

In this lab thinning and branchpoint and end endpoint detection techniques were used to recognize letters in an image of text.

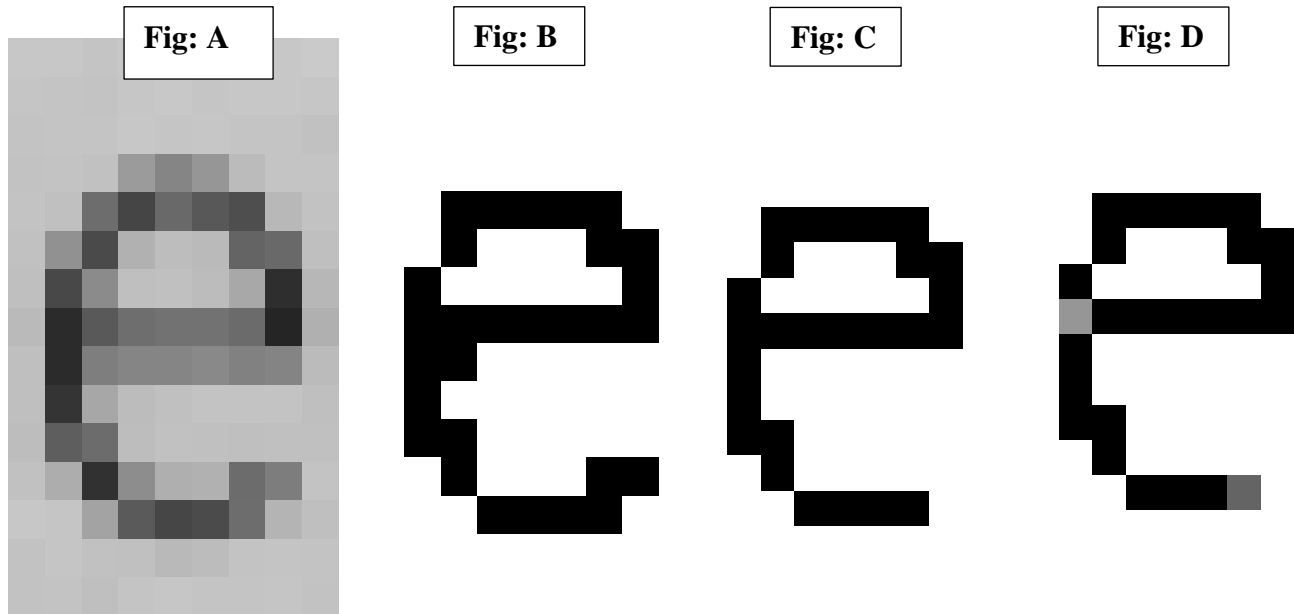
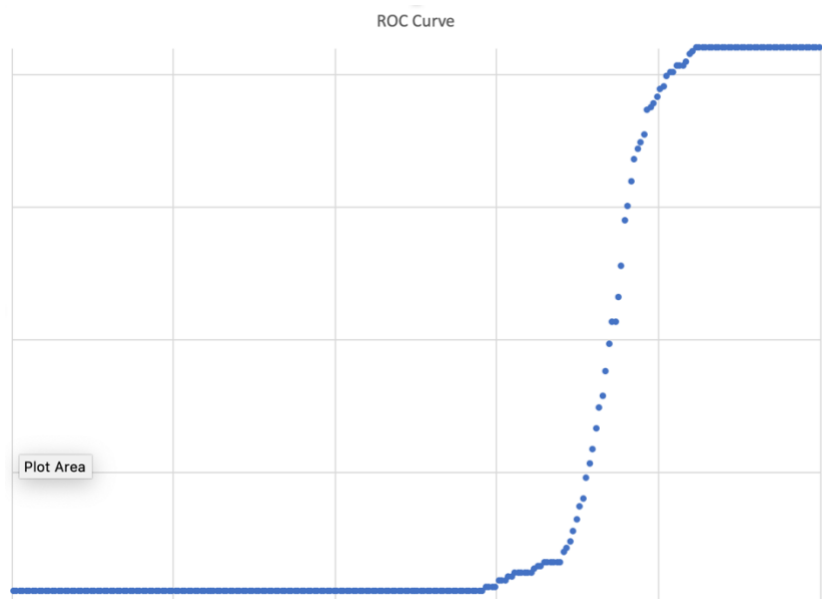


Figure A shows the pixel image extracted from the original image. Figure B shows the binary extracted image (step iv). Figure C shows the image after thinning (step v) and Figure D shows the detection of branchpoints and endpoints (step vi) where the branch points are shown as lighter grey and endpoints as darker grey. Here is an output confirming the branchpoints and endpoints were equal to 1 for this letter.

