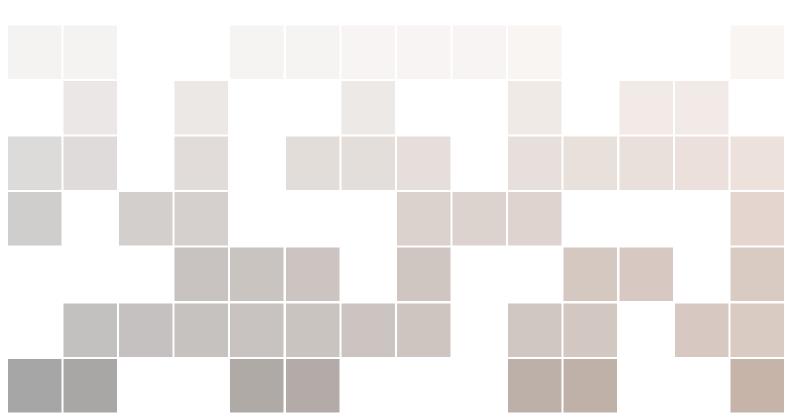


# Representation and Reasoning for Intelligent Systems

Stefan Klaus



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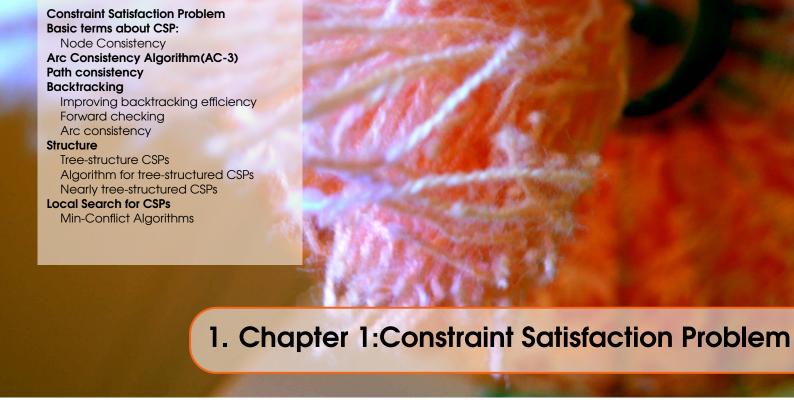
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#### 1.1 Constraint Satisfaction Problem

Constraint satisfaction problems(CSP) are mathematical problems defined as a set of objects whose state must satisfy a number of constraints or limitations. One example of a CSP is the game "Sudoku"

#### 1.2 Basic terms about CSP:

- an assignment is to assign values to some or all variables
- an assignment that does not violate any constraints is called a consistent assignment. With values from domain D\_i
- A complete assignment is one in which each variable is assigned
- a partial assignment is one that assigns value to some of the variables

#### **Constraint graph**

Binary CSP: each constraint relates at most two variables, e.g. WASA constraint graph: nodes are variables(e.g. region WA), arcs show constraints(e.g. WASA)

#### Varieties of Variables

Discrete variables

- Finite Domains
- boolean CSPs, include: boolean satisfiability(NP complete)
- Sudoku
- Infinite Domains(Integers, Strings, etc.)
- job scheduling, variables are start/end days for each job, need a constraint language, e.g.  $StartJob_1 + 5 \le StarJob_3$

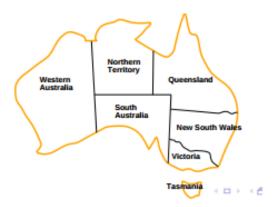
#### Continuous variables

- start /end times for Hubble Telescope observations
- Unary constraints involve a single variable
  - $SA \neq Green$

- binary constraints involve pairs of variables
  - $SA \neq WA$
- Higher-order constraints involve 3 or more variables
  - cryptarithmetic column constraints
- Preferences(soft) constraints
  - red is better than green
  - CSPs with preference are often with optimization search algorithms constraints optimization problems

#### 1.2.1 Node Consistency

If a node is node-consistent if all the value's domain satisfy the variable's unary constraints.



Example:

D = Red, Green, Blue

Variable X

X dislikes green, then X starts with D = Red, Green, Blue, and becomes node consistent after eliminating Green. X is node consistent with the reduced domain, D=Red, Blue.

