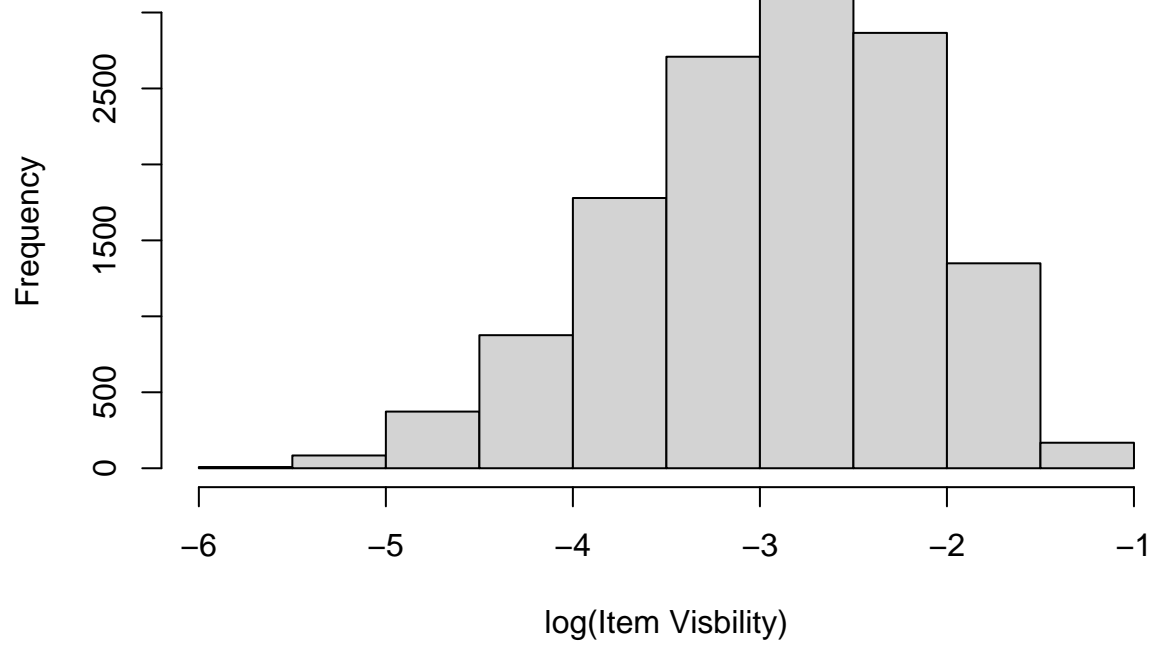
**Histogram of Item Visibility**



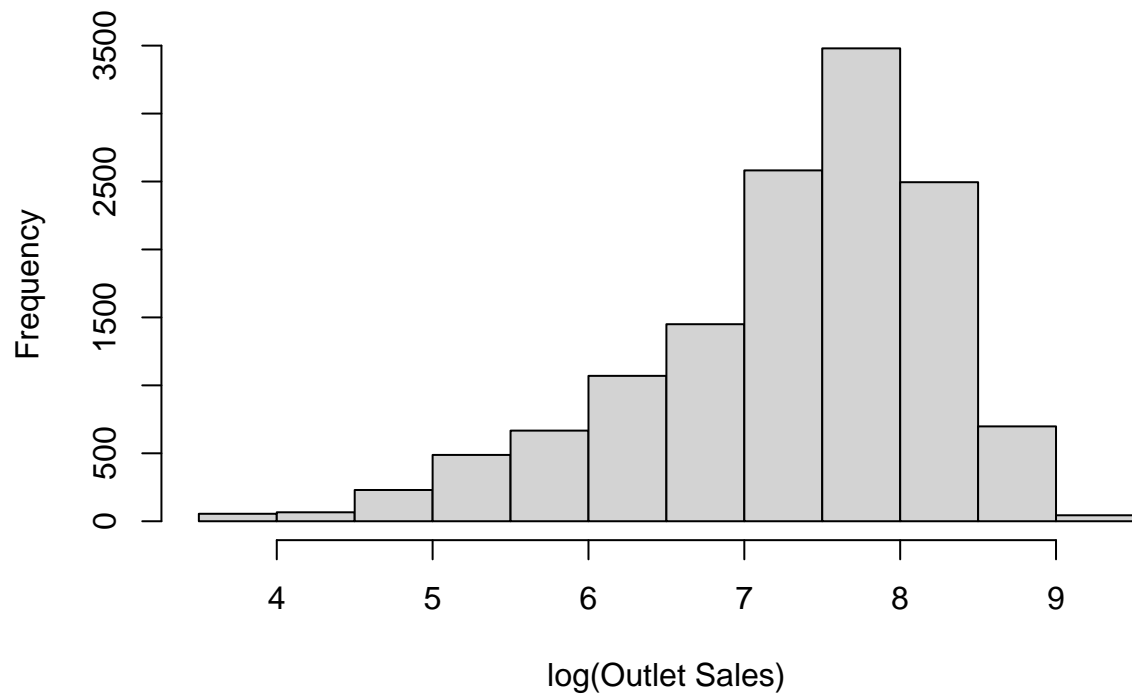
**Histogram of Outlet Sales**



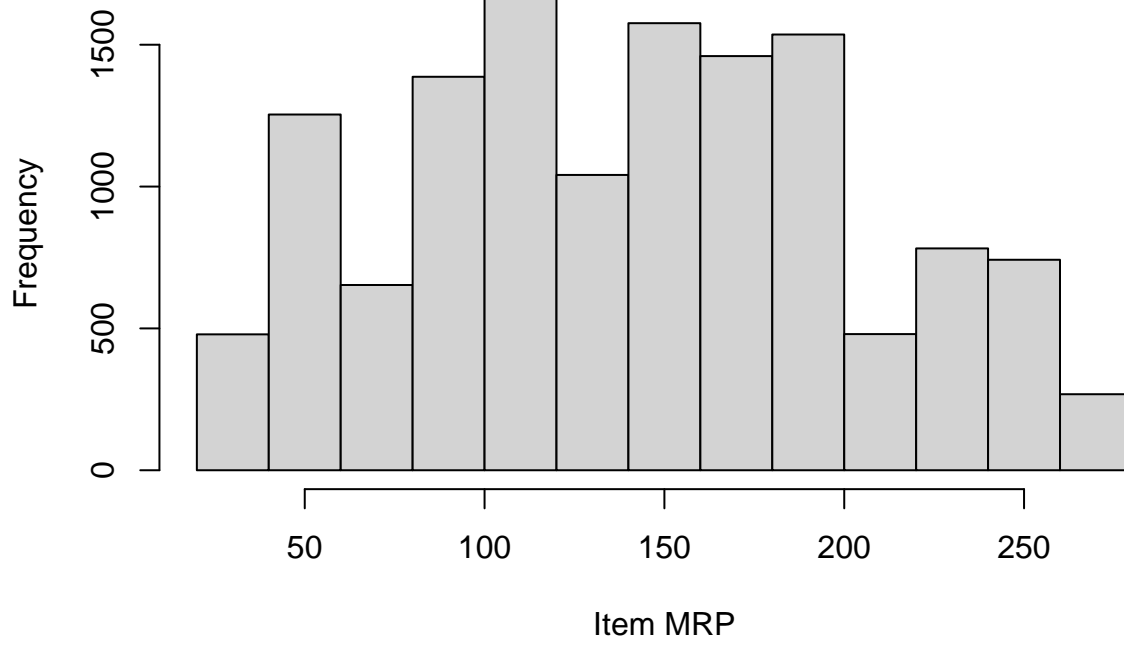
**Histogram of Log Item Visibility**



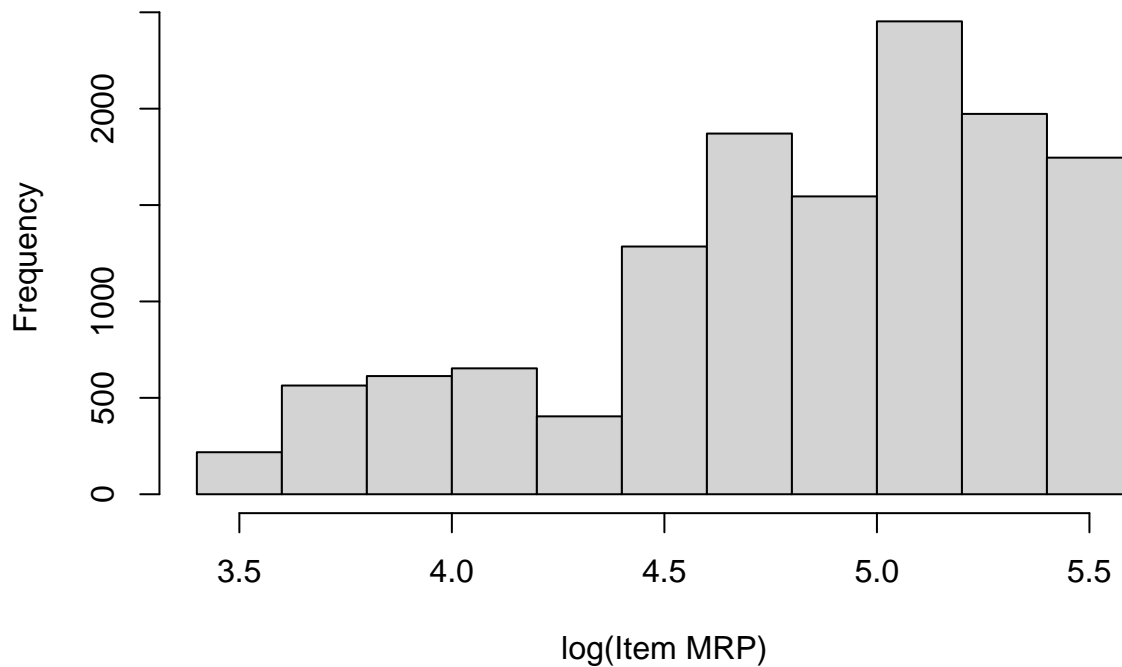
**Histogram of Log Outlet Sales**



**Histogram of Item MRP**



## Histogram of Log Item MRP



```
## Item_Identifier    Item_Weight    Item_Fat_Content    Item_Visibility
## Length:3998       Min.   : 4.555    Length:3998         Min.   :0.003598
## Class :character  1st Qu.: 8.645    Class :character    1st Qu.:0.031431
## Mode  :character  Median :12.600    Mode  :character    Median :0.057367
##                               Mean   :12.813                Mean   :0.070460
##                               3rd Qu.:16.750                3rd Qu.:0.097753
##                               Max.    :21.350                Max.    :0.325781
## Item_Type          Item_MRP        Outlet_Identifier
## Length:3998       Min.   : 31.29    Length:3998
## Class :character  1st Qu.: 93.81    Class :character
## Mode  :character  Median :141.91    Mode  :character
##                               Mean   :140.98
##                               3rd Qu.:186.58
##                               Max.    :266.69
## Outlet_Establishment_Year Outlet_Size    Outlet_Location_Type
## Min.   :1985         Length:3998    Length:3998
## 1st Qu.:1987         Class :character Class :character
## Median :1999         Mode  :character Mode  :character
## Mean   :1998
## 3rd Qu.:2004
## Max.    :2009
## Outlet_Type          Item_Outlet_Sales
## Length:3998       Min.   : 33.96
## Class :character  1st Qu.: 867.48
## Mode  :character  Median : 1824.82
##                               Mean   : 2102.60
```



```

##          3rd Qu.: 2965.59
##          Max.    :10306.58

## Item_Identifier  Item_Weight  Item_Fat_Content  Item_Visibility
## Length:9327      Min.      : 4.555      Length:9327      Min.      :0.003575
## Class :character  1st Qu.: 8.770      Class :character  1st Qu.:0.031388
## Mode  :character  Median :12.500      Mode  :character  Median :0.057993
##                      Mean   :12.805                      Mean   :0.070236
##                      3rd Qu.:16.750                      3rd Qu.:0.097605
##                      Max.    :21.350                      Max.    :0.328391
## Item_Type        Item_MRP      Outlet_Identifier
## Length:9327      Min.      : 31.89      Length:9327
## Class :character  1st Qu.: 94.34      Class :character
## Mode  :character  Median :142.42      Mode  :character
##                      Mean   :141.16
##                      3rd Qu.:185.66
##                      Max.    :266.89
## Outlet_Establishment_Year Outlet_Size      Outlet_Location_Type
## Min.      :1985      Length:9327      Length:9327
## 1st Qu.:1987      Class :character  Class :character
## Median :1999      Mode  :character  Mode  :character
## Mean     :1998
## 3rd Qu.:2004
## Max.     :2009
## Outlet_Type        Item_Outlet_Sales
## Length:9327      Min.      : 33.29
## Class :character  1st Qu.: 884.18
## Mode  :character  Median : 1821.63
##                      Mean   : 2093.85
##                      3rd Qu.: 2931.52
##                      Max.    :13086.97

## Analysis of Variance Table
##
## Model 1: log(Item_Outlet_Sales) ~ log(Item_Visibility)
## Model 2: log(Item_Outlet_Sales) ~ log(Item_Visibility) * Item_MRP
## Model 3: log(Item_Outlet_Sales) ~ log(Item_Visibility) * Item_MRP + Outlet_Type
##   Res.Df    RSS Df Sum of Sq    F    Pr(>F)
## 1     3996 3727.0
## 2     3994 2630.7  2     1096.3 3000.1 < 2.2e-16 ***
## 3     3991  729.2  3     1901.5 3468.9 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

##
## Call:
## lm(formula = log(Item_Outlet_Sales) ~ log(Item_Visibility), data = train_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.8772 -0.5390  0.1882  0.6938  1.9750
##
## Coefficients:

