

# 1 Type $(2, 0)$ geometry

## 1.1 Datasets

Name: 20180608

Dimension:  $20 \times 20$

Range  $g_2$ :  $[-4 : -1.5]$  51 values

Samples: 2200

Name: 20180610

Dimension:  $25 \times 25$

Range  $g_2$ :  $[-4 : -1.5]$  51 values

Samples: 1152

Name: 20180611

Dimension:  $30 \times 30$

Range  $g_2$ :  $[-4 : -1.5]$  51 values

Samples: 1152

## 1.2 Action monitoring in $A$ and $B$ modes

Figure: 2

Dataset: 20180608

Data analysis script: 20\_ABaction\_monitoring.py

Gnuplot script:

```
plot "20180608_varG_ABaction.txt" u 1:2 w lines title "{/Symbol r  
  }^2", "20180608_varG_ABaction.txt" u 1:3 w lines title "(TrAB)  
  ^2", "20180608_varG_ABaction.txt" u 1:4 w lines title "TrA^2",  
  "20180608_varG_ABaction.txt" u 1:5 w lines lt 3 dt 2 title "TrA  
  ^3", "20180608_varG_ABaction.txt" u 1:6 w lines lt 3 dt 4 title  
  "TrA^4", "20180608_varG_ABaction.txt" u 1:7 w lines lt 4 title "  
  TrB^2", "20180608_varG_ABaction.txt" u 1:8 w lines lt 4 dt 2  
  title "TrB^4", "20180608_varG_ABaction.txt" u 1:9 w lines lt 5
```

```

title "TrA^2B^2", "20180608_varG_ABaction.txt" u 1:10 w lines lt
6 title "TrABAB", "20180608_varG_ABaction.txt" u 1:11 w lines
lt 7 title "TrB^2A"

```

### 1.3 Shift of $\rho^2$ from stationary solution

Figure: 1

Dataset: 20180608

Data analysis script: 20\_soft\_monitoring.py

Gnuplot script:

```

plot "20180608_varG_ALL.txt" u 1:3 w lines title "1/N Tr W^+ W",
      "20180608_varG_ALL.txt" u 1:2 w lines title "1/N^2 |TrW|^2",
      "20180608_varG_ALL.txt" u 1:4 w lines title "1/N TrB^2",
      "20180608_varG_ALL.txt" u 1:5 w lines title "1/N TrA^2", -x/8 lt
7 dt 2 title "-g/8"

```

### 1.4 Scaling of $\text{Tr } B^2$ and $\text{Tr } B^4$

Figure: 3

Dataset: 20180608, 20180610, 20180611

Data analysis script: 20\_ABaction\_monitoring.py

Gnuplot script:

```

plot "20180608/20180608_varG_ABaction.txt" u 1:($8/20) w lines
      title "1/N TrB^4", "20180610/20180610_varG_ABaction.txt" u 1:($8
/25) w lines notitle, "20180611/20180611_varG_ABaction.txt" u
1:($8/30) w lines notitle, "20180608/20180608_varG_ABaction.txt"
u 1:($7/20) w lines lt 1 dt 2 title "1/N TrB^2",
      "20180610/20180610_varG_ABaction.txt" u 1:($7/25) w lines lt 2
dt 2 notitle, "20180611/20180611_varG_ABaction.txt" u 1:($7/30)
w lines lt 3 dt 2 notitle

```

## 1.5 $B$ modes matrix elements

Figure: 4, 5

Dataset: 20180608

Data analysis script: 20\_Bexp\_monitoring.py

Gnuplot script:

```
set key font ",11"
plot "20180608_varG_B2exp.txt" u 1:2:3 w yerrorbars title "|B_{ii}
      |^2", "20180608_varG_B2exp.txt" u 1:4:5 w yerrorbars title "|B_
      {ij}|^2"

set key font ",11"
plot "20180608_varG_B4exp.txt" u 1:2:3 w yerrorbars title "|B_{ii}
      |^4", "20180608_varG_B4exp.txt" u 1:4:5 w yerrorbars title "|B_
      {ij}|^4"
```

