



Linear Data Structures

Lists, Stacks, Queues

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1. Abstract Data Types (ADT)
2. Lists – The `List<T>` Class
 - ♦ Static and Linked
3. Stacks – The `Stack<T>` Class
 - ♦ Static and Linked
4. Queues – The `Queue<T>` Class
 - ♦ Circular and Linked
 - ♦ Priority Queue
 - ♦ C# Implementation



Abstract Data Types

Basic Data Structures



Abstract Data Types

- ◆ An Abstract Data Type (ADT) is a data type together with the operations, whose properties are specified independently of any particular implementation
 - ◆ ADT are set of definitions of operations (like the interfaces in C#)
 - ◆ Can have several different implementations
 - ◆ Different implementations can have different efficiency

- ◆ Linear structures
 - ◆ Lists: fixed size and variable size
 - ◆ Stacks: LIFO (Last In First Out) structure
 - ◆ Queues: FIFO (First In First Out) structure
- ◆ Trees
 - ◆ Binary, ordered, balanced, etc.
- ◆ Dictionaries (maps)
 - ◆ Contain pairs (key, value)
 - ◆ Hash tables: use hash functions to search/insert

Lists

Static and Dynamic
Implementations



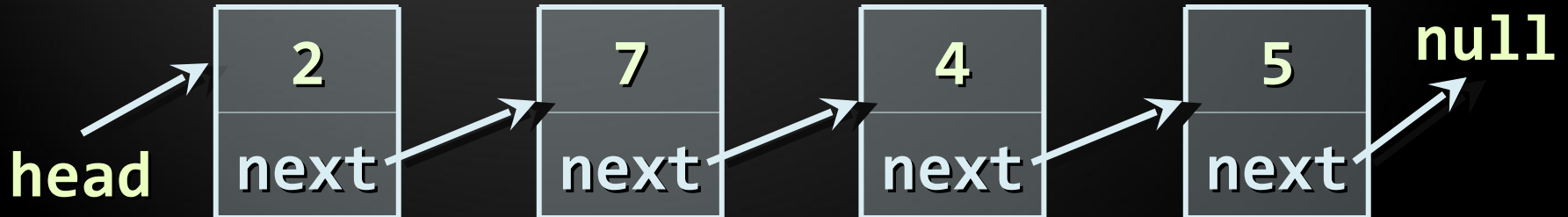
- ◆ Data structure (container) that contains a sequence of elements
 - ◆ Can have variable size
 - ◆ Elements are arranged linearly, in sequence
- ◆ Can be implemented in several ways
 - ◆ Statically (using array → fixed size)
 - ◆ Dynamically (linked implementation)
 - ◆ Using resizable array (the `List<T>` class)

- ◆ Implemented by an array
 - ◆ Provides direct access by index
 - ◆ Has fixed capacity
 - ◆ Insertion, deletion and resizing are slow operations

