The Coin Change Problem



Given an amount and the denominations of coins available, determine how many ways change can be made for amount. There is a limitless supply of each coin type.

Example

$$n=3$$
 $c=[8,3,1,2]$

There are 3 ways to make change for n=3: $\{1,1,1\}$, $\{1,2\}$, and $\{3\}$.

Function Description

Complete the getWays function in the editor below.

getWays has the following parameter(s):

- int n: the amount to make change for
- int c[m]: the available coin denominations

Returns

• *int:* the number of ways to make change

Input Format

The first line contains two space-separated integers n and m, where:

n is the amount to change

m is the number of coin types

The second line contains m space-separated integers that describe the values of each coin type.

Constraints

- $1 \le c[i] \le 50$
- $1 \le n \le 250$
- $1 \le m \le 50$
- ullet Each $oldsymbol{c[i]}$ is guaranteed to be distinct.

Hints

Solve overlapping subproblems using Dynamic Programming (DP):

You can solve this problem recursively but will not pass all the test cases without optimizing to eliminate the overlapping subproblems. Think of a way to store and reference previously computed solutions to avoid solving the same subproblem multiple times. * Consider the degenerate cases:

- How many ways can you make change for 0 cents? How many ways can you make change for >0 cents if you have no coins? * If you're having trouble defining your solutions store, then think about it in terms of the base case (n=0)
- . The answer may be larger than a 32-bit integer.

Sample Input 0

```
4 3
1 2 3
```

Sample Output 0

4

Explanation 0

There are four ways to make change for n=4 using coins with values given by C=[1,2,3]:

- 1. {1, 1, 1, 1}
- 2. $\{1, 1, 2\}$
- 3. **{2, 2}**
- 4. {1, 3}

Sample Input 1

```
10 4
2 5 3 6
```

Sample Output 1

5

Explanation 1

There are five ways to make change for n=10 units using coins with values given by C=[2,5,3,6]:

- 1. $\{2, 2, 2, 2, 2\}$
- 2. $\{2, 2, 3, 3\}$
- 3. **{2, 2, 6}**
- 4. $\{2, 3, 5\}$
- 5. **{5, 5**}