```

```

##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)      6.62848    0.05921  111.94  <2e-16 ***
## log(Item_Visibility) -0.22635    0.01956  -11.57  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9658 on 3996 degrees of freedom
## Multiple R-squared:  0.03241, Adjusted R-squared:  0.03217
## F-statistic: 133.8 on 1 and 3996 DF, p-value: < 2.2e-16

##
## Call:
## lm(formula = log(Item_Outlet_Sales) ~ log(Item_Visibility) *
##     Item_MRP, data = train_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.1425 -0.2266  0.2070  0.4991  1.6907
##
## Coefficients:
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)      5.3951221    0.1233659  43.733  < 2e-16 ***
## log(Item_Visibility) -0.2412542    0.0410961  -5.870  4.7e-09 ***
## Item_MRP          0.0088424    0.0008068  10.960  < 2e-16 ***
## log(Item_Visibility):Item_MRP 0.0001377    0.0002689   0.512   0.609
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8116 on 3994 degrees of freedom
## Multiple R-squared:  0.317, Adjusted R-squared:  0.3165
## F-statistic: 618 on 3 and 3994 DF, p-value: < 2.2e-16

##
## Call:
## lm(formula = log(Item_Outlet_Sales) ~ log(Item_Visibility) *
##     Item_MRP + Outlet_Type, data = train_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.23221 -0.18391  0.04723  0.22635  1.34806
##
## Coefficients:
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)      4.2447043    0.0660345  64.280  <2e-16 ***
## log(Item_Visibility) -0.0490431    0.0217316  -2.257   0.0241 *
## Item_MRP          0.0089782    0.0004250  21.124  <2e-16 ***
## Outlet_TypeSupermarket Type1  1.9471448    0.0206992  94.069  <2e-16 ***
## Outlet_TypeSupermarket Type2  1.8098845    0.0280190  64.595  <2e-16 ***
## Outlet_TypeSupermarket Type3  2.4757051    0.0277120  89.337  <2e-16 ***
## log(Item_Visibility):Item_MRP 0.0002159    0.0001417   1.524   0.1275
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4274 on 3991 degrees of freedom

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```
## Multiple R-squared:  0.8107, Adjusted R-squared:  0.8104
## F-statistic:  2848 on 6 and 3991 DF,  p-value: < 2.2e-16
```

```
##           Group.1      x
## 1      Grocery Store 157.9325
## 2 Supermarket Type1 148.9183
## 3 Supermarket Type2 146.3910
## 4 Supermarket Type3 154.1648
```

```
##           Group.1      x
## 1      Grocery Store 141.9583
## 2 Supermarket Type1 145.1227
## 3 Supermarket Type2 146.1616
## 4 Supermarket Type3 143.5479
```

```
##           Group.1      x
## 1      Grocery Store 146.7284
## 2 Supermarket Type1 136.0410
## 3 Supermarket Type2 133.6612
## 4 Supermarket Type3 131.8238
```

```
##           Group.1      x
## 1      Grocery Store 150.0489
## 2 Supermarket Type1 145.8780
## 3 Supermarket Type2 146.9438
## 4 Supermarket Type3 142.0538
```

```
##
## Call:
## lm(formula = log(Item_Outlet_Sales) ~ log(Item_Visibility) *
##     Item_MRP + Outlet_Type, data = test_data)
##
```

```
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.3558 -0.1938  0.0527  0.2346  1.3780
```

```
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    4.470e+00  4.453e-02 100.375  <2e-16 ***
## log(Item_Visibility)  2.815e-02  1.459e-02   1.929   0.0537 .
## Item_MRP        7.661e-03  2.847e-04  26.907  <2e-16 ***
## Outlet_TypeSupermarket Type1  1.954e+00  1.448e-02 134.890  <2e-16 ***
## Outlet_TypeSupermarket Type2  1.774e+00  1.921e-02  92.325  <2e-16 ***
## Outlet_TypeSupermarket Type3  2.476e+00  1.920e-02 128.976  <2e-16 ***
## log(Item_Visibility):Item_MRP -1.998e-04  9.493e-05  -2.105   0.0353 *
```

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
## Residual standard error: 0.44 on 9320 degrees of freedom
## Multiple R-squared:  0.789, Adjusted R-squared:  0.7888
## F-statistic:  5808 on 6 and 9320 DF,  p-value: < 2.2e-16
```

```
##
```

```
## Call:
## lm(formula = log(Item_Outlet_Sales) ~ log(Item_Visibility) *
##      Item_MRP + Outlet_Type, data = fruits_and_veg)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.23396 -0.17294  0.04911  0.24525  1.15991
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      4.4716271   0.1306289  34.232  <2e-16 ***
## log(Item_Visibility)  0.0301549   0.0440031   0.685    0.493
## Item_MRP          0.0078560   0.0008388   9.365  <2e-16 ***
## Outlet_TypeSupermarket Type1  1.9661645   0.0375470  52.365  <2e-16 ***
## Outlet_TypeSupermarket Type2  1.7966618   0.0500597  35.890  <2e-16 ***
## Outlet_TypeSupermarket Type3  2.5930834   0.0503167  51.535  <2e-16 ***
## log(Item_Visibility):Item_MRP -0.0001098   0.0002825  -0.389    0.698
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4419 on 1320 degrees of freedom
## Multiple R-squared:  0.7958, Adjusted R-squared:  0.7949
## F-statistic: 857.6 on 6 and 1320 DF,  p-value: < 2.2e-16