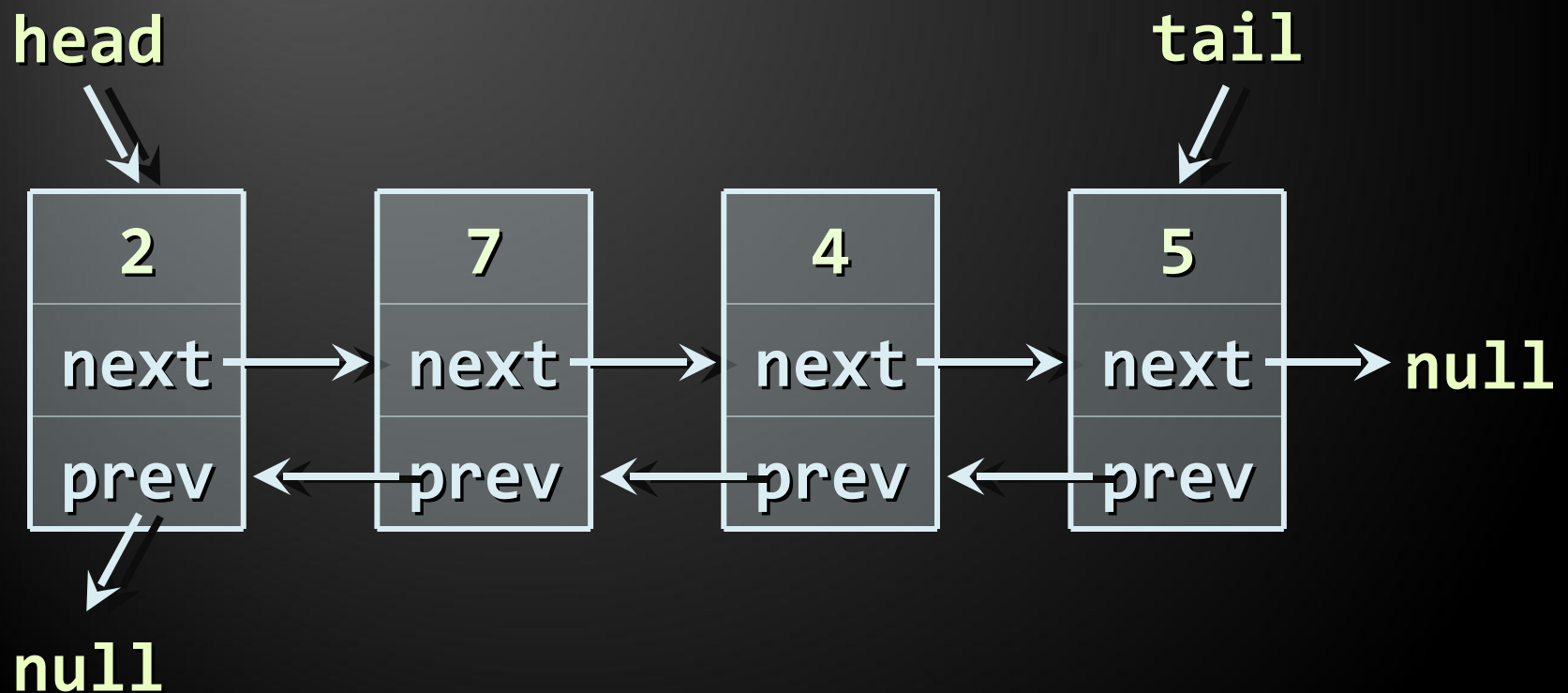


	0	1	2	3	4	5	6	7
L	2	18	7	12	3	6	11	9

- ◆ Dynamic (pointer-based) implementation
- ◆ Different forms
 - ◆ Singly-linked and doubly-linked
 - ◆ Sorted and unsorted
- ◆ Singly-linked list
 - ◆ Each item has 2 fields: value and next



- ◆ Doubly-linked List
 - ◆ Each item has 3 fields: value, next and prev



The List<T> Class

Auto-Resizable Indexed Lists



- ◆ Implements the abstract data structure list using an array
 - ◆ All elements are of the same type T
 - ◆ T can be any type, e.g. List<int>, List<string>, List<DateTime>
 - ◆ Size is dynamically increased as needed
- ◆ Basic functionality:
 - ◆ Count – returns the number of elements
 - ◆ Add(T) – appends given element at the end

List<T> – Simple Example

```
static void Main()
{
    List<string> list = new List<string>() { "C#",
    "Java" };

    list.Add("SQL");
    list.Add("Python");

    foreach (string item in list)
    {
        Console.WriteLine(item);
    }

    // Result:
    //      C#
    //      Java
    //      SQL
    //      Python
}
```

Inline initialization:
the compiler adds
specified elements
to the list.



List<T> – Simple Example

Live Demo

List<T> – Functionality

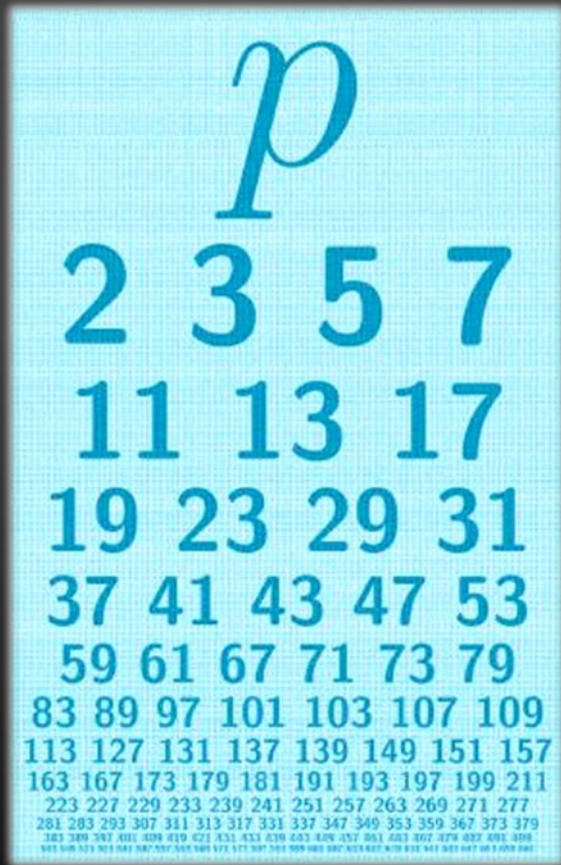
- ◆ `list[index]` – access element by index
- ◆ `Insert(index, T)` – inserts given element to the list at a specified position
- ◆ `Remove(T)` – removes the first occurrence of given element
- ◆ `RemoveAt(index)` – removes the element at the specified position
- ◆ `Clear()` – removes all elements
- ◆ `Contains(T)` – determines whether an element is part of the list

