# Assignment 5 Sorting: Putting your affairs in order

Prof. Darrell Long CSE 13S – Winter 2020

Due: February 16<sup>th</sup> at 11:59 pm

Any inaccuracies in this index may be explained by the fact that it has been sorted with the help of a computer.

—Donald Knuth, Vol. III, Sorting and Searching

# 1 Introduction

Putting items into a sorted order is one of the most common tasks in Computer Science. As a result, there are a myriad of library routines that will do this task for you, but that does not absolve you of the obligation of understanding how it is done. In fact it behooves you to understand the various algorithms in order to make wise choices.

The best execution time that can be accomplished, also referred to as the *lower bound*, for sorting using *comparisons* is  $\Omega(n \log n)$ , where n is the number is elements to be sorted. If the universe of elements to be sorted is small, then we can do better using a *Count Sort* or a *Radix Sort* both of which have a time complexity of O(n). The idea of *Count Sort* is to count the number of occurrences of each element in an array. For *Radix Sort*, a digit by digit sort is done by starting from the least significant digit to the most significant digit. It may also use *Count Sort* as a subroutine.

What is this O and  $\Omega$  stuff? It's how we talk about the execution time (or space used) by a program. We will discuss it in class, and you will see it again in your Data Structures and Algorithms class.

The sorting algorithms that you are expected to implement are Bubble Sort, Shell Sort, Quick Sort and Binary Insertion Sort. The purpose of this assignment is to get you fully familiarized with each sorting algorithm. They are well-known sorts. You can use the Python pseudocode provided to you as guidelines. Do not get the code for the sorts from the Internet or you will be referred to for cheating.

#### 1.1 Bubble Sort

C is peculiar in a lot of ways, but it, like many other successful things, has a certain unity of approach that stems from development in a small group.

—Dennis Ritchie

Bubble sort works by examining adjacent pairs of items. If the second item is smaller than the first, swap

them. As a result, the largest element falls to the bottom of the array in a single pass. Since it is in fact the largest, we do not need to consider it again. So in the next pass, we only need to consider n-1 pairs of items. The first pass requires n pairs to be examined; the second pass, n-1 pairs; the third pass n-2 pairs, and so forth. If you can pass over the entire array and no pairs are out of order, then the array is sorted.

#### Pre-lab Part 1

- 1. How many rounds of swapping do you think you will need to sort the numbers 8,22,7,9,31,5,13 in ascending order using Bubble Sort?
- 2. How many comparisons can we expect to see in the worse case scenario for Bubble Sort? Hint: make a list of numbers and attempt to sort them using Bubble Sort.

In 1784, when Carl Friedrich Gauss was only 7 years old, he was reported to have amazed his elementary school teacher by how quickly he summed up the integers from 1 to 100. The precocious little Gauss produced the correct answer immediately after he quickly observed that the sum was actually 50 pairs of numbers, with each pair summing to 101 totaling to 5,050. We can then see that:

$$n+(n-1)+(n-2)+\ldots+1=\frac{n(n+1)}{2},$$

So the *worst case* time complexity is  $O(n^2)$ . However, it could be much better if the list is already sorted. If you haven't seen the inductive proof for this yet, you will in the applied discrete math class.

```
def Bubble_Sort(arr):
    for i in range(len(arr) - 1):
        j = len(arr) - 1
    while j > i:
        if arr[j] < arr[j - 1]:
        arr[j], arr[j - 1] = arr[j - 1], arr[j]
        j -= 1
    return</pre>
```

Bubble Sort (pseudocode)

#### 1.2 Shell Sort

There are two ways of constructing a software design. One way is to make it so simple that there are obviously no deficiencies, and the other way is to make it so complicated that there are no obvious deficiencies. The first method is far more difficult.

-C.A.R. Hoare

Shell Sort is a variation of insertion sort, which sorts pairs of elements which are far apart from each other. The interval (or gap) between the compared items being sorted is continuously reduced. Shell Sort starts with distant elements and moves out-of-place elements into position faster than a simple nearest neighbor exchange. In the following code, an array of intervals is created by using gap(n) for an unsorted list of n elements. For example, for n = 20 unsorted elements, the set of gaps is  $\{9,4,1\}$ .

What is the expected time complexity of Shell Sort? All this depends upon the gap sequence. The number of elements in the gap sequence and their respective size scales with the number of elements n being sorted. The first loop is executed len(s)-step times and that number decreases as the gap size decreases.

The following is the pseudocode for Shell Sort. Given the length of array n, the function gap(n) produces an array of gaps. The rules is that if  $n \le 2$ , n = 1, else n = 5 \* n//11, in which // dumps the digits after the decimal. The array will be ranked from large to small. In the  $Shell\_Sort(n)$ , for each step in the array of gaps, it compares all the pairs that are away from each other by step in index and switches the elements in the pair if they are not sorted.

# Pre-lab Part 2

1. The worst time complexity for Shell sort depends on the size of the gap. Investigate why this is the case. How can you improve the time complexity of this sort by changing the gap size? Cite any sources you used.

