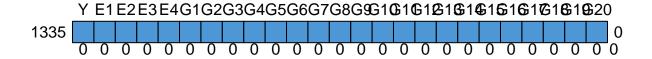
# Project 2 Code

```
getwd()
## [1] "C:/Users/Darian/Documents/Project2Files"
wdir <- "C:\\Users\\Darian\\Documents\\Project2Files"</pre>
setwd(wdir)
Project2 <- read.csv('Project2File.csv', header = TRUE)</pre>
View(Project2)
library(mice)
## Attaching package: 'mice'
## The following object is masked from 'package:stats':
##
##
       filter
## The following objects are masked from 'package:base':
##
       cbind, rbind
md.pattern(Project2)
## /\ /\
## { '---' }
## { 0 0 }
\#\# ==> V <== No need for mice. This data set is completely observed.
## \ \|/ /
   · ____,
##
```



```
Y E1 E2 E3 E4 G1 G2 G3 G4 G5 G6 G7 G8 G9 G10 G11 G12 G13 G14 G15 G16 G17
## 1335 1 1 1 1 1 1 1 1 1 1 1 1 1 1
                                                                                                                                                                                                                                                                         1
                                                                                                                                                                                                                                     1
##
                                    \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \ \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 \  \, 0 
                                                                                                                                                                                                                                     0
                                                                                                                                                                                                                                                                                            0
                                    G18 G19 G20
##
## 1335
                                      1 1 1 0
                                            0 0 0 0
##
# so there's no missing data!
#Fit a model with only environmental variables
M_E \leftarrow lm(Y \sim E1+E2+E3+E4, data=Project2)
summary(M E)
##
## Call:
## lm(formula = Y ~ E1 + E2 + E3 + E4, data = Project2)
##
## Residuals:
                                   Min
                                                                             1Q Median
                                                                                                                                                                  3Q
## -117.340 -33.634
                                                                                                 -6.576
                                                                                                                                                30.291 156.161
##
## Coefficients:
                                                                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 52.4416
                                                                                                                        13.7526
                                                                                                                                                                      3.813 0.000143 ***
## E1
                                                                     5.4026
                                                                                                                           0.9497
                                                                                                                                                                      5.689 1.57e-08 ***
```

9.196 < 2e-16 \*\*\*

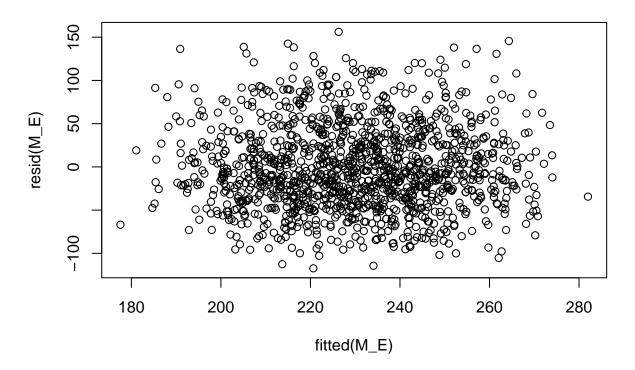
## E2

8.5733

0.9323

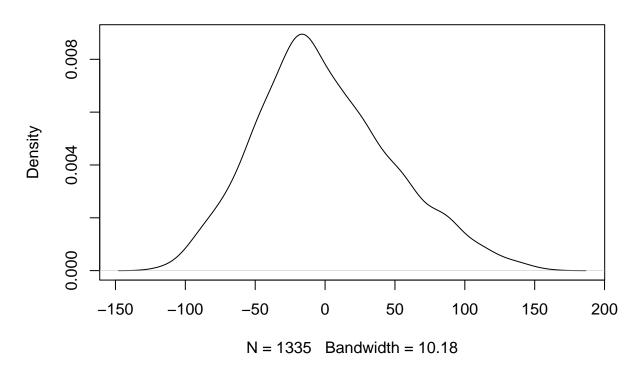
```
## E3
                7.5022
                                    8.074 1.51e-15 ***
                           0.9292
## E4
                2.1189
                           0.9379
                                    2.259 0.024028 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 48.71 on 1330 degrees of freedom
## Multiple R-squared: 0.13, Adjusted R-squared: 0.1274
## F-statistic: 49.69 on 4 and 1330 DF, p-value: < 2.2e-16
summary(M_E)$adj.r.squared
## [1] 0.1273887
plot(resid(M_E) ~ fitted(M_E), main='Environmental Residual Plot')
```

#### **Enviromental Residual Plot**



EnvironmentalDensityPlot <- resid(M\_E)
plot(density(EnvironmentalDensityPlot))</pre>

### density(x = EnvironmentalDensityPlot)



```
# Note: The above is for the model of solely environmental variables
M \text{ raw } \leftarrow lm(Y \sim
            +G17+G18+G19+G20)<sup>2</sup>, data=Project2)
summary(M_raw)
##
## Call:
G6 + G7 + G8 + G9 + G10 + G11 + G12 + G13 + G14 + G15 + G16 +
      G17 + G18 + G19 + G20)^2, data = Project2)
##
##
## Residuals:
     Min
            1Q Median
                        3Q
                              Max
## -89.06 -19.67
                0.14 19.98 89.81
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.080e+02 7.695e+01
                                  1.403 0.160774
             -4.813e+00 7.144e+00
## E1
                                 -0.674 0.500644
## E2
              5.721e+00
                       7.266e+00
                                  0.787 0.431289
## E3
              4.402e+00 7.216e+00
                                  0.610 0.542026
## E4
             -1.088e+00 7.059e+00
                                 -0.154 0.877524
## G1
              2.831e+01 2.472e+01
                                  1.145 0.252284
## G2
             -4.268e+01 2.629e+01
                                -1.624 0.104787
```