List<T> – Functionality (2)

- ◆ **IndexOf()** – returns the index of the first occurrence of a value in the list (zero-based)
- ◆ **Reverse()** – reverses the order of the elements in the list or a portion of it
- ◆ **Sort()** – sorts the elements in the list or a portion of it
- ◆ **ToArray()** – converts the elements of the list to an array
- ◆ **TrimExcess()** – sets the capacity to the actual number of elements

✂telerik Primes in an Interval – Example

```
static List<int> FindPrimes(int start, int end)
{
    List<int> primesList = new List<int>();
    for (int num = start; num <= end; num++)
    {
        bool prime = true;
        for (int div = 2; div <= Math.Sqrt(num); div++)
        {
            if (num % div == 0)
            {
                prime = false;
                break;
            }
        }
        if (prime)
        {
            primesList.Add(num);
        }
    }
}
```



Primes in an Interval

Live Demo

Union and Intersection – Example

```
int[] Union(int[] firstArr, int[] secondArr)
{
    List<int> union = new List<int>();
    union.AddRange(firstArray);
    foreach (int item in secondArray)
        if (! union.Contains(item))
            union.Add(item);
    return union.ToArray();
}

int[] Intersection(int[] firstArr, int[] secondArr)
{
    List<int> intersect = new List<int>();
    foreach (int item in firstArray)
        if (Array.IndexOf(secondArray, item) != -1)
            intersect.Add(item);
    return intersect.ToArray();
}
```



Union and Intersection

Live Demo



Stacks

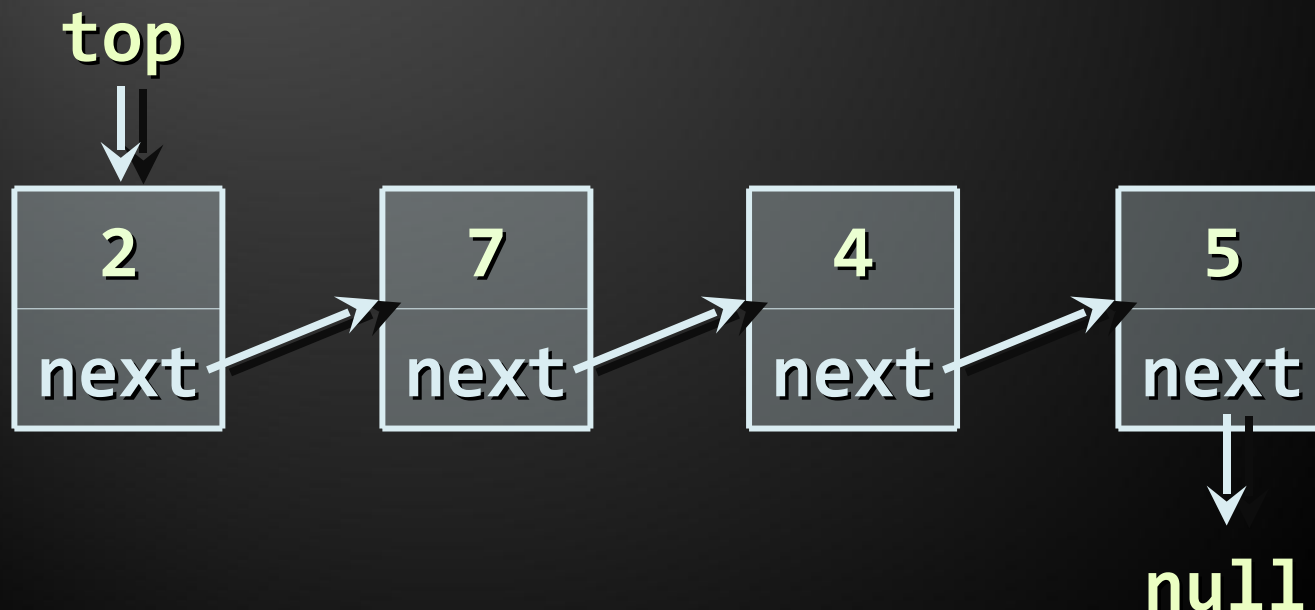
Static and Dynamic Implementation

- ◆ LIFO (Last In First Out) structure
- ◆ Elements inserted (push) at “top”
- ◆ Elements removed (pop) from “top”
- ◆ Useful in many situations
 - ◆ E.g. the execution stack of the program
- ◆ Can be implemented in several ways
 - ◆ Statically (using array)
 - ◆ Dynamically (linked implementation)
 - ◆ Using the `Stack<T>` class