For letter e, the number of branch points is 1 and endpoints is 1

To the right is the ROC curve generated given the output of the program:



For this lab, I chose the optimal threshold value to be 203. Below are the TP and FP values at this threshold

Threshold = 203

TP = 100

FP = 7

Below is the output of all values for the different thresholds.

| | | | | |
|----------------|-------------|----------|---------|----------|
| Threshold = 0 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 1 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 2 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 3 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 4 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 5 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 6 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 7 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 8 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 9 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 10 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 11 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 12 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 13 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 14 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 15 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 16 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 17 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 18 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 19 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 20 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 21 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |

[illegible]

[illegible]

[illegible]

[illegible]

| | | | | |
|-----------------|-------------|----------|---------|----------|
| Threshold = 134 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 135 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 136 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 137 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 138 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 139 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 140 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 141 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 142 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 143 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 144 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 145 | TP = 102 | FP = 154 | FN = 49 | TN = 957 |
| TPR = 0.675 | FPR = 0.139 | | | |
| Threshold = 146 | TP = 102 | FP = 153 | FN = 49 | TN = 958 |
| TPR = 0.675 | FPR = 0.138 | | | |
| Threshold = 147 | TP = 102 | FP = 153 | FN = 49 | TN = 958 |
| TPR = 0.675 | FPR = 0.138 | | | |
| Threshold = 148 | TP = 102 | FP = 153 | FN = 49 | TN = 958 |
| TPR = 0.675 | FPR = 0.138 | | | |
| Threshold = 149 | TP = 102 | FP = 153 | FN = 49 | TN = 958 |
| TPR = 0.675 | FPR = 0.138 | | | |
| Threshold = 150 | TP = 102 | FP = 151 | FN = 49 | TN = 960 |
| TPR = 0.675 | FPR = 0.136 | | | |
| Threshold = 151 | TP = 102 | FP = 151 | FN = 49 | TN = 960 |
| TPR = 0.675 | FPR = 0.136 | | | |
| Threshold = 152 | TP = 102 | FP = 151 | FN = 49 | TN = 960 |
| TPR = 0.675 | FPR = 0.136 | | | |
| Threshold = 153 | TP = 102 | FP = 150 | FN = 49 | TN = 961 |
| TPR = 0.675 | FPR = 0.135 | | | |
| Threshold = 154 | TP = 102 | FP = 150 | FN = 49 | TN = 961 |
| TPR = 0.675 | FPR = 0.135 | | | |
| Threshold = 155 | TP = 102 | FP = 149 | FN = 49 | TN = 962 |
| TPR = 0.675 | FPR = 0.134 | | | |
| Threshold = 156 | TP = 102 | FP = 149 | FN = 49 | TN = 962 |
| TPR = 0.675 | FPR = 0.134 | | | |
| Threshold = 157 | TP = 102 | FP = 149 | FN = 49 | TN = 962 |
| TPR = 0.675 | FPR = 0.134 | | | |
| Threshold = 158 | TP = 102 | FP = 149 | FN = 49 | TN = 962 |
| TPR = 0.675 | FPR = 0.134 | | | |
| Threshold = 159 | TP = 102 | FP = 149 | FN = 49 | TN = 962 |
| TPR = 0.675 | FPR = 0.134 | | | |
| Threshold = 160 | TP = 102 | FP = 149 | FN = 49 | TN = 962 |
| TPR = 0.675 | FPR = 0.134 | | | |
| Threshold = 161 | TP = 102 | FP = 148 | FN = 49 | TN = 963 |
| TPR = 0.675 | FPR = 0.133 | | | |

