

# Computer Science Course Notes — 1st Semester

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# Distributed Systems

## First Lecture

DA RECUPERARE !!!

A Space-Time diagram shows the evolution of a distributed system over time, it is composed of a number of timelines, each associated to a process  $p_i$ . Events, occur across this timelines, and are represented by points on the diagram. If an event  $e_1$  is causally related to another event  $e_2$ , then  $e_1$  is to the left of  $e_2$  and there is a line connecting them.

## Second Lecture

### Definitions

We now give a set of formal definitions for very natural concepts in distributed systems.

We define the *history* of a process  $p_i$  as the sequence of all events that occur in the timeline of  $p_i$ .

$$h_i = \langle e_i^1, e_i^2, \dots, e_i^n \rangle$$

We can then have the history of the computation, which is a collection of all the histories of all the processes.

$$H = \langle h_1, h_2, \dots, h_n \rangle$$

A *prefix history* is a sequence of events that occur in the timeline of a process up to a certain point.

$$h_i^k = \langle e_i^1, e_i^2, \dots, e_i^k \rangle$$

A *local state* of process  $i$  after event  $e_i^k$  is the result of the computation up to that point, and is denoted as  $\sigma_i^k$ .

A *global state* is the collection of all local states of all processes at a certain point in time.

$$\sigma^k = \langle \sigma_1^k, \sigma_2^k, \dots, \sigma_n^k \rangle$$

A *run*  $k'$  is a total re-ordering of the events such that the internal order of every process is preserved. This means that a *run* allows the interleaving of the events of different processes, but does not break the order of events in the history of a single process.

A *cut*  $C$  is a collection of the prefixes of every processes' history up to a certain point.

### Consistency

A cut  $C$  is said to be *consistent* iff:

$$e \rightarrow e' \wedge e' \in C \Rightarrow e \in C$$

Or, in other words, if an event is in the cut, then all the events that causally precede it are also in the cut.

By sequentializing the events in a run and extracting a prefix, we can trivially obtain a consistent cut.

### Consistency of Intersection

A possible course exercise is, given two cuts  $C_1$  and  $C_2$ , to prove that their intersection is also a consistent cut.

Given the definition of consistency accommodated for the intersection of two cuts:

$$e \rightarrow e' \wedge e' \in C_1 \cap C_2 \Rightarrow e \in C_1 \cap C_2$$

We know that if  $e'$  is in the intersection, then it is in both  $C_1$  and  $C_2$ . By the definition of consistency, we know that  $e$  must be in both  $C_1$  and  $C_2$ , and therefore in their intersection.

Formally:

$$e \rightarrow e' \wedge e' \in C_1 \rightarrow e \in C_1$$

$$e \rightarrow e' \wedge e' \in C_2 \rightarrow e \in C_2$$

Therefore:

$$e \rightarrow e' \wedge e' \in C_1 \cap C_2 \rightarrow e \in C_1 \wedge e \in C_2 \rightarrow e \in C_1 \cap C_2$$

### Consistency of Union

Given two consistent cuts  $C_1$  and  $C_2$ , we can prove that their union is also a consistent cut.

Given the definition of consistency accomodated for the union of two cuts:

$$e \rightarrow e' \wedge e' \in C_1 \cup C_2 \Rightarrow e \in C_1 \cup C_2$$

Then, formally:

$$e \rightarrow e' \wedge e' \in C_1 \rightarrow e \in C_1$$

$$e \rightarrow e' \wedge e' \in C_2 \rightarrow e \in C_2$$

Therefore:

$$e \rightarrow e' \wedge e' \in C_1 \cup C_2 \rightarrow e \in C_1 \vee e \in C_2 \rightarrow e \in C_1 \cup C_2$$

### Run Reconstruction

Assume that we have a set of processes  $P = \{p_1, p_2, p_3, \dots\}$ , and a monitor process  $p_0$  that is responsible for detecting deadlocks.

Everytime that an event is generated, its responsible process sends a message to the monitor, which then updates its local state.

The monitor process can then reconstruct the run by aggregating the local process states into a global state.

Assuming asynchrony and unbounded message delays, the monitor process does not reconstruct a run, since the order of the individual processes can be inverted.

If we assume a FIFO message delivery, then the monitor process can reconstruct a run. This can be trivially achieved by having a sequence number, in a system such as TCP.

This does *not* recover consistency, since the order of separate processes can still be inverted. However, this level of *local consistency* is sufficient for deadlock detection.

### Simplifying Assumptions for Consistency

Assume that I have:

1. A finite  $\delta_i$  notification delay on each process  $p_i$ .
2. A global clock  $C$  that is synchronized with all processes. We call an idealized version of this clock *Real Clock* (RC).