##
## Call:
## lm(formula = log(Item_Outlet_Sales) ~ log(Item_Visibility) *
##      Item_MRP + Outlet_Type, data = snacks)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.89306 -0.20161  0.04725  0.23347  1.26247
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      4.4848276   0.1313971  34.132  <2e-16 ***
## log(Item_Visibility)  0.0326450   0.0418966   0.779    0.436
## Item_MRP          0.0075692   0.0008176   9.257  <2e-16 ***
## Outlet_TypeSupermarket Type1  2.0025889   0.0402930  49.701  <2e-16 ***
## Outlet_TypeSupermarket Type2  1.8556303   0.0530473  34.981  <2e-16 ***
## Outlet_TypeSupermarket Type3  2.5264493   0.0533528  47.354  <2e-16 ***
## log(Item_Visibility):Item_MRP -0.0001221   0.0002667  -0.458    0.647
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4502 on 1308 degrees of freedom
## Multiple R-squared:  0.7676, Adjusted R-squared:  0.7665
## F-statistic: 720 on 6 and 1308 DF,  p-value: < 2.2e-16

## [1] 15.19786 15.19786

##              GVIF Df GVIF^(1/(2*Df))      Interacts With
## Item_Visibility 15.20331  1          3.899142              Item_MRP
```

```

## Item_MRP      15.20331  1      3.899142 log(Item_Visibility)
## Outlet_Type   1.05888  3      1.009581      --
##              Other Predictors
## Item_Visibility Item_Visibility, Outlet_Type
## Item_MRP        Item_Visibility, Outlet_Type
## Outlet_Type     Item_Visibility, Item_MRP

```

Table 1: Regression Model Results Comparing Models

	<i>Dependent variable:</i>		
	Log(Outlet Sales)		
	(1)	(2)	(3)
Log(Visibility)	−0.226*** (0.020)	−0.241*** (0.041)	−0.049** (0.022)
Maximum Retail Price (MRP)		0.009*** (0.001)	0.009*** (0.0004)
