

ANSWERS

Chapter 2

- 2.1** (a) 10^{-6} ; (b) 1.5×10^4 ; (c) 5; (d) 11.3, 1.13×10^4 .
- 2.2** (a) 10^7 ; (b) 10^{-16} ; (c) 3.9×10^4 ; (d) 6.67×10^{-8} .
- 2.5** 500
- 2.6** (c)
- 2.7** 0.035 mm
- 2.9** 94.1
- 2.10** (a) 1; (b) 3; (c) 4; (d) 4; (e) 4; (f) 4.
- 2.11** 8.72 m^2 ; 0.0855 m^3
- 2.12** (a) 2.3 kg; (b) 0.02 g
- 2.13** 13%; 3.8
- 2.14** (b) and (c) are wrong on dimensional grounds. Hint: The argument of a trigonometric function must always be dimensionless.
- 2.15** The correct formula is $m = m_0(1 - v^2/c^2)^{-1/2}$
- 2.16** $\cong 3 \times 10^{-7} \text{ m}^3$
- 2.17** $\cong 10^4$; intermolecular separation in a gas is much larger than the size of a molecule.
- 2.18** Near objects make greater angle than distant (far off) objects at the eye of the observer. When you are moving, the angular change is less for distant objects than nearer objects. So, these distant objects seem to move along with you, but the nearer objects in opposite direction.
- 2.19** $\cong 3 \times 10^{16} \text{ m}$; as a unit of length 1 parsec is defined to be equal to $3.084 \times 10^{16} \text{ m}$.
- 2.20** 1.32 parsec; $2.64''$ (second of arc)
- 2.23** $1.4 \times 10^3 \text{ kg m}^{-3}$; the mass density of the Sun is in the range of densities of liquids / solids and *not* gases. This high density arises due to inward gravitational attraction on outer layers due to inner layers of the Sun.
- 2.24** $1.429 \times 10^5 \text{ km}$

- 2.25** Hint: $\tan \theta$ must be dimensionless. The correct formula is $\tan \theta = v/v'$ where v' is the speed of rainfall.
- 2.26** Accuracy of 1 part in 10^{11} to 10^{12}
- 2.27** $\cong 0.7 \times 10^3 \text{ kg m}^{-3}$. In the solid phase atoms are tightly packed, so the atomic mass density is close to the mass density of the solid.
- 2.28** $\cong 0.3 \times 10^{18} \text{ kg m}^{-3}$ – Nuclear density is typically 10^{15} times atomic density of matter.
- 2.29** $3.84 \times 10^8 \text{ m}$
- 2.30** 55.8 km
- 2.31** $2.8 \times 10^{22} \text{ km}$
- 2.32** 3,581 km
- 2.33** Hint: the quantity $e^4 / (16 \pi^2 \epsilon_0^2 m_p m_e c^3 G)$ has the dimension of time.

Chapter 3

- 3.1** (a), (b)
- 3.2** (a) A....B, (b) A....B, (c) B....A, (d) Same, (e) B....A....once.
- 3.4** 37 s
- 3.5** 1000 km/h
- 3.6** 3.06 m s^{-2} ; 11.4 s
- 3.7** 1250 m (Hint: view the motion of B relative to A)
- 3.8** 1 m s^{-2} (Hint: view the motion of B and C relative to A)
- 3.9** $T = 9 \text{ min}$, speed = 40 km/h. Hint: $vT / (v - 20) = 18$; $vT / (v + 20) = 6$
- 3.10** (a) Vertically downwards; (b) zero velocity, acceleration of 9.8 m s^{-2} downwards; (c) $x > 0$ (upward and downward motion); $v < 0$ (upward), $v > 0$ (downward), $a > 0$ throughout; (d) 44.1 m, 6 s.
- 3.11** (a) True; (b) False; (c) True (if the particle rebounds instantly with the same speed, it implies infinite acceleration which is unphysical); (d) False (true only when the chosen positive direction is along the direction of motion)
- 3.14** (a) 5 km h^{-1} , 5 km h^{-1} ; (b) 0, 6 km h^{-1} ; (c) $\frac{15}{8} \text{ km h}^{-1}$, $\frac{45}{8} \text{ km h}^{-1}$
- 3.15** Because, for an arbitrarily small interval of time, the magnitude of displacement is equal to the length of the path.
- 3.16** All the four graphs are impossible. (a) a particle cannot have two different positions at the same time; (b) a particle cannot have velocity in opposite directions at the same time; (c) speed is always non-negative; (d) total path length of a particle can never decrease with time. (Note, the arrows on the graphs are meaningless).
- 3.17** No, wrong. $x-t$ plot does not show the trajectory of a particle. Context: A body is dropped from a tower ($x = 0$) at $t = 0$.
- 3.18** 105 m s^{-1}