Then, the monitor process can offline-reconstruct a run by using the global clock to order the events.

Online-reconstruction can be achieved (and is preferred) by exploiting the additional  $\delta_i$  information. Once we receive a notification, we await time  $\max \delta_i$  before committing the event to the global state, in the meantime, we store the event in a buffer that is ordered by the global clock.

### Real Clock Property

The clock property relates the *happens before* relation of messages to the real time of the system.

$$e \rightarrow e' \Rightarrow TS(e) < TS(e')$$

We can obtain a trivial clock by designing a system as such:

1. Each process has associates a sequence number  $k \in \mathbb{N}$  to each event.
2. Each event  $i$ , which receives a message  $m$  from event  $j$ , has a sequence number given by the formula  $\max(k_i, k_j) + 1$ .

This gives us the clock property *by construction*, since each event has a sequence number that is always greater than the sequence number of the event that caused it and of any event that it is casually related to.

This device is called a *Lamport Clock*, or a *Logical Clock*.

### History of an event

Given an event  $e$ , we can define its history as the sequence of events that causally precede it. These are all the events that the monitor process must have received before the event  $e$  is committed to the global state.

$$\Theta(e) = \{e' \mid e' \rightarrow e\}$$

This is a *consistent* cut.



**Opaque detection of consistent cuts**

Given a notification about an event, for example,  $e_5^4$ , the monitor process can ensure that  $e_1^4$  can be committed to global state by checking that for every process, we have received a notification with lamport clock  $\geq 4$ .

We might have some processes that consistently lag behind, and therefore do not reach the lamport clock in a timely manner. We can trivially solve this by sending a liveness check to all processes for which a sufficiently high lamport number has not been received. If the process is alive but not working, it will re-adjust its lamport clock and send a notification.

This will not impact throughput, since the monitor process is not a bottleneck, and the liveness check is a very lightweight operation, that is performed only when necessary.

**Building a Better Clock**

We can build a *better clock*, that is, one with the enhanced property:

$$e \rightarrow e' \iff TS(e) < TS(e')$$

This is called a *Vector Clock*.

It works by communicating the history of the current event in a compact way, we do this by sending a vector of length  $n$  where  $n$  is the number of processes in the system. The vector's entries are updated to be the highest lamport number detected for that relative process, either from a message that has been received, or from the local lamport clock (in the case of the current process).

This allows us to check whether:

$$VC(e) \subseteq VC(e')$$

$$e \rightarrow e' \iff VC(e) \subseteq VC(e')$$

When messages are sent, the vector clock is attached to the message, and the receiving process updates its vector clock by taking the maximum of the two vectors, and summing 1 to the current process.

The monitor process  $p_0$  keeps track of its own vector, where each entry is the highest lamport number that it has received from each process. When it receives a notification, if the vector clock is consistent with the monitor's vector clock, then the event is committed to the global state.

Since vectors are *not* sets, we have to use component-wise comparison to check for causality.

$$VC(e) < VC(e') \iff \forall i \in \{1, 2, \dots, n\} \quad VC(e)_i < VC(e')_i$$

So we are back to the original definition of the happens before relation.

## Third Lecture

We now discuss some more advanced vector clock properties.

### Vector Clock Properties

#### Strong Clock Property

Assume we have two events  $e$  and  $e'$ . Then, we have that:

$$e \rightarrow e' \iff VC(e) \leq^* VC(e')$$

Where  $\leq^*$  is a *partial order* relation, such as:

$$\forall VC(e_i)[k] \leq VC(e_j)[k] \quad \wedge \quad \exists k' VC(e_i)[k'] < VC(e_j)[k']$$

Meaning that all the elements of the vector clock of  $e$  are less than or equal to the corresponding elements of the vector clock of  $e'$ , and at least one element is strictly less, so that we have a *strict* partial order.

#### Retrieving History Cardinality

Given a vector clock  $VC(e)$ , we can retrieve the number of events that causally precede it by taking the sum of all the elements of the vector clock.

$$|\Theta(e)| = \sum_{i=1}^n VC(e)[i]$$

#### Retrieving Causality

Given two events  $e_i$  and  $e_j$ , we can check whether they are causally related by checking the vector clocks.

$$e_i \rightarrow e_j \iff VC(e_i)[i] \leq VC(e_j)[i]$$

#### Existence of a Causal Event

We want to check whether

$$\exists e_k : \neg(e_k \rightarrow e_i) \wedge (e_k \rightarrow e_j)$$

This is true if and only if:

$$\exists k : VC(e_i)[k] < VC(e_j)[k]$$

Meaning that there is a certain event that ticked the clock of  $e_j$  but not the clock of  $e_i$ .