-1.187e+01 2.601e+01 -0.456 0.648295

## G3

```
## G4
               -1.008e+01 2.577e+01
                                        -0.391 0.695733
## G5
                3.466e+01
                            2.599e+01
                                         1.333 0.182703
                                         1.668 0.095673
## G6
                4.258e+01
                            2.553e+01
## G7
                                        0.316 0.751714
                8.463e+00
                            2.674e+01
## G8
               -3.026e+01
                            2.606e+01
                                        -1.161 0.245828
## G9
                2.308e+01
                            2.638e+01
                                        0.875 0.381901
## G10
                3.376e+01
                            2.527e+01
                                        1.336 0.181845
## G11
                4.980e+01
                            2.748e+01
                                        1.812 0.070222 .
## G12
               -4.104e+01
                            2.750e+01
                                        -1.492 0.135934
## G13
                4.275e+01
                            2.778e+01
                                         1.539 0.124183
## G14
               -1.158e+00
                            2.799e+01
                                        -0.041 0.967020
## G15
                1.172e+01
                            2.667e+01
                                        0.440 0.660347
## G16
                                        -2.439 0.014892 *
               -6.418e+01
                            2.631e+01
## G17
               -2.828e+00
                            2.598e+01
                                        -0.109 0.913350
## G18
                1.038e+01
                            2.602e+01
                                        0.399 0.690005
## G19
                -5.651e+01
                            2.738e+01
                                        -2.064 0.039269 *
## G20
               -8.071e+00
                                        -0.299 0.764989
                            2.699e+01
## E1:E2
                5.544e-01
                            5.354e-01
                                         1.036 0.300651
## E1:E3
                8.948e-01
                            5.394e-01
                                         1.659 0.097407
## E1:E4
                1.702e-01
                            5.465e-01
                                        0.311 0.755540
## E1:G1
               -1.020e+00
                            1.770e+00
                                        -0.577 0.564360
## E1:G2
                1.319e+00
                            1.956e+00
                                        0.674 0.500254
## E1:G3
               -1.691e+00
                            1.774e+00
                                        -0.954 0.340484
## E1:G4
                1.066e+00
                            1.718e+00
                                        0.621 0.534809
## E1:G5
               -6.853e-01
                            1.760e+00
                                        -0.389 0.697010
## E1:G6
               -2.472e+00
                            1.822e+00
                                        -1.357 0.175202
## E1:G7
                1.328e+00
                            1.714e+00
                                        0.775 0.438612
## E1:G8
                1.673e+00
                            1.802e+00
                                        0.928 0.353458
## E1:G9
               -2.810e+00
                            1.739e+00
                                        -1.616 0.106427
## E1:G10
               -4.647e+00
                            1.776e+00
                                        -2.617 0.009011 **
## E1:G11
               -3.092e+00
                            1.798e+00
                                        -1.720 0.085785
## E1:G12
               -7.069e-01
                            1.856e+00
                                        -0.381 0.703431
## E1:G13
                8.584e-05
                            1.806e+00
                                         0.000 0.999962
## E1:G14
               -4.543e-01
                            1.770e+00
                                        -0.257 0.797512
## E1:G15
               -1.345e+00
                            1.800e+00
                                        -0.747 0.455199
## E1:G16
                3.008e+00
                            1.854e+00
                                        1.623 0.104975
## E1:G17
                4.894e-01
                            1.769e+00
                                        0.277 0.782053
## E1:G18
                            1.760e+00
                                         1.623 0.104857
                2.857e+00
## E1:G19
                                         0.478 0.632426
                8.562e-01
                            1.789e+00
## E1:G20
               -2.332e+00
                            1.811e+00
                                        -1.288 0.198190
## E2:E3
               -2.010e-01
                            5.310e-01
                                        -0.379 0.705062
## E2:E4
                                        -0.222 0.824176
               -1.197e-01
                            5.387e-01
## E2:G1
               -3.327e-01
                            1.664e+00
                                        -0.200 0.841525
## E2:G2
               -4.534e-01
                            1.893e+00
                                        -0.240 0.810728
## E2:G3
               -3.238e-01
                            1.806e+00
                                        -0.179 0.857741
## E2:G4
                1.206e+00
                            1.780e+00
                                        0.678 0.498178
## E2:G5
               -1.293e-01
                            1.736e+00
                                        -0.074 0.940647
## E2:G6
                6.614e-01
                            1.759e+00
                                         0.376 0.706917
## E2:G7
                2.055e+00
                            1.789e+00
                                         1.149 0.250781
## E2:G8
                -5.851e-01
                            1.823e+00
                                        -0.321 0.748294
## E2:G9
                3.107e+00
                            1.786e+00
                                        1.739 0.082255 .
## E2:G10
                3.430e+00
                            1.777e+00
                                        1.930 0.053824 .
## E2:G11
               -1.656e+00
                           1.745e+00
                                        -0.949 0.342838
## E2:G12
               -4.293e-01 1.849e+00
                                       -0.232 0.816432
```

```
## E2:G13
               -1.432e+00 1.816e+00
                                       -0.789 0.430554
## E2:G14
               -6.236e-01
                            1.752e+00
                                       -0.356 0.722005
## E2:G15
               -1.817e-01
                            1.834e+00
                                       -0.099 0.921109
## E2:G16
                1.326e+00
                                        0.737 0.461243
                            1.798e+00
## E2:G17
               -1.564e-01
                            1.762e+00
                                       -0.089 0.929300
## E2:G18
               -4.105e+00
                            1.710e+00
                                       -2.401 0.016516 *
## E2:G19
                2.006e+00
                            1.728e+00
                                        1.161 0.245862
## E2:G20
               -9.477e-01
                            1.842e+00
                                       -0.515 0.606974
## E3:E4
               -9.079e-02
                            5.154e-01
                                        -0.176 0.860218
## E3:G1
               -1.210e+00
                            1.703e+00
                                       -0.711 0.477551
## E3:G2
                3.773e-01
                            1.800e+00
                                        0.210 0.834026
## E3:G3
                3.272e+00
                            1.799e+00
                                        1.819 0.069206
## E3:G4
               -1.157e+00
                                       -0.658 0.510912
                            1.759e+00
                                       -0.839 0.401887
## E3:G5
               -1.424e+00
                            1.698e+00
## E3:G6
                                       -0.727 0.467104
               -1.273e+00
                            1.749e+00
## E3:G7
               -1.505e+00
                            1.738e+00
                                        -0.866 0.386542
## E3:G8
                2.180e+00
                                         1.231 0.218452
                            1.770e+00
## E3:G9
               -1.705e+00
                            1.757e+00
                                        -0.970 0.332185
## E3:G10
               -2.744e+00