- 3.19** (a) A ball at rest on a smooth floor is kicked, it rebounds from a wall with reduced speed and moves to the opposite wall which stops it; (b) A ball thrown up with some initial velocity rebounding from the floor with reduced speed after each hit; (c) A uniformly moving cricket ball turned back by hitting it with a bat for a very short time-interval.
- 3.20** $x < 0, v < 0, a > 0$; $x > 0, v > 0, a < 0$; $x < 0, v > 0, a > 0$.
- 3.21** Greatest in 3, least in 2; $v > 0$ in 1 and 2, $v < 0$ in 3.
- 3.22** Acceleration magnitude greatest in 2; speed greatest in 3; $v > 0$ in 1, 2 and 3; $a > 0$ in 1 and 3, $a < 0$ in 2; $a = 0$ at A, B, C, D.
- 3.23** A straight line inclined with the time-axis for uniformly accelerated motion; parallel to the time-axis for uniform motion.
- 3.24** 10 s, 10 s
- 3.25** (a) 13 km h^{-1} ; (b) 5 km h^{-1} ; (c) 20 s in either direction, viewed by any one of the parents, the speed of the child is 9 km h^{-1} in either direction; answer to (c) is unaltered.
- 3.26** $x_2 - x_1 = 15 t$ (linear part); $x_2 - x_1 = 200 + 30 t - 5 t^2$ (curved part).
- 3.27** (a) 60 m, 6 m s^{-1} ; (b) 36 m, 9 m s^{-1}
- 3.28** (c), (d), (f)

Chapter 4

- 4.1** Volume, mass, speed, density, number of moles, angular frequency are scalars; the rest are vectors.
- 4.2** Work, current
- 4.3** Impulse
- 4.4** Only (c) and (d) are permissible
- 4.5** (a) T, (b) F, (c) F, (d) T, (e) T
- 4.6** Hint: The sum (difference) of any two sides of a triangle is never less (greater) than the third side. Equality holds for collinear vectors.
- 4.7** All statements except (a) are correct
- 4.8** 400 m for each; B
- 4.9** (a) O; (b) O; (c) 21.4 km h^{-1}
- 4.10** Displacement of magnitude 1 km and direction 60° with the initial direction; total path length = 1.5 km (third turn); null displacement vector; path length = 3 km (sixth turn); 866 m, 30° , 4 km (eighth turn)
- 4.11** (a) 49.3 km h^{-1} ; (b) 21.4 km h^{-1} . No, the average speed equals average velocity magnitude only for a straight path.
- 4.12** About 18° with the vertical, towards the south.
- 4.13** 15 min, 750 m
- 4.14** East (approximately)
- 4.15** 150.5 m
- 4.16** 50 m

- 4.17** 9.9 m s^{-2} , along the radius at every point towards the centre.
- 4.18** 6.4 g
- 4.19** (a) False (true only for uniform circular motion)
(b) True, (c) True.
- 4.20** (a) $\mathbf{v}(t) = (3.0 \hat{\mathbf{i}} - 4.0t \hat{\mathbf{j}})$ $\hat{\mathbf{a}}(t) = -4.0 \hat{\mathbf{j}}$
(b) 8.54 m s^{-1} , 70° with x -axis.
- 4.21** (a) 2 s , 24 m , 21.26 m s^{-1}
- 4.22** $\sqrt{2}$, 45° with the x -axis; $\sqrt{2}$, -45° with the x -axis, $(5/\sqrt{2}, -1/\sqrt{2})$.
- 4.23** (b) and (e)
- 4.24** Only (e) is true
- 4.25** 182 m s^{-1}
- 4.27** No. Rotations in *general* cannot be associated with vectors
- 4.28** A vector can be associated with a plane area
- 4.29** No
- 4.30** At an angle of $\sin^{-1}(1/3) = 19.5^\circ$ with the vertical; 16 km .
- 4.31** 0.86 m s^{-2} , 54.5° with the direction of velocity

