

Digital Communications and Laboratory

Second Homework

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MATLAB code

```
clc; close all; clear global; clearvars;

N = [1:1:20];
L = [31 63 127 255 511 1023];
sigdB = -8;
sigmaw = 10^(sigdB/10);
a1 = -0.9635;
a2 = 0.4642;
noise = wgn(4*max(L),1,sigdB);
% save('good_noise3','noise')
load good_noise3

%%
index=0;
for l=1:length(L)
    index = index+1;
    for n=1:length(N)
        w = noise(1:4*L(l));
        w_0 = w([1:2:end]);
        w_1 = w([2:2:end]);
        PN = PNSeq(L(l));           % ML sequence repeated once
        x=[PN ; PN];

        h = impz(1, [1 a1 a2]);      % Analytical h
        [h_even,h_odd] = polyphase(h,length(h));

        % scheme pag 239
        z_0=filter(h_even, 1, x);
        z_1=filter(h_odd, 1, x);
        d_0 = z_0 + w_0;
        d_1 = z_1 + w_1;
        d = PS(d_0, d_1);
```

```

% Correlation method
h0_cor=corr_method(x, d_0);
h1_cor=corr_method(x, d_1);
if N(n)<L(1)
    h0_cor=h0_cor(1:ceil(N(n)/2));
    h1_cor=h1_cor(1:floor(N(n)/2));
end
h_cor = PS(h0_cor, h1_cor);

% Cost function
d0_hat = filter(h0_cor,1,x);
d1_hat = filter(h1_cor,1,x);
d_hat_cor = PS(d0_hat, d1_hat);
error_cor = d - d_hat_cor;
E_cor = sum(error_cor(L(1):2*L(1)).^2);
E_L_cor(1,n) = 10*log10(E_cor/L(1));

% ls method
h0_ls=LS(x, d_0, L(1));
h1_ls=LS(x, d_1, L(1));
if N(n)<L(1)
    h0_ls=h0_ls(1:ceil(N(n)/2));
    h1_ls=h1_ls(1:floor(N(n)/2));
end
h_ls = PS(h0_ls, h1_ls);

% Cost Function
d0_hat = filter(h0_ls,1,x);
d1_hat = filter(h1_ls,1,x);
d_hat_ls = PS(d0_hat, d1_hat);
error_ls = d - d_hat_ls;
E_ls = sum(error_ls(L(1):2*L(1)).^2);
E_L_ls(1,n) = 10*log10(E_ls/L(1));

end
Cost_cor(:,index) = E_L_cor;
Cost_ls(:,index) = E_L_ls;

end

plot_est(Cost_cor, Cost_ls, sigdB);

```

```

clc; close all; clear global; clearvars;

```

```

L=63;                                % length of PN sequence
Nh=6;                                % Bound on the length of h
% Additive noise
sigdB = -8;
sigmaw = 10^(sigdB/10);
load good_noise3.mat
w = noise(1:4*L)
% w = wgn(4*L,1,sigdB);
w_0 = w([1:2:end-1]);
w_1 = w([2:2:end]);

PN = PNSeq(L);                       % ML sequence repeated once
x=[PN ; PN];

%% POLYPHASE REALIZATION
a1 = -0.9635;
a2 = 0.4642;
h = impz(1, [1 a1 a2]);
[h_even,h_odd] = polyphase(h,Nh);

%% ESTIMATE OF h0 WITH THE CORRELATION METHOD
z_0=filter(h_even, 1, x);
d_0 = z_0 + w_0;
h0_cor=corr_method(x, d_0);          % correlation method
var_h0_cor = sigmaw/(L/2);           % variance of the
                                     estimate

%% ESTIMATE OF h1 WITH THE CORRELATION METHOD
z_1=filter(h_odd, 1, x);
d_1 = z_1 + w_1;
h1_cor=corr_method(x, d_1);          % correlation method
var_h1_cor = sigmaw/(L/2);           % variance of the
                                     estimate

% Estimated impulse response
h_cor=zeros(Nh,1);
h0_spaced=zeros(Nh,1);
h1_spaced=zeros(Nh,1);
for i=1:Nh
    if (i<=L)
        h_cor(2*i-1)=h0_cor(i);
        h_cor(2*i)=h1_cor(i);
        h0_spaced(2*i-1) = h0_cor(i);
        h1_spaced(2*i) = h1_cor(i);
    end
end
end