                            1.731e+00
                                       -1.585 0.113353
## E3:G11
                1.086e+00
                            1.737e+00
                                        0.625 0.531923
## E3:G12
                1.442e+00
                            1.813e+00
                                        0.795 0.426581
## E3:G13
               -3.903e+00
                                        -2.079 0.037890 *
                            1.878e+00
## E3:G14
                1.633e+00
                            1.826e+00
                                        0.894 0.371386
## E3:G15
                1.197e+00
                            1.811e+00
                                         0.661 0.508945
## E3:G16
                1.165e+00
                            1.730e+00
                                         0.673 0.500904
## E3:G17
                6.982e-01
                            1.713e+00
                                         0.408 0.683623
## E3:G18
               -7.821e-01
                            1.714e+00
                                        -0.456 0.648205
## E3:G19
                4.636e-01
                            1.757e+00
                                        0.264 0.791896
## E3:G20
                2.628e+00
                            1.816e+00
                                         1.447 0.148111
## E4:G1
               -2.497e+00
                                        -1.454 0.146365
                            1.718e+00
## E4:G2
                3.647e+00
                            1.817e+00
                                         2.007 0.044961 *
## E4:G3
                3.310e-01
                            1.801e+00
                                         0.184 0.854255
## E4:G4
                1.524e+00
                            1.725e+00
                                         0.884 0.377136
## E4:G5
                8.257e+00
                            1.801e+00
                                         4.584 5.13e-06 ***
## E4:G6
               -1.533e+00
                                        -0.896 0.370611
                            1.711e+00
## E4:G7
               -7.419e-01
                            1.810e+00
                                       -0.410 0.681993
## E4:G8
                2.557e-01
                            1.744e+00
                                        0.147 0.883445
## E4:G9
               -7.231e-01
                            1.774e+00
                                       -0.408 0.683569
## E4:G10
               -6.259e-01
                                       -0.359 0.720012
                            1.746e+00
                                       -0.772 0.440085
## E4:G11
               -1.350e+00
                            1.748e+00
## E4:G12
                4.796e+00
                            1.812e+00
                                         2.647 0.008255 **
## E4:G13
               -1.258e-01
                                        -0.070 0.944444
                            1.806e+00
## E4:G14
               -2.042e-01
                            1.839e+00
                                        -0.111 0.911625
## E4:G15
                4.446e-02
                            1.774e+00
                                        0.025 0.980015
## E4:G16
                2.740e+00
                            1.830e+00
                                         1.497 0.134617
## E4:G17
                7.803e-01
                            1.757e+00
                                         0.444 0.657047
## E4:G18
                3.920e-01
                            1.820e+00
                                         0.215 0.829447
## E4:G19
                3.057e+00
                            1.771e+00
                                         1.726 0.084576
## E4:G20
                6.959e-01
                            1.794e+00
                                         0.388 0.698109
## G1:G2
                2.149e+00
                            6.188e+00
                                         0.347 0.728421
## G1:G3
               -5.943e+00
                            5.873e+00
                                        -1.012 0.311799
## G1:G4
                1.697e-01
                            5.540e+00
                                        0.031 0.975576
## G1:G5
                7.924e+00 5.672e+00
                                        1.397 0.162706
## G1:G6
               -6.301e-01 5.907e+00
                                       -0.107 0.915066
```

```
## G1:G7
                -7.373e-01 5.886e+00
                                        -0.125 0.900342
## G1:G8
               -8.978e+00
                            5.644e+00
                                        -1.591 0.111974
## G1:G9
                2.479e-01
                            5.672e+00
                                         0.044 0.965144
## G1:G10
                4.085e+00
                            5.712e+00
                                         0.715 0.474659
## G1:G11
               -1.010e+01
                            5.736e+00
                                        -1.761 0.078476
## G1:G12
               -8.038e+00
                            6.132e+00
                                        -1.311 0.190212
## G1:G13
               -4.158e+00
                            5.926e+00
                                        -0.702 0.483030
## G1:G14
                9.273e+00
                            5.743e+00
                                         1.615 0.106683
## G1:G15
               -8.438e+00
                            6.008e+00
                                        -1.405 0.160464
## G1:G16
                1.126e+01
                            5.926e+00
                                         1.900 0.057676
## G1:G17
               -2.588e+00
                            5.667e+00
                                        -0.457 0.648031
## G1:G18
                1.605e+01
                            5.940e+00
                                         2.702 0.007009
## G1:G19
                            5.964e+00
                                         1.163 0.245300
                6.933e+00
## G1:G20
                5.570e+00
                            5.770e+00
                                         0.965 0.334568
## G2:G3
                2.632e+00
                            6.212e+00
                                         0.424 0.671877
## G2:G4
                8.062e+00
                            5.965e+00
                                         1.352 0.176806
## G2:G5
                                         0.894 0.371546
                5.377e+00
                            6.015e+00
## G2:G6
                -2.682e+00
                            6.358e+00
                                        -0.422 0.673308
## G2:G7
                -1.478e+01
                                        -2.185 0.029081 *
                            6.761e+00
## G2:G8
                9.342e+00
                            6.144e+00
                                         1.520 0.128695
               -4.003e+00
## G2:G9
                            5.986e+00
                                        -0.669 0.503785
## G2:G10
                            6.238e+00
                                         0.969 0.332972
                6.042e+00
## G2:G11
               -3.579e-01
                            6.151e+00
                                        -0.058 0.953615
## G2:G12
                1.379e+01
                            6.594e+00
                                         2.090 0.036821 *
## G2:G13
                5.723e+00
                            6.785e+00
                                         0.844 0.399128
## G2:G14
                4.171e+00
                            6.268e+00
                                         0.665 0.505960
## G2:G15
               -4.527e+00
                            6.188e+00
                                        -0.732 0.464620
## G2:G16
               -8.021e+00
                            6.259e+00
                                        -1.281 0.200311
## G2:G17
                2.971e+00
                            6.522e+00
                                         0.455 0.648860
## G2:G18
                            6.780e+00
                                         0.030 0.975726
                2.063e-01
## G2:G19
               -5.082e-01
                            6.274e+00
                                        -0.081 0.935452
## G2:G20
                6.407e+00
                            6.269e+00
                                         1.022 0.307012
## G3:G4
                5.060e-02
                            6.236e+00
                                         0.008 0.993528
## G3:G5
                5.065e+00
                            6.249e+00
                                         0.811 0.417818
## G3:G6
                            5.795e+00
                -6.345e+00
                                        -1.095 0.273799
## G3:G7
               -4.631e-01
                            5.754e+00
                                        -0.080 0.935866
## G3:G8
                4.058e+00