Type 1 Supermarket			1.947*** (0.021)
Type 2 Supermarket			1.810*** (0.028)
Type 3 Supermarket			2.476*** (0.028)
Log(Visibility) - MRP Interaction		0.0001 (0.0003)	0.0002 (0.0001)
Constant	6.628*** (0.059)	5.395*** (0.123)	4.245*** (0.066)
Observations	3,998	3,998	3,998
R <sup>2</sup>	0.032	0.317	0.811
Adjusted R <sup>2</sup>	0.032	0.317	0.810
Residual Std. Error	0.966 (df = 3996)	0.812 (df = 3994)	0.427 (df = 3991)
F Statistic	133.843*** (df = 1; 3996)	618.009*** (df = 3; 3994)	2,848.379*** (df = 6; 3991)

*Note:*

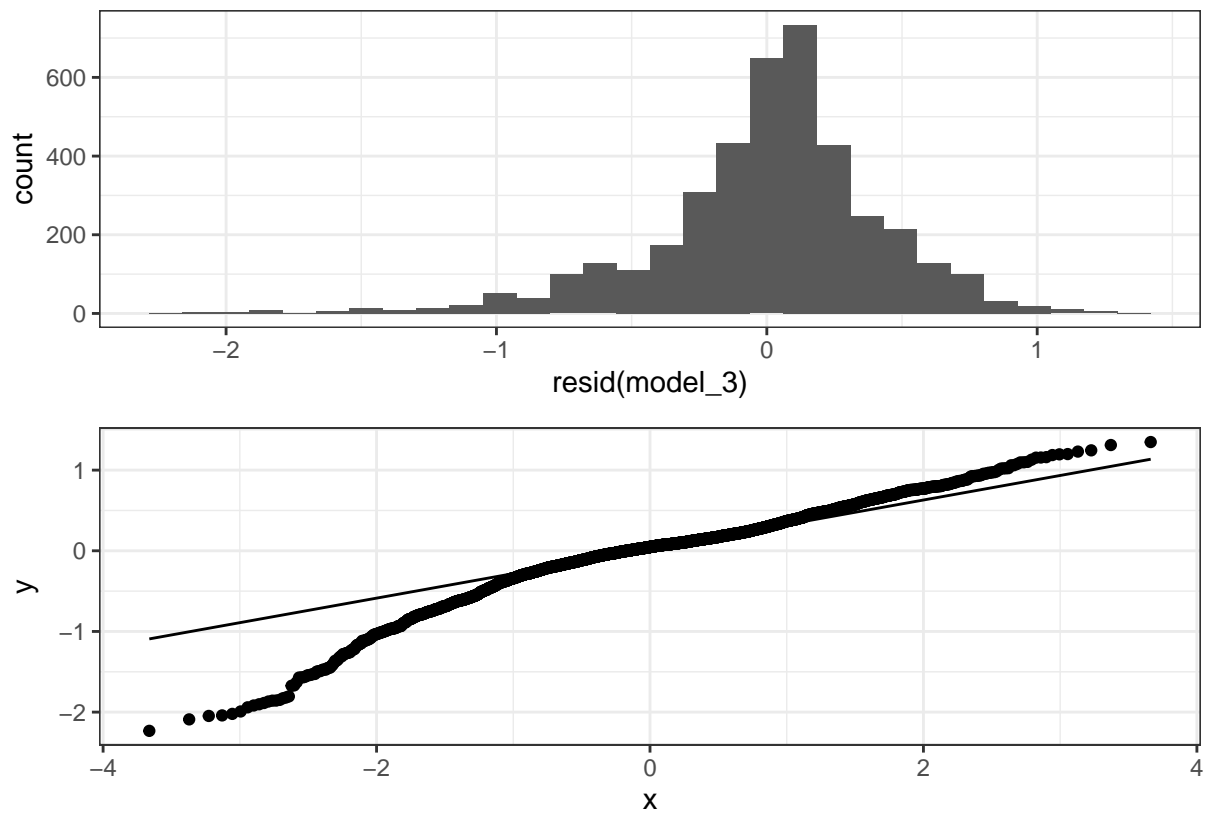
\*p<0.1; \*\*p<0.05; \*\*\*p<0.01

Table 2: Regression Model Results Comparing Item Data

	<i>Dependent variable:</i>		
	Log(Outlet Sales)		
	(1)	(2)	(3)
Log(Visibility)	0.028* (0.015)	0.030 (0.044)	0.033 (0.042)
Maximum Retail Price (MRP)	0.008*** (0.0003)	0.008*** (0.001)	0.008*** (0.001)
Type 1 Supermarket	1.954*** (0.014)	1.966*** (0.038)	2.003*** (0.040)
Type 2 Supermarket	1.774*** (0.019)	1.797*** (0.050)	1.856*** (0.053)
Type 3 Supermarket	2.476*** (0.019)	2.593*** (0.050)	2.526*** (0.053)
Log(Visibility) - MRP Interaction	-0.0002** (0.0001)	-0.0001 (0.0003)	-0.0001 (0.0003)
Constant	4.470*** (0.045)	4.472*** (0.131)	4.485*** (0.131)
Observations	9,327	1,327	1,315
R <sup>2</sup>	0.789	0.796	0.768
Adjusted R <sup>2</sup>	0.789	0.795	0.767
Residual Std. Error	0.440 (df = 9320)	0.442 (df = 1320)	0.450 (df = 1308)
F Statistic	5,807.752*** (df = 6; 9320)	857.568*** (df = 6; 1320)	720.034*** (df = 6; 1308)

Note:

\*p<0.1; \*\*p<0.05; \*\*\*p<0.01



```
##  
## studentized Breusch-Pagan test  
##  
## data: model_3  
## BP = 14.595, df = 6, p-value = 0.02365
```