```

```

h_cor=h_cor(1:Nh);
var_cor = var_h0_cor + var_h1_cor;
h0_spaced=h0_spaced(1:Nh);
h1_spaced=h1_spaced(1:Nh);

% Plot
figure,
stem(0:Nh-1,h0_spaced,'ro'), hold on
stem(0:Nh-1,h1_spaced,'ko'), hold on
plot([0:Nh-1],h(1:Nh),'bx','LineWidth',1.5);
legend('h_0 component','h_1 component','Analytic impulse
response');
xlabel('n'), ylim([-0.4 1.2]);
title('Polyphase components with the Correlation method')
grid on

%% ESTIMATE WITH THE LS METHOD
h0_ls=LS(x, d_0, L);
h1_ls=LS(x, d_1, L);

h_ls=zeros(Nh,1);
h0_spaced_ls=zeros(Nh,1);
h1_spaced_ls=zeros(Nh,1);
for i=1:Nh
    if (i<=L)
        h_ls(2*i-1)=h0_ls(i);
        h_ls(2*i)=h1_ls(i);
        h0_spaced_ls(2*i-1) = h0_ls(i);
        h1_spaced_ls(2*i) = h1_ls(i);
    end
end
h_ls=h_ls(1:Nh);
h0_spaced_ls=h0_spaced_ls(1:Nh);
h1_spaced_ls=h1_spaced_ls(1:Nh);

% Plot
figure,
stem(0:Nh-1,h0_spaced_ls,'ro'), hold on
stem(0:Nh-1,h1_spaced_ls,'ko'), hold on
plot([0:Nh-1],h(1:Nh),'bx','LineWidth',1.5);
legend('h_0 component','h_1 component','Analytic impulse
response');
xlabel('n'), ylim([-0.4 1.2]);
title('Polyphase components with the LS method')
grid on

```

```

%% comparison cor vs ls
figure ,
stem(0:Nh-1,h_cor,'bo')
hold on
stem(0:Nh-1,h_ls,'ro')
grid on
plot([0:Nh-1],h,'bx','LineWidth',1.5);
legend('h_cor','h_ls','Analytic impulse response');

%% VALUES FOR THE TABLE
table = zeros(Nh,3)
for i=1:Nh
    table(i,:) = [h(i) h_cor(i) h_ls(i)];
end
table'

```

```

function [rx]=autocorrelation_Unb(x)
% Unbiased autocorrelation estimator
%INPUT: r.p. x, length of the autocorrelation Lcorr
%OUTPUT: autocorrelation estimate vector rx of length K=
        length(x)
%every index is augmented by 1 because matlab starts from
        1 and not 0
K=length(x);
rx=zeros(K, 1);
    for n=1:K
        %first x that has k as argument
        xnk=x(n:K);
        %second x that has k-n as argument and the
            conjugate
        xconj=conj(x(1:(K-n+1)));
        rx(n)=(xnk.'*xconj)/(K-n+1);
    end
end

```

```

function [rx]=corr_method(x,d)
% INPUT
% x the input sequence of length 2*L
% r the output of the filter
% OUTPUT
% rx the cross correlation of d and x of length L=length(
    x)/2

L=length(x)/2;

```

```

rx=zeros(L, 1);
for m=1:L-1
    rtemp=zeros(L,1);
    for k=1:L
        %starts using the samples of d after a transient
        %of engh L-1
        rtemp(k)=d(L-2+k)*conj(x(L-1+k-m));
    end
    rx(m)=sum(rtemp)/L;
end
end

```

```

function [h_ls]=LS(x,d,L)
% INPUT
% x the input seq
% d filter output
% L half length PN seq
% OUTPUT
% h_ls the least squares estimate of h

%build matrix Phi and theta by I and o (page 246)
I=zeros(L);
for k=1:L
    I(:,k)=x(L-k+1:(2*L-k));
end
o=d(L:2*L-1);
Phi=I'*I;
theta=I'*o;

h_ls=inv(Phi)*theta;
%h_ls=h_ls(1:N);
end

```

```

function [pn] = PNSeq(L)

r = log2(L+1);
pn = zeros(L,1);

% Initial conditions (set to one, arbitrary)
% Must not be ALL zeros
pn(1:r) = ones(1,r)';

for l=r+1:L
    switch r
        case 1