                            6.373e+00
                                         0.637 0.524361
## G3:G9
                            6.006e+00
                                        -0.347 0.728366
               -2.087e+00
                                         0.094 0.924864
## G3:G10
                5.427e-01
                            5.754e+00
## G3:G11
               -6.848e+00
                            5.914e+00
                                        -1.158 0.247163
## G3:G12
               -4.750e+00
                            6.082e+00
                                        -0.781 0.435011
## G3:G13
                                        -0.198 0.843442
               -1.210e+00
                            6.127e+00
## G3:G14
               -4.493e+00
                            6.038e+00
                                        -0.744 0.457024
## G3:G15
               -2.827e+00
                                        -0.464 0.642859
                            6.095e+00
## G3:G16
               -6.615e+00
                            6.422e+00
                                        -1.030 0.303250
## G3:G17
               -9.871e+00
                            6.168e+00
                                        -1.600 0.109800
## G3:G18
                8.043e+00
                            5.841e+00
                                         1.377 0.168859
## G3:G19
                1.052e+01
                            5.955e+00
                                         1.767 0.077587
## G3:G20
                7.284e-01
                            6.298e+00
                                         0.116 0.907953
## G4:G5
                7.893e-01
                            5.670e+00
                                         0.139 0.889320
## G4:G6
               -4.104e+00
                            5.782e+00
                                        -0.710 0.477927
## G4:G7
               -3.736e+00
                            5.970e+00
                                        -0.626 0.531551
## G4:G8
               -1.167e+00
                            5.827e+00
                                        -0.200 0.841308
## G4:G9
               -8.843e+00 5.867e+00
                                       -1.507 0.132034
```

```
## G4:G10
               -9.484e+00
                            5.655e+00
                                        -1.677 0.093852 .
## G4:G11
               -3.139e+00
                            5.805e+00
                                        -0.541 0.588764
               -5.479e+00
                            6.326e+00
                                        -0.866 0.386621
## G4:G12
## G4:G13
               -4.990e+00
                            5.875e+00
                                        -0.849 0.395889
## G4:G14
                7.257e-01
                            6.073e+00
                                         0.120 0.904900
## G4:G15
               -5.436e+00
                            6.026e+00
                                        -0.902 0.367189
## G4:G16
               -4.992e+00
                            5.861e+00
                                        -0.852 0.394555
## G4:G17
                1.735e+00
                            5.804e+00
                                         0.299 0.765041
## G4:G18
               -2.303e-01
                            6.000e+00
                                        -0.038 0.969386
## G4:G19
               -6.938e+00
                            6.046e+00
                                        -1.147 0.251479
## G4:G20
                4.159e+00
                            5.842e+00
                                         0.712 0.476652
## G5:G6
               -4.745e-01
                            6.085e+00
                                        -0.078 0.937858
## G5:G7
               -6.354e+00
                            6.075e+00
                                        -1.046 0.295886
                                        -0.204 0.838301
## G5:G8
               -1.176e+00
                            5.763e+00
## G5:G9
               -4.084e+00
                            5.887e+00
                                        -0.694 0.488016
## G5:G10
                -3.863e+00
                            5.711e+00
                                        -0.676 0.498949
## G5:G11
               -2.368e+00
                            6.276e+00
                                        -0.377 0.706013
## G5:G12
               -7.350e-01
                            6.093e+00
                                        -0.121 0.903999
## G5:G13
                1.274e-01
                            6.109e+00
                                         0.021 0.983369
## G5:G14
                -5.997e-01
                            6.144e+00
                                        -0.098 0.922269
               -2.681e+00
## G5:G15
                            6.140e+00
                                        -0.437 0.662446
## G5:G16
                6.539e+00
                            6.308e+00
                                         1.037 0.300158
## G5:G17
                            6.197e+00
                                        -0.292 0.770250
               -1.810e+00
## G5:G18
               -8.879e+00
                            6.210e+00
                                        -1.430 0.153057
## G5:G19
                9.053e+00
                            5.830e+00
                                         1.553 0.120737
## G5:G20
                8.215e-01
                            5.884e+00
                                         0.140 0.888995
## G6:G7
                -1.538e+01
                            5.968e+00
                                        -2.577 0.010114 *
## G6:G8
               -7.579e-01
                            5.942e+00
                                        -0.128 0.898543
## G6:G9
               -3.707e+00
                            5.775e+00
                                        -0.642 0.521042
## G6:G10
                            5.722e+00
                                        -0.022 0.982396
               -1.263e-01
## G6:G11
               -1.194e+01
                            5.959e+00
                                        -2.003 0.045429 *
## G6:G12
               -6.149e+00
                            6.103e+00
                                        -1.007 0.313954
## G6:G13
               -4.837e+00
                            6.264e+00
                                        -0.772 0.440188
## G6:G14
                2.295e+00
                            5.752e+00
                                         0.399 0.690043
## G6:G15
               -2.034e+00
                                        -0.340 0.734066
                            5.985e+00
## G6:G16
               -3.067e+00
                            5.999e+00
                                        -0.511 0.609337
## G6:G17
               -9.114e+00
                            5.915e+00
                                        -1.541 0.123701
## G6:G18
               -5.751e+00
                                        -1.002 0.316742
                            5.741e+00
                            5.828e+00
## G6:G19
                1.227e+01
                                         2.106 0.035433 *
## G6:G20
                9.568e+00
                            6.293e+00
                                         1.520 0.128702
## G7:G8
               -4.312e+00
                            5.670e+00
                                        -0.761 0.447128
## G7:G9
                                        -0.200 0.841207
                -1.142e+00
                            5.700e+00
## G7:G10
                2.295e+00
                            5.767e+00
                                         0.398 0.690701
## G7:G11
                3.878e+00
                            5.714e+00
                                         0.679 0.497455
## G7:G12
                4.036e+00
                            5.995e+00
                                         0.673 0.500920
## G7:G13
               -3.441e+00
                            5.931e+00
                                        -0.580 0.561877
## G7:G14
               -1.416e+01
                            5.620e+00
                                        -2.520 0.011874 *
## G7:G15
               -2.297e+00
                            5.924e+00
                                        -0.388 0.698337
                                        -0.262 0.793082
## G7:G16
               -1.564e+00
                            5.960e+00
## G7:G17
                3.621e+00
                            5.856e+00
                                         0.618 0.536523
## G7:G18
               -5.434e+00
                            5.861e+00
                                        -0.927 0.354082
## G7:G19
               -3.076e-03
                            5.988e+00
                                        -0.001 0.999590
## G7:G20
               -1.489e+00
                            6.273e+00
                                        -0.237 0.812398
## G8:G9
                1.482e+01 5.765e+00
                                         2.570 0.010311 *
```