#### **Arc Consistency**

 $X_i$  is arc-consistent with respect to another variables  $X_j$  if for every value in  $X_i$ 's current domain  $D_i$  there is one value in  $X_i$ 's domain  $D_j$  that satisfies the binary constraint on the arc  $(X_i, X_j)$ 

#### Example:

Given two variables  $X_i$ ,  $X_j$  with values in 0,1,2,...9 and constraints (0,0),(1,1),(2,4),(3,9). To make  $X_i$  arc-consistent with respect to  $X_j$ , we reduce  $X_i$ 's domain to 0,1,2,3. To make  $X_j$  arc-consistent with respect to  $X_i$ , we reduce  $X_j$ 's domain to 0,1,4,9.

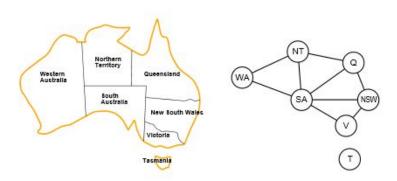
#### 1.3 Arc Consistency Algorithm(AC-3)

```
Input:
 A set of variables X
 A set of domains D(x) for each variable x in X. D(x) contains vx0, vx1...
     vxn, the possible values of x
 A set of unary constraints R1(x) on variable x that must be satisfied
 A set of binary constraints R2(x, y) on variables x and y that must be
     satisfied
Output:
 Arc consistent domains for each variable.
function ac3 (X, D, R1, R2)
// Initial domains are made consistent with unary constraints.
   for each x in X
       D(x) := \{ x \text{ in } D(x) \mid R1(x) \}
   // 'worklist' contains all arcs we wish to prove consistent or not.
   worklist := { (x, y) | there exists a relation R2(x, y) or a relation
       R2(y, x) }
   do
       select any arc (x, y) from worklist
       worklist := worklist - (x, y)
       if arc-reduce (x, y)
           if D(x) is empty
               return failure
               worklist := worklist + \{(z, x) \mid z != y \text{ and there exists a }
                  relation R2(x, z) or a relation R2(z, x) }
   while worklist not empty
function arc-reduce (x, y)
   bool change = false
   for each vx in D(x)
       find a value vy in D(y) such that vx and vy satisfy the constraint
           R2(x, y)
       if there is no such vy {
           D(x) := D(x) - vx
           change := true
   return change
```

- 1. initially let a queue contain all arcs
- 2. remove an arc  $(X_i, X_i)$  from the queue and make the variable  $X_i$  arc-consistent to  $X_i$ 
  - (a) IF $X_i$  domain  $D_i$  is unchanged, then check the next arc in the queue
  - (b) IF  $X_i$  's domain  $D_i$  is revised(smaller), then add all arcs  $(X_k, X_i)$  in the queue
  - (c) If  $X_i$  's domain  $D_i$  is empty, then CSP no solution
- 3. Keep checking all arcs in the queue until the queue is empty

#### 1.4 Path consistency

A two variable set  $X_i, X_j$  is path consistency with respect to a third variable  $X_m$  if for every assignment  $X_i = a, X_j = b$  consistent with the constraints on  $X_i, X_j$ , where is an assignment to  $X_m$ 



,that satisfies the constraints on  $X_i, X_m$  and  $X_m, X_j$ 

#### Example:

Can we color the Australia map with two colors? Make the set WA, SA path consistent with respect to NT? Assignments: WA = blue, SA = red or WA =blue, SA=red But no assignment exists for NT

#### **Constraint propagation**

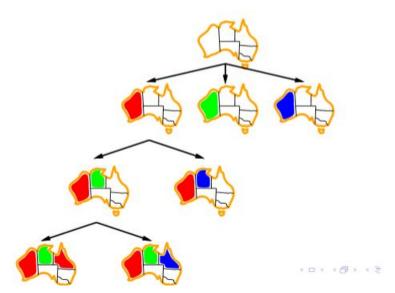
- constraint propagation is a specific type of inference
  - use the constraints to reduce the number of legal values for a variable, which in turn can reduce the legal values for another variable, and so on
- node consistency
- arc consistency
- path consistency
- k-consistency: k variables involved
- Global consistency

#### Limits

- Indeed AC-3 works for the easiest Sudoku puzzles
- slightly harder ones can be solved by PC-2, but at a greater computational cost: there are 255,960 different path constraints to consider in a Sudoku puzzle
- To solve the hardest puzzles and to make efficient progress, we will have to be more clever

1.5 Backtracking 9

#### 1.5 Backtracking



- 1. Select an unassigned value
- 2. assign values
- 3. Depth-first search

return failure

4. If an inconsistency is detected, then BACKTRACK returns failure, causing the previous call to try another value

Backtracking search is a depth-first search for CSPs

- choose values for one variable at a time
- backtrack when a variables has no legal left to assign

Backtracking search is the basic uninformed algorithm for CSP. Can solve n-queens for  $n \approx 25$ .