Chapter 5

- 5.1** (a) to (d) No net force according to the First Law
(e) No force, since it is far away from all material agencies producing electromagnetic and gravitational forces.
- 5.2** The only force in each case is the force of gravity, (neglecting effects of air) equal to 0.5 N vertically downward. The answers do not change, even if the motion of the pebble is not along the vertical. The pebble is not at rest at the highest point. It has a constant horizontal component of velocity throughout its motion.
- 5.3** (a) 1 N vertically downwards (b) same as in (a)
(c) same as in (a); force at an instant depends on the situation at that instant, not on history.
(d) 0.1 N in the direction of motion of the train.
- 5.4** (i) T
- 5.5** $a = -2.5 \text{ m s}^{-2}$. Using $v = u + at$, $0 = 15 - 2.5t$ i.e., $t = 6.0 \text{ s}$
- 5.6** $a = 1.5/25 = 0.06 \text{ m s}^{-2}$
 $F = 3 \times 0.06 = 0.18 \text{ N}$ in the direction of motion.
- 5.7** Resultant force = 10 N at an angle of $\tan^{-1}(3/4) = 37^\circ$ with the direction of 8 N force.
Acceleration = 2 m s^{-2} in the direction of the resultant force.
- 5.8** $a = -2.5 \text{ m s}^{-2}$, Retarding force = $465 \times 2.5 = 1.2 \times 10^3 \text{ N}$
- 5.9** $F - 20,000 \times 10 = 20000 \times 5.0$, i.e., $F = 3.0 \times 10^5 \text{ N}$
- 5.10** $a = -20 \text{ m s}^{-2}$ $0 \leq t \leq 30 \text{ s}$

$$t = -5 \text{ s} : x = u t = -10 \times 5 = -50 \text{ m}$$

$$t = 25 \text{ s} : x = u t + (\frac{1}{2}) a t^2 = (10 \times 25 - 10 \times 625) \text{ m} = -6 \text{ km}$$

$t = 100 \text{ s}$: First consider motion up to 30 s

$$x_1 = 10 \times 30 - 10 \times 900 = -8700 \text{ m}$$

$$\text{At } t = 30 \text{ s, } v = 10 - 20 \times 30 = -590 \text{ m s}^{-1}$$

$$\text{For motion from 30 s to 100 s : } x_2 = -590 \times 70 = -41300 \text{ m}$$

$$x = x_1 + x_2 = -50 \text{ km}$$

- 5.11** (a) Velocity of car (at $t = 10 \text{ s}$) $= 0 + 2 \times 10 = 20 \text{ m s}^{-1}$

By the First Law, the horizontal component of velocity is 20 m s^{-1} throughout.

Vertical component of velocity (at $t = 11 \text{ s}$) $= 0 + 10 \times 1 = 10 \text{ m s}^{-1}$

Velocity of stone (at $t = 11 \text{ s}$) $= \sqrt{20^2 + 10^2} = \sqrt{500} = 22.4 \text{ m s}^{-1}$ at an angle of $\tan^{-1}(\frac{1}{2})$ with the horizontal.

(b) 10 m s^{-2} vertically downwards.

- 5.12** (a) At the extreme position, the speed of the bob is zero. If the string is cut, it will fall vertically downwards.

(b) At the mean position, the bob has a horizontal velocity. If the string is cut, it will fall along a parabolic path.

- 5.13** The reading on the scale is a measure of the force on the floor by the man. By the Third Law, this is equal and opposite to the normal force N on the man by the floor.

(a) $N = 70 \times 10 = 700 \text{ N}$; Reading is 70 kg

(b) $70 \times 10 - N = 70 \times 5$; Reading is 35 kg

(c) $N - 70 \times 10 = 70 \times 5$; Reading is 105 kg

(d) $70 \times 10 - N = 70 \times 10$; Reading would be zero; the scale would read zero.