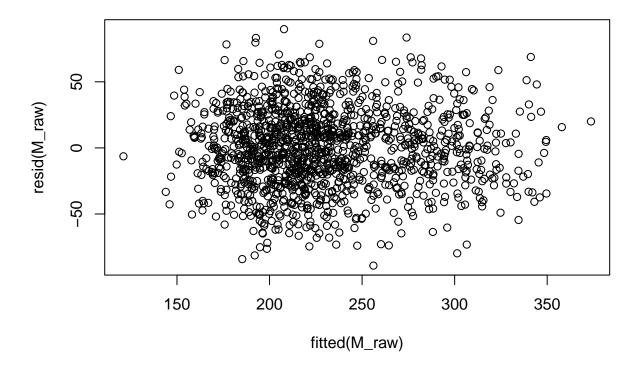
```
## G8:G10
               -1.440e+01
                            6.031e+00
                                        -2.387 0.017165 *
## G8:G11
               -3.596e+00
                            5.869e+00
                                        -0.613 0.540126
## G8:G12
                7.272e+00
                            5.856e+00
                                         1.242 0.214569
## G8:G13
                1.710e+00
                                         0.277 0.781547
                            6.165e+00
## G8:G14
                5.826e+00
                            5.879e+00
                                         0.991 0.321934
## G8:G15
               -5.837e+00
                            6.143e+00
                                        -0.950 0.342258
## G8:G16
                4.542e+00
                            6.272e+00
                                         0.724 0.469200
## G8:G17
               -3.664e+00
                            6.078e+00
                                        -0.603 0.546780
## G8:G18
                1.062e+01
                            6.004e+00
                                         1.769 0.077194 .
## G8:G19
               -2.410e+00
                            6.108e+00
                                        -0.395 0.693214
## G8:G20
               -5.548e+00
                            6.141e+00
                                        -0.903 0.366546
## G9:G10
               -4.262e+00
                            5.750e+00
                                        -0.741 0.458813
## G9:G11
               -2.308e+00
                            5.709e+00
                                        -0.404 0.686163
## G9:G12
                4.027e+00
                            6.097e+00
                                         0.660 0.509112
## G9:G13
                8.747e+00
                            5.941e+00
                                         1.472 0.141227
## G9:G14
                1.966e+00
                            5.841e+00
                                         0.337 0.736420
## G9:G15
                            5.848e+00
                                         0.605 0.545163
                3.539e+00
## G9:G16
                            5.854e+00
                                        -1.309 0.190715
               -7.665e+00
## G9:G17
                            5.884e+00
                                        -0.333 0.739563
               -1.957e+00
## G9:G18
               -1.169e+00
                            5.800e+00
                                        -0.201 0.840363
## G9:G19
               -2.246e-01
                            5.793e+00
                                        -0.039 0.969080
## G9:G20
               -9.235e+00
                            5.921e+00
                                        -1.560 0.119116
## G10:G11
                1.222e+01
                            5.957e+00
                                         2.052 0.040459 *
## G10:G12
               -3.593e+00
                            6.330e+00
                                        -0.568 0.570405
## G10:G13
                5.799e+00
                            6.143e+00
                                         0.944 0.345371
## G10:G14
                1.305e+00
                            5.701e+00
                                         0.229 0.818964
## G10:G15
                4.161e+00
                            5.616e+00
                                         0.741 0.458927
## G10:G16
               -6.996e+00
                            6.158e+00
                                        -1.136 0.256148
## G10:G17
                1.322e+00
                            5.679e+00
                                         0.233 0.816019
## G10:G18
                                        -0.694 0.487922
               -3.851e+00
                            5.550e+00
## G10:G19
               -5.286e-01
                            6.099e+00
                                        -0.087 0.930955
## G10:G20
                3.206e+00
                            5.999e+00
                                         0.534 0.593217
## G11:G12
                3.865e-01
                            5.879e+00
                                         0.066 0.947597
               -2.631e+00
## G11:G13
                            5.872e+00
                                        -0.448 0.654172
## G11:G14
                            5.849e+00
                                        -1.304 0.192496
                -7.627e+00
## G11:G15
               -3.362e+00
                            6.084e+00
                                        -0.553 0.580674
## G11:G16
                8.907e+00
                            5.699e+00
                                         1.563 0.118421
## G11:G17
                                        -1.589 0.112461
               -9.479e+00
                            5.967e+00
                                        -0.845 0.398274
## G11:G18
               -5.376e+00
                            6.361e+00
## G11:G19
               -4.387e+00
                            5.703e+00
                                        -0.769 0.441878
## G11:G20
                3.656e+00
                            5.986e+00
                                         0.611 0.541449
## G12:G13
                                         1.257 0.209094
                8.192e+00
                            6.518e+00
## G12:G14
               -1.419e-01
                            6.014e+00
                                        -0.024 0.981185
## G12:G15
               -2.982e+00
                            6.069e+00
                                        -0.491 0.623291
## G12:G16
                1.577e-01
                            6.080e+00
                                         0.026 0.979309
                                        -0.227 0.820628
## G12:G17
               -1.439e+00
                            6.346e+00
## G12:G18
               -1.023e+01
                            6.152e+00
                                        -1.664 0.096484 .
## G12:G19
               -3.146e-01
                            5.736e+00
                                        -0.055 0.956270
## G12:G20
                1.002e+01
                            6.409e+00
                                         1.563 0.118409
## G13:G14
                -1.150e+01
                            6.230e+00
                                        -1.846 0.065185
## G13:G15
               -3.707e+00
                            6.122e+00
                                        -0.606 0.544914
## G13:G16
               -1.138e+00
                            6.580e+00
                                        -0.173 0.862773
## G13:G17
               -1.668e+00
                            6.261e+00
                                        -0.266 0.790017
## G13:G18
                1.276e+01 6.180e+00
                                         2.064 0.039265 *
```

```
## G13:G19
              5.577e+00 5.968e+00 0.934 0.350302
## G13:G20
              -1.600e+00 6.206e+00 -0.258 0.796622
## G14:G15
              -1.636e+00 5.794e+00 -0.282 0.777782
## G14:G16
              4.161e+00 6.155e+00 0.676 0.499195
## G14:G17
              -1.219e+00 5.792e+00 -0.211 0.833307
## G14:G18
             -3.272e+00 6.003e+00 -0.545 0.585828
## G14:G19
              -5.776e-01 6.001e+00 -0.096 0.923346
              1.886e+00 6.007e+00 0.314 0.753591
## G14:G20
## G15:G16
              -1.869e+00 6.203e+00 -0.301 0.763179
## G15:G17
              -4.719e+00 5.867e+00 -0.804 0.421355
## G15:G18
              -7.342e-01 5.760e+00 -0.127 0.898605
## G15:G19
              -9.768e+00 6.346e+00 -1.539 0.124076
## G15:G20
              -3.235e+00 6.176e+00 -0.524 0.600528
## G16:G17
              -6.417e-01 6.040e+00 -0.106 0.915405
## G16:G18
             2.352e+01 6.602e+00 3.563 0.000384 ***
## G16:G19
              5.504e+00 6.153e+00 0.895 0.371254
## G16:G20
              -2.586e-01 6.053e+00 -0.043 0.965935
## G17:G18
              -5.580e+00 5.929e+00 -0.941 0.346881
## G17:G19
              2.738e+00 5.964e+00
                                    0.459 0.646346
## G17:G20
              -1.025e+01 5.891e+00 -1.740 0.082130 .
## G18:G19
              4.706e+00 5.960e+00 0.790 0.429918
## G18:G20
              1.629e+00 6.192e+00
                                    0.263 0.792533
## G19:G20
              4.131e+00 6.286e+00 0.657 0.511179
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 34.1 on 1034 degrees of freedom
## Multiple R-squared: 0.6686, Adjusted R-squared: 0.5725
## F-statistic: 6.955 on 300 and 1034 DF, p-value: < 2.2e-16
summary(M_raw)$adj.r.squared
```