```

```

        pn(1) = pn(1-1);
    case 2
        pn(1) = xor(pn(1-1), pn(1-2));
    case 3
        pn(1) = xor(pn(1-2), pn(1-3));
    case 4
        pn(1) = xor(pn(1-3), pn(1-4));
    case 5
        pn(1) = xor(pn(1-3), pn(1-5));
    case 6
        pn(1) = xor(pn(1-5), pn(1-6));
    case 7
        pn(1) = xor(pn(1-6), pn(1-7));
    case 8
        pn(1) = xor(xor(pn(1-2),pn(1-3)),xor(pn(1-4),
            pn(1-8)));
    case 9
        pn(1) = xor(pn(1-5), pn(1-9));
    case 10
        pn(1) = xor(pn(1-7), pn(1-10));

    end
end

% Bits are {-1, 1}
pn = 2*pn -1;

end

```

```

function [h_even h_odd] = polyphase(h,Nlim)

% Even samples
h_even=zeros(ceil(Nlim/2),1);
for k=1:(Nlim/2)
    h_even(k)=h(2*k-1);
end

% Odd samples
h_odd=zeros(floor(Nlim/2),1);
for k=1:Nlim/2
    h_odd(k)=h(2*k);
end

```

end	15
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<pre> function [h] = PS(h0, h1) temp = length(h0)+length(h1); h=zeros(temp,1); if mod(temp,2)==0 for i=1:temp/2 h(2*i-1)=h0(i); h(2*i)=h1(i); end elseif length(h0)==1 h(1)=h0(1); else for i=1:length(h0)-1 h(2*i-1)=h0(i); h(2*i)=h1(i); end h(2*(i+1)-1) = h0(i+1); end end </pre>	<div style="text-align: right;">5</div> <div style="text-align: right;">10</div> <div style="text-align: right;">15</div> <div style="text-align: right;">20</div>
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<pre> function plot_est(cor, ls, sigdB) set(0,'defaultTextInterpreter','latex') % <i>figure()</i> scrsz = get(0,'ScreenSize'); figure('Position',[15 scrsz(4)/5 scrsz(3)/1.5 scrsz(4)/1.5]) [N,lengL] = size(cor); N = [1:1:N]; a = sigdB*ones(1,20); plot(N,ls(:,1),'b-*') hold on, plot(N,ls(:,2),'c*-') hold on, plot(N,ls(:,3),'g*-') hold on, plot(N,ls(:,4),'y*-') hold on, plot(N,ls(:,5),'m*-') hold on, plot(N,ls(:,6),'r*-') hold on, plot(N,cor(:,1),'bo—') hold on, plot(N,cor(:,2),'co—') hold on, plot(N,cor(:,3),'go—') hold on, plot(N,cor(:,4),'yo—') hold on, plot(N,cor(:,5),'mo—') </pre>	<div style="text-align: right;">5</div> <div style="text-align: right;">10</div> <div style="text-align: right;">15</div> <div style="text-align: right;">20</div>
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```

hold on, plot(N, cor(:,6), 'ro—')

hold on, plot(a, 'b—', 'LineWidth', 2);
text(2, -7.7, '\sigma_w^2', 'FontSize', 16, 'Color', 'blue'); 25

xlabel('N_h');
ylabel('mathcal{E}/L [dB]');
xlim([1 20]);
legend('L31', 'L63', 'L127', 'L255', 'L511', 'L1023') 30
set(gca, 'FontSize', 15);
grid on

end

```

```

clc
clearvars
close all
set(0,'defaultTextInterpreter','latex')    % latex format
5
% Given Parameters
Tc = 1;
fd = (40*10-5)/Tc;          % Doppler spread given
Tp = 1/10*(1/fd);
N_h0 = 7500;                % samples first plot
N_t = 80000;                % samples of second plot
10
K_dB = 2;                   % Rice Factor in dB
K = 10(K_dB/10);            % Rice Factor in linear
    units
C = sqrt(K/(K+1));          15

[a_ds, b_ds] = ClassicalDS();    % Parameters of the
    IIR filter which implement
    % the classical
    Doppler Spectrum
    (page 317)
h_dopp = impz(b_ds, a_ds);      % Impulse response of
    DS
E_d = sum(h_dopp.2);           % Energy of the
    impulse response
b_ds = b_ds/sqrt(E_d);
Md = 1-C2;                   % normalization of the
    statistical power
20

% Doppler spectrum
[H_dopp,w]=freqz(h_dopp,1,1024,'whole',1/Tp);
DS = abs(H_dopp).2;
25

