# **Midterm Review Answers**

#### Problem 2

#### Question:

A researcher is studying the association between a new drug and disease remission across two different hospitals. The data collected is summarized in the following stratified contingency tables:

	emission (-) Total
20	60
30	60
	_~

	Remission (+)	Remission (-)	Total
Drug	50	30	80
Placebo	20	40	60

Using the Mantel-Haenszel method, calculate the common odds ratio across both hospitals. Interpret the result in the context of the study.

#### **Solution:**

To calculate the Mantel-Haenszel Common Odds Ratio (MH OR), we use the formula:

$$OR_{MH} = \frac{\sum \frac{a_i d_i}{n_i}}{\sum \frac{b_i c_i}{n_i}}$$

where for each stratum i:

- $b_i = {\rm number~of~exposed~non\text{-}cases}$  (Drug & Remission -)

- $c_i$  = number of unexposed cases (Placebo & Remission +)
- $d_i$  = number of unexposed non-cases (Placebo & Remission -)
- $n_i$  = total number of observations in the stratum

#### Step 1: Extract Data from Each Hospital

### For Hospital 1:

$$a_1 = 40$$
,  $b_1 = 20$ ,  $c_1 = 30$ ,  $d_1 = 30$ ,  $n_1 = 120$ 

#### For **Hospital 2**:

$$a_2 = 50$$
,  $b_2 = 30$ ,  $c_2 = 20$ ,  $d_2 = 40$ ,  $n_2 = 140$ 

#### Step 2: Compute the Mantel-Haenszel Components

$$\sum \frac{a_i d_i}{n_i} = \frac{(40 \times 30)}{120} + \frac{(50 \times 40)}{140}$$

$$= \frac{1200}{120} + \frac{2000}{140}$$

$$= 10 + 14.29 = 24.29$$

$$\sum \frac{b_i c_i}{n_i} = \frac{(20 \times 30)}{120} + \frac{(30 \times 20)}{140}$$

$$= \frac{600}{120} + \frac{600}{140}$$

$$= 5 + 4.29 = 9.29$$

## Step 3: Compute the Mantel-Haenszel Common Odds Ratio

$$OR_{MH} = \frac{24.29}{9.29} = 2.61$$

#### Step 4: Interpretation

Since the Mantel-Haenszel common odds ratio is 2.61, this suggests that across both hospitals, patients receiving the drug have 2.61 times higher odds of experiencing remission compared to those receiving the placebo. This indicates a strong positive association between the drug and disease remission.

#### **Problem 3**

A researcher is conducting a cohort study to investigate the effect of smoking on lung cancer incidence. The study follows two groups of individuals: Smokers and Non-Smokers. However, since age is a confounding variable, the researcher stratifies the participants into two age groups: Young ( $\leq 50$  years) and Old (> 50 years).

Age Group	Smokers (Cases / Total)	Non-Smokers (Cases / Total)
Young $(\le 50)$	50 / 5,000	20 / 6,000
Old $(> 50)$	200 / 3,000	100 / 4,000

Additionally, the researcher uses a standard population with the following age distribution:

• Young ( $\leq$  50 years): 7,000 individuals

• Old (> 50 years): 5,000 individuals

## Part (A)

Compute the age-stratified risk of lung cancer in both smokers and non-smokers.

Solution: The risk of lung cancer in each stratum is given by:

For Smokers:

• Young ( $\leq 50$  years):

$$\hat{p}_{smoker,young} = \frac{50}{500}$$

• Old (> 50 years):

$$\hat{p}_{smoker,old} = \frac{200}{3000} = 0.0667$$

For Non-Smokers:

• Young ( $\leq 50$  years):

$$\hat{p}_{nonsmoker,young} = \frac{20}{6000} = 0.0033$$

• Old (> 50 years):

$$\hat{p}_{nonsmoker,old} = \frac{100}{4000} = 0.025$$

## Part (B)

Perform direct standardization to calculate the adjusted risk for both smokers and non-smokers using the standard population.

**Solution:** We first define the standard reference distribution:

$$t_{young}=7000,\ t_{old}=5000$$

For Smokers:

$$\hat{p}_{smoker} = \frac{t_{young} \cdot \hat{p}_{young,smoker} + t_{old} \cdot \hat{p}_{old,smoker}}{t_{young} + t_{old}} = 0.0336$$

For Non-Smokers:

$$\hat{p}_{nonsmoker} = \frac{t_{young} \cdot \hat{p}_{young,nonsmoker} + t_{old} \cdot \hat{p}_{old,nonsmoker}}{t_{young} + t_{old}} = 0.0123$$

#### Part (C)

Compute the adjusted risk difference (RD) and the adjusted risk ratio (RR) between smokers and non-smokers.

#### Solution:

Risk Difference is defined as

$$\hat{RD} = \hat{p}_{smoker} - \hat{p}_{nonsmoker} = 0.0213.$$

The Risk Ratio is defined as

$$\hat{RR} = \frac{\hat{p}_{smoker}}{\hat{p}_{nonsmoker}} = 2.73.$$

## Part (D)

Does smoking increase the risk of lung cancer after adjusting for age?

## Solution:

Smokers are 2.73 times more likely to develop lung cancer than non-smokers, even after adjusting for age.

The risk difference of 21.3 per 1,000 suggests that if smoking were eliminated, about 21.3 cases per 1,000 individuals could potentially be prevented in a similar population.