# function BACKTRACKING-SEARCH(csp) returns a solution, or failure return BACKTRACK({}, csp)

function BACKTRACK(assignment, csp) returns a solution, or failure
 if assignment is complete then return assignment
 var ← SELECT-UNASSIGNED-VARIABLE(csp)
 for each value in ORDER-DOMAIN-VALUES(var, assignment, csp) do
 if value is consistent with assignment then
 add {var = value} to assignment
 inferences ← INFERENCE(csp, var, value)
 if inferences ≠ failure then
 add inferences to assignment
 result ← BACKTRACK(assignment, csp)
 if result ≠ failure then
 return result
 remove {var = value} and inferences from assignment

#### 1.5.1 Improving backtracking efficiency

General-purpose methods can give huge gains in speed:

- 1. which variable should be assigned next?
- 2. in what order should values be tried'?
- 3. can we detect inevitable failure early?
- 4. Can we take advantage of problem structure?

#### Minimum remaining values

Minimum remaining values (MRV): choose the variable with the fewest legal values.

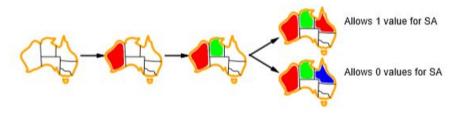
#### Degree heuristic

- Tie-breaker among MRV variables
- Degree heuristic: choose the variable with the most constraints on remaining variables



#### Least constraining value

Given a variable, choose the least constraining value: the one that rules out the fewest values in the remaining variables.



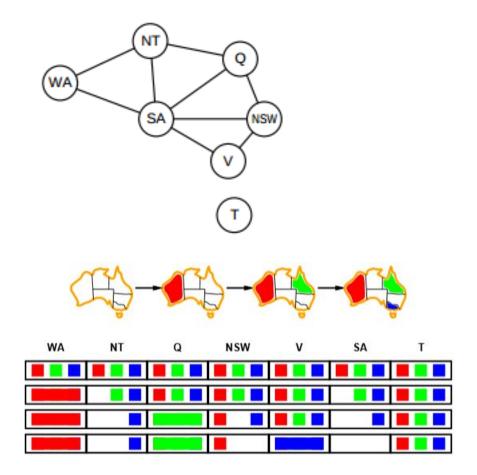
Combining

these heuristics makes 1000 queens feasible.

#### 1.5.2 Forward checking

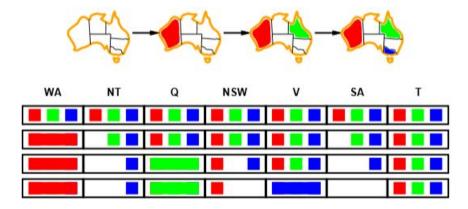
Idea: Keep track if remaining legal values for unassigned variables. Terminates search when any variable has no legal values.

1.5 Backtracking



#### **Constraint propagation**

Forward checking propagates information from assigned to unassigned variables, but doesn't provide early detection for all failures:



NT and SA cannot both be blue!

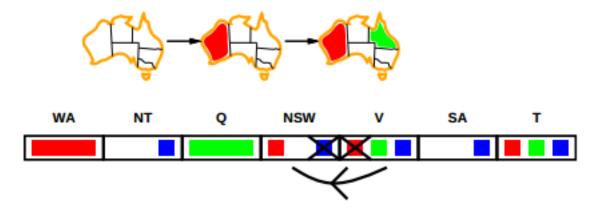
Constraint propagation repeatedly enforces constraints locally.

# 1.5.3 Arc consistency

Simplest form of propagation makes each arc consistent.

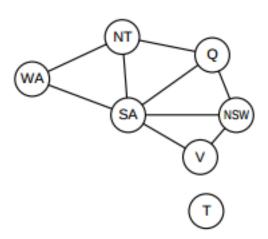
 $X \rightarrow Y$  is consistent if for every value x of X there is some allowed y

If X looses a value, neighbours needs to be rechecked.



Arc consistency detects failure earlier than forward checking. Can be run as a predecessor or after each assignment.

#### 1.6 Structure



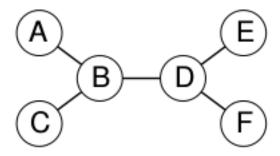
Tasmania and mainland Australia are independent subsections which can be identified as connected components of constraint graph.