% figure
subplot(121), plot(h_dopp,'r'), ylabel(' $|h_{ds}|$ '),
    hold on
stem(1:length(h_dopp),real(h_dopp));
axis([0 Tp -0.15 0.25]), grid on
legend('continuous  $|h_{ds}|$ ','sampled  $|h_{ds}|$ ');
title('Impulse response of the IIR filter');
subplot(122), plot(w,10*log10(DS)), ylabel(' $10\log_{10}|D(f)|$ '),
    grid on;
hold on, plot([fd fd], [-60 20], 'r—'), text(4.1e-4, 10,
    ' $f_{ds}$ ');
35

```

```

xlim([0 3*fd]), xlabel('f');
ylim([-60 20]);
legend('Doppler Spectrum');
title('Doppler Spectrum')

% Transient is determined by the pole closest to the unit
% circle
poles = abs(roots(a_ds)); % poles' magnitude
most_imp = max(poles);
tr = 5*Tp*ceil(-1/log(most_imp)); % transient as 5*
% Neq*Tp

h_samples_needed = N_t+tr; % total length
% including the transient
w_samples_needed = ceil(h_samples_needed/Tp);
% w = wgn(w_samples_needed,1,0,'complex'); % w ~ CN
% (0,1)
load ex2_noise
hprime = filter(b_ds, a_ds, w);

t = 1:length(hprime); % interpolation to
% Tq
Tq = Tc/Tp;
t_fine = Tq:Tq:length(hprime);
h_fine = interp1(t, hprime, t_fine, 'spline');
sigma = sqrt(Md);
h_fine = h_fine*sigma; % impose the
% desired power delay profile
h0 = h_fine(tr+1:end)+C; % remove the
% transient and add C

% figure, plot(abs(h0(1:N_h0)))
% xlabel('$nT_c$')
% ylabel('$|h_0(nT_c)|$')
% xlim([1 N_h0]), grid on
% title('Impulse response of the channel')

% ESTIMATE OF THE PDF OF  $H_p = |h_0|/\sqrt{M}$ 
h_p = h0/sqrt(C^2+Md); % the normalization here
% does not make much sense
% as  $M_h0 = 1 - C^2$ , but it's
% to keep the formulas
% as in the book

abs_h = abs(h_p); % magnitude
a=linspace(0,10,3000);
% Rice distribution

```

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th_pdf = 2*(1+K).*a.*exp(-K-(1+K).*a.^2).*besseli(0,2.*a.*
    sqrt(K*(1+K)));
% Estimate of the pdf
[y,t] = hist(abs_h,30);
est_pdf = y/max(y);

figure
bar(t,est_pdf,'g'), hold on, plot(a,th_pdf,'r—',',
    LineWidth',2);
ylabel('Number of samples')
xlabel('Value')
title('Histogram of  $\frac{|h_0|}{\sqrt{M_{|h_0|}}}$ ')
legend('estimate pdf','theoretical pdf');
axis([0 3 0 1.3]);
grid on

%% SPECTRUM ESTIMATION
% Theoretical PSD
Npoints=N_t*1/Tp;
[H_dopp,w]=freqz(h_dopp,1,Npoints,'whole');
H_dopp=(1/Npoints)*abs(H_dopp).^2;
DS = fftshift(H_dopp);

% Welch estimator
D = ceil(N_t/2); % window length
D = 40000;
S = D/2; % overlap
w_welch=window(@bartlett,D);
[Welch_P, N] = welchPSD(h0', w_welch, S);
Welch_P = Welch_P/N;
Welch_cent=fftshift(Welch_P);

C_comp = 10*log10(C^2);
PSD_theo = 10*log10(Md*DS);
PSD_theo(length(PSD_theo)/2) = C_comp;

f1=[-N/2+1:N/2];
f2=[-Npoints/2+1:Npoints/2];

figure,
plot(f1-1, 10*log10(Welch_cent)), hold on, plot(f2,
    PSD_theo,'r')
ylim([-40 0])
xlim([-5*N*fd 5*N*fd]);
xticks([-5*N*fd -4*N*fd -3*N*fd -2*N*fd -1*N*fd 0 1*N*fd

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        2*N*fd 3*N*fd 4*N*fd 5*N*fd])
xticklabels({ '-5f_d', '-4f_d', '-3f_d', '-2f_d', '-f_d', '0', '
        f_d', '2f_d', '3f_d', '4f_d', '5f_d'});
ylabel('H(f) [dB]')
xlabel('f')
legend('Welch Periodogram', 'Theoretical PSD')
title('Spectrum Estimate')
grid on

%%
f1=[-N/2+1:N/2];
f2=[-Npoints/2+1:Npoints/2];

% Comparison of different S,D
D = [10000 15000 20000 40000];
S = D./2;
for i=1:length(S)
    w_welch=window(@hamming,D(i));
    [Welch_P(:,i), N] = welchPSD(h0', w_welch, S(i));
end
Welch_P = Welch_P/N;
Welch_cent=fftshift(Welch_P);

figure,
plot(f1, 10*log10(Welch_cent)), hold on
plot(f2, 10*log10(Md*DS), 'r', 'LineWidth', 1.5)
ylim([-50 0])
xlim([-5*N*fd 5*N*fd]);
xticks([-5*N*fd -4*N*fd -3*N*fd -2*N*fd -1*N*fd 0 1*N*fd
        2*N*fd 3*N*fd 4*N*fd 5*N*fd])
xticklabels({ '-5f_d', '-4f_d', '-3f_d', '-2f_d', '-f_d', '0', '
        f_d', '2f_d', '3f_d', '4f_d', '5f_d'});
ylabel('H(f) [dB]')
xlabel('f')
legend(['D = ' int2str(D(1)) ' and S = ' int2str(S(1)) ],
        ['D = ' int2str(D(2)) ' and S = ' int2str(S(2)) ],[
        'D = ' int2str(DS(3)) ' and S = ' int2str(S(3)) ],[
        D = ' int2str(DS(4)) ' and S = ' int2str(S(4)) ]);

clc; close all; clear global; clearvars;

N = [1:1:20];
L = [31 63 127 255 511 1023];
sigdB = -8;
sigmaw = 10^(sigdB/10);