Figure: 6

Dataset: 20180608

Data analysis script: 20\_Bij\_ik\_l\_monitoring.py

Gnuplot script:

```
set key font ",11"
plot "20180608_varG_Bij_ik_l.txt" u 1:2:3 w yerrorbars title "E[ |
      B_{ij}|^2 |B_{il}|^2 ]", "20180608_varG_Bij_ik_l.txt" u 1:4:5 w
      yerrorbars title "E[ |B_{ij}|^2|B_{kl}|^2 ]"
```

Figure: 7

Dataset: 20180608

Data analysis script: 20\_Bstatind\_monitoring.py

Gnuplot script:

```
set title font ",11"
set title "E[|B_{ij}|^2|B_{kl}|^2] - E[|B_{ij}|^2]E[|B_{kl}|^2]"
plot "20180608_varG_Bstatind.txt" u 1:2:3 w yerrorbars notitle
```

Figure: 8

Dataset: 20180608

Data analysis script: 20\_4Bexp\_monitoring.py

Gnuplot script:

```
set title font ",11"
set key font ",11"
set key left bottom
set title "E[ B_{kl} B_{lm} B_{mn} B_{nk} ] with m != k and n != l"
plot "20180608_varG_4Bexp.txt" u 1:2:3 w yerrorbars title "real
      part", "20180608_varG_4Bexp.txt" u 1:4:5 w yerrorbars title "
      imaginary part"
```

## 1.6 Plots

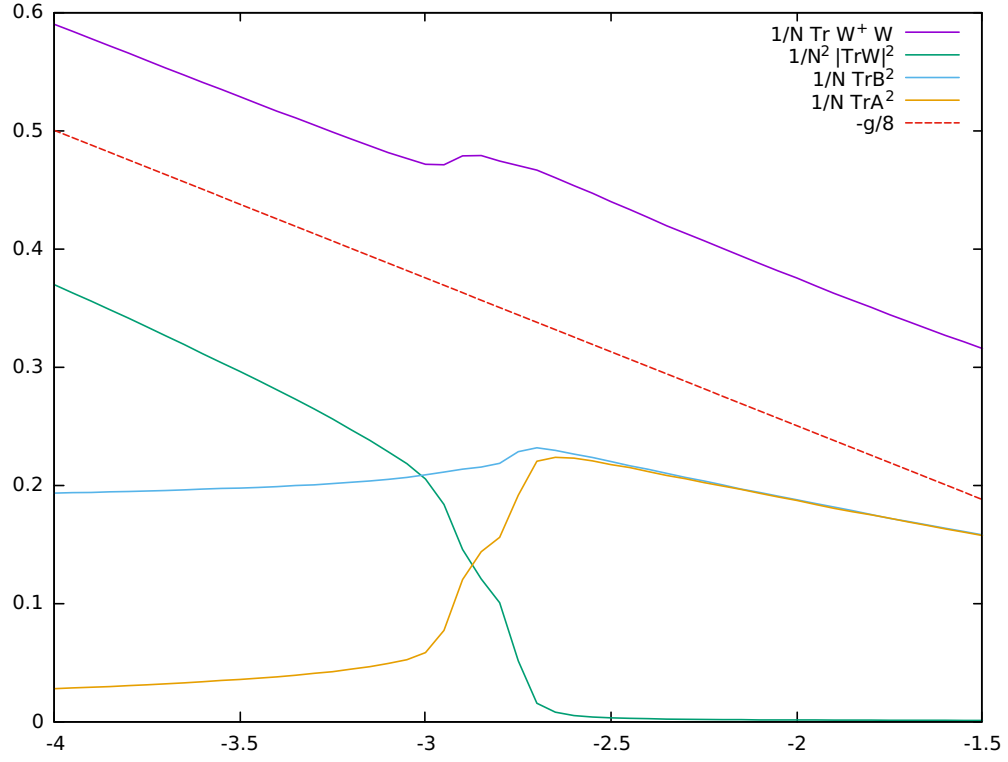


Figure 1: Shift of  $\rho^2$  (green line) from stationary solution (red dashed line). Matrix size 20x20.