## Snapshots

Now we assume that the processes do *not* send notifications, rather, the monitoring process  $p_0$  polls processes with a snapshot request.

This was already discussed in the first lecture, and we know that what we retrieve cannot retrieve a consistent cut.

We can change the protocol to improve this method. Now  $p_0$  sends a snapshot request to all processes, however, when a process receives a snapshot request, it has to broadcast it to any other process.

Only requests from  $p_0$  are broadcasted, so that we do not flood the network with snapshot requests.

When a process receives a snapshot request, it sends a snapshot of its local state to  $p_0$ .

With this behavior, under the reasonable FIFO-channel assumption, we can reconstruct a consistent cut.

## Proof of Consistency

Assume that we have  $e_i$  and  $e_j$  such that  $e_i \rightarrow e_j$ , and that  $e_j$  is in the snapshot  $C$ , we want to prove that  $e_i$  is also in the snapshot.

By contradiction, assume that  $e_i \notin C$ , then  $p_i$  received the snapshot request before  $e_i$ , but then, since the channels are FIFO, and  $e_j$  was spawned by a received message from  $p_i$ , then the broadcasted snapshot request sent to  $p_j$  reached  $p_j$  before  $e_j$  was spawned, and therefore  $e_j$  is also *not* in the snapshot.

This protocol is known as the *Chandy-Lamport* protocol.

## Fourth Lecture

We want to design a protocol for *atomic commits*, this protocol should have the following properties:

1. If processes reach a decision (commit/abort), it must be the same one.
2. A process cannot reverse its decision after reaching it.
3. The commit decision can be reached only if all processes vote *Yes*.
4. If *there are no failures*, and all processes vote *Yes*, then the commit decision is reached.

Naturally, this could be satisfied by a *trivial* protocol, such as one that *always* aborts, or one that *always* commits. These protocols are not useful since they are not *safe*.

## Generic Properties of Distributed Systems

Usually, there are two sets in which properties can be divided:

1. *Safety* properties, which basically ask “*if* something happens, it does not go *wrong*”.
2. *Liveness* properties, which basically ask “*if* time goes on, *something* will happen”.

You can trivially satisfy safety by doing nothing, you can trivially satisfy liveness by doing anything.

You *want* a tradeoff, such that you get as much liveness as possible while preserving safety.

## Two-Phase Commit

We assume the existence of *two* different processes, *coordinators* and *participants*, we describe the protocol as follows:

1. The coordinator sends a *Prepare* message to all participants.
2. The participants decide Yes/No and send the vote to the coordinator. If a participant votes *No*, then the coordinator must abort.
3. The coordinator receives all votes, if all votes are *Yes*, then the coordinator sends a *Commit* message to all participants, otherwise it sends an *Abort* message.
4. The participants apply the decision.

If the coordinator fails, then the participants will communicate with each other to reach a decision.

If a vote fails to reach the coordinator after a certain timeout period, it will be assumed to be a *No* vote. This preserves the safety property.

This protocol satisfies the properties of atomic commits, and is known as the *Two-Phase Commit* protocol. This is *not* a *live* protocol, since it can deadlock/timeout.

## Logs

Logs are a sequence of events that are written to a file, and are used to recover the state of a system in case of failure. We assume the records to be consistent, so that system failures do not corrupt the log. This means that the log is written to a stable storage, such as a disk.

Logs allow a system to be fault-tolerant since they can be used to recover the state of the system in case of failure.

You can have *two* types of behavior when logging, depending on the order of the operations:

- Log and then act
- Act and then log

In both cases, you might *die* in the middle of the operation, and you might have to recover the state of the system. Both systems are recoverable as a coordinator, but you *must* act in a consistent way to recover the state of the system.

As a participant, recoverability is *not* guaranteed if you act before you log. The best way to ensure recoverability is to log before you act, so that you can be sure about if you voted *Yes* or *No* before you die.

If your vote was *No*, then you can *always* abort, if your vote was *Yes*, then you can re-send the vote to the coordinator, and await the decision.

## Fifth Lecture

### Paxos

The previous lecture was a specific case of a more general problem, that of *consensus*.

In the consensus problem, we have a set of processes that must agree on a certain value, and we want to ensure that the value is agreed upon by all processes.

#### Informal Description

Paxos is an asynchronous protocol that solves the consensus problem. It has been developed by Leslie Lamport, and is used in many distributed systems.

Paxos is *more* live than the Two-Phase Commit protocol, since it can recover from failures and timeouts.