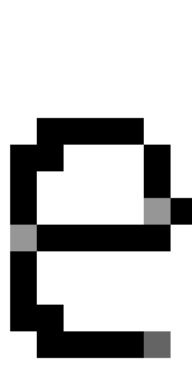
| | | | | |
|-----------------|-------------|----------|---------|-----------|
| Threshold = 162 | TP = 102 | FP = 147 | FN = 49 | TN = 964 |
| TPR = 0.675 | FPR = 0.132 | | | |
| Threshold = 163 | TP = 102 | FP = 147 | FN = 49 | TN = 964 |
| TPR = 0.675 | FPR = 0.132 | | | |
| Threshold = 164 | TP = 102 | FP = 146 | FN = 49 | TN = 965 |
| TPR = 0.675 | FPR = 0.131 | | | |
| Threshold = 165 | TP = 102 | FP = 146 | FN = 49 | TN = 965 |
| TPR = 0.675 | FPR = 0.131 | | | |
| Threshold = 166 | TP = 102 | FP = 146 | FN = 49 | TN = 965 |
| TPR = 0.675 | FPR = 0.131 | | | |
| Threshold = 167 | TP = 102 | FP = 146 | FN = 49 | TN = 965 |
| TPR = 0.675 | FPR = 0.131 | | | |
| Threshold = 168 | TP = 102 | FP = 146 | FN = 49 | TN = 965 |
| TPR = 0.675 | FPR = 0.131 | | | |
| Threshold = 169 | TP = 102 | FP = 146 | FN = 49 | TN = 965 |
| TPR = 0.675 | FPR = 0.131 | | | |
| Threshold = 170 | TP = 102 | FP = 143 | FN = 49 | TN = 968 |
| TPR = 0.675 | FPR = 0.129 | | | |
| Threshold = 171 | TP = 102 | FP = 142 | FN = 49 | TN = 969 |
| TPR = 0.675 | FPR = 0.128 | | | |
| Threshold = 172 | TP = 102 | FP = 140 | FN = 49 | TN = 971 |
| TPR = 0.675 | FPR = 0.126 | | | |
| Threshold = 173 | TP = 102 | FP = 137 | FN = 49 | TN = 974 |
| TPR = 0.675 | FPR = 0.123 | | | |
| Threshold = 174 | TP = 102 | FP = 134 | FN = 49 | TN = 977 |
| TPR = 0.675 | FPR = 0.121 | | | |
| Threshold = 175 | TP = 102 | FP = 130 | FN = 49 | TN = 981 |
| TPR = 0.675 | FPR = 0.117 | | | |
| Threshold = 176 | TP = 102 | FP = 128 | FN = 49 | TN = 983 |
| TPR = 0.675 | FPR = 0.115 | | | |
| Threshold = 177 | TP = 102 | FP = 122 | FN = 49 | TN = 989 |
| TPR = 0.675 | FPR = 0.110 | | | |
| Threshold = 178 | TP = 102 | FP = 118 | FN = 49 | TN = 993 |
| TPR = 0.675 | FPR = 0.106 | | | |
| Threshold = 179 | TP = 102 | FP = 114 | FN = 49 | TN = 997 |
| TPR = 0.675 | FPR = 0.103 | | | |
| Threshold = 180 | TP = 102 | FP = 108 | FN = 49 | TN = 1003 |
| TPR = 0.675 | FPR = 0.097 | | | |
| Threshold = 181 | TP = 102 | FP = 102 | FN = 49 | TN = 1009 |
| TPR = 0.675 | FPR = 0.092 | | | |
| Threshold = 182 | TP = 102 | FP = 99 | FN = 49 | TN = 1012 |
| TPR = 0.675 | FPR = 0.089 | | | |
| Threshold = 183 | TP = 102 | FP = 92 | FN = 49 | TN = 1019 |
| TPR = 0.675 | FPR = 0.083 | | | |
| Threshold = 184 | TP = 102 | FP = 84 | FN = 49 | TN = 1027 |
| TPR = 0.675 | FPR = 0.076 | | | |
| Threshold = 185 | TP = 102 | FP = 78 | FN = 49 | TN = 1033 |
| TPR = 0.675 | FPR = 0.070 | | | |
| Threshold = 186 | TP = 102 | FP = 78 | FN = 49 | TN = 1033 |
| TPR = 0.675 | FPR = 0.070 | | | |
| Threshold = 187 | TP = 102 | FP = 71 | FN = 49 | TN = 1040 |
| TPR = 0.675 | FPR = 0.064 | | | |
| Threshold = 188 | TP = 102 | FP = 62 | FN = 49 | TN = 1049 |
| TPR = 0.675 | FPR = 0.056 | | | |
| Threshold = 189 | TP = 102 | FP = 49 | FN = 49 | TN = 1062 |
| TPR = 0.675 | FPR = 0.044 | | | |

