

Понятие о вероятностном пространстве общего вида. Аксиоматическое задание вероятности, основные свойства вероятности.

Def. Bepostuocruse apacipaucibo coctait uj tpoúku
$$(A, F, P)$$

$$A - np.60 \text{ sneh. ucxogob}$$

$$F - unumcecibo noghumcecib $A (|F| = 2^{2})$

$$P: F \to [0,1] - bepostuscib.$$$$

AKCUONUN BEPOSTUDETU:

$$\gamma P(\Omega) = 1$$

2) Ecne
$$A_1, \dots, A_n, \dots$$
 - nonapus wegab. $(\forall i \neq j \mid A_i \cap A_j = \emptyset)$, to
$$P(\bigcup_{i=1}^{\infty} A_i) = \sum_{i=1}^{\infty} P(A_i)$$

Uz arcuon buteravot chaiciba:

1)
$$P(\phi) = 0$$

$$A_{i} = \begin{cases} A_{i} & i = 1 \\ \phi_{i} & i > 1 \end{cases}$$
Nonapuo uozabucu mu

$$A_{i} = \begin{cases} A, & i = 1 \\ \emptyset, & i > 1 \end{cases}$$

$$P(A_{1} \cup ... \cup A_{n}) = P(A_{1}) + P(A_{2}) + ... + P(A_{n})$$

$$P(A \cup \emptyset \cup ... \cup \emptyset) = P(A) + P(\emptyset) + ... + P(\emptyset)$$

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2)
$$A_1, \dots, A_n$$
 - nonapuo wegab. $\Rightarrow P(\bigcup_{i=1}^n A_i) = \sum_{i=1}^n P(A_i)$

3)
$$P(A) + P(\overline{A}) = 1$$

 $P(A) + P(\overline{A}) = P(A \cup \overline{A}) = P(A) = 1$

$$\mathbb{P}(A) = 1 - \mathbb{P}(A)$$

$$\mathcal{A} = A \cup \overline{A} \cup \emptyset \cup \emptyset \cup \dots$$

$$P(\Omega) = P(A) + P(A)$$

$$1 - \underline{P}(\overline{A}) = \underline{P}(A)$$

$$5)$$
 $A \subseteq B \Rightarrow P(A) \in P(B)$

$$B = A \cup B \setminus A$$

$$P(B) = P(A) + P(B \setminus A)$$

$$70$$

6)
$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$(A \cup B) = (A \setminus B) \cup (B \setminus A) \cup (A \cap B)$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

7) Непреривисть вероятисти.

• Early
$$A_1 \subset A_2 \subset A_3 \subset ...$$
, To $P(\bigcup_i A_i) = \lim_{n \to \infty} P(A_n)$

$$\bigcup_i A_i = A_1 \cup (A_1 \setminus A_2) \cup (A_2 \setminus A_3) \cup ...$$

$$P(\bigcup_i A_i) = P(A_1) + P(A_1 \setminus A_2) + P(A_2 \setminus A_3) + ...$$

$$P(\bigcup_i A_i) = \lim_{n \to \infty} \left[P(A_1) + P(A_1 \setminus A_2) + ... + P(A_n \setminus A_{n-1}) \right] = \lim_{n \to \infty} P(A_n)$$

° Ecry
$$A_1 > A_2 > A_3 > \dots$$
 To $\lim_{n \to \infty} P(A_n) = P(\bigcap_{i=1}^{\infty} A_i)$

$$\overline{A}_1 \subset \overline{A}_2 \subset \overline{A}_3 \subset \dots$$

$$\lim_{n \to \infty} P(\overline{A}_n) = P(\bigcup_{i=1}^{\infty} \overline{A}_i); \quad \lim_{n \to \infty} P(A_n) = 1 - \lim_{n \to \infty} P(A_n) = 1 - P(\overline{U}\overline{A}_i) = 1 - P(\overline{U}\overline{$$