- ◆ Static (array-based) implementation
 - ◆ Has limited (fixed) capacity
 - ◆ The current index (**top**) moves left / right with each pop / push



- ◆ Dynamic (pointer-based) implementation
 - ◆ Each item has 2 fields: value and next
 - ◆ Special pointer keeps the top element





The Stack<T> Class

The Standard Stack Implementation in .NET

- ◆ Implements the stack data structure using an array
 - ◆ Elements are from the same type T
 - ◆ T can be any type, e.g. Stack<int>
 - ◆ Size is dynamically increased as needed
- ◆ Basic functionality:
 - ◆ Push(T) – inserts elements to the stack
 - ◆ Pop() – removes and returns the top element from the stack

- ◆ **Basic functionality:**
 - ◆ **Peek()** – returns the top element of the stack without removing it
 - ◆ **Count** – returns the number of elements
 - ◆ **Clear()** – removes all elements
 - ◆ **Contains(T)** – determines whether given element is in the stack
 - ◆ **ToArray()** – converts the stack to an array
 - ◆ **TrimExcess()** – sets the capacity to the actual number of elements

- ◆ Using Push(), Pop() and Peek() methods

```
static void Main()
{
    Stack<string> stack = new Stack<string>();
    stack.Push("1. Ivan");
    stack.Push("2. Nikolay");
    stack.Push("3. Maria");
    stack.Push("4. George");
    Console.WriteLine("Top = {0}", stack.Peek());
    while (stack.Count > 0)
    {
        string personName = stack.Pop();
        Console.WriteLine(personName);
    }
}
```



Stack<T>

Live Demo

Matching Brackets – Example

- ◆ We are given an arithmetical expression with brackets that can be nested
- ◆ Goal: extract all sub-expressions in brackets
- ◆ Example:
 - ◆ $1 + (2 - (2+3) * 4 / (3+1)) * 5$
- ◆ Result:
 - ◆ $(2+3) \mid (3+1) \mid (2 - (2+3) * 4 / (3+1))$
- ◆ Algorithm:
 - ◆ For each '(' push its index in a stack
 - ◆ For each ')' pop the corresponding start index

Matching Brackets – Solution

```
string expression = "1 + (2 - (2+3) * 4 / (3+1)) * 5";
Stack<int> stack = new Stack<int>();
for (int index = 0; index < expression.Length; index++)
{
    char ch = expression[index];
    if (ch == '(')
    {
        stack.Push(index);
    }
    else if (ch == ')')
    {
        int startIndex = stack.Pop();
        int length = index - startIndex + 1;
        string contents =
            expression.Substring(startIndex, length);
        Console.WriteLine(contents);
    }
}
```