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|-----------------|-------------|---------|---------|-----------|-------|
| Threshold = 190 | TP = 102 | FP = 45 | FN = 49 | TN = 1066 | |
| TPR = 0.675 | FPR = 0.041 | | | | |
| Threshold = 191 | TP = 102 | FP = 38 | FN = 49 | TN = 1073 | |
| TPR = 0.675 | FPR = 0.034 | | | | |
| Threshold = 192 | TP = 102 | FP = 32 | FN = 49 | TN = 1079 | |
| TPR = 0.675 | FPR = 0.029 | | | | |
| Threshold = 193 | TP = 102 | FP = 29 | FN = 49 | TN = 1082 | |
| TPR = 0.675 | FPR = 0.026 | | | | |
| Threshold = 194 | TP = 102 | FP = 27 | FN = 49 | TN = 1084 | |
| TPR = 0.675 | FPR = 0.024 | | | | |
| Threshold = 195 | TP = 102 | FP = 25 | FN = 49 | TN = 1086 | |
| TPR = 0.675 | FPR = 0.023 | | | | |
| Threshold = 196 | TP = 102 | FP = 18 | FN = 49 | TN = 1093 | |
| TPR = 0.675 | FPR = 0.016 | | | | |
| Threshold = 197 | TP = 102 | FP = 17 | FN = 49 | TN = 1094 | |
| TPR = 0.675 | FPR = 0.015 | | | | |
| Threshold = 198 | TP = 102 | FP = 16 | FN = 49 | TN = 1095 | |
| TPR = 0.675 | FPR = 0.014 | | | | |
| Threshold = 199 | TP = 102 | FP = 14 | FN = 49 | TN = 1097 | |
| TPR = 0.675 | FPR = 0.013 | | | | |
| Threshold = 200 | TP = 101 | FP = 12 | FN = 50 | TN = 1099 | |
| TPR = 0.669 | FPR = 0.011 | | | | |
| Threshold = 201 | TP = 101 | FP = 11 | FN = 50 | TN = 1100 | |
| TPR = 0.669 | FPR = 0.010 | | | | |
| Threshold = 202 | TP = 101 | FP = 8 | FN = 50 | TN = 1103 | |
| TPR = 0.669 | FPR = 0.007 | | | | |
| Threshold = 203 | TP = 100 | FP = 7 | FN = 51 | TN = 1104 | |
| TPR = 0.662 | FPR = 0.006 | | | | |
| Threshold = 204 | TP = 99 | FP = 7 | FN = 52 | TN = 1104 | TPR = |
| 0.656 | FPR = 0.006 | | | | |
| Threshold = 205 | TP = 98 | FP = 5 | FN = 53 | TN = 1106 | TPR = |
| 0.649 | FPR = 0.005 | | | | |
| Threshold = 206 | TP = 98 | FP = 5 | FN = 53 | TN = 1106 | TPR = |
| 0.649 | FPR = 0.005 | | | | |
| Threshold = 207 | TP = 97 | FP = 5 | FN = 54 | TN = 1106 | TPR = |
| 0.642 | FPR = 0.005 | | | | |
| Threshold = 208 | TP = 96 | FP = 4 | FN = 55 | TN = 1107 | TPR = |
| 0.636 | FPR = 0.004 | | | | |
| Threshold = 209 | TP = 95 | FP = 2 | FN = 56 | TN = 1109 | TPR = |
| 0.629 | FPR = 0.002 | | | | |
| Threshold = 210 | TP = 95 | FP = 1 | FN = 56 | TN = 1110 | TPR = |
| 0.629 | FPR = 0.001 | | | | |
| Threshold = 211 | TP = 95 | FP = 0 | FN = 56 | TN = 1111 | TPR = |
| 0.629 | FPR = 0.000 | | | | |
| Threshold = 212 | TP = 94 | FP = 0 | FN = 57 | TN = 1111 | TPR = |
| 0.623 | FPR = 0.000 | | | | |
| Threshold = 213 | TP = 93 | FP = 0 | FN = 58 | TN = 1111 | TPR = |
| 0.616 | FPR = 0.000 | | | | |
| Threshold = 214 | TP = 90 | FP = 0 | FN = 61 | TN = 1111 | TPR = |
| 0.596 | FPR = 0.000 | | | | |
| Threshold = 215 | TP = 90 | FP = 0 | FN = 61 | TN = 1111 | TPR = |
| 0.596 | FPR = 0.000 | | | | |
| Threshold = 216 | TP = 88 | FP = 0 | FN = 63 | TN = 1111 | TPR = |
| 0.583 | FPR = 0.000 | | | | |
| Threshold = 217 | TP = 86 | FP = 0 | FN = 65 | TN = 1111 | TPR = |
| 0.570 | FPR = 0.000 | | | | |

