

Time Synchronous Averaging

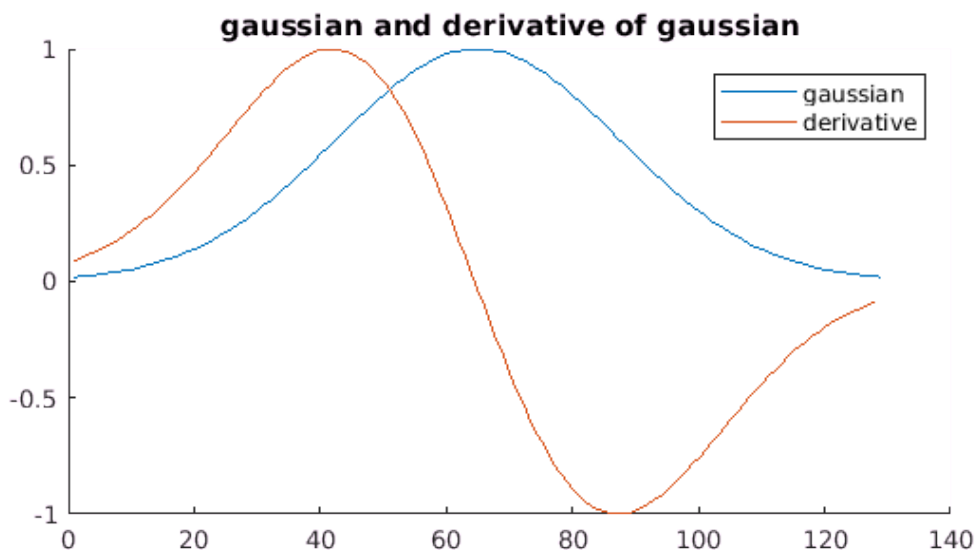
- http://www.phmsociety.org/sites/phmsociety.org/files/phm_submission/2009/phmc_09_5.pdf

Create a signal (use derivative of gaussian)

```
k = 128; %duration
gauss = exp(-linspace(-2,2,k+1).^2);
gauss_dx = diff(gauss);
gauss_dx = gauss_dx./max(gauss_dx); %normalize
```

- plot the event of interest

```
figure('Position', [0,0,600,300]); clf;
hold on;
gauss_plot = plot(gauss);
dx_plot = plot(gauss_dx);
title("gaussian and derivative of gaussian");
legend([gauss_plot, dx_plot], ["gaussian", "derivative"]);
hold off;
```