- Suppose each subproblem has a c variable out of n total
- Worst-case solution cost is  $n/c * d^c$  liniar in n
- E.g. n = 80, d = 2, c = 20

  - $-2^{80} = 4$  billion years at 10 million nodes/sec  $-2 * 2^{20} = 0.4$  seconds at 10 million nodes/sec

1.6 Structure

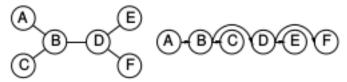
#### 1.6.1 Tree-structure CSPs



- Theorem: if the constraint graph has no loops, the CSP can be solved in  $O(nd^2)$  time
- Compare to general CSPs, where worst-case time is  $O(d^n)$
- This property also applies to logical and probabilistic reasoning: an important example of the relation between syntactic restrictions and the complexity of reasoning

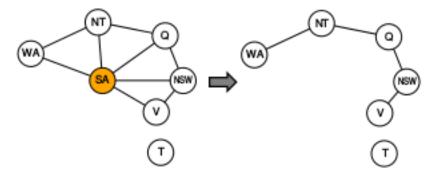
#### 1.6.2 Algorithm for tree-structured CSPs

- 1. Choose a variable as root, order variables from root to leaves such that every node's parent precedes it in the ordering
- 2. For j from n down to 2, apply RemoveInconsistent(Parent( $X_i$ ),  $x_i$ )
- 3. For j from 1 to n, assign  $X_i$  consistently with  $Parent(X_i)$



#### 1.6.3 Nearly tree-structured CSPs

- Conditioning: instantiate a variable, prune its neighbours domains
- Cutset conditioning: instantiate(in all ways) a set of variables such that the remaining constraint graph is a tree
- Cutset size  $c \Rightarrow runtimeO(d^c * (n-c)d^2)$ , very fast for small c



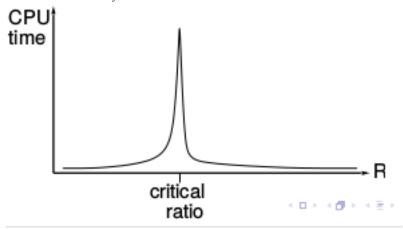
- Choose a subset S from VARIABLE[csp] such that the constraint graph becomes a tree after removal of S
- For each possible assignment to the variables in S satisfies all constraint on S
  - remove from the domains of the remaining variables any values that are inconsistent with the assignment of *S*
  - If the remaining CSP has solution, then return it together the assignment to S

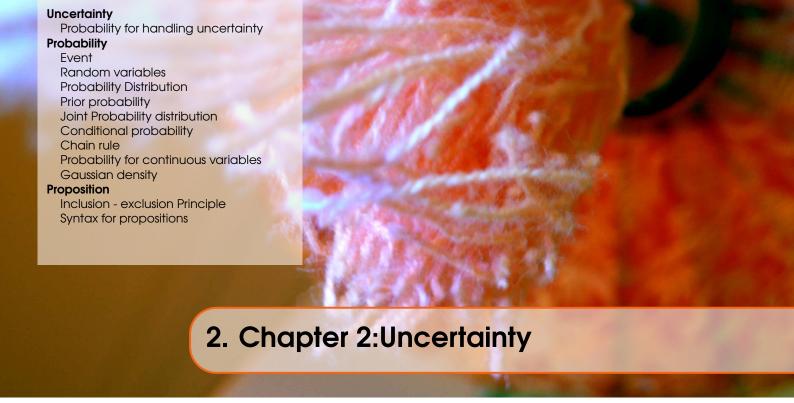
#### 1.7 Local Search for CSPs

- Local search, e.g. hill-climbing, simulated annealing for CSP
  - typically start with a "complete" state, i.e. all variables assigned to values, but may violated constraints
  - then search changes the value of one variable at each time for violated constraints
- Variable selection: randomly select any conflicted variable
- Value selection by min-conflicts heuristics:
  - choose value that violates the fewest constraints i.e. hillclimb with h(n) =total number of violated constraints

#### 1.7.1 Min-Conflict Algorithms

- Given random initial state, can solve *n*-queens in almost constant time for arbitrary n with high probability (e.g. n = 10000000)
- The same to be true for any randomly-generated CSP *except* in a narrow range of the ratio  $R = \frac{number of constraints}{number of variables}$





#### 2.1 Uncertainty

A purely logical approach may not work very well for statements which include multiple uncertain factors(e.g. Road accident on your way to the airport? Road work? Flooding? Nazi Zombies?

A purely logical approach would state: "A<sub>8</sub> will get me there on time."