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|-----------------|-------------|--------|----------|-----------|-------|
| Threshold = 218 | TP = 82 | FP = 0 | FN = 69 | TN = 1111 | TPR = |
| 0.543 | FPR = 0.000 | | | | |
| Threshold = 219 | TP = 82 | FP = 0 | FN = 69 | TN = 1111 | TPR = |
| 0.543 | FPR = 0.000 | | | | |
| Threshold = 220 | TP = 80 | FP = 0 | FN = 71 | TN = 1111 | TPR = |
| 0.530 | FPR = 0.000 | | | | |
| Threshold = 221 | TP = 79 | FP = 0 | FN = 72 | TN = 1111 | TPR = |
| 0.523 | FPR = 0.000 | | | | |
| Threshold = 222 | TP = 75 | FP = 0 | FN = 76 | TN = 1111 | TPR = |
| 0.497 | FPR = 0.000 | | | | |
| Threshold = 223 | TP = 72 | FP = 0 | FN = 79 | TN = 1111 | TPR = |
| 0.477 | FPR = 0.000 | | | | |
| Threshold = 224 | TP = 70 | FP = 0 | FN = 81 | TN = 1111 | TPR = |
| 0.464 | FPR = 0.000 | | | | |
| Threshold = 225 | TP = 69 | FP = 0 | FN = 82 | TN = 1111 | TPR = |
| 0.457 | FPR = 0.000 | | | | |
| Threshold = 226 | TP = 64 | FP = 0 | FN = 87 | TN = 1111 | TPR = |
| 0.424 | FPR = 0.000 | | | | |
| Threshold = 227 | TP = 61 | FP = 0 | FN = 90 | TN = 1111 | TPR = |
| 0.404 | FPR = 0.000 | | | | |
| Threshold = 228 | TP = 55 | FP = 0 | FN = 96 | TN = 1111 | TPR = |
| 0.364 | FPR = 0.000 | | | | |
| Threshold = 229 | TP = 52 | FP = 0 | FN = 99 | TN = 1111 | TPR = |
| 0.344 | FPR = 0.000 | | | | |
| Threshold = 230 | TP = 48 | FP = 0 | FN = 103 | TN = 1111 | |
| TPR = 0.318 | FPR = 0.000 | | | | |
| Threshold = 231 | TP = 45 | FP = 0 | FN = 106 | TN = 1111 | |
| TPR = 0.298 | FPR = 0.000 | | | | |
| Threshold = 232 | TP = 43 | FP = 0 | FN = 108 | TN = 1111 | |
| TPR = 0.285 | FPR = 0.000 | | | | |
| Threshold = 233 | TP = 39 | FP = 0 | FN = 112 | TN = 1111 | |
| TPR = 0.258 | FPR = 0.000 | | | | |
| Threshold = 234 | TP = 34 | FP = 0 | FN = 117 | TN = 1111 | |
| TPR = 0.225 | FPR = 0.000 | | | | |
| Threshold = 235 | TP = 30 | FP = 0 | FN = 121 | TN = 1111 | |
| TPR = 0.199 | FPR = 0.000 | | | | |
| Threshold = 236 | TP = 29 | FP = 0 | FN = 122 | TN = 1111 | |
| TPR = 0.192 | FPR = 0.000 | | | | |
| Threshold = 237 | TP = 28 | FP = 0 | FN = 123 | TN = 1111 | |
| TPR = 0.185 | FPR = 0.000 | | | | |
| Threshold = 238 | TP = 24 | FP = 0 | FN = 127 | TN = 1111 | |
| TPR = 0.159 | FPR = 0.000 | | | | |
| Threshold = 239 | TP = 23 | FP = 0 | FN = 128 | TN = 1111 | |
| TPR = 0.152 | FPR = 0.000 | | | | |
| Threshold = 240 | TP = 21 | FP = 0 | FN = 130 | TN = 1111 | |
| TPR = 0.139 | FPR = 0.000 | | | | |
| Threshold = 241 | TP = 18 | FP = 0 | FN = 133 | TN = 1111 | |
| TPR = 0.119 | FPR = 0.000 | | | | |
| Threshold = 242 | TP = 17 | FP = 0 | FN = 134 | TN = 1111 | |
| TPR = 0.113 | FPR = 0.000 | | | | |
| Threshold = 243 | TP = 16 | FP = 0 | FN = 135 | TN = 1111 | |
| TPR = 0.106 | FPR = 0.000 | | | | |
| Threshold = 244 | TP = 13 | FP = 0 | FN = 138 | TN = 1111 | |
| TPR = 0.086 | FPR = 0.000 | | | | |
| Threshold = 245 | TP = 10 | FP = 0 | FN = 141 | TN = 1111 | |
| TPR = 0.066 | FPR = 0.000 | | | | |