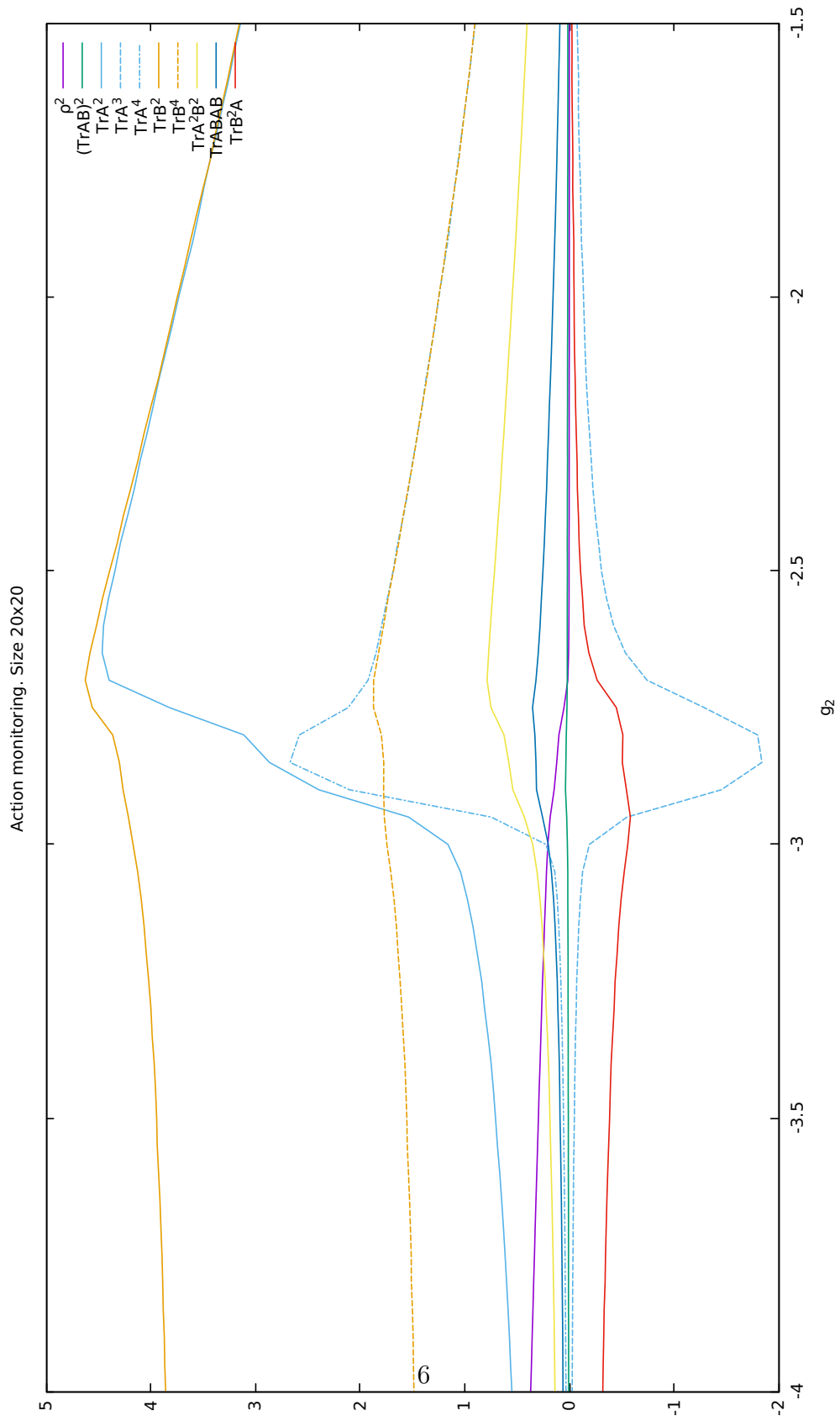


Figure 2: Monitoring of  $A$  and  $B$  modes in the action for matrix size 20x20.  
Dataset: 20180608