Matching Brackets

Live Demo

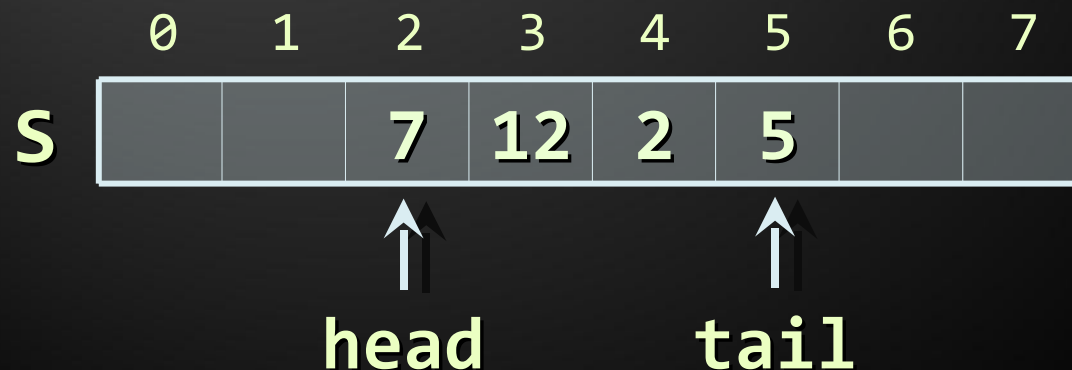
Queues

Static and Dynamic Implementation

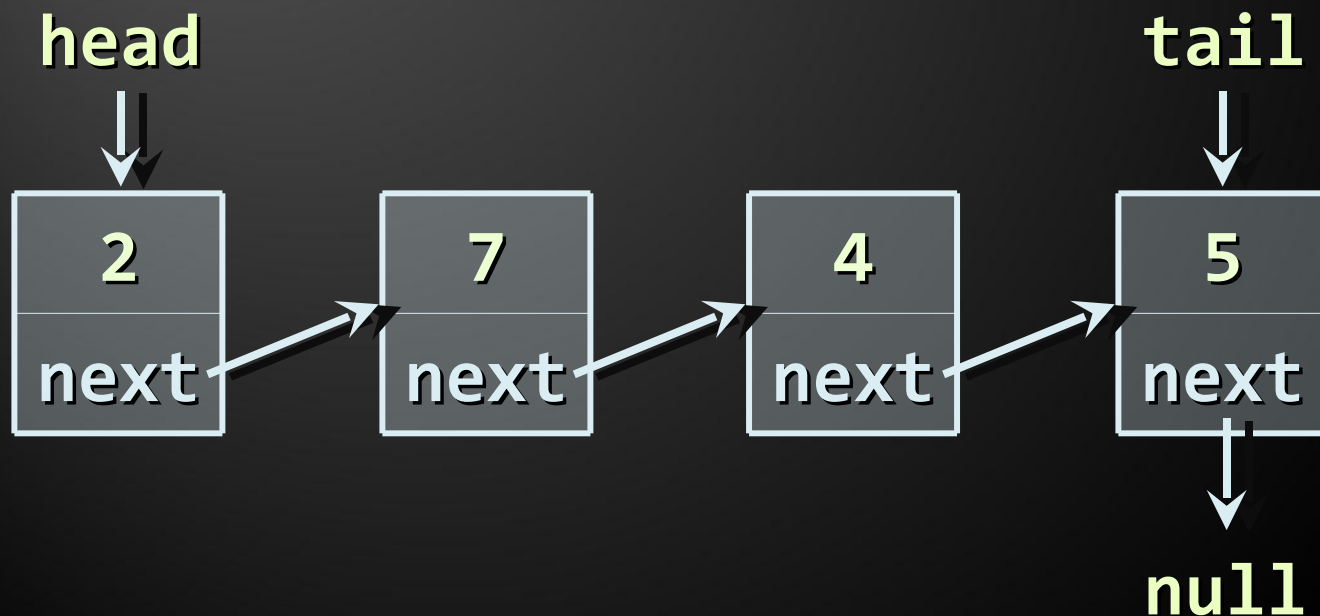


- ◆ FIFO (First In First Out) structure
- ◆ Elements inserted at the tail (Enqueue)
- ◆ Elements removed from the head (Dequeue)
- ◆ Useful in many situations
 - ◆ Print queues, message queues, etc.
- ◆ Can be implemented in several ways
 - ◆ Statically (using array)
 - ◆ Dynamically (using pointers)
 - ◆ Using the `Queue<T>` class

- ◆ Static (array-based) implementation
 - ◆ Has limited (fixed) capacity
 - ◆ Implement as a “circular array”
 - ◆ Has **head** and **tail** indices, pointing to the head and the tail of the cyclic queue



- ◆ Dynamic (pointer-based) implementation
 - ◆ Each item has 2 fields: value and next
 - ◆ Dynamically create and delete objects





The Queue<T> Class

Standard Queue Implementation in .NET

The Queue<T> Class

- ◆ Implements the queue data structure using a circular resizable array
 - ◆ Elements are from the same type T
 - ◆ T can be any type, e.g. Stack<int>
 - ◆ Size is dynamically increased as needed
- ◆ Basic functionality:
 - ◆ Enqueue(T) – adds an element to the end of the queue
 - ◆ Dequeue() – removes and returns the element at the beginning of the queue

- ◆ **Basic functionality:**
 - ◆ **Peek()** – returns the element at the beginning of the queue without removing it
 - ◆ **Count** – returns the number of elements
 - ◆ **Clear()** – removes all elements
 - ◆ **Contains(T)** – determines whether given element is in the queue
 - ◆ **ToArray()** – converts the queue to an array
 - ◆ **TrimExcess()** – sets the capacity to the actual number of elements in the queue

Queue<T> – Example

- ◆ Using Enqueue() and Dequeue() methods

```
static void Main()
{
    Queue<string> queue = new Queue<string>();
    queue.Enqueue("Message One");
    queue.Enqueue("Message Two");
    queue.Enqueue("Message Three");
    queue.Enqueue("Message Four");
    while (queue.Count > 0)
    {
        string message = queue.Dequeue();
        Console.WriteLine(message);
    }
}
```