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|-----------------|--------|-------------|----------|-----------|
| Threshold = 246 | TP = 9 | FP = 0 | FN = 142 | TN = 1111 |
| TPR = 0.060 | | FPR = 0.000 | | |
| Threshold = 247 | TP = 6 | FP = 0 | FN = 145 | TN = 1111 |
| TPR = 0.040 | | FPR = 0.000 | | |
| Threshold = 248 | TP = 5 | FP = 0 | FN = 146 | TN = 1111 |
| TPR = 0.033 | | FPR = 0.000 | | |
| Threshold = 249 | TP = 4 | FP = 0 | FN = 147 | TN = 1111 |
| TPR = 0.026 | | FPR = 0.000 | | |
| Threshold = 250 | TP = 0 | FP = 0 | FN = 151 | TN = 1111 |
| TPR = 0.000 | | FPR = 0.000 | | |
| Threshold = 251 | TP = 0 | FP = 0 | FN = 151 | TN = 1111 |
| TPR = 0.000 | | FPR = 0.000 | | |
| Threshold = 252 | TP = 0 | FP = 0 | FN = 151 | TN = 1111 |
| TPR = 0.000 | | FPR = 0.000 | | |
| Threshold = 253 | TP = 0 | FP = 0 | FN = 151 | TN = 1111 |
| TPR = 0.000 | | FPR = 0.000 | | |
| Threshold = 254 | TP = 0 | FP = 0 | FN = 151 | TN = 1111 |
| TPR = 0.000 | | FPR = 0.000 | | |
| Threshold = 255 | TP = 0 | FP = 0 | FN = 151 | TN = 1111 |
| TPR = 0.000 | | FPR = 0.000 | | |

The reason for having numerous false negatives was due to the ignoring of the edge pixels which I was told to do by John Lawler. Below is an example of a false negative e.



As can be seen the reason it detected 2 branch points was because the edge cases were ignored as instructed to do.