#### ## [1] 0.5724978

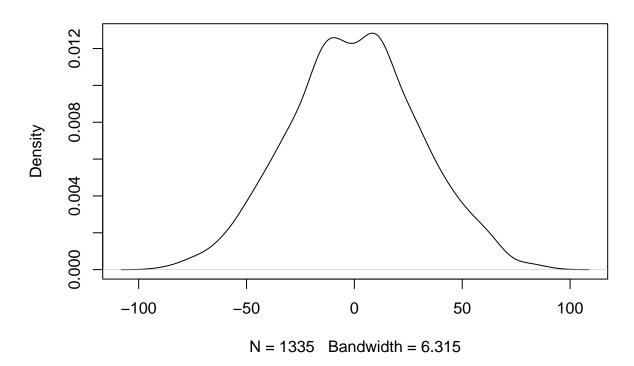
```
plot(resid(M_raw) ~ fitted(M_raw), main='Residual Plot of E and G variables')
```

# Residual Plot of E and G variables



EandGVariables <- resid(M\_raw)
plot(density(EandGVariables))</pre>

# density(x = EandGVariables)



#Note: The above is when you add the Genetic Risk variables (G1-G20)
#to the model of solely Environmental Variables (E1-E4)
library(MASS)
boxcox(M\_raw)