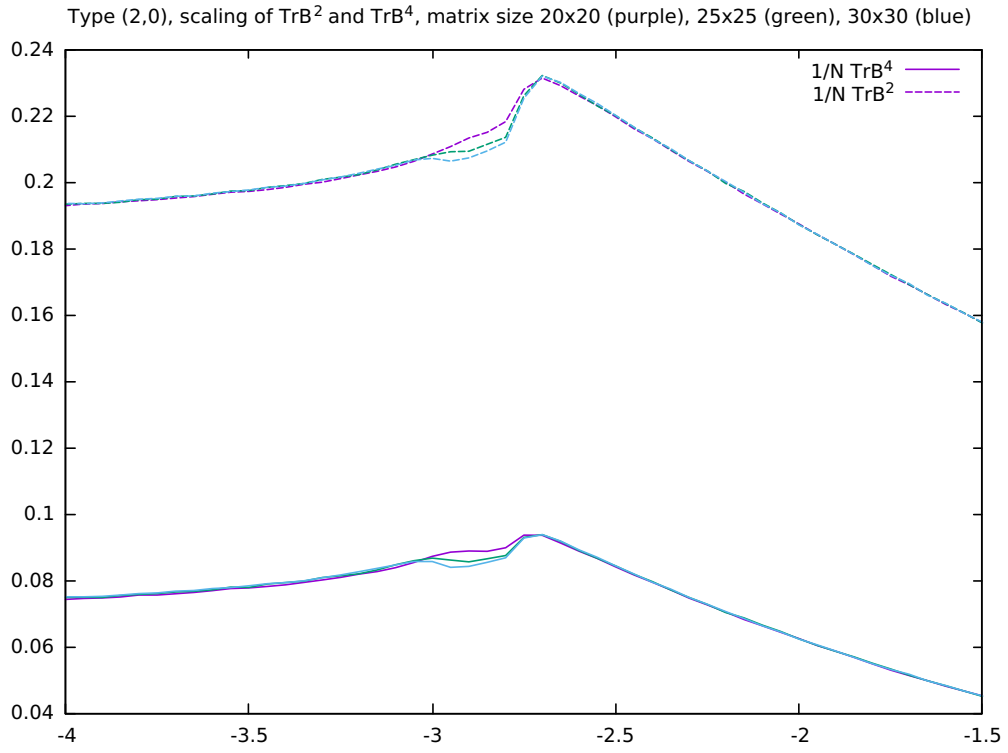


Figure 3: Scaling of  $\text{Tr} B^2$  and  $\text{Tr} B^4$ . Both quantities scale like  $N$ .