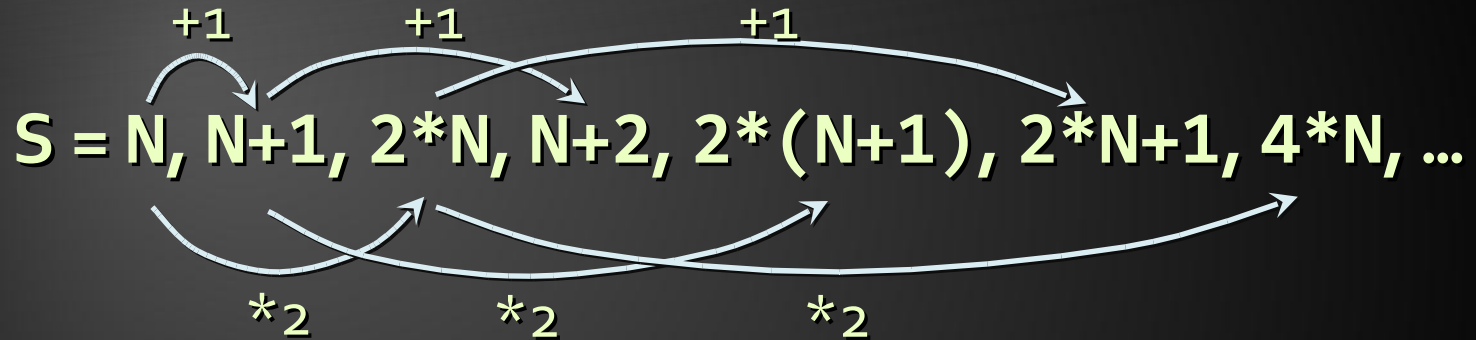


The Queue<T> Class

Live Demo

Sequence $N, N+1, 2*N$

- ◆ We are given the sequence:



- ◆ Find the first index of given number P
- ◆ Example: $N = 3, P = 16$

$S = 3, 4, 6, 5, 8, 7, 12, 6, 10, 9, \boxed{16}, 8, 14, \dots$

Index of $P = 11$

Sequence – Solution with a Queue

```
int n = 3, p = 16;

Queue<int> queue = new Queue<int>();
queue.Enqueue(n);
int index = 0;
while (queue.Count > 0)
{
    int current = queue.Dequeue();
    index++;
    if (current == p)
    {
        Console.WriteLine("Index = {0}", index);
        return;
    }
    queue.Enqueue(current+1);
    queue.Enqueue(2*current);
}
```