Shell Sort (pseudocode)

2. How would you improve the runtime of this sort without changing the gapp size?

### 1.3 Quicksort

If debugging is the process of removing software bugs, then programming must be the process of putting them in.

-Edsger Dijkstra

Quicksort is a divide-and-conquer algorithm. It partitions arrays into two subarrays by selecting an element from the array and designating it as a pivot. Elements in the array that are less than the pivot go to the left subarray, and elements in the array that are greater than or equal to the pivot go to the right subarray. Note that Quicksort is an *in-place* algorithm, meaning it doesn't allocate additional memory for subarrays to hold partitioned elements. Instead, Quicksort utilizes a subroutine called Partition()

that places elements less than the pivot into the left side of the array and elements greater than or equal to the pivot into the right side and returns the index that indicates the division between the partitioned parts of the array. Quicksort is then run recursively on the partitioned parts of the array, thereby sorting each array partition containing at least one element.

```
def Partition(arr, left, right):
   pivot = arr[left]
   lo = left + 1
   hi = right
   while True:
      while lo <= hi and arr[hi] >= pivot:
        hi -= 1
     while lo <= hi and arr[lo] <= pivot:</pre>
10
        1o += 1
11
      if lo <= hi:</pre>
        arr[lo], arr[hi] = arr[hi], arr[lo]
        break
16
    arr[left], arr[hi] = arr[hi], arr[left]
   return hi
19
21 def Quick_Sort(arr, left, right):
   if left < right:</pre>
      index = Partition(arr, left, right)
      Quick_Sort(arr, left, index - 1)
      Quick_Sort(arr, index + 1, right)
   return
```

Quicksort (pseudocode)

# Pre-lab Part 3

1. Quicksort, with a worse case time complexity of  $O(n^2)$ , doesn't seem to live up to its name. Investigate and explain why Quicksort isn't doomed by its worst case scenario. Make sure to cite any sources you use.

#### 1.4 Binary Insertion Sort

Increasingly, people seem to misinterpret complexity as sophistication, which is baffling – the incomprehensible should cause suspicion rather than admiration.

-Niklaus Wirth

Binary Insertion Sort is a special type of insertion sort which uses the binary search algorithm to find the correct position of an inserted element in an array. Insertion sort works by finding the correct position of the element in the array and then inserting it into its correct position. Searching for an element using binary search is much like searching for a book on a shelf that is sorted alphabetically. First, identify the book sitting approximately at the midpoint between either end of the shelf. If it's the book you're looking for, then great! If the book you're looking for has a name that precedes the current book alphabetically, you only need to consider the left half of the shelf. Else, you only need to consider the right half of the shelf. Thus, it's clear that we are *halving* the search space each time we do a comparison, hence the name, binary search. Binary Insertion Sort uses binary search in order to determine where each element should go, reducing the number of comparisons between array elements we would ordinarily need for Insertion sort. For each element in the array, simply run a binary search through the elements to the left of the current element in order to find the index in which it should go.

```
1 def Binary_Insertion_Sort(arr):
   for i in range(1, len(arr)):
      value = arr[i]
      left = 0
      right = i
      while left < right:
        mid = left + ((right - left) // 2)
        if value >= arr[mid]:
          left = mid + 1
11
        else:
12
          right = mid
      for j in range(i, left, -1):
        arr[j - 1], arr[j] = arr[j], arr[j - 1]
16
   return
18
```

Binary Insertion Sort (pseudocode)

Each round in insertion sort involves picking a single element from the input array and finding a location in the sorted array where it can be placed. In the Binary Insertion Sort algorithm, this location is found using the binary search algorithm.

#### Pre-lab Part 4

1. Can you figure out what effect the binary search algorithm has on the complexity when it is combined with the insertion sort algorithm?

# 2 Your Task

Die Narrheit hat ein großes Zelt; Es lagert bei ihr alle Welt, Zumal wer Macht hat und viel Geld.

-Sebastian Brant, Das Narrenschiff

For this assignment you have 3 tasks:

- Task 1: Implement a testing harness for sorting algorithms. You will do this using getopt.
- Task 2: Implement the four sorting algorithms Bubble Sort, Shell Sort, Quicksort and Binary Insertion Sort, whose pseudocode have been provided in the above section.
- **Task 3:** Gather statistics about each sort and its performance such as the *size* of the array, the number of moves required, and the number of *comparisons* required (comparisons for *elements*, not for the logic).

# 3 Specifics

Vielleicht sind alle Drachen unseres Lebens Prinzessinnen, die nur darauf warten uns einmal schön und mutig zu sehen. Vielleicht ist alles Schreckliche im Grunde das Hilflose, das von uns Hilfe will.

—Rainer Maria Rilke

You must use getopt to parse the command line arguments. To get you started, here is a hint.

```
while ((c = getopt(argc, argv, "Absqip:r:n:")) != -1)
```

- -A means employ *all* sorting algorithms.
- -b means enable Bubble Sort.
- -s means enable Shell Sort.
- -q means enable QuickSort.
- -i means enable Binary Insertion Sort.
- -p n means print the first n elements of the array. However if the -p n flag is not specified, your program should print the first 100 elements. The *default* n value is 100.

