

Question 1 Linear Embedding - GLoVe.

(a) Given the vocabulary size V and embedding dimensionality d , how many trainable parameters does the GLoVe model have?

$$V(d + 1)$$

(b) Write the gradient of the loss function with respect to one parameter vector w_i .

$$\begin{aligned}\frac{\partial L}{\partial w_i} &= 4(w_i^T w_i + 2b_i - \log X_{ii})w_i + 2 \sum_{j=1, j \neq i}^V 2(w_i^T w_j + b_i + b_j - \log X_{ij})w_j \\ &= 4(w_i^T w_i + 2b_i - \log X_{ii})w_i + \sum_{j=1, j \neq i}^V 4(w_i^T w_j + b_i + b_j - \log X_{ij})w_j \\ &= \sum_{j=1}^V 4(w_i^T w_j + b_i + b_j - \log X_{ij})w_j\end{aligned}$$

Or vectorized format,

$$\frac{\partial L}{\partial w} = 4(WW^T + b\mathbf{1}^T + \mathbf{1}b^T - \log X)W$$

(c) Implement the gradient update of GLoVe in language model.ipynb.

(d) Train the model with varying dimensionality d . Which d leads to optimal validation performance? Why does / doesn't larger d always lead to better validation error?

$d = 12$ (with learning rate 0.2) leads to the optimal validation performance.

Larger d doesn't always lead to better validation error.

As d increases, the model over-fits, causing more validation error.

Question 2 Network architecture.

(a) As above, assume we have 250 words in the dictionary and use the previous 3 words as inputs. Suppose we use a 16-dimensional word embedding and a hidden layer with 128 units. The trainable parameters of the model consist of 3 weight matrices and 2 sets of biases. What is the total number of trainable parameters in the model? Which part of the model has the largest number of trainable parameters?

For Word Embedding layer, there are $250 \times 16 = 4,000$ weight parameters. For Hidden layer, there are $48 \times 128 = 6,144$ weight parameters and 128 bias parameters. For Output layer, there are $128 \times 250 = 32,000$ weight parameters and 250 bias parameters. Totally, 42,144 weight parameters and 378 bias parameters. The Output layer has the largest number of trainable parameters.

(b) Another method for predicting the next word is an n -gram model, which was mentioned in Lecture 7. If we wanted to use an n -gram model with the same context length as our network, we'd need to store the counts of all possible 4-grams. If we stored all the counts explicitly, how many entries would this table have?

To store all the counts of 4-grams explicitly, we will get a table with $250^4 = 3,906,250,000$ entries.

Question 3 Training the Neural Network.

Write the output of `print_gradients()`.

```
loss_derivative[2, 5] 0.001112231773782498
loss_derivative[2, 121] -0.9991004720395987
loss_derivative[5, 33] 0.0001903237803173703
loss_derivative[5, 31] -0.7999757709589483

param_gradient.word_embedding_weights[27, 2] -0.27199539981936866
param_gradient.word_embedding_weights[43, 3] 0.8641722267354154
param_gradient.word_embedding_weights[22, 4] -0.2546730202374648
param_gradient.word_embedding_weights[2, 5] 0.0

param_gradient.embed_to_hid_weights[10, 2] -0.6526990313918258
param_gradient.embed_to_hid_weights[15, 3] -0.13106433000472612
param_gradient.embed_to_hid_weights[30, 9] 0.118467746181694
param_gradient.embed_to_hid_weights[35, 21] -0.10004526104604389

param_gradient.hid_bias[10] 0.2537663873815643
param_gradient.hid_bias[20] -0.03326739163635357

param_gradient.output_bias[0] -2.0627596032173052
param_gradient.output_bias[1] 0.0390200857392169
param_gradient.output_bias[2] -0.7561537928318482
param_gradient.output_bias[3] 0.21235172051123635
```

Question 4 Training the Neural Network.

(a) Pick three words from the vocabulary that go well together (for example, ‘government of united’, ‘city of new’, ‘life in the’, ‘he is the’ etc.). Use the model to predict the next word. Does the model give sensible predictions? Try to find an example where it makes a plausible prediction even though the 4-gram wasn’t present in the dataset (`raw_sentences.txt`). To help you out, the function `find_occurrences` lists the words that appear after a given 3-gram in the training set.

(b) Plot the 2-dimensional visualization using the method `tsne_plot_representation`. Look at the plot and find a few clusters of related words. What do the words in each cluster have in common? Plot the 2-dimensional visualization using the method `tsne_plot_GLoVE_representation` for a 256 dimensional embedding. How do the t-SNE embeddings for both models compare? Plot the 2-dimensional visualization using the method `plot_2d_GLoVE_representation`. How does this compare to the t-SNE embeddings? (You don’t need to include the plots with your submission.)

(c) Are the words ‘new’ and ‘york’ close together in the learned representation? Why or why not?

(d) Which pair of words is closer together in the learned representation: (‘government’, ‘political’), or (‘government’, ‘university’)? Why do you think this is?