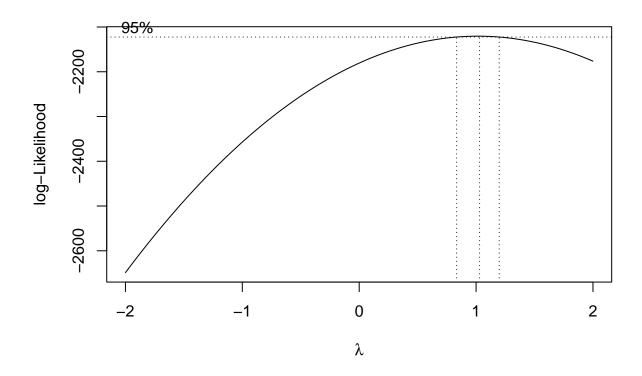


Table 1: Model Summary

model	adjR2	BIC
(Intercept)+E4:G5	0.43196826092255	-741.654359289457
(Intercept)+E2:E3+E4:G5	0.545292974444172	-1032.52906776033
(Intercept)+E1+E2:E3+E4:G5	0.564726664912446	-1084.64663692343
(Intercept)+E1+E2:E3+E4:G5+G8:G10	0.569154992455663	-1092.10474370241
(Intercept)+E1+E2:E3+E4:G5+G8:G10+G16:G18	0.571429463384136	-1092.97845159909

```
#3rd model seems best
M_main <- lm( I(Y) ~ ., data=Project2)
# . here means include all variable from E1 to E4 and from G1 to G20 to the model
temp <- summary(M_main)
kable(temp$coefficients[ abs(temp$coefficients[,4]) <= 0.001,], caption='Significant
Coefficients')</pre>
```

Table 2: Significant Coefficients

	Estimate	Std. Error	t value	$\Pr(> t )$
$\overline{\mathrm{E1}}$	5.302005	0.6801322	7.795551	0.00e+00
E2	8.425682	0.6679685	12.613891	0.00e+00
E3	8.681027	0.6681455	12.992719	0.00e+00
E4	2.650846	0.6721911	3.943590	8.45 e-05
G5	80.129066	2.2351989	35.848740	0.00e+00

```
M_2nd <- lm(I(Y) ~ (.)^2, data=Project2)
temp <- summary(M_2nd)
kable(temp$coefficients[ abs(temp$coefficients[,4]) <= 0.001,], caption='2nd Interaction')</pre>
```

Table 3: 2nd Interaction

	Estimate	Std. Error	t value	$\Pr(> t )$
E4:G5 G16:G18	$8.256925 \\ 23.519912$	$\begin{array}{c} 1.801432 \\ 6.601676 \end{array}$	1.000001	0.0000051 $0.0003838$

```
#variables that have significant 2nd interaction effects
M_3rd <- lm(I(Y) ~ (E1+E2+E3+E4+G5)^3, data=Project2)
temp <- summary(M_3rd)
kable(temp$coefficients[ abs(temp$coefficients[,4]) <= 0.001,], caption='3nd Interaction')</pre>
```

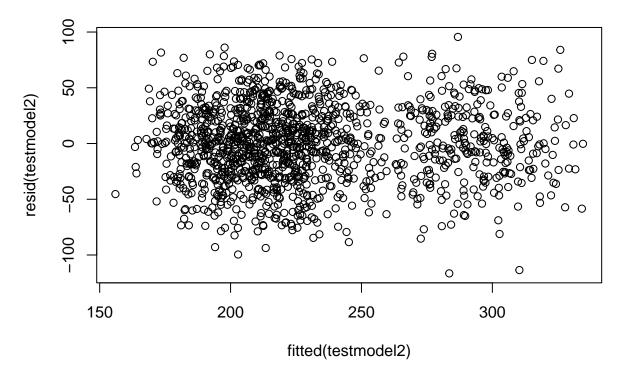
Table 4: 3nd Interaction

```
Estimate Std. Error t value Pr(>|t|)
```

```
#The variables that I use as candidate variables for inclusion are: E1, E2, E3, E4, G5, testmodel2 <- lm(Y \sim (E1 + E2 + E3 + E4 + G5), data=Project2) summary(testmodel2)
```

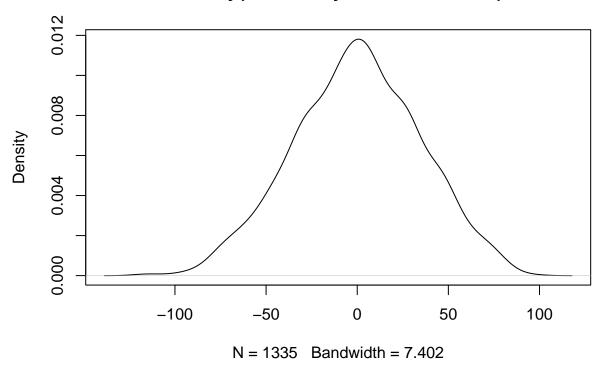
```
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                            9.8470
  (Intercept) 22.4559
                                     2.280
                 5.2817
                            0.6776
                                     7.795 1.29e-14 ***
## E1
## E2
                 8.4961
                            0.6651
                                    12.774
                                           < 2e-16
## E3
                 8.5514
                            0.6635
                                    12.888
                                           < 2e-16 ***
## E4
                 2.6919
                            0.6693
                                     4.022 6.10e-05 ***
                79.7722
                            2.2261
                                    35.835
                                           < 2e-16 ***
## G5
##
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 34.75 on 1329 degrees of freedom
## Multiple R-squared: 0.5575, Adjusted R-squared: 0.5559
## F-statistic: 334.9 on 5 and 1329 DF, p-value: < 2.2e-16
plot(resid(testmodel2)~fitted(testmodel2), main = 'Residual Plot of Final Model')
```

