

# CS2040 Tutorial 2 Suggested Solution

Week 4, starting 29 Aug 2022

## Q1 ADTs

What is the difference between these 3 pieces of code?

```
ArrayList<String> findNames() {  
    ArrayList<String> ls = new ArrayList<>();  
    // fill ls  
    return ls;  
}
```

vs

```
List<String> findNames() {  
    ArrayList<String> ls = new ArrayList<>();  
    // fill ls  
    return ls;  
}
```

vs

```
Collection<String> findNames() {  
    ArrayList<String> ls = new ArrayList<>();  
    // fill ls  
    return ls;  
}
```

## Answer

An `ArrayList<String>` is a `Collection<String>`, so all 3 pieces of code work. If a method returns `Collection<String>`, the caller (calling method) can only use functionality available to any general `Collection<String>` as that is the datatype of the reference, but not List- or ArrayList-specific methods like `get(i)`, `indexOf(i)`, `add(i, elm)`

This can be good if you want to guide the caller to just view the result as an unordered bag of names, and discourage access by index

Draw a diagram of how `Collection<E>`, `List<E>`, `ArrayList<E>`, `LinkedList<E>` are related. Each week where new Java API ADTs / data structures (e.g. `Queue<E>`, `Stack<E>`, `Set<E>`, `Map<E>`, ...) are discussed, add them to your diagram, so you don't need to memorize the operations that each one has. For example, `LinkedList<E>` has `contains()` because it is a `Collection<E>`, has `add(int, E)` because it is a `List<E>`, has `getFirst()` and `getLast()` because it is a `Deque<E>`

## Q2 List ADT Implementations

In lectures, we have learned two general List implementations – array-based and reference-based. ArrayList and Vector are array-based list implementations, while LinkedList is a reference-based implementation. Let us compare and contrast the two implementations

For a list containing  $N$  elements, around how many elements would be accessed/modified when:

- (a) Adding to end of the list (new index ==  $N$  / tail)
- (b) Adding to front of the list (index == 0 / head)
- (c) Removing from front of the list (index == 0 / head)
- (d) Getting (accessing) any element, on average (from index == 0 to index ==  $N-1$ )

Assume the linked list has a tail reference, and is doubly-linked

## Answer

### (a)

For **array-based** implementation, **most of the time** only **1** element is accessed/modified as no shifting is required. However, when the array is already at capacity, the entire underlying array has to be **reallocated** to another array with a larger capacity, which involves copying all  **$N$**  elements to the new array

However, when adding a large number of elements to an empty array-based list, the **average** number of elements modified per add operation is **always a constant**

For a linked list, only 1 node is accessed, or 2 nodes if you also count the new node

### (b), (c)

Adding to front: In a typical **array-based** implementation,  **$N$**  elements from the insertion point onward have to be copied away from the front (to the right) before insertion

Removing from front: Efficiency same as (b),  $N-1$  elements left shifted instead for array-based impl

For a **linked list**, only **1 or 2** nodes are accessed/modified. The second node onwards need not be accessed/modified

### (d)

In an **array-based** implementation, only **1** access is needed to move to any index, because arrays have random access. For a doubly linked list with head and tail references, the average number of accesses is  **$N/4$**  if your algorithm can choose to start from either end

Therefore, insertion/removal from an array-based list, except at one end, is inefficient

On the other hand, array-based list is good for random access, unlike a linked list

### Q3 Linked List Operations

When mutating a linked list, we sometimes can:

- create/instantiate **new nodes** containing the desired elements
- manipulate **next pointers**, so that no node is created or removed
- manipulate the **items** (elements) in two of the nodes without rearranging next pointers

Implement a method `swap(int index)` in the `CircularLinkedList<E>` class given to you below, to swap the node at the given index with the next node. The `toString()` method allows you to test your program

```
class CircularLinkedList<E> {  
  
    int _size;  
    ListNode<E> _head, _tail;  
  
    void addFirst(E element) {  
        _size++;  
        _head = new ListNode<E>(element, _head);  
        if (_tail == null) _tail = _head;  
        _tail.next = _head;  
    }  
  
    public String toString() {  
        if (_head == null) return "[]";  
        StringBuilder sb = new StringBuilder();  
        sb.append("head ->[" + _head.item);  
        for (ListNode<E> curr = _head.next; curr != _head; curr=curr.next)  
            sb.append(", " + curr.item);  
        sb.append("]<- tail");  
        return sb.toString();  
    }  
    void swap(int index) { ... }  
}
```

A pre-condition is that `index` will be non-negative. If the index is larger than the size of the list, then the index wraps around. For example, if the list has 13 elements, then `swap(15)` will swap nodes at indexes 2 and 3

**Restriction:** You are NOT allowed to:

- create any new nodes
- modify the element in any node

[Hint: Consider all cases, and remember to update the necessary instance variables!]

## Answer

In a singly-linked list, to physically reorder/remove a node, the previous node's next reference needs to be mutated. Modulo can also be used to eliminate repeatedly traversing the list more than once per operation. There is also a need to handle a few special cases depending on the size of the list, and whether head and tail references need to be updated

```
void swap(int index) {
    if (_size < 2) return; // if 0 or 1 nodes, don't bother

    if (_size == 2) { // if 2 nodes, only need to swap head and tail refs
        ListNode<E> newTail = _head;
        _head = _tail;
        _tail = newTail;
        return;
    } // At this point, the list has >2 nodes

    index %= _size; // ensure that index < size of list first

    // get the 3 desired nodes
    ListNode<E> prev = _tail;
    for (int times = 0; times < index; times++) prev = prev.next;

    ListNode<E> curr = prev.next; // curr now at left node to be swapped
    ListNode<E> succ = curr.next;

    // swap the 2 nodes: Note the order!
    curr.next = succ.next;
    succ.next = curr;
    prev.next = succ;

    if (index == 0) {
        _head = succ; // head incorrect
    } else if (index == _size - 2) {
        _tail = curr; // swap(tail-1), tail incorrect
    } else if (index == _size - 1) {
        _head = curr; // swap(tail), both head & tail swapped
        _tail = succ;
    }
}
```

#### Question 4 (Online Discussion) – Merging Linked Lists

We are now going to add new functionality **within** the `TailedLinkedList<E>` class:

```
static TailedLinkedList<Integer> merge(  
    TailedLinkedList<Integer> left,  
    TailedLinkedList<Integer> right) {...}
```

Implement the `merge()` class method **efficiently**. Given two linked lists in which all elements are sorted, create a **new linked list** in which all elements are in **sorted** order. Where there is a draw, always take the element from the `left` list. Although a third linked list object is created, be reminded that **NO new nodes** (node objects) are to be created

##### Restrictions:

- You are NOT allowed to use additional data structure, but you may maintain a few node references
- You are NOT allowed to create any new nodes

As an example:

- `left` before merge: [1 3 4 5 5 7]  
  `right` before merge: [2 2 3 3 5 6]
- New returned list: [1 2 2 3 3 3 4 5 5 5 6 7]  
  `left` after merge: []  
  `right` after merge: []

As the original lists will be corrupted, and could potentially corrupt the new list, the method should **clean up** the original lists by emptying them. To simplify this question, you may assume both `left` and `right` are non-empty.

**Tip:** Think of an idea in which you have a few steps that can be repeated many times... How would you merge 2 lists if they were array-based?

Can be done efficiently in  $O(N)$  time

The `addFirst()/addLast()` operations of the `TailedLinkedList` class do create new nodes, so using any of them is NOT acceptable