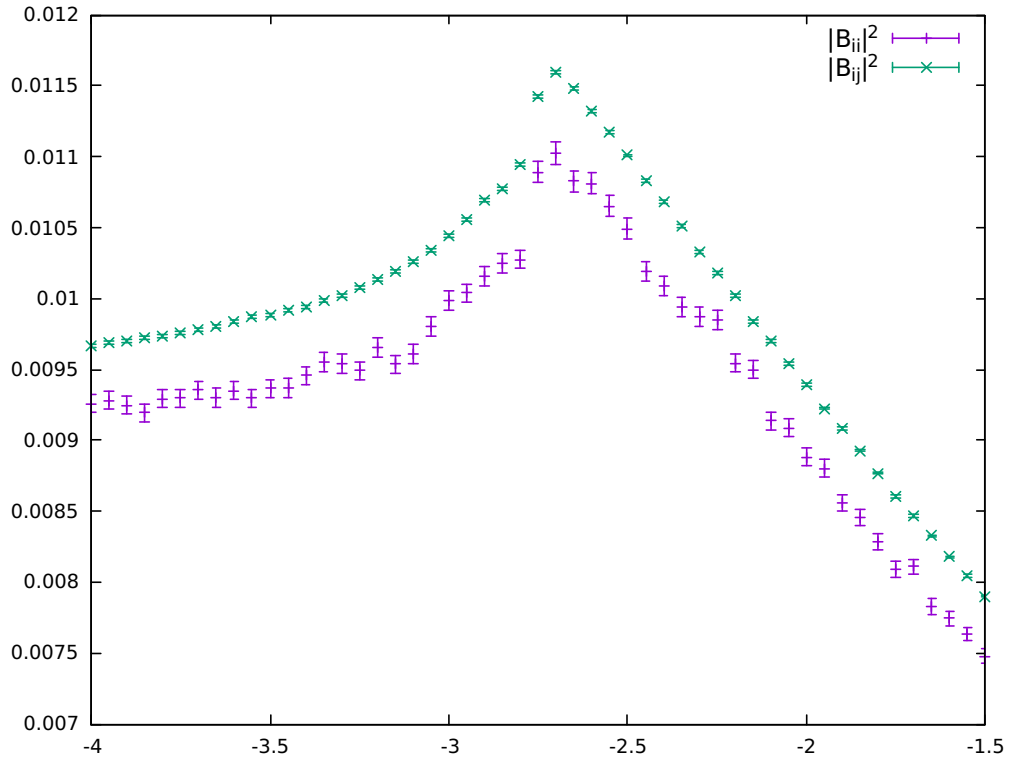


Figure 4: Expectation value of  $|B_{ii}|^2$  (purple) and  $|B_{ij}|^2$  (green) versus  $g_2$ . Matrix size 20x20.



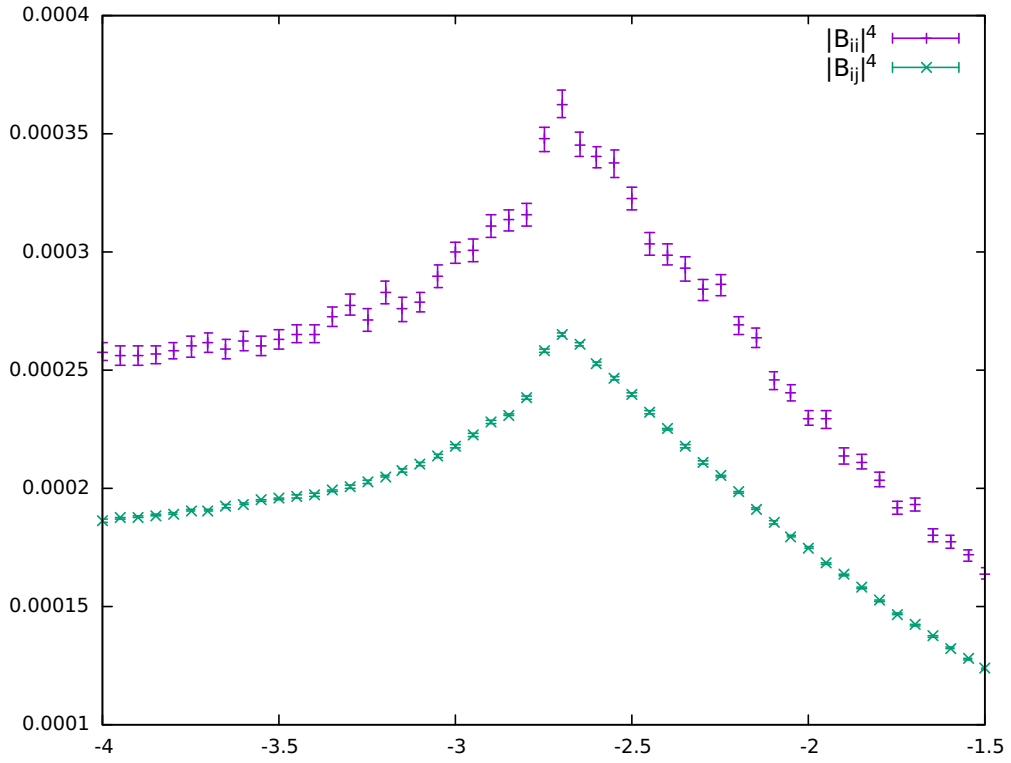


Figure 5: Expectation value of  $|B_{ii}|^4$  (purple) and  $|B_{ij}|^4$  (green) versus  $g_2$ . Matrix size 20x20.