- 5.14** (a) In all the three intervals, acceleration and, therefore, force are zero.

(b) 3 kg m s^{-1} at $t = 0$; (c) -3 kg m s^{-1} at $t = 4 \text{ s}$.

- 5.15** If the 20 kg mass is pulled,

$$600 - T = 20 a, \quad T = 10 a$$

$$a = 20 \text{ m s}^{-2}, \quad T = 200 \text{ N}$$

If the 10 kg mass is pulled, $a = 20 \text{ m s}^{-2}$, $T = 400 \text{ N}$

- 5.16** $T - 8 \times 10 = 8 a, 12 \times 10 - T = 12 a$

i.e. $a = 2 \text{ m s}^{-2}$, $T = 96 \text{ N}$

- 5.17** By momentum conservation principle, total final momentum is zero. Two momentum vectors cannot sum to a null momentum unless they are equal and opposite.

- 5.18** Impulse on each ball $= 0.05 \times 12 = 0.6 \text{ kg m s}^{-1}$ in magnitude. The two impulses are opposite in direction.

- 5.19** Use momentum conservation : $100 v = 0.02 \times 80$

$$v = 0.016 \text{ m s}^{-1} = 1.6 \text{ cm s}^{-1}$$

- 5.20** Impulse is directed along the bisector of the initial and final directions. Its magnitude is $0.15 \times 2 \times 15 \times \cos 22.5^\circ = 4.2 \text{ kg m s}^{-1}$

- 5.21** $v = 2\pi \times 1.5 \times \frac{40}{60} = 2\pi \text{ m s}^{-1}$

$$T = \frac{mv^2}{R} = \frac{0.25 \times 4\pi^2}{1.5} = 6.6 \text{ N}$$

$$200 = \frac{mv_{\max}^2}{R}, \text{ which gives } v_{\max} = 35 \text{ m s}^{-1}$$

5.22 Alternative (b) is correct, according to the First Law

5.23 (a) The horse-cart system has no external force in empty space. The mutual forces between the horse and the cart cancel (Third Law). On the ground, the contact force between the system and the ground (friction) causes their motion from rest.

(b) Due to inertia of the body not directly in contact with the seat.

(c) A lawn mower is pulled or pushed by applying force at an angle. When you push, the normal force (N) must be more than its weight, for equilibrium in the vertical direction. This results in greater friction ($f \propto N$) and, therefore, a greater applied force to move. Just the opposite happens while pulling.

(d) To reduce the rate of change of momentum and hence to reduce the force necessary to stop the ball.

5.24 A body with a constant speed of 1 cm s^{-1} receives impulse of magnitude $0.04 \text{ kg} \times 0.02 \text{ m s}^{-1} = 8 \times 10^{-4} \text{ kg m s}^{-1}$ after every 2 s from the walls at $x = 0$ and $x = 2 \text{ cm}$.

5.25 Net force = $65 \text{ kg} \times 1 \text{ m s}^{-2} = 65 \text{ N}$

$$a_{\max} = \mu_s g = 2 \text{ m s}^{-2}$$

5.26 Alternative (a) is correct. Note $mg + T_2 = mv_2^2/R$; $T_1 - mg = mv_1^2/R$

The moral is : do not confuse the actual material forces on a body (tension, gravitational force, etc) with the effects they produce : centripetal acceleration v_2^2/R or v_1^2/R in this example.

5.27 (a) 'Free body' : crew and passengers

Force on the system by the floor = F upwards; weight of system = mg downwards;

$$\therefore F - mg = ma$$

$$F - 300 \times 10 = 300 \times 15$$

$$F = 7.5 \times 10^3 \text{ N upward}$$

By the Third Law, force on the floor by the crew and passengers = $7.5 \times 10^3 \text{ N}$ downwards.

(b) 'Free body' : helicopter plus the crew and passengers

Force by air on the system = R upwards; weight of system = mg downwards

$$\therefore R - mg = ma$$

$$R - 1300 \times 10 = 1300 \times 15$$

$$R = 3.25 \times 10^4 \text{ N upwards}$$

By the Third Law, force (action) on the air by the helicopter = $3.25 \times 10^4 \text{ N}$ downwards.