Considering uncertain factors this would change to: "If there's no accident on the bridge, and it does not rain, and my tires remain intact etc, THEN  $A_8$  will get me there on time"

#### Reasons for that:

- Failure to enumerate exceptions, qualifications etc.
- No complete theory for the domain
- Lack of relevant facts, initial conditions and so on

#### 2.1.1 Probability for handling uncertainty

Probabilistic provides a way of summarizing the uncertainty. An example for that would be: conditional probabilities can be used to represent:

- Given the available evidence,  $A_8$  will get me there on time with probability 0.8
- Given the available evidence,  $A_10$  will get me there on time with probability 0.9
- Given the available evidence,  $A_12$  will get me there on time with probability 0.99

Condition	Result	Probability
Given the available evidence	$A_8$	0.9 0.99
Given the available evidence	$A_10$	0.99
Given the available evidence	$A_12$	0.999

Table 2.1: Table representation of the different plans

Probability theory is a main tool for dealing with degrees of belief.

#### Making decisions

Suppose given the following statements:

 $P(A_8 \text{ gets me there on time } | \text{Condition} = 0.9$   $P(A_{10} \text{ gets me there on time } | \text{Condition} = 0.99$   $P(A_{12} \text{ gets me there on time } | \text{Condition} = 0.999$  $P(A_{24} \text{ gets me there on time } | \text{Condition} = 0.9999$ 

Given that, what actions to choose?

• Depends on preferences, e.g. the length of the wait at the airport Utility theory is used to represent and infer preferences.

Decision theory = utility theory + probability theory

#### 2.2 Probability

Subjective or Bayesian probability:

- Probabilities relate propositions to one's own state of knowledge, e.g.  $P(A_8|noreportedaccidents) = 0.9$
- But might be learned from past experience from past experiences of similar situations
- Probabilities of propositions change with new evidence: e.g.  $P(A_8|noreportedaccidents, leave at 5am) = 0.95$

Sample point:

A set *Omega*- the sample space:  $\omega \in \Omega$  is a sample point or atomic event, e.g. 6 possible rolls of a dice.

A probability model/space is a sample space with assigning a probability for every  $\omega \in \Omega$ 

- P(1) = P(2) = P(3) = P(4) = P(5) = P(6) = 1/6
- Property:  $0 \le P(\omega) \le 1$  for every  $\omega \in \Omega$ ,  $\sum_{\omega \in \Omega} P(\omega) = 1$

#### 2.2.1 **Event**

An event A is any subset of  $\Omega$ .

$$P(A) = \sigma_{\omega \in A} P(\omega) \tag{2.1}$$

- An event is 'dice roll is less than 4'
- The probability of the event happening is P(diceroll < 4) = P(1) + P(2) + P(3) = 1/2In AI's language, the sets are decribed by propositions:
- $\phi$  is "dice roll is less than 4"
- $P(\phi) = \Sigma_{\omega \in \phi} P(\omega)$

#### 2.2.2 Random variables

A random variable  $X : \Omega \to R$  is a function from sample points to some range, e.g., the reals or Boolean.

Let  $X(\omega)$  be a Boolean variable to represent whether a dicing result  $\omega$  is odd, then:

2.2 Probability

$$X(1) = true$$
  
 $X(2) = False$ 

But usually written in short Odd P(Odd)

#### 2.2.3 Probability Distribution

For a random variable *X* taking values from  $x_1, \ldots, x_k$  probability distribution  $P(X = x_i)$  is the probability of *X* taking the value of  $x_i$ :

$$P(odd = true) = P(1) + P(3) + P(5)$$

$$= 1/6 + 1/6 + 1/6$$

$$= 1/2$$

$$P(Odd = false) = P(2) + P(4) + P(6)$$

$$= 1/6 + 1/6 + 1/6$$

$$= 1/2$$

#### 2.2.4 Prior probability

Prior or unconditional probabilities refer to degrees of belief in propositions in the absence of any other information

- P(Cavity = true) = 0.1
- P(Weather = Sunny) = 0.72

Probability distribution gives values for all possible probabilities:

P(Weather) = <0.72, 0.1, 0.08, 0.1 > normalized, i.e. sums to 1.

$$P(Weather = sunny) = 0.72$$
  
 $P(Weather = rain) = 0.1$   
 $P(Weather = cloudy) = 0.08$   
 $P(Weather = snow) = 0.1$ 

#### 2.2.5 Joint Probability distribution

Joint Probability distribution for a set of r.v.s gives the probability of every atomic event on those r.v.s(i.e. every sample point)

	Toothache		¬ Toothache	
	catch   ¬catch		catch	$\neq$ catch
cavity	0.108	0.012	0.072	0.008
¬cavity	0.016	0.064	0.144	0.576

#### 2.2.6 Conditional probability

Conditional or posterior probabilities:

given some information, sometimes called evidence, the probability of an event happening under the evidence.

