# **CS2040 Tutorial 4**

Week 6, starting 12 Sep 2022

### Q1 Simple Recursion – Sum of Natural Numbers

Write a recursive method int sum(int n), which returns the sum of the natural numbers from 1 to n, where  $n \ge 1$ . Do NOT use the formula for arithmetic series in your solution

For example, Sum(4) returns 10, but prints out:

```
Sum(4) = 4 + Sum(3)

Sum(3) = 3 + Sum(2)

Sum(2) = 2 + Sum(1)

Sum(1) = 1
```

#### **Q2 Paint Bucket**

You have a 2-D array of Integers, named <code>colorMatrix</code>. Each cell denotes a number, 0, 1, or 2 which represents a colour (here white, light gray and dark gray respectively). You have to implement the Paint Bucket tool. If you fill one cell in the 2-D array with a colour **c**, the surrounding cells are coloured till it reaches the border of the original colour. The paint gets filled by spreading to the neighbouring cells (each cell has 4 neighbours: left, top, right and bottom), the neighbours' neighbours, and so on...

Implement a recursive paintBucketFill() method that takes in these 4 parameters:

- the 2D array
- the row and column index of the cell where the filling starts
- 0, 1, or 2, representing the intended fill colour

You may write a private paintBucketFill() overloaded method that calls the recursive method, to avoid repeated computation, and to allow the recursive problem to take additional parameters without letting the user be concerned with the value of those parameters

1	1	1	1	2	2	2	1
1	1	1	0	0	0	0	2
2	1	0	0	0	0	2	2
1	0	0	0	0	0	2	2
2	0	0	2	2	2	1	1
2	0	0	2	2	0	0	0
1	1	1	0	0	0	0	0
0	0	0	0	0	0	0	2

1	1	1	1	2	2	2	1
1	1	1	2	2	2	2	2
2	1	2	2	2	2	2	2
1	2	2	2	2	2	2	2
2	2	2	2	2	2	1	1
2	2	2	2	2	0	0	0
1	1	1	0	0	0	0	0
0	0	0	0	0	0	0	2

Use the skeleton provided to help you test your program:

```
public static void printMatrix(int[][] matrix){
   for (int[] row : matrix) {
      for (int col : row) {
         System.out.print(col + " ");
      } // not particular about extra trailing space here
      System.out.println();
   }
}
public static void main(String[] args) {
   int[][] colorMatrix = {
      \{1,1,1,1,2,2,2,1\},\
      \{1,1,1,0,0,0,0,2\},\
      \{2,1,0,0,0,0,2,2\},
      \{1,0,0,0,0,0,2,2\},\
      \{2,0,0,2,2,2,1,1\},
      \{2,0,0,2,2,0,0,0\},
      \{1,1,1,0,0,0,0,0,0\},\
      \{0,0,0,0,0,0,0,0,2\}
   };
   System.out.println("Before fill...");
   printMatrix(colorMatrix);
   System.out.println();
   paintBucketFill(colorMatrix, 2, 3, 2); /* TODO : Implement that */
   System.out.println("After fill...");
   printMatrix(colorMatrix);
```

### Q3 Knapsack Problem

A storage facility provides box storage services to hostel students who are moving out temporarily. Being a poor student, you can only afford to store one large box of items. The given box width is **W** cm and can take at most **K** kg weight. You have **N** items whose lengths and height are exactly the same as the lengths and height of the box

To fully utilize the box space in the box and the weight allowed, you want to:

- Prioritize taking up as much space in the box as possible
- If there are multiple ways to occupy the most space, clear as much total weight as possible You don't really care what items you should place in the box, you just want to get rid of 'as much clutter' as possible (at least according to the thought process spelled out above)

For example, if you have items with (width, weight) pairs (4,8), (3,2), (2,3), (1,3), (4,3) as well as box limits  $\mathbf{W} = 10$ cm and  $\mathbf{K} = 10$  kg, the optimal answer will be Result(Width=9, Weight=8) by selecting these 3 pairs:  $\{(3, 2), (2, 3), (4, 3)\}$ 

You realize that this problem can be solved brute-force with "choose / don't choose"-styled recursion. Each item can either be chosen, or not chosen, in order to arrive at the best result

(a) Complete the compareTo() method so that the better of two results (disregarding the width and weight limit of the box) will compare greater:

```
class Result implements Comparable<Result> {
   int totalWidth;
   int totalWeight;
   Result(int wd, int wt) { totalWidth = wd; totalWeight = wt; }
   public String toString() {
     return "Width=" + totalWidth + ", Weight=" + totalWeight;
   }
   public int compareTo(Result other) { ... }
}
class Item {
   int width, weight;
   Item(int wd, int wt) { width = wd; weight = wt; }
}
```

**(b)** Implement the algorithm to find the best result recursively:

```
public Result findMaxSpaceWeight(Item[] items, int W, int K) {
    ...
} // recurse using an overloaded private method if it helps you
```

## Question 4 (Online Discussion) – Can Walk?

You are given an **N** x **N** char[][] grid, where '-' is a footpath and '#' are bushes. If you can only walk on footpaths and move left/right/up/down, find if there is a way to get from one given cell to another

Use recursion to solve this problem, worry less about efficiency. What is the time complexity of your algorithm? What do you think the time complexity of the best algorithm to solve this problem is?