- -r s means set the random seed to s. The *default* s value is 8222022.
- -n c means set the array size to c. The *default* c value is 100.

It is important to read this *carefully*. None of these options are *exclusive* of any other (you may specify any number of them, including *zero*). The most natural data structure for this problem is a *set*.

- Your random numbers should be 30 bits, no larger  $(2^{30} 1 = 1073741823)$ . (*Hint*: bit masking will help you here.)
- You must use rand() and srand(), not because they are good (they are not), but because they are what is specified by the C99 standard.
- Your program *must* be able to sort any number of random integers *up to the memory limit of the computer*. That means that you will need to dynamically allocate the array using calloc().
- Your program should have no *memory leaks*. Make sure you free before exiting. Valgrind should build without any errors.
- Your program must pass infer cleanly. Fix or explain any complaints by infer in your README.
- The executable file produced by the compiler *must be called* sorting.
- Your algorithms *must* correctly sort. If it does not sort, then for that sort you receive a *zero*.

A large part of this assignment is understanding and comparing the performance of various sorting algorithms. You essentially conducting an experiment. Consequently, you *must* collect some simple statistics on each algorithm. In particular,

- The *size* of the array,
- The number of *moves* required (each time you transfer an element in the array, that counts), and
- The number of *comparisons* required (comparisons *only* count for *elements*, not for logic).

#### Pre-lab Part 5

1. Explain how you plan on keeping track of the number of moves and comparisons since each sort will reside within its own file.

#### 4 Deliverables

Dr. Long, put down the Rilke and step away from the computer.

-Michael Olson

You will need to turn in:

1. Your program *must* have the following source and header files:

- Each sorting method will have its own pair of header file and source file.
  - bubble.h specifies the interface to bubble.c.
  - bubble.c implements Bubble Sort.
  - shell.h specifies the interface to shell.c.
  - shell.c implements Shell Sort.
  - quick.h specifies the interface to quick.c.
  - quick.c implements Quicksort.
  - binary.h specifies the interface to binary.c.
  - binary.c implements Binary Insertion Sort.
- sorting.c contains main() and *may* contain any other functions necessary to complete the assignment.

You will have other source and header files, but *do not try to be overly clever*.

- 2. Makefile: This is a file that will allow the grader to type make to compile your program. Typing make must build your program and ./sorting alone as well as flags must run your program.
  - CFLAGS=-Wall -Wextra -Werror -Wpedantic -std=c99 must be included.
  - CC=clang must be specified.
  - make clean must remove all files that are compiler generated.
  - make valgrind must build your program to check for memory mismanagement errors.
  - make infer must build and run infer on your program, passing without errors. Again, any errors that you cannot fix should be documented in your README.
  - make should build your program, as should make all.
  - Your program executable *must* be named sorting.
- 3. README.md: This must be in markdown. This must describe how to use your program and Makefile.
- 4. DESIGN.pdf: This *must* be a PDF. The design document should contain answers to the pre-lab questions at the beginning and describe your design for your program with enough detail that a sufficiently knowledgeable programmer would be able to replicate your implementation. This does not mean copying your entire program in verbatim. You should instead describe how your program works with supporting pseudo-code.

You *must* push the DESIGN.pdf before you push *any* code.

- 5. WRITEUP.pdf: This document *must* be a PDF. The writeup must include the following:
  - Identify the respective time complexity for each sort and include what you have to say about the constant.
  - What you learned from the different sorting algorithms.
  - How you experimented with the sorts.

Points will be assigned according to the difficulty of the sort involved.

• 10% – Bubble sort

- 15% Shell Sort
- 20% Quick Sort
- 20% Binary Insertion Sort

A sort is not considered to be implemented if it does not sort *correctly every time*. If it does not sort correctly then that sort receives a zero. Additional criteria are:

- 10% Code quality: this includes passing infer and consistent style.
- 10% Completeness: which includes things like the Makefile.
- 15% Supporting Documents: This includes your WRITEUP.pdf, DESIGN.pdf, and README.md.

# 5 Submission

Daß Gott ohn Arbeit Lohn verspricht, Verlaß dich darauf und backe nicht Und wart, bis dir 'ne Taube gebraten Vom Himmel könnt in den Mund geraten!

-Sebastian Brant, Das Narrenschiff

To submit your assignment, refer back to assignment0 for the steps on how to submit your assignment through git. Remember: *add, commit,* and *push*!

Your assignment is turned in *only* after you have pushed *and* submitted the commit ID on Canvas. If you forget to push, you have not turned in your assignment and you will get a *zero*. "I forgot to push" is not a valid excuse. It is *highly* recommended to commit and push your changes *often*.

# 6 Supplemental Readings

The more you read, the more things you will know. The more that you learn, the more places you'll go.

—Dr. Seuss

- The C Programming Language by Kernighan & Ritchie
  - Chapter 1 \$1.10
  - Chapter 4 \$4.10-4.11
  - Chapter 5 \$5.1-5.3