Paxos is in essence a *replication system*, meaning that you want to replicate values across multiple processes (that are potentially distributed across multiple machines) in a fault-tolerant way.

Paxos is capable of obtaining consensus on a *single value*, obtaining consensus across a *sequence* requires running *multiple instances* of the protocol.

By *faults* we are referring to *crashes*, that is, the possibility that a process might stop working. Processes could eventually recover, but there is no way to know and no way to guarantee that they will.

#### Structure of the Problem

We first start by defining different classes of processes that participate in the protocol:

1. *Acceptors*: Their role is to vote on whether a value is accepted or not.
2. *Proposers*: Their role is to propose a value to be accepted.
3. *Learners*: Their role is to learn the value that has been accepted.

The idea is that if I get enough votes from the acceptors, then I can be sure that the value is accepted.

The definition of *enough* is flexible, and can be defined by the system designer. Naturally, requiring more votes leads to more fault-tolerance, but also less liveness.

Asking for *all* the acceptors to vote coherently essentially degrades the protocol to a Two-Phase Commit protocol.

The threshold chosen is called a *Quorum* (akin to parliamentary democracy).

We also have the notion of a *Round*, which are statically associated to proposers by some rule. A round must be started whenever a proposer wants to propose a value.

A simple rule for round selection is, given  $n$  proposers, the proposer  $i$  always starts rounds  $k \cdot n + i$ . They also have to start the smallest round that is greater than the round of the last proposal that they have seen.

### Phases of the protocol

1. A proposer sends a `prepare(r)` message to all acceptors, proposing a value relative to round  $r$ , here we do not need to send the value but merely receive some promises that the acceptors will vote for us on this round.
2. Acceptors then respond with `promise(r, last_round, last_value)`, where `last_round` is the round of the last proposal that the acceptor has seen, and `last_value` is the value of the last proposal that the acceptor has seen. For the first proposal, `last_round` is set to  $-\infty$  or some other sentinel value.
3. An `accept(r, value)` message is sent to all acceptors, where `value` is the value that the proposer wants to propose.
4. Learners receive an `accepted(r, value)` message, and learn the value.

### How to choose a value

A proposer follows the following rules to choose a value:

1. Take the promise message with the highest `last_round` value.
2. The value is the `last_value` of the promise message with the highest `last_round` value.
3. If no promise messages were received by any acceptor in my quorum, then I can propose any value that I want.

## Sixth Lecture

Today we give another proof of the Paxos protocol, in a more formal way.

Theorem:

If acceptor  $a$  votes for  $x$  in round  $i$ , then no value  $x' \neq x$  can be chosen in previous rounds

Proof:

By induction, assume  $i = 0$ , the theorem is trivially true, since there is no previous round. Assume now that we are in round  $i > 0$  and that the theorem holds  $\forall k < i$ .

We now have a set of acceptors  $A$  and a Quorum set  $Q \subseteq A$ . With  $|Q| > |A|/2$ . Given that the last votes for any acceptor in  $Q$  was on a round  $j$ , we can assume that from  $j + 1$  to  $i - 1$  the acceptors in  $Q$  did *not* vote (otherwise we would have a contradiction). The only guys that could have voted are in the set  $A \setminus Q$ , but since  $|Q| > |A|/2$ , then  $|A \setminus Q| < |A|/2$ , and therefore we cannot have a quorum of votes for any value  $x' \neq x$ .

Assume now that  $j$  is *not* -1 (meaning that the acceptors in  $Q$  *never voted*), for the case in which  $j = -1$  the theorem holds by induction.

We now prove for the case in which  $j \geq 1$ . In this case, in round  $j$ , at *least* one member of the quorum voted for  $x$ . Since it is impossible that two proposers propose two different values, and a proposer *cannot* send two different values in the same round, then *no other value* different from  $x$  can be chosen in round  $j$ .

## Paxos Coordinator

We now discuss the role of a *coordinator* in the Paxos protocol. The coordinator is a process that is responsible for starting the protocol, and for ensuring that the protocol is run correctly.

Leader election is as *hard* as consensus, but once a leader is elected, consensus can be made easier. It is often a good idea to *try* to elect a leader, but not to *depend* on the leader.

Electing a leader for Paxos at least ensures that, if the leader selection fails and we have, for example, two leaders, we can at least be sure that consensus will be safe.

Given an *oracle* that can solve the election problem, Paxos becomes a *live* protocol.

## Eight Lecture

If we have an asynchronous system, even only *one* crash leads to the impossibility of reaching consensus.

Many other problems can be reduced to the consensus problem, such as leader election (which we saw in the previous lectures).