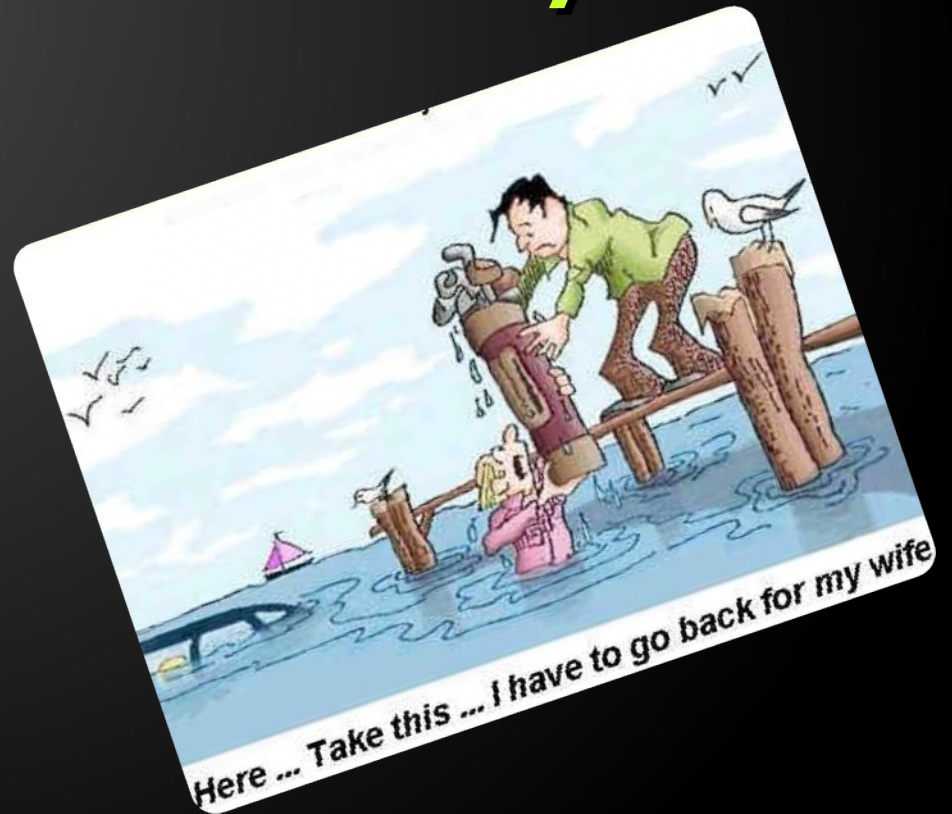


Sequence N , $N+1$, $2*N$

Live Demo



Priority Queue



- ◆ What is a Priority Queue
 - ◆ Data type to efficiently support finding the item with the highest priority
 - ◆ Basic operations
 - ◆ Enqueue(T element)
 - ◆ Dequeue
- ◆ There is no build-in Priority Queue in .NET
 - ◆ Can be easily implemented using PowerCollections

✂telerik Priority Queue Implementation

```
class PriorityQueue<T> where T:IComparable<T>
{
    private OrderedBag<T> bag;
    public int Count
    {
        get { return bag.Count; }
        private set{ }
    }
    public PriorityQueue()
    {
        bag = new OrderedBag<T>();
    }
    public void Enqueue(T element)
    {
        bag.Add(element);
    }
    public T Dequeue()
    {
        var element = bag.GetFirst();
        bag.RemoveFirst();
        return element;
    }
}
```

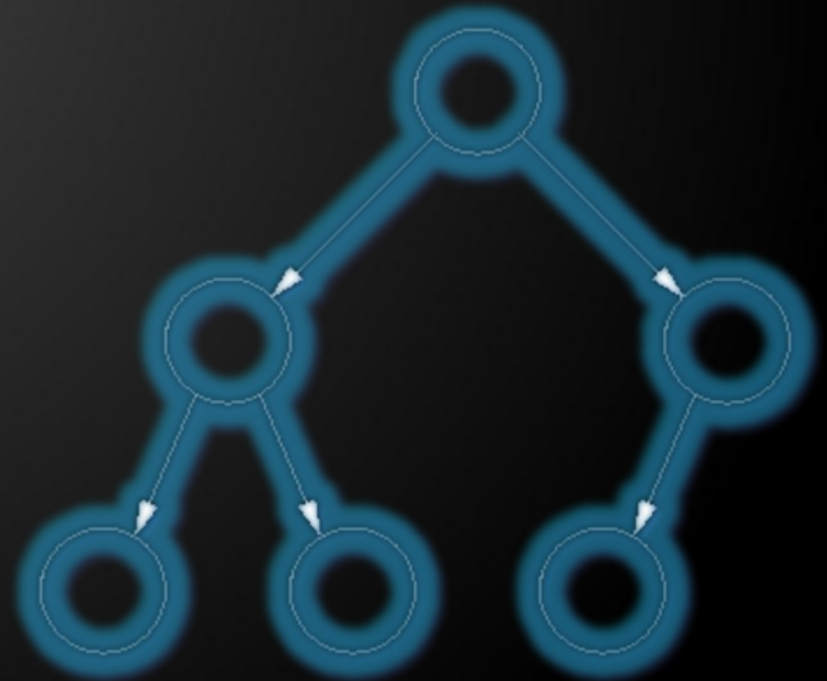
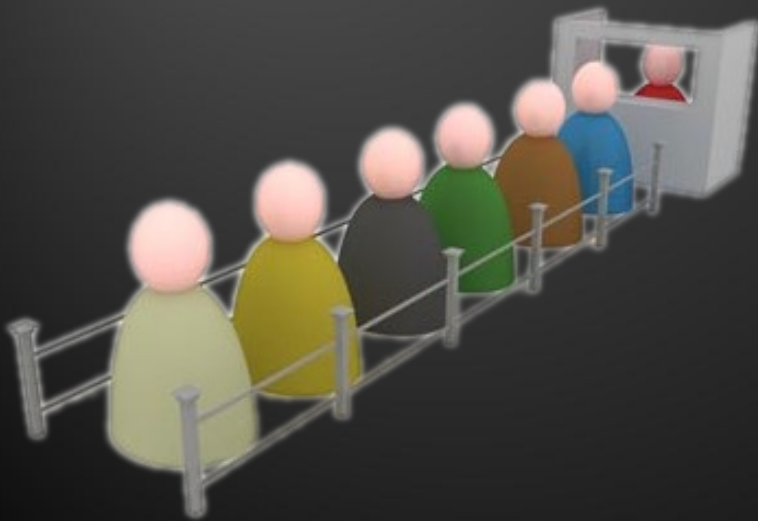
Necessary to provide
comparable elements

