CS2040 Tutorial 7

Week 9, starting 10 Oct 2022

Q1 Other BST Operations

You are given a BST implementation below:

```
class Node {
  int item;
  Node left, right;
  Node (int i, Node l, Node r) { item = i; left = l; right = r; }
class BST {
  int numNodes;
  Node root;
  int floor(int key) {} // to implement, may create helper method
  void insert(int key) { root = insert(key, root); }
  private Node insert(int key, Node curr) {
     if (curr == null) { numNodes++; return new Node(key, null, null); }
     if (key == curr.item) return curr; // no insertion
     if (key < curr.item) curr.left = insert(key, curr.left);</pre>
     else curr.right = insert(key, curr.right);
     return curr;
  }
  void preOrderPrint(Node root) {
     if (root == null) return;
     System.out.print(root.item + " ");
     preOrderPrint(root.left);
     preOrderPrint(root.right);
  }
  void inOrderPrint(Node root) {
     if (root == null) return;
     inOrderPrint(root.left);
     System.out.print(root.item + " ");
     inOrderPrint(root.right);
  void postOrderPrint(Node root) {
     if (root == null) return;
     postOrderPrint(root.left);
    postOrderPrint(root.right);
     System.out.print(root.item + " ");
  }
```

```
void print() {
    System.out.print("Size: " + numNodes + "\nPreorder: [ ");
    preOrderPrint(root);
    System.out.print("]\nInorder: [ ");
    inOrderPrint(root);
    System.out.print("]\nPostorder: [ ");
    postOrderPrint(root);
    System.out.print("]\n");
  }
}
```

- (a) Write another method int ceil (int key) in the BST class that finds the *smallest* element that is more than or equals to key, or Integer.MAX_VALUE if none exists (i.e. the ceiling).
- **(b)** Can ceil (int) be tweaked to implement int higher (int key) that returns the *smallest* element strictly greater than key, or Integer.MAX VALUE if none exists? (i.e. the successor)

What is the time complexity of: one call to higher (int), as well as repeated calls to higher (currentKey), starting with currentKey being the smallest key in the tree, till we get Integer.MAX_VALUE?

(c) How does the BST implementation need to be changed to support Node succ (Node curr) (note the different parameter from (b)), that works similarly to higher (int) in (b) but returns the Node instead of the desired element?

Design and implement <code>succ(Node)</code> . Why is such an implementation more efficient?

Q2 Contiguous Strip with Same Colour

Given positive integers \mathbf{N} and \mathbf{K} , suppose you have created a computer game where there is a large 1 x \mathbf{N} strip of land painted black (colour = 0). The leftmost cell is indexed 0 while the rightmost cell is indexed \mathbf{N} -1. Each cell has a colour value within 0 to \mathbf{K} (a positive integer which could be >> \mathbf{N}) inclusive.

Design and implement a solution to perform the following operations, **each** running in $O(\log N)$ time or better:

```
void paint(int cell, int newColor)
paints the cell at the given index with a different new colour
int findContigLength(int cell)
returns the length of the longest contiguous sub-strip of land with the same colour that includes the (valid) cell with the given index
```

You may perform some initialization in O(1) time.

e.g. $\mathbf{N} = 5$, so the 5 cells start off with colours [0, 0, 0, 0, 0]. findContigLength(1) returns 5 Next paint(3, 5) causes the colours to become [0, 0, 0, 5, 0]. findContigLength(1) returns 3 Then paint is called 3 more times, giving colours [0, 5, 5, 5, 5]. findContigLength(1) returns 4 Finally, paint(3, 4) is called, colours is now [0, 5, 5, 4, 5]. findContigLength(1) returns 2

Question 3 (Online Discussion) – Conditional Average

Modify the BST and or Node class in Q1, without changing the time complexity of any operation, such that it is possible to implement double findCondAverage (int upperBound) that returns, in O(h) time, the average of all elements in the BST that are ≤ upperBound.