$$P(X_1,...,X_n) = P(X_1,...,X_{n-1})P(X_n|X_1,...,X_{n-1})$$

$$= P(X_1,...,X_{n-2})P(X_{n-1}|X_1,...,X_{n-2})P(X_n|X_1,...,X_{n-1})$$

$$= ...$$

$$= \prod_{i=1}^n P(X_i|X_1,...,X_{i-1})$$

- If a patient is observed to have toothache and no other information is yet available, then the probability of having cavity is 0.8
- P(cavityltootache) = 0.8

$$Tootache = true \Rightarrow P(cavity|tootache) = 0.8$$
 (2.2)

If we know more facts e.g. cavity is also given, then we have:

P(cavity|tootache, cavity) = 1 The less specific belief *remains valid* after more evidence arrives, but is not always *useful*. New evidence may be irrelevant, allowing simplification, e.g.:

$$P(cavity|tootache, dice = 1) = P(cavity|tootache) = 0.8$$
 (2.3)

This kind of inference, sanctioned by domain knowledge, is crucial.

#### Theorem 2.2.1 — Definition of conditional probability.

$$P(a|b) = \frac{P(a \cap b)}{P(b)} if P(b) \neq 0$$
(2.4)

When the example used so far is applied to this theorem we will get this:

$$P(cavity|tootache) = \frac{P(cavity, foothache)}{P(tootache)}$$
(2.5)

If the product rule is applied, it gives an alternative formulation:

$$P(a \cap b) = P(a|b)P(b) = P(b|a)P(a) \tag{2.6}$$

A general version holds for whole distributions, e.g.:

$$P(weather, cavity) = P(weather|cavity)P(cavity)$$
(2.7)

#### 2.2.7 Chain rule

Chain rule is derived by successive application of product rule:

#### 2.2.8 Probability for continuous variables

Where X is a real r.V., express distribution as a parametrized function of value, as shown in the next theorem:

2.2 Probability

$$D(x = x)$$
 =  $U[18.26](x)$   
= uniform density between [19, 26]

Theorem 2.2.2 — Probability density function D(x).

$$P(a < X < b) = \int_{a}^{b} D(x)dx$$
 (2.8)

Let X be a random variable a represent a student's age *x* in the university. Suppose that:

D(X = 20.5) = 0.125 really means:

$$\lim_{dx\to 0} P(20.5 \le X \le 20.5 + dx) = 0.125 \tag{2.9}$$

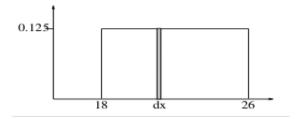


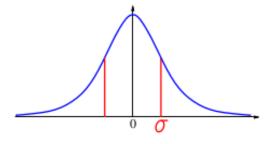
Figure 2.1: Probability density function for equation: 2.9

#### 2.2.9 Gaussian density

Theorem 2.2.3 — Gaussian density function. Is a widely used density function

$$D(X = x) = \frac{1}{\sqrt{2\pi\sigma}} e^{-(x-\mu)^2/2\sigma^2}$$
 (2.10)

When  $\mu = 0$  the functions looks like this:



Probability in  $X \in (a,b)$  is calculated by using the *probability density function* shown in equation: 2.9.

#### 2.3 Proposition

A proposition can be seen as an event(a set of sample points), where the following proposition is true:

A is "dice roll is less than 4"

$$P(A) = \sum_{\omega \in A} P(\omega) \tag{2.11}$$

Given Boolean random variables A and B:

- event a = the set of sample points where  $A(\omega) =$  true
- event  $\neg a$  = the set of sample points where  $A(\omega)$  = false
- event  $a \cap b$  = points where  $A(\omega)$  and  $B(\omega)$  = true

Often in AI applications, the sample points are defined by the values of a set of random variables, i.e., the sample space is the Cartesian product of the ranges of the variables. With Boolean variables, a sample points = propositional logic model.

• e.g. A = true, B = false, or  $a \cap \neg b$ Proposition = disjunction of atomic events in which it is true.

$$\begin{array}{lll} (a \cup b) & = & (\neg a \cap b) \cup (a \cap \neg b) \cup (a \cap b) \\ \Rightarrow P(a \cup b) & = & P(\neg a \cap b) + P(a \cap \neg b) + P(a \cap b) \end{array}$$

#### 2.3.1 Inclusion - exclusion Principle

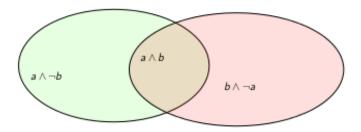


Figure 2.2: Inclusion-Exclusion Principle

The definitions imply that certain logically related events must have related probabilities(see figure 2.3.1).