We recap some properties of consensus protocols:

- Agreement: All non-faulty processes decide the same value.
- Validity: If someone decides a value, then it must have been proposed by someone.

- Termination: All non-faulty processes eventually decide.

We do not care about computational complexity.

In consensus each process first chooses a value, then tries to reach agreement on the value.

Assume that I have a consensus problem over a binary set of values  $\{0, 1\}$ , and that I have a set of processes  $\{p_1, p_2, \dots, p_n\}$ .

We have a 0-valent state, in which all processes vote 0, and a 1-valent state, in which all processes vote 1. Here consensus is trivially reached by agreement and validity.

Now we list each possible  $2^n$  states of the systems in a truth-table manner, but we use a code in which only one bit is changed at a time (such as Gray code).

We then must have two configurations that are *adjacent* in the table, and that are *not* in the same valent state (one is 0-valent, the other is 1-valent). Then, naturally, there must be a single bit that *discriminates* inbetween these two states. It follows that a single crash can invalidate the protocol.

This proves that *any* FLP protocol is impossible even only with *one* crash.

## Ninth Lecture

We discuss *Randomized Consensus*

In this problem we have  $n$  processes, each process proposes a value. The inter-process communication is *asynchronous*, and the processes can *crash*.

The algorithm that we will introduce is called *Ben-Or*, it can tolerate up to  $t = \lfloor \frac{n-1}{2} \rfloor$  failures.

We follow up with some python-like pseudocode

```

preference = input_data
round_n = 1

while True:
    send(1, round_n, preference) # to everyone
    wait(1, round_n, *) # for all n-t process IDs
    if received more than n/2 (1, round_n, v) messages:
        send(2, round_n, 2, ratify) # to everyone
    else:
        send(2, round_n, ???) # to everyone
    wait(2, round_n, *) # for all n-t process IDs
    if received one (2, round_n, v, ratify) message:
        preference = v
    if received more than t (2, round_n, v, ratify) messages:
        return v

```



```

else:
    preference = random() # between 0 and 1
    round_n += 1

```

We then list some properties:

1. At most one value can get a majority in phase 1.
2. If some process sees  $t + 1$  (2, round,  $v$ , ratify) messages, then everybody sees at least one (2, round,  $v$ , ratify) message.
3. If every process has received at least one (2, round,  $v$ , ratify) then every process will vote for  $v$  in round  $round + 1$ .

This protocol is not important for practical purposes, but it is important for theoretical purposes, since we prove that randomization can overcome the FLP impossibility result.

## Tenth Lecture

This lecture is a seminar dedicated to *Internet Privacy*. We choose two main topics:

1. WiFi privacy
2. The dark web (TOR)

### WiFi Privacy

We discuss how to gather information from a crowd based on the WiFi signals that they emit.

At the time of the creation of the seminar's slides, 5G networks were not yet widespread, hence people tended to use WiFi networks more often.

Apparently, smartphone WiFi protocols are terrible for privacy, since they broadcast the SSID of the networks *every* time they try to connect to a network. Moreover, the SSID is broadcasted in *clear text*, and can be easily intercepted.

Also, to save energy, smartphones periodically broadcast this signal (instead of waiting for an access point constantly).

### What was done

Various events with high attendance were exploited to sniff packets, obtaining a huge sample size, the following attributes were analyzed:

1. SSID of Networks
2. Travel history
3. Gender
4. Homes
5. etc...

Every attribute aside from number one can be inferred from patterns in the data

By using SSIDs contained in these connection attempts, one can use online services to look for GPS positions of SSIDs. This happens if your SSID is unique (as is often the case with UUIDs generated by internet providers).

Geolocalization can then be used in combination with services such as google maps to further infer the role of various SSIDs (hairdresser, homes, airports, etc. . .)

This kind of data could even be utilized to perform election forecasting, by spoofing packets from a political rally and then backtracking each attendant to his home city, one can possibly approximate the distribution of voters in each city.

After this work (done in 2013) both android and apple changed their protocols in a way so that the client only sends a periodic ping message, and the Access Points have to prove that their are known by the smartphone.

Smartphones then started avoiding fingerprinting by MAC address by using a randomized one that refreshes in a matter of *seconds*.

## Dark Web

Another attempt was made to analyze some aggregate data about users of The Silk Road, a late deep-web market that was involved in the narcotics trade.

By assuming that people have a more intense posting frequency around a particular time (after dinner), one can retrieve the distribution of timezones (mixture of gaussians) of the users.

One can perform *continuous* aggregation of the population horizontally (on timezones) and can use daylight savings to *eventually* split the population across the equator.

The geography of Earth is convenient in this sense because it allows us to split North/South america and Africa/Europe, which are very different demographics