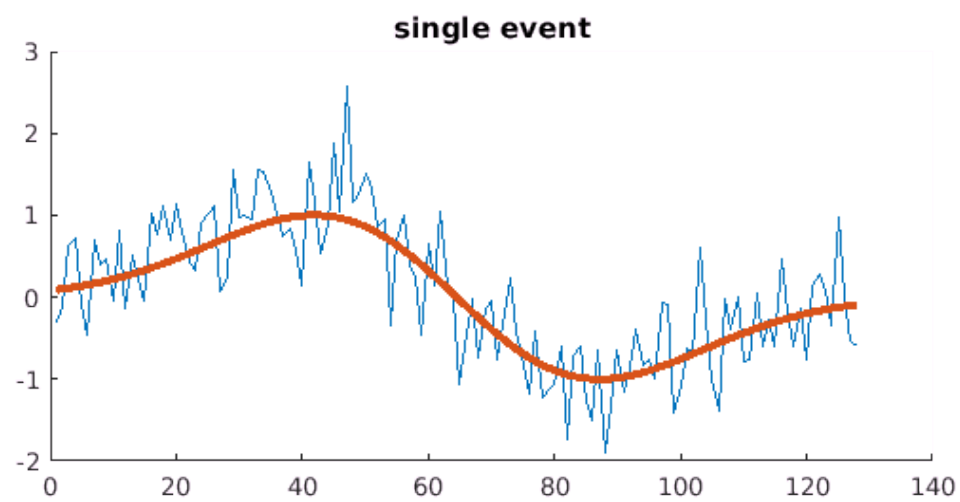
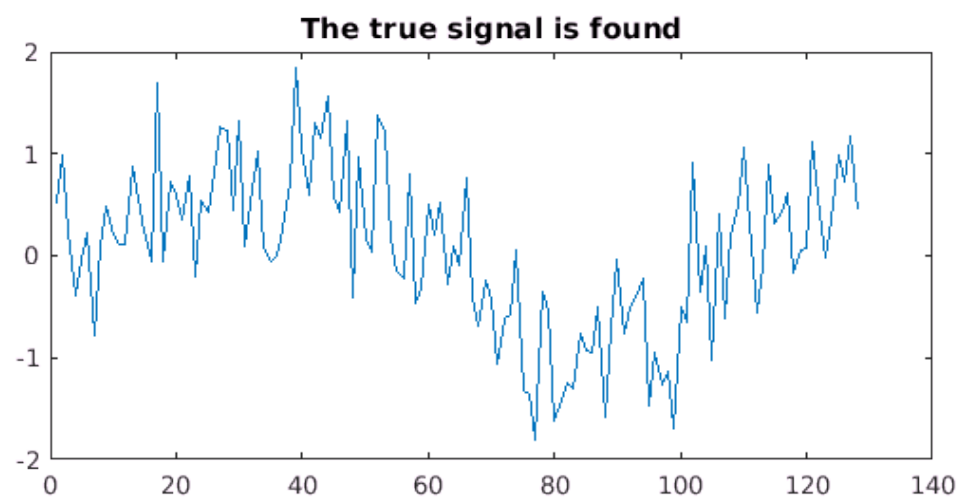
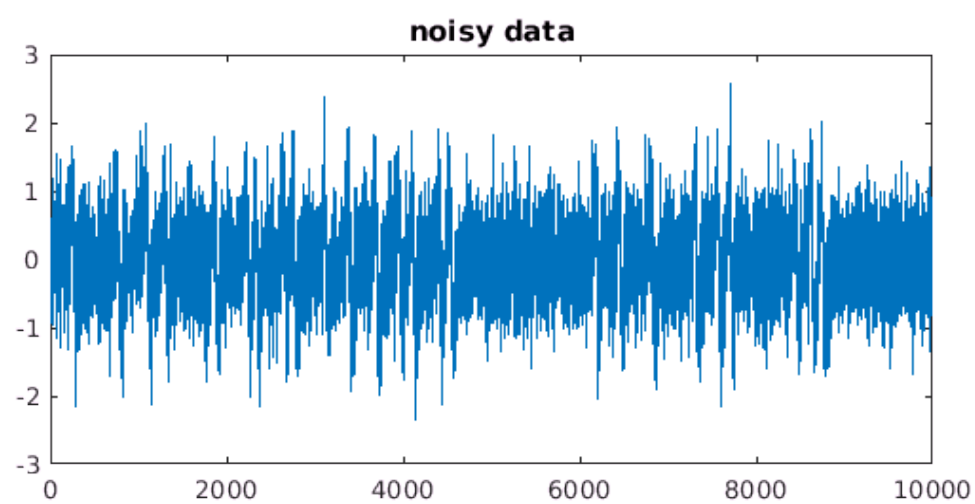
Duplicate the events (gauss_dx)

```
num_events = 32;
times = randperm(10000-k);
times = times(1:num_events);
data = zeros(1,10000);

for i = 1:num_events
    data(times(i):times(i)+k-1) = gauss_dx;
end
```

```
data = data + .5*randn(size(data));
```

```
figure('Position', [0,0,600,1000]);clf;  
subplot(311);  
plot(data);  
title("noisy data");  
  
subplot(312);  
plot(1:k, data(times(3):times(3)+k-1)); %3 chosen at random  
title("The true signal is found");  
  
subplot(313);  
hold on;  
plot(1:k, data(times(10):times(10)+k-1)); %10 chosen at random  
plot(1:k, gauss_dx, 'linew',3);  
title("single event");  
hold off;
```