```

```

a1 = -0.9635;
a2 = 0.4642;
noise = wgn(4*max(L),1,sigdB);
% save('good_noise3','noise')
load good_noise3

%%
index=0;
for l=1:length(L)
    index = index+1;
for n=1:length(N)
    w = noise(1:4*L(l));
    w_0 = w([1:2:end]);
    w_1 = w([2:2:end]);
    PN = PNSeq(L(l));           % ML sequence repeated once
    x=[PN ; PN];

    h = impz(1, [1 a1 a2]);     % Analytical h
    [h_even,h_odd] = polyphase(h,length(h));

    % scheme pag 239
    z_0=filter(h_even, 1, x);
    z_1=filter(h_odd, 1, x);
    d_0 = z_0 + w_0;
    d_1 = z_1 + w_1;
    d = PS(d_0, d_1);

    % Correlation method
    h0_cor=corr_method(x, d_0);
    h1_cor=corr_method(x, d_1);
    if N(n)<L(l)
        h0_cor=h0_cor(1:ceil(N(n)/2));
        h1_cor=h1_cor(1:floor(N(n)/2));
    end
    h_cor = PS(h0_cor, h1_cor);

    % Cost function
    d0_hat = filter(h0_cor,1,x);
    d1_hat = filter(h1_cor,1,x);
    d_hat_cor = PS(d0_hat, d1_hat);
    error_cor = d - d_hat_cor;
    E_cor = sum(error_cor(L(1):2*L(1)).^2);
    E_L_cor(1,n) = 10*log10(E_cor/L(1));

    % ls method
    h0_ls=LS(x, d_0, L(1));

```

<pre> h1_ls=LS(x, d_1, L(1)); if N(n)<L(1) h0_ls=h0_ls(1:ceil(N(n)/2)); h1_ls=h1_ls(1:floor(N(n)/2)); end h_ls = PS(h0_ls, h1_ls); % Cost Function d0_hat = filter(h0_ls,1,x); d1_hat = filter(h1_ls,1,x); d_hat_ls = PS(d0_hat, d1_hat); error_ls = d - d_hat_ls; E_ls = sum(error_ls(L(1):2*L(1)).^2); E_L_ls(1,n) = 10*log10(E_ls/L(1)); end Cost_cor(:,index) = E_L_cor; Cost_ls(:,index) = E_L_ls; end plot_est(Cost_cor, Cost_ls, sigdB); </pre>	55 60 65 70
<pre> clc; close all; clear global; clearvars; N = [1:1:20]; L = [31 63 127 255 511 1023]; sigdB = -8; sigmaw = 10^(sigdB/10); a1 = -0.9635; a2 = 0.4642; noise = wgn(4*max(L),1,sigdB); % save('good_noise3','noise') load good_noise3 %% index=0; for l=1:length(L) index = index+1; for n=1:length(N) w = noise(1:4*L(l)); w_0 = w([1:2:end]); w_1 = w([2:2:end]); PN = PNSeq(L(1)); x=[PN ; PN]; </pre>	5 10 15 20

```

h = impz(1, [1 a1 a2]); % Analytical h
[h_even,h_odd] = polyphase(h,length(h));

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% scheme pag 239

