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$$1. T(n) = 5 = O(1)$$

$$O(1) = 5$$

$$5 \leq 5 \cdot 1$$

maka, untuk $n \geq 1$ ($C=5$ dan $n_0=1$)

$$2. T(n) = \frac{n(n-1)}{2} + n - 1 = O(n^2)$$

$$O(n^2) = \frac{n^2}{2} + \frac{n}{2} - 1$$

$$\frac{n^2}{2} + \frac{n}{2} - 1 \leq \frac{n^2}{2} + \frac{n^2}{2} + n^2 = 2n^2$$

untuk $n \geq 1$ ($C=2$ dan $n_0=1$)

$$3. T(n) = 6 \cdot 2^n + 2n^2 = O(2^n)$$

$$O(2^n) = 6 \cdot 2^n + 2n^2$$

$$6 \cdot 2^n + 2n^2 \leq 6 \cdot 2^n + 2 \cdot 2^n = 8 \cdot 2^n$$

untuk $n \geq 1$ ($C=8$ dan $n_0=1$)

$$4. T(n) = 1+2+\dots+n = O(n^2)$$

$$O(n^2) = 1+2+\dots+n$$

$$1+2+\dots+n \leq n+n+\dots+n = n^2$$

untuk $n \geq 1$ ($C=1$ dan $n_0=1$)

$$5. T(n) = n! = O(n^n)$$

$$n! = 1 \cdot 2 \cdot \dots \cdot n \leq n \cdot n \cdot \dots \cdot n = n^n$$

untuk $n \geq 1$ ($C=1$ dan $n_0=1$)

~~4.6~~

$$6. T(n) = 1^k + 2^k + \dots + n^k = O(n^{k+1})$$

$$1^k + 2^k + \dots + n^k \leq n^k + n^k + \dots + n^k = n^{k+1}$$

untuk $n \geq 1$ ($C=1$ dan $n_0=1$)

$$7. T(n) = 5 \log(3^n) = O(n)$$

$$5 \log(3^n) \leq 5n = 5n$$

untuk $n \geq 1$ ($C=5$ dan $n_0=1$)

$$8. T(n) = \log(n!) = O(n \log(n))$$

$$\log(n!) \leq n \log n$$

untuk $n \geq 1$ ($C=1$ dan $n_0=1$)

$$9. T(n) = an^2 + bn + c$$

$$\begin{array}{ccccccc} 0 & 1 & 3 & 6 & 10 & & \\ \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & & & \\ 1 & 2 & 3 & 4 & & & \\ \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & & & & \\ 1 & 1 & 1 & & & & \end{array}$$

$$T(1) = a + b + c = 0$$

$$T(2) = 4a + 2b + c = 1$$

$$T(3) = 9a + 3b + c = 3$$

$$T(4) = 16a + 4b + c = 6$$

$$T(5) = 25a + 5b + c = 10$$

$$8a + 2b = 3$$

$$6a + 2b = 2 \quad -$$

$$2a = 1$$

$$a = \frac{1}{2}$$

$$b = -\frac{1}{2}$$

$$c = 0$$