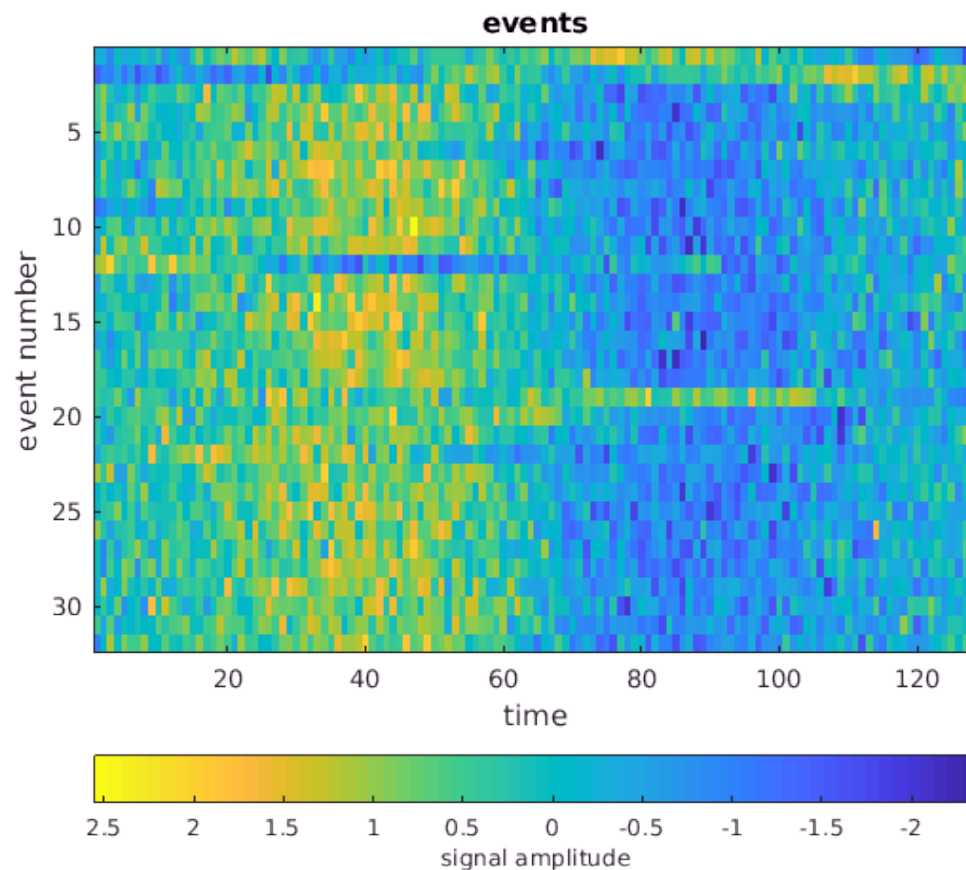
Average the events in the signal

- assumed it is known the time of each event
- for rotating machinery this a function of angular velocity

```
events = zeros(num_events, k);  
for i=1:num_events  
    events(i,:) = data(times(i):times(i)+k-1);  
end  
  
events_avg = mean(events);
```

- plot the events
- <https://www.mathworks.com/help/matlab/ref/imagesc.html>

```
figure('Position', [0,0,600,500]);  
imagesc(events);  
c = colorbar('southoutside', 'Direction', 'reverse');  
c.Label.String = "signal amplitude";  
xlabel("time");  
ylabel("event number");  
title("events");
```



```
figure('Position', [0,0,600,300]);
```

```
hold on;  
avg_plot = plot(1:k, events_avg); %the average  
true_plot = plot(1:k, gauss_dx, 'linewidth', 3); %true signal  
xlabel("time");  
ylabel("amplitude");  
legend([avg_plot, true_plot], ["averaged signal", "true signal"]);  
title({""; "time synchronous averaged signal"});
```