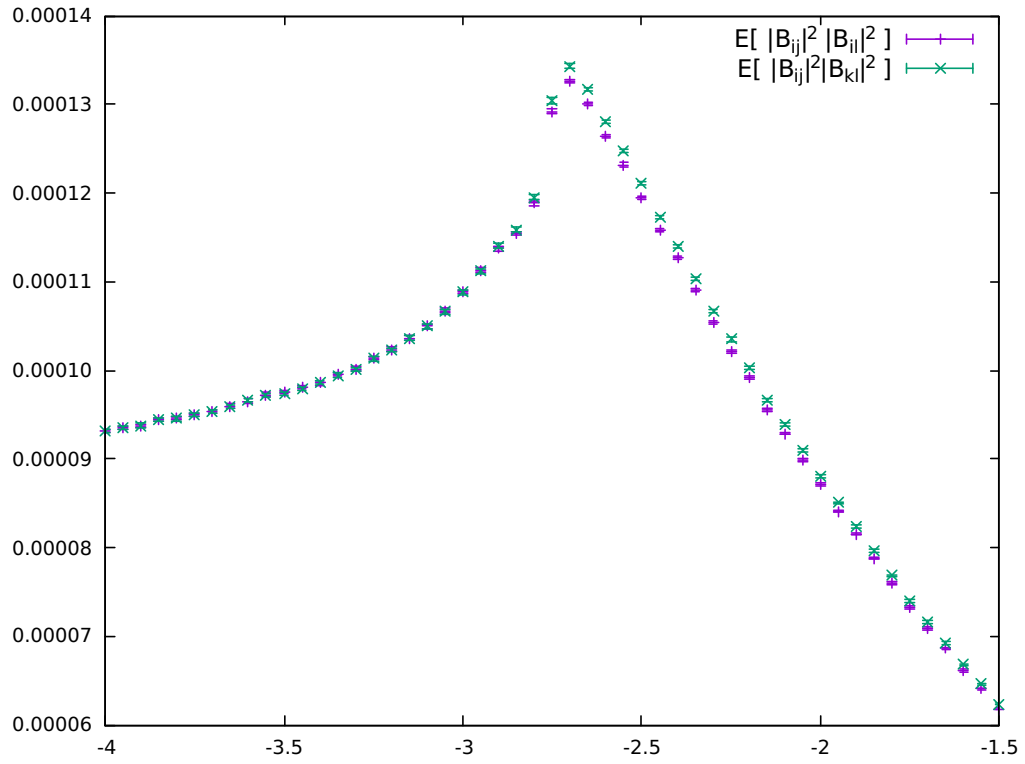


Figure 6: Expectation value of  $|B_{ij}|^2|B_{il}|^2$  (purple) and  $|B_{ij}|^2|B_{kl}|^2$  (green) versus  $g_2$ . Matrix size 20x20.