$$P(a \cup b) = P(a) + P(b) - P(a \cap b)$$

$$\tag{2.12}$$

#### 2.3.2 Syntax for propositions

Propositional or Boolean random variables:

- e.g. Cavity(do I have a cavity?)
- Cavity = *true* is a proposition, also written cavity

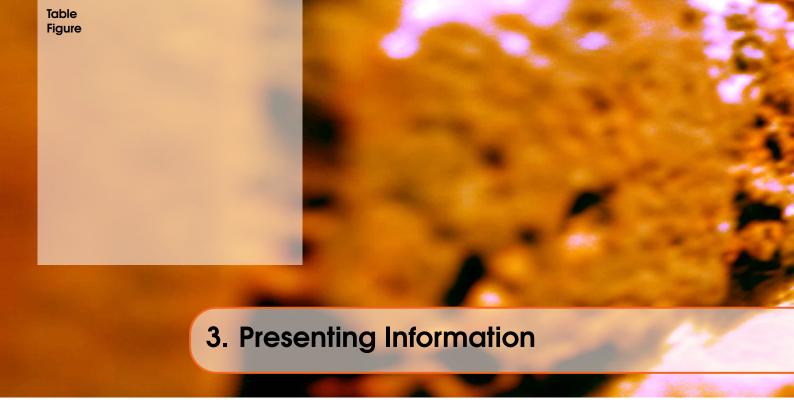
Discrete random variables(finite or infinite):

2.3 Proposition 21

- e.g., Weather is one of < sunny, rain, cloudy, snow>
- Weather = rain is a proposition
- Values must be exhaustive and mutually exclusive

Continuous random variables(bounded or unbounded):

- e.g., Temp = 21.6
- also allow, e.g. Temp < 22.0



# 3.1 Table

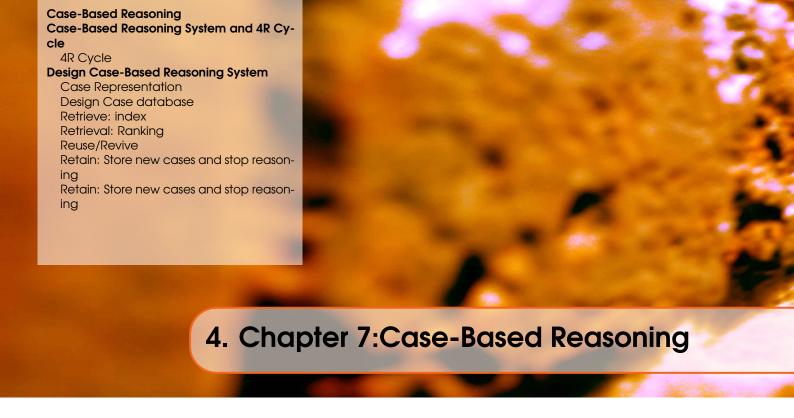
Treatments	Response 1	Response 2
Treatment 1	0.0003262	0.562
Treatment 2	0.0015681	0.910
Treatment 3	0.0009271	0.296

Table 3.1: Table caption

# 3.2 Figure

Placeholder Image

Figure 3.1: Figure caption



# 4.1 Case-Based Reasoning

- Case law: made up of, and from, hundred and thousands of precedent cases
- Principle: cases with similar facts should be treated in similar ways
- In cases where the parties disagree on what the law is: looking to past precedential decisions of relevant courts
- If a similar dispute has been resolved in the past: following the reasoning used in the prior decision
- If the current dispute is fundamentally distinct from all previous cases: creating new
- CBR: analogous to human experts solving a problem through employing their relevant past experience
  - exemplar-based reasoning
  - instance-based reasoning
  - memory-based reasoning
  - case-based reasoning
  - analogy-based reasoning
- if the new problem has some novel aspects, aspects, then the solution to the new problem is added to the case base
- Different from diagnostic fault tree or rule-based system
  - memory-based problem-solving
  - reusing past experiences

#### Domains that CBR Works well:

- Broad but shallow domain
  - not a single tree, but a forest of small trees
  - a number of loosely connected problems that must be dealt with
  - need different kinds of expertise
- Experience, rather than theory, is the primary source of knowledge
  - Many past examples of problems that occur
  - rather than having a deep understanding of the domain
- solutions are reusable
  - old solution is useful for a new problem
  - if each problem is different, then there is little to be gained by trying to reuse past

solutions

#### 4.2 Case-Based Reasoning System and 4R Cycle

- Input: new problem
- Output: a solution to the new problem
- case base
  - store cases(experience)

