

Computer Organization

Lab6 In

Integer Arithmetic

Integer Arithmetic





- Arithmetic
 - ✓ Adder
 - ✓ Subtraction
 - ✓ Multiplication
 - ✓ Division
- Practice



Adder with overflow detector (1)

- > The rule about overflow if result out of range on adder:
 - ✓ no overflow, if adding +ve and -ve operands
 - ✓ overflow, if

endmodule

```
• adding two +ve operands, get -ve operand 001 + 011 = 110
```

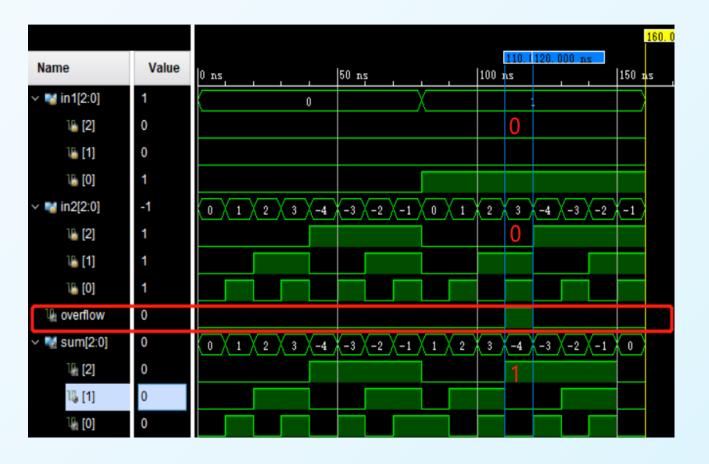
• adding two -ve operands, get +ve operand 101 + 101 = (1) 010

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Adder with overflow detector (2)

- > The figure is the waveform of the circuit "adder"
 - √ in1 is the addend and in2 is the addend.
 - ✓ while the value of overflow is 1'b1, it means there is a overflow, otherwise means not.



- Observe the waveform from 110ns to 120ns
- √ the in1 is 3'b001 and in2 is
 3'b011, the sum is 3'b100
- ✓ The signed bit of in1 and in2 is 0 (means they are both +ve), the singed bit of sum is 1(means it is -ve)
- ✓ In this situation, an overflow is detected



Subtraction (1)

- Implement the subtraction with adder: add negation of second operand
- How to get the negation of a number? Which of the following option(s) is(are) right?
 - ✓ Option1:
 - step1: Invert the sign bit. e.g. vin2p1 = ~in2[2]
 - step2: add 1 after inverting the value bits. e.g. ~in2[1:0] + 1
 - ✓ Option2:
 - Inverting the bits and adding on 1. e.g.
 ~in2+1

```
module subO1(in1,in2,result); //verilog
input [2:0] in1;
input [2:0] in2;
wire vin2p1;
wire [1:0] vin2p2;
output [2:0] result;
assign vin2p1 = ~in2[2];
assign vin2p2 = ~in2[1:0] + 1;
assign result = in1 + {vin2p1,vin2p2};
endmodule
```

```
module subO2(in1,in2,result); //verilog
input [2:0] in1;
input [2:0] in2;
output [2:0] result;
wire [2:0] vin2;
assign vin2= ~in2 + 1;
assign result = in1 + vin2;
endmodule
```



Subtraction (2)

Verify the function of the circuit 'subO1', 'subO2', Which implement(s) of sub is(are) correct?

```
module subO1(in1,in2,result); //verilog
input [2:0] in1;
input [2:0] in2;
wire vin2p1;
wire [1:0] vin2p2;
output [2:0] result;
assign vin2p1 = ~in2[2];
assign vin2p2 = ~in2[1:0] + 1;
assign result = in1 + {vin2p1,vin2p2};
endmodule
```

```
module subO2(in1,in2,result); //verilog
input [2:0] in1;
input [2:0] in2;
output [2:0] result;
wire [2:0] vin2;
assign vin2= ~in2 + 1;
assign result = in1 + vin2;
endmodule
```

```
module subTb():
                        //verilog
reg [2:0] in1,in2;
wire [2:0] rO1, rO2;
subO1 usubO1(in1,in2,rO1);
subO2 usubO2(in1,in2,rO2);
initial begin
  \{in1,in2\} = 6'b0;
  $monitor( "%3b(%d)-%3b(%d): ro1 = %3b(%d),
ro2 = %3b(%d)''
in1,$signed(in1),in2,$signed(in2),rO1,$signed(rO
1) ,rO2,$signed(rO2) );
  repeat(63) #10 \{in1,in2\} = \{in1,in2\} + 1;
  #10 $finish();
end
                         × Messages
               Tcl Console
                                     Log
endmodule
                 000(0)-111(-1): ro1 = 001(1), ro2 = 001(1)
                 001(1)-000(0): ro1 = 101(-3), ro2 = 001(1)
                  001(1)-001(1): ro1 = 000(0), ro2 = 000(0)
```

Question:

When in1 = 3'b000, in2 = 3'b100, what are the outputs of the two circuits? Try to explain the reason.