#### **Residual Plot of Final Model**



```
DensityPlotOfFinalModel <- resid(testmodel2)
plot(density(DensityPlotOfFinalModel))</pre>
```

### density(x = DensityPlotOfFinalModel)

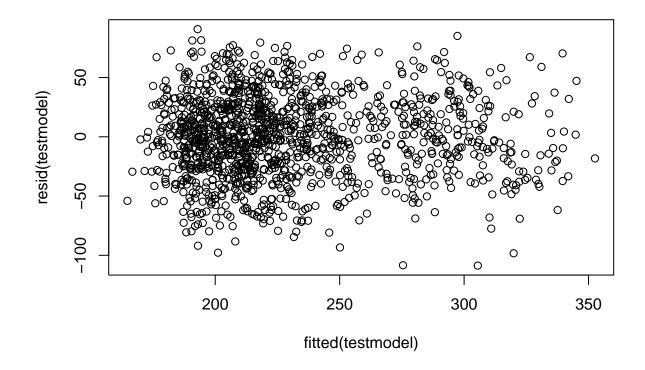


```
#adjusted r^2 is .5559
testmodel <- lm(Y ~ (E1+E2:E3+E4:G5), data=Project2)
summary(testmodel)</pre>
```

```
##
## lm(formula = Y \sim (E1 + E2:E3 + E4:G5), data = Project2)
##
## Residuals:
       Min
                       Median
##
                  1Q
                                    ЗQ
                                            Max
## -108.699 -24.004
                       -0.286
                                24.377
                                         90.845
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 108.90384
                            6.07912 17.914 < 2e-16 ***
## E1
                 5.20955
                            0.66993
                                     7.776 1.49e-14 ***
## E2:E3
                            0.06007 18.409 < 2e-16 ***
                 1.10583
                            0.28905 36.829 < 2e-16 ***
## E4:G5
                10.64537
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
\#\# Residual standard error: 34.4 on 1331 degrees of freedom
## Multiple R-squared: 0.5657, Adjusted R-squared: 0.5647
## F-statistic: 577.9 on 3 and 1331 DF, p-value: < 2.2e-16
```

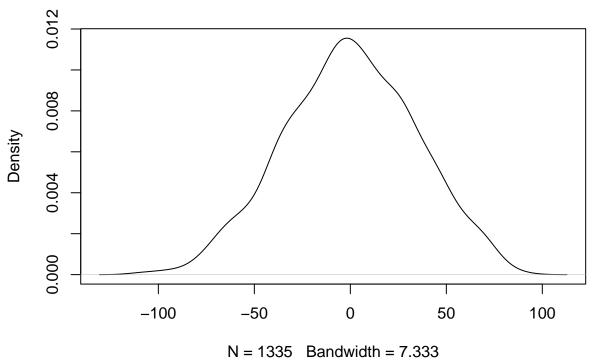
```
#adjusted r^2 is .5647
plot(resid(testmodel)~fitted(testmodel), main = 'Residual Plot of 3rd model')
```

# **Residual Plot of 3rd model**



ThirdModel<- resid(testmodel)
plot(density(ThirdModel))</pre>

## density(x = ThirdModel)



```
M_2stage <- lm( I(Y) ~ (E1+E2+E3+E4+G5)^3, data=Project2)
temp <- summary(M_2stage)
temp$coefficients</pre>
```

```
##
                   Estimate
                            Std. Error
                                            t value Pr(>|t|)
   (Intercept) -48.38368484 299.6529535 -0.161465737 0.8717515
##
## E1
                36.18423563
                            34.2392242
                                        1.056806526 0.2907949
## E2
               -2.72619425
                            34.8315815 -0.078267886 0.9376269
## E3
                                        0.349068439 0.7270941
                11.46773114
                            32.8523861
## E4
                17.33802245
                            33.8415116
                                        0.512330024 0.6085065
## G5
               -24.26368451 148.8058183 -0.163056020 0.8704995
## E1:E2
                -0.99824932
                             3.7428223 -0.266710317 0.7897342
                -3.15375325
                             3.6090690 -0.873841208 0.3823650
## E1:E3
## E1:E4
                -4.68161986
                             3.6336264 -1.288415295 0.1978291
                0.99838004
## E1:G5
                            14.3483782 0.069581386 0.9445375
## E2:E3
                2.36607300
                             3.5682169
                                        0.663096736 0.5073853
## E2:E4
                0.65171461
                             3.6708674
                                        0.177536953 0.8591141
## E2:G5
                18.38661933
                            13.8890572
                                        1.323820549 0.1857938
## E3:E4
                -0.14961669
                             3.5892511 -0.041684653 0.9667564
## E3:G5
                3.00945323
                            13.9141246
                                        0.216287644 0.8287972
## E4:G5
                0.09331295
                            14.2699040
                                        0.006539144 0.9947836
## E1:E2:E3
                             0.3336071
                                        0.118644812 0.9055750
                0.03958075
## E1:E2:E4
                 0.22578120
                             ## E1:E2:G5
                -1.78575436
                             1.1154576 -1.600916363 0.1096367
## E1:E3:E4
                 0.36856326
                             0.3332076 1.106107057 0.2688834
```

```
0.35640396
## E1:E3:G5
                        1.0722618  0.332385196  0.7396516
## E1:E4:G5
             1.04094601 1.1997806 0.867613655 0.3857649
## E2:E3:E4
             ## E2:E3:G5
             -0.91992062
                        1.0245983 -0.897835364 0.3694384
                        1.1039916 0.067118778 0.9464974
## E2:E4:G5
              0.07409856
## E3:E4:G5
              0.08974351
                        1.0598332 0.084677020 0.9325311
temp$coefficients[abs(temp$coefficients[,3]) >= 4]
```

## numeric(0)