Priority Queue Additional Notes

- ◆ The generic type is needed to implement `Comparable<T>`
- ◆ It is not necessary to use `OrderedBag`
 - ◆ Other Data Structures also can be used
- ◆ Adding and Removing Element in the Priority Queue is with complexity $\log N$
- ◆ Keeps the elements Sorted
 - ◆ Always returns the best element that fulfills some condition
 - ◆ E.g. the smallest or the biggest element

Priority Queue

Live Demo



- ◆ ADT are defined by list of operations independent of their implementation
- ◆ The basic linear data structures in the computer programming are:
 - ◆ List (static, linked)
 - ◆ Implemented by the `List<T>` class in .NET
 - ◆ Stack (static, linked)
 - ◆ Implemented by the `Stack<T>` class in .NET
 - ◆ Queue (static, linked)
 - ◆ Implemented by the `Queue<T>` class in .NET
 - ◆ Priority Queue
 - ◆ Implemented by the `OrderedBag<T>` class



Questions?

1. Write a program that reads from the console a sequence of positive integer numbers. The sequence ends when empty line is entered. Calculate and print the sum and average of the elements of the sequence. Keep the sequence in `List<int>`.
2. Write a program that reads N integers from the console and reverses them using a stack. Use the `Stack<int>` class.
3. Write a program that reads a sequence of integers (`List<int>`) ending with an empty line and sorts them in an increasing order.

1. Write a method that finds the longest subsequence of equal numbers in given `List<int>` and returns the result as new `List<int>`. Write a program to test whether the method works correctly.
2. Write a program that removes from given sequence all negative numbers.
3. Write a program that removes from given sequence all numbers that occur odd number of times.

Example:

$\{4, 2, 2, 5, 2, 3, 2, 3, 1, 5, 2\} \rightarrow \{5, 3, 3, 5\}$

1. Write a program that finds in given array of integers (all belonging to the range [0..1000]) how many times each of them occurs.

Example: array = {3, 4, 4, 2, 3, 3, 4, 3, 2}

2 → 2 times

3 → 4 times

4 → 3 times

2. * The majorant of an array of size N is a value that occurs in it at least $N/2 + 1$ times. Write a program to find the majorant of given array (if exists). Example:

{2, 2, 3, 3, 2, 3, 4, 3, 3} → 3

1. We are given the following sequence:

$$S_1 = N;$$

$$S_2 = S_1 + 1;$$

$$S_3 = 2*S_1 + 1;$$

$$S_4 = S_1 + 2;$$

$$S_5 = S_2 + 1;$$

$$S_6 = 2*S_2 + 1;$$

$$S_7 = S_2 + 2;$$

...

Using the `Queue<T>` class write a program to print its first 50 members for given N.

Example: $N=2 \rightarrow 2, 3, 5, 4, 4, 7, 5, 6, 11, 7, 5, 9, 6, \dots$

1. We are given numbers N and M and the following operations:

a) $N = N + 1$

b) $N = N + 2$

c) $N = N * 2$

Write a program that finds the shortest sequence of operations from the list above that starts from N and finishes in M . Hint: use a queue.

- ♦ Example: $N = 5, M = 16$
- ♦ Sequence: $5 \rightarrow 7 \rightarrow 8 \rightarrow 16$

1. Write a class `Student`, that has three fields: `name (String)`, `age(Integer)` and `paidSemesterOnline(Boolean)`. When in a queue the students who paid online are with higher priority than those who are about to pay the semester. Write a program which with a given queue of student determine whose turn it is. Hint: use priority queue

1. Implement the data structure linked list. Define a class `ListItem<T>` that has two fields: `value` (of type `T`) and `nextItem` (of type `ListItem<T>`). Define additionally a class `LinkedList<T>` with a single field `firstElement` (of type `ListItem<T>`).
2. Implement the ADT stack as auto-resizable array. Resize the capacity on demand (when no space is available to add / insert a new element).
3. Implement the ADT queue as dynamic linked list. Use generics (`LinkedListQueue<T>`) to allow storing different data types in the queue.

1. * We are given a labyrinth of size $N \times N$. Some of its cells are empty (0) and some are full (x). We can move from an empty cell to another empty cell if they share common wall. Given a starting position (*) calculate and fill in the array the minimal distance from this position to any other cell in the array. Use "u" for all unreachable cells. Example:

0	0	0	x	0	x
0	x	0	x	0	x
0	*	x	0	x	0
0	x	0	0	0	0
0	0	0	x	x	0
0	0	0	x	0	x

→

3	4	5	x	u	x
2	x	6	x	u	x
1	*	x	8	x	10
2	x	6	7	8	9
3	4	5	x	x	10
4	5	6	x	u	x