Tips:

\$monitor is a system service in **Verilog**, which is valid only in **simulation**. It monitors the data: whenever any of them changes, it prints the data in the specified format.

In Vivado, the print information is shown in tcl window.

%3b: means print the data in **binary**, the bitwidth is **3**

%d: means print the data in decimal

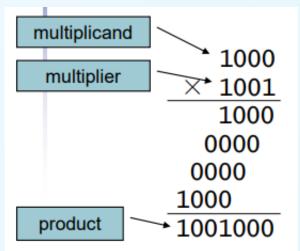
\$signed is a system service in Verilog, which change the data to be signed value.

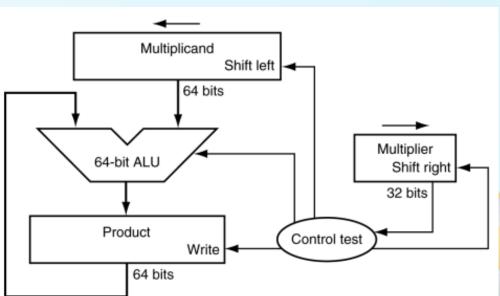
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Multiplication (1)

- > Here is a digital circuit which implement the long-multiplication approach:
 - ✓ Shift registers for multiplicand and multiplier
 - store and shift
 - ✓ Adder with two inputs and a control signal
 - add or not
 - ✓ A register to store the product
 - when to get the data from the product register?



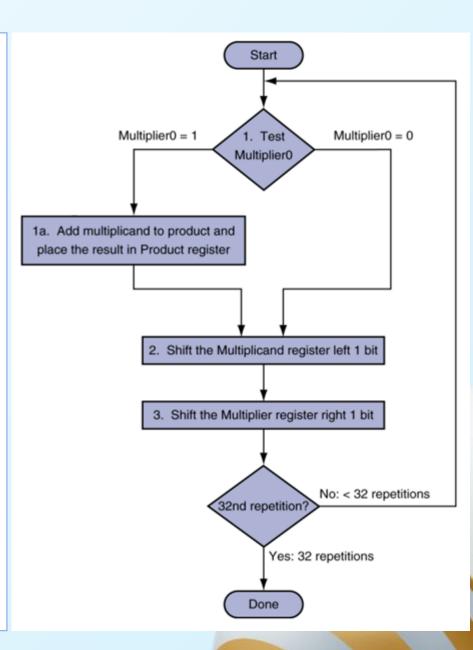




Multiplication (2)

- Can this piece of codes get the correct product result?
- If the length of multiplier is less than 4, could the assembly code work more effectively?

```
# Piece 6-1
.data
      m1:.byte 8
                      # multiplicand
      m2:.byte 9
                      # multiplier
.text
      lb t0, m1
      lb t1. m2
      add t2, zero, zero
loop:
      li s1, 1
      and s2, s1, t1 #to determine the lowest bit of t1
      beq s2, zero, jumpAdd
      add t2, t0, t2
jumpAdd:
      slli t0, t0, 1
      srli t1, t1, 1
      addi a0, a0,1
      li a1, 4
                      # 4 is the length of 9 in binary
      blt a0, a1, loop
      mv a0, t2
      li a7, 1
      ecall
      li a7, 35
      ecall
```





Multiplication instructions in RISC-V

- RV32M multiply extension
- > mul, mulh, mulhsu, mulhu

Inst	Name	FMT	Opcode	funct3	funct7	Description (C)
mul	MUL	R	0110011	0x0	0x01	rd = (rs1 * rs2)[31:0]
mulh	MUL High	R	0110011	0x1	0x01	rd = (rs1 * rs2)[63:32]
mulhsu	MUL High (S) (U)	R	0110011	0x2	0x01	rd = (rs1 * rs2)[63:32]
mulhu	MUL High (U)	R	0110011	0x3	0x01	rd = (rs1 * rs2)[63:32]