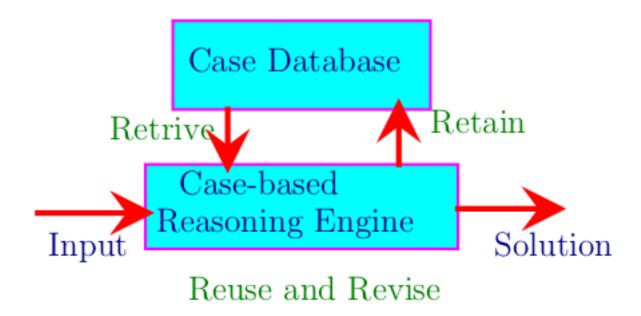


Figure 4.1: The Case-Based Reasoning System

#### 4.2.1 4R Cycle

- Retrieve: relevant cases, match most similar cases, retrieve solutions from theses cases
- Reuse: solutions in stored cases
- Revise: the retrieved solution(s) to reflect differences between new case and retrieved case(s)
- Retain: new cases into database

See figure 4.2 for visualisation.

#### New Problem vs Old Case

- Observations define a new problem
- Compare similarity of each feature
- Not all feature values may be known
- Some features may be more important
- New problem = case without a solution
- Similarity by weighted average

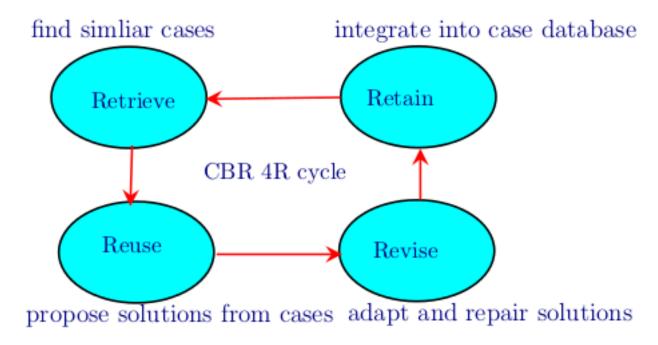


Figure 4.2: The Case-Based 4R cycle

#### 4.3 Design Case-Based Reasoning System

### 4.3.1 Case Representation

A case in diagnosis represents one diagnostic situation, include two parts:

- 1. Features
  - (a) symptoms
  - (b) failure
  - (c) feature values
  - (d) repair strategies
  - (e) test time and cost
- 2. Solutions
  - (a) cause of failure
  - (b) replace or repair fault unit

#### 4.3.2 Design Case database

- Dependent on the structure and content of its collection of cases
  - Deciding what to store in a case
  - Finding an appropriate structure for describing case contents
  - Deciding how the case memory should be organized and indexed for effective retrieval and reuse

#### 4.3.3 Retrieve: index

- Retrieve a case from case database
- Select indexes
  - Similar to books in library, index may help search cases in case database

#### **Match Case**

- Compare features and their value between the stored case and new problem
- Nearest-neighbour matching algorithm

#### 4.3.4 Retrieval: Ranking

- Possibly more than one case is matched
- Among matched cases, ranking may be used to choose a case to reuse
- If a matched case cannot provide the solution to the problem, lower rank cases may be taken as the candidate for the problem
- Ranking value will depend on observation time and cost
  - Higher the rank → better solution(cheaper, faster, etc.)
  - Ranking Observation cost, observation time and case frequency need to be considered

#### 4.3.5 Reuse/Revive

• Adapt/repair old solutions «««< HEAD

#### 4.3.6 Retain: Store new cases and stop reasoning

- Different approaches
  - Substitution
  - Parameter adjustment(via specialized heuristics, e.g. Judge)
  - Local search(replacing fruits in a recipe)
  - Special purpose adaptation and repair
  - Model-based

#### 4.3.7 Retain: Store new cases and stop reasoning

- Store all new cases
- Or store selected new cases(based on certain criteria?)
- The reasoning stops until a satisfied solution(from a solved case) is found
- or stop the reasoning procedure by the system



# 5.1 Rough sets

# 5.2 History

Rough set theory was created by some polish dude

# 5.3 Indivisibility

#### **5.4** Approximations

#### **5.4.1** Lower Approximations

Let A = (U,A) and let  $B \subseteq A$  and  $C \subseteq U$ . Define B-lower approximation of X, denoted B(C), to be:

#### 5.5 Dependency

Given a decision system  $A = U, A \cup d$ . The number of

	Age	LEMS
x1	16-30	50
x2	16-30	0
x3	31-45	1-25
x4	31-45	1-25

Table 5.1: Some table



Books Articles



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