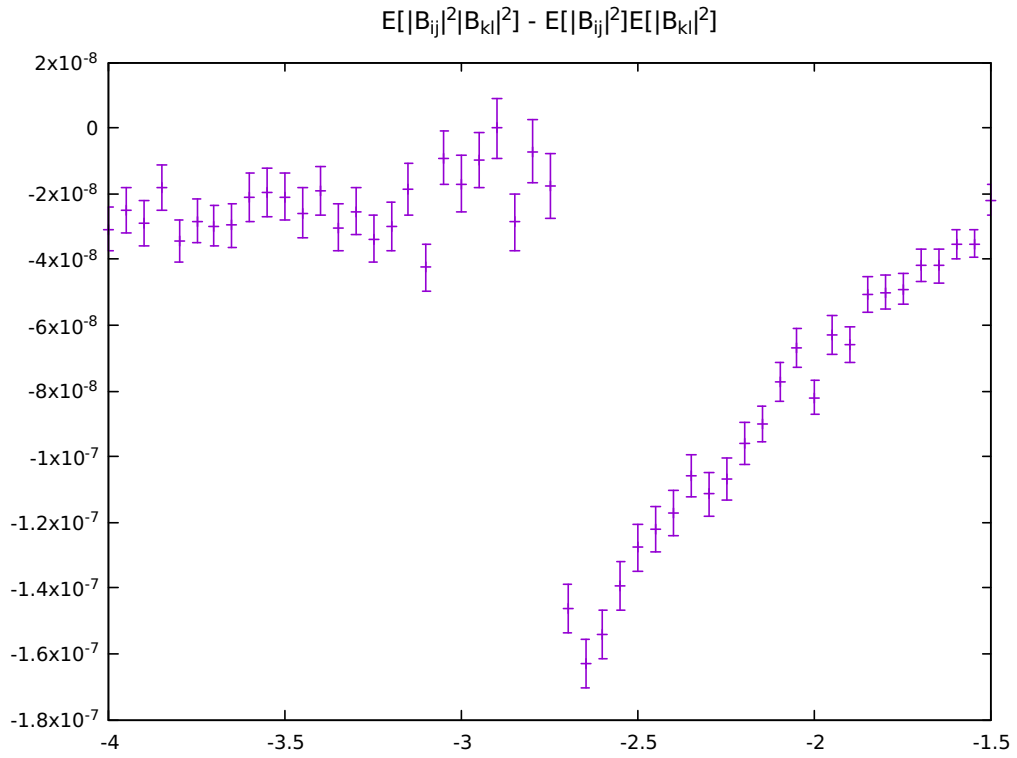


Figure 7: Statistical independence of matrix elements.  $E[|B_{ij}|^2|B_{kl}|^2] - E[|B_{ij}|^2]E[|B_{kl}|^2]$  versus  $g_2$ . Matrix size 20x20.

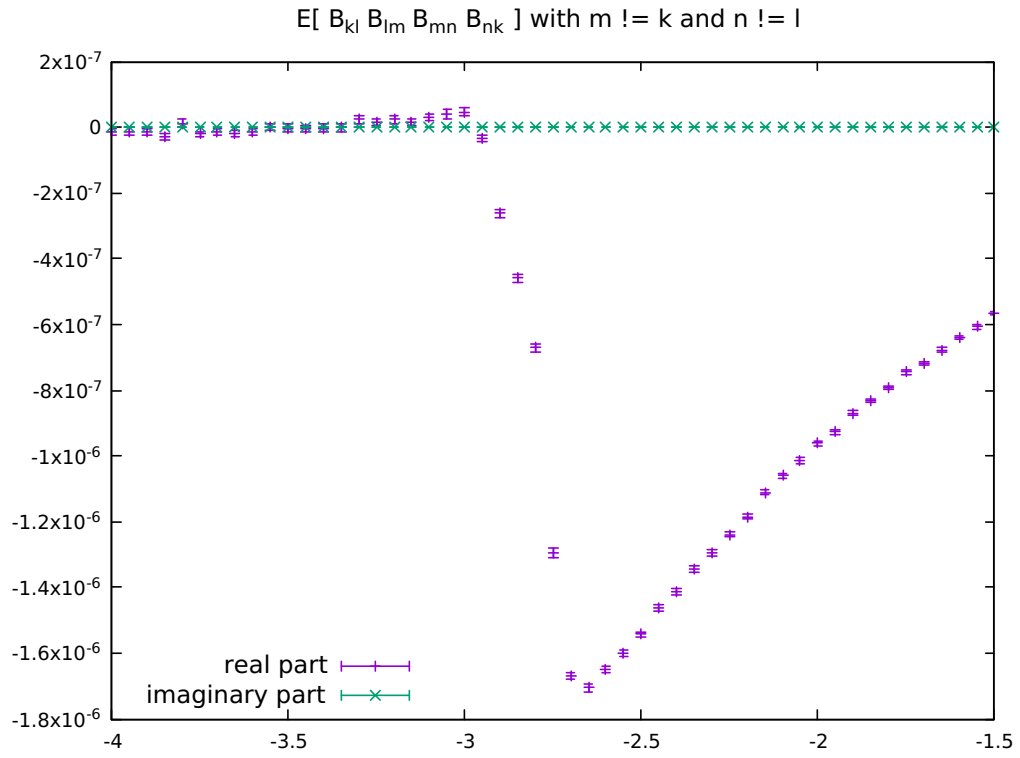


Figure 8: Expectation value of  $B_{kl}B_{lm}B_{mn}B_{nk}$  with,  $m \neq k$  and  $n \neq l$  versus  $g_2$ . Real part in purple, imaginary part in green. Matrix size 20x20.