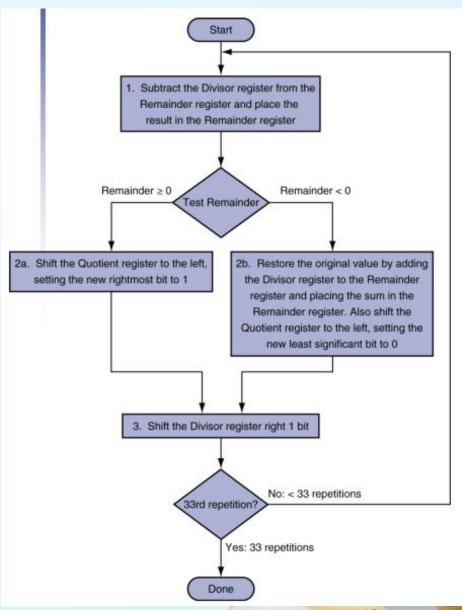
➤ If both high and low 32-bit multiplication product are required, the general code order is:

mulh rdh, rs1, rs2 #or mulhsu rdh, rs1, rs2 or mulhu rdh, rs1, rs2 mul rdl, rs1, rs2



Division (1)

- Check for 0 divisor by software.
- Long division approach
 - ✓ If divisor ≤ dividend bits: 1 bit in quotient, subtract
 - Otherwise: 0 bit in quotient, bring down next dividend bit
- Restoring division
 - ✓ Do the subtract, and if remainder goes < 0, add divisor back
- Signed division
 - Divide using absolute values
 - Adjust sign of quotient and remainder as required





Division (2) long division approach

> Step0: prepare for the long division approach

```
# Piece 6-3
# Piece 6-3-1
.include "macro_print_str.asm"
.data
      dividend: .word 7
      divisor: .word 2
      x: .word 0x8000
      looptimes: .byte 5
.text
      la t5, dividend
      lw t1, (t5) # t1 : dividend
      la t5, divisor
      lw t2, (t5) # t2 : divisor
      slli t2, t2, 4
      la t5, dividend
      lw t3, (t5) # t3 store the remainder
      add t4, zero, zero # t4 quotient
      la t5, x
      lw a1, (t5)
                        #a1 used to get the highest bit of remainder
      add t0, zero, zero # t0: loop cnt
      la t5, looptimes
      lb s1, (t5)
                        #s1: loop times
```

■ Divide 7_{dec} (0000 0111_{bin}) by 2_{dec} (0010_{bin})

Iter	Step	Quot	Divisor	Remainder
0	Initial values	0000	0010 0000	0000 0111
1	Rem = Rem – Div	0000	0010 0000	1110 0111
	Rem < 0 → +Div, shift 0 into Q	0000	0010 0000	0000 0111
	Shift Div right	0000	0001 0000	0000 0111
2	Same steps as 1	0000	0001 0000	1111 0111
		0000	0001 0000	0000 0111
		0000	0000 1000	0000 0111
3	Same steps as 1	0000	0000 0100	0000 0111
4	Rem = Rem – Div	0000	0000 0100	0000 0011
	Rem >= 0 → shift 1 into Q	0001	0000 0100	0000 0011
	Shift Div right	0001	0000 0010	0000 0011
5	Same steps as 4	0011	0000 0001	0000 0001



Division (3) long division approach

Step1-5: Do the long division approach

```
# Piece 6-3-2
loopb:
     # t1: dividend, t2: divisor, t3: remainder, t4: quotient
     # a1: 0x8000. s1: 5
     sub t3, t3, t2
                              #dividend - divisor
                              # get the highest bit of remainder to check if rem<0
     and s0, t3, a1
                       # shift left quot with 1bit
     slli t4, t4, 1
     beq s0, zero, SdrUq
                             # if rem>=0, shift Div right
     add t3, t3, t2
                              # if rem<0, rem=rem+div
     srli t2, t2, 1
     addi t4, t4, 0
                                        # Piece 6-3-3
     i loope
                                              li a7, 1
                                              mv a0, t4 #print quotient
SdrUq:
                                              ecall
     srli t2, t2, 1
                                              print_string("\n")
     addi t4, t4, 1
                                              li a7. 1
                                              mv a0, t3 #print remainder
loope:
                                              ecall
     addi t0, t0, 1
     bne t0, s1, loopb
                                              li a7, 10
                                              ecall
```

Divide 7_{dec} (0000 0111_{bin}) by 2_{dec} (0010_{bin})

