

# Particle Swarm Optimization

- meta heuristic algorithm
- contains a population of candidate solutions
- particle  $i$  position  $\rightarrow x_i(t)$  where  $x_i(t)$  is a vector in the set of  $X$
- particle  $i$  velocity  $\rightarrow v_i(t)$
- particle  $i$  memory  $\rightarrow p_i(t)$  where  $p_i(t)$  is the best solution for particle  $i$
- $g(t)$  is the common swarm experience, no  $i$

## Particle Update Functions

- $v_i(t+1) = a \cdot v_i(t) + b \cdot (p_i(t) - x_i(t)) + c \cdot (g(t) - x_i(t))$
- $x_i(t+1) = x_i(t) + v_i(t+1)$
- $v_{ij}(t+1) = \text{inertia} + \text{cognitive} + \text{social}$  where  $v_{ij}$  is the  $j$ th scalar
- $x_{ij}(t+1) = x_{ij}(t) + v_{ij}(t+1)$

```
% EXAMPLE
%
% inertia = coef*velocity(i,j);
% cognitive = rand()*accel1*(particleBest(i,j) - particlePos(i,j));
% social = rand()*accel2*(globalBest(j) - particlePos(i,j));
```

## The Problem

- The sphere function
- <http://benchmarkfcns.xyz/benchmarkfcns/spherefcn.html>

## The Algorithm

- problem definition

```
% define the cost function
costFcn = @(x) sphere(x);

% number of unknown variables
vars = 5;

% matrix size of solutions
size = [1 vars];

% variable range
varMin = -20;
varMax = 20;
```

- parameters

```
% number of iterations
iterations = 100;

% number of particles
swarmSize = 50;

% inertia coefficient
w = 1;

% personal acceleration coefficient
accel1 = 2;

% social acceleration coefficient
accel2 = 2;
```

- initialization

## Functions

sphere:

- the function to optimize

```
function z = sphere(x)
    z = sum(x.^2);
end
```