

AMS 151 Final Exam Fall 2024 (1-7 are 14 points each. 8 is worth 2 points.)

Name:

1. Find  $\frac{dy}{dx}$  if  $y = (\tan(6x))\sqrt{\sin x}$

2. Compute  $\int x\sqrt{7x-1}dx$ .

3. Graph  $f(x) = -2x^3 + 6x^2 - 3$  with critical points using the first derivative test. (X intercepts not required.)

4. Calculate the following limit:

$$\lim_{x \rightarrow 0^+} x(\ln x)^2$$

5. Use left, right, and midpoint Riemann sums ( $n=4$ ) to estimate  $\int_0^8 2x dx$ .

6. Find the exact area between  $y = x^2 + 2$  and the x axis from  $x=1$  to  $x=3$ .

7. You have been asked to design a one liter can shaped like a right cylinder. What should the radius be to minimize surface area? The volume is  $\pi r^2 h$  and the surface area is  $2\pi r^2 + 2\pi r h$ .

8. True or false: The horizontal asymptote of  $y = e^{-2x}$  is  $y=0$ .