```

```

z_0=filter(h_even, 1, x);
z_1=filter(h_odd, 1, x);
d_0 = z_0 + w_0;
d_1 = z_1 + w_1;
d = PS(d_0, d_1);

```

```

% Correlation method

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```

h0_cor=corr_method(x, d_0);
h1_cor=corr_method(x, d_1);
if N(n)<L(1)
    h0_cor=h0_cor(1:ceil(N(n)/2));
    h1_cor=h1_cor(1:floor(N(n)/2));
end
h_cor = PS(h0_cor, h1_cor);

```

```

% Cost function

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```

d0_hat = filter(h0_cor,1,x);
d1_hat = filter(h1_cor,1,x);
d_hat_cor = PS(d0_hat, d1_hat);
error_cor = d - d_hat_cor;
E_cor = sum(error_cor(L(1):2*L(1)).^2);
E_L_cor(1,n) = 10*log10(E_cor/L(1));

```

```

% ls method

```

```

h0_ls=LS(x, d_0, L(1));
h1_ls=LS(x, d_1, L(1));
if N(n)<L(1)
    h0_ls=h0_ls(1:ceil(N(n)/2));
    h1_ls=h1_ls(1:floor(N(n)/2));
end
h_ls = PS(h0_ls, h1_ls);

```

```

% Cost Function

```

```

d0_hat = filter(h0_ls,1,x);
d1_hat = filter(h1_ls,1,x);
d_hat_ls = PS(d0_hat, d1_hat);
error_ls = d - d_hat_ls;
E_ls = sum(error_ls(L(1):2*L(1)).^2);
E_L_ls(1,n) = 10*log10(E_ls/L(1));

```

```

end

```



```

Cost_cor(:,index) = E_L_cor;
Cost_ls(:,index) = E_L_ls;

end

plot_est(Cost_cor, Cost_ls, sigdB);

```

```

function [a,b] = ClassicalDS()

a = [1, -4.4153, 8.6283, -9.4592, 6.1051, -1.3542,
     -3.3622, 7.2390, -7.9361, 5.1221, -1.8401, 2.8706e
     -1];
b = [1.3651e-4, 8.1905e-4, 2.0476e-3, 2.7302e-3, 2.0476e
     -3, 9.0939e-4, 6.7852e-4, 1.3550e-3, 1.8076e-3,
     1.3550e-3, 5.3726e-4, 6.1818e-5, -7.1294e-5, ...
     -9.5058e-5, -7.1294e-5, -2.5505e-5, 1.3321e-5,
     4.5186e-5, 6.0248e-5, 4.5186e-5, 1.8074e-5,
     3.0124e-6];

end

```

```

function [welch_est, Ns] = welchPSD(inputsig, window,
    overlaps)
% REQUIRES COLUMN VECTOR FOR THE INPUT DATA

% Length of the window
D = length(window);
% Length of input signal
K = length(inputsig);
% Normalized energy of the window
Mw = sum(window.^2) * (1/D);
% Number of subsequences
N_s = floor((K-D)/(D-overlaps) + 1);
% Initialization of each periodogram
P_per = zeros(K, N_s);

for s = 0:(N_s-1)
    % Windowed input
    x_s = window .* inputsig(s*(D-overlaps)+1:s*(D-
        overlaps)+D);
    % DFT on K samples of windowed input
    X_s = fft(x_s, K);
    % Periodogram for the window
    P_per(:,s+1) = (abs(X_s)).^2 * (1/(D*Mw)); % Tc = 1;
end

```

```
% Sum of all periodograms  
welch_est = sum(P_per, 2) * (1/N_s);  
Ns = length(welch_est);  
end
```

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