Iter	Step	Quot	Divisor	Remainder
0	Initial values	0000	0010 0000	0000 0111
1	Rem = Rem – Div	0000	0010 0000	1110 0111
	Rem < 0 → +Div, shift 0 into Q	0000	0010 0000	0000 0111
	Shift Div right	0000	0001 0000	0000 0111
2	Same steps as 1	0000	0001 0000	1111 0111
		0000	0001 0000	0000 0111
		0000	0000 1000	0000 0111
3	Same steps as 1	0000	0000 0100	0000 0111
4	Rem = Rem – Div	0000	0000 0100	0000 0011
	Rem >= 0 → shift 1 into Q	0001	0000 0100	0000 0011
	Shift Div right	0001	0000 0010	0000 0011
5	Same steps as 4	0011	0000 0001	0000 0001



Division instructions in RISC-V

> div, divu, rem, remu

Inst	Name	FMT	Opcode	funct3	funct7	Description (C)
div	DIV	R	0110011	0x4	0x01	rd = rs1 / rs2
divu	DIV (U)	R	0110011	0x5	0x01	rd = rs1 / rs2
rem	Remainder	R	0110011	0x6	0x01	rd = rs1 % rs2
remu	Remainder (U)	R	0110011	0x7	0x01	rd = rs1 % rs2

> If both quotient and remainder are required, the general code order is:

```
div rdq, rs1, rs2 # or divu rdq, rs1, rs2 rem rdr, rs1, rs2 # or remu rdr, rs1, rs2
```



Practice 1-1: Adder with overflow detector

- Please complete the test bench to finding all of the legal combinations of the two inputs, verify the function of the circuit "adder".
- > A test bench on the bottom is for the reference.

```
module adderTb( ); //verilog
reg [2:0] in1,in2;
wire overflow;
wire [2:0] sum;
adder ua(in1,in2,sum,overflow);
initial begin
  \{in1,in2\} = 6'b0;
  repeat(63) #10 {in1,in2} = {in1,in2} + 1;
  #10 $finish;
end
endmodule
```



Practice 1-2: Subtraction with overflow detector

- Please complete the circuit to detect the overflow of the subtraction.
- > Build a test bench to verify the function of the circuit.
- The description about the overflow of the subtraction is described as bellow:
- Overflow if result out of range
 - No overflow, if subtracting two +ve or two –ve operands
 - Overflow, if:
 - Subtracting +ve from –ve operand, and the result sign is 0 (+ve)
 - Subtracting –ve from +ve operand, and the result sign is 1 (-ve)

```
//verilog
module subtraction(in1,in2,result,overflow);
input [2:0]in1,in2;
output [2:0] result;
output overflow;
assign result = in1 - in2;
assign overflow = _____
endmodule
```



Practice 2-1: Multiplication

- The assembly code on the right hand is just for the multiplier whose width is not larger than 4, and only for the unsigned multiplication, modify the code to achieve the following function:
 - ✓ 1) The width of multiplicand and multiplier is 16.
 - ✓ 2) The highest bit is take as the sign bit, to implement the signed multiplication.
 - ✓ Note: Don't use the mul instruction.

```
# Piece 6-1
.data
                      # multiplicand
      m1:.byte 8
                      # multiplier
      m2:.byte 9
.text
      lb t0, m1
      lb t1. m2
      add t2, zero, zero
loop:
      li s1, 1
      and s2, s1, t1 #to determine the lowest bit of t1
      beq s2, zero, jumpAdd
      add t2, t0, t2
jumpAdd:
      slli t0, t0, 1
      srli t1, t1, 1
      addi a0, a0,1
      li a1, 4
                     # 4 is the length of 9 in binary
      blt a0, a1, loop
      mv a0, t2
      li a7, 1
      ecall
      li a7, 35
      ecall
```



Practice 2-2: Division

- ➤ The piece of assembly code of piece 6-3 on Page 11 and 12 is just for the 8 bit unsigned division. Take piece 6-3 as reference, do the following tasks:
- > 1) To implement a 32 bit division with detecting exception while the divisor is 0.
- > 2) The highest bit is taken as the sign bit, to implement the signed division.
- For signed division:
 - ✓ Step1: Divide using absolute values.
 - ✓ Step2: Adjust sign of quotient and remainder as required.
 - ✓ The quotient is "+", if the signs of divisor and dividend agrees, otherwise, quotient is "-".
 - ✓ The sign of the remainder matches that of the dividend.
 - \checkmark (+7) \div (-2) = (-3) \cdots (+1) (-7) \div (-2) = (+3) \cdots (-1)
- Note: Don't use the div instruction.