(c) $3.25 \times 10^4 \text{ N}$ upwards

5.28 Mass of water hitting the wall per second

$$= 10^3 \text{ kg m}^{-3} \times 10^{-2} \text{ m}^2 \times 15 \text{ m s}^{-1} = 150 \text{ kg s}^{-1}$$

Force by the wall = momentum loss of water per second = $150 \text{ kg s}^{-1} \times 15 \text{ m s}^{-1} = 2.25 \times 10^3 \text{ N}$

5.29 (a) $3mg$ (down) (b) $3mg$ (down) (c) $4mg$ (up)

5.30 If N is the normal force on the wings,

$$N \cos \theta = mg, \quad N \sin \theta = \frac{mv^2}{R}$$

$$\text{which give } R = \frac{v^2}{g \tan \theta} = \frac{200 \times 200}{10 \times \tan 15^\circ} = 15 \text{ km}$$

- 5.31** The centripetal force is provided by the lateral thrust by the rail on the flanges of the wheels. By the Third Law, the train exerts an equal and opposite thrust on the rail causing its wear and tear.

$$\text{Angle of banking} = \tan^{-1} \left(\frac{v^2}{Rg} \right) = \tan^{-1} \left(\frac{15 \times 15}{30 \times 10} \right) \approx 37^\circ$$

- 5.32** Consider the forces on the man in equilibrium : his weight, force due to the rope and normal force due to the floor.

(a) 750 N (b) 250 N; mode (b) should be adopted.

- 5.33** (a) $T - 400 = 240$, $T = 640 \text{ N}$

(b) $400 - T = 160$, $T = 240 \text{ N}$

(c) $T = 400 \text{ N}$

(d) $T = 0$

The rope will break in case (a).

- 5.34** We assume perfect contact between bodies A and B and the rigid partition. In that case, the self-adjusting normal force on B by the partition (reaction) equals 200 N. There is no impending motion and no friction. The action-reaction forces between A and B are also 200 N. When the partition is removed, kinetic friction comes into play.

$$\text{Acceleration of A + B} = [200 - (150 \times 0.15)] / 15 = 11.8 \text{ m s}^{-2}$$

$$\text{Friction on A} = 0.15 \times 50 = 7.5 \text{ N}$$

$$200 - 7.5 - F_{AB} = 5 \times 11.8$$

$$F_{AB} = 1.3 \times 10^2 \text{ N; opposite to motion.}$$

$$F_{BA} = 1.3 \times 10^2 \text{ N; in the direction of motion.}$$

- 5.35** (a) Maximum frictional force possible for opposing impending relative motion between the block and the trolley = $150 \times 0.18 = 27 \text{ N}$, which is more than the frictional force of $15 \times 0.5 = 7.5 \text{ N}$ needed to accelerate the box with the trolley. When the trolley moves with uniform velocity, there is no force of friction acting on the block.

(b) For the accelerated (non-inertial) observer, frictional force is opposed by the pseudo-force of the same magnitude, keeping the box at rest relative to the observer. When the trolley moves with uniform velocity there is no pseudo-force for the moving (inertial) observer and no friction.

- 5.36** Acceleration of the box due to friction = $\mu g = 0.15 \times 10 = 1.5 \text{ m s}^{-2}$. But the acceleration of the truck is greater. The acceleration of the box relative to the truck is 0.5 m s^{-2}

$$\text{towards the rear end. The time taken for the box to fall off the truck} = \sqrt{\frac{2 \times 5}{0.5}} = \sqrt{20} \text{ s.}$$

$$\text{During this time, the truck covers a distance} = \frac{1}{2} \times 2 \times 20 = 20 \text{ m.}$$

5.37 For the coin to revolve with the disc, the force of friction should be enough to provide the necessary centripetal force, i.e. $\frac{mv^2}{r} \leq \mu mg$. Now $v = r\omega$, where $\omega = \frac{2\pi}{T}$ is the angular frequency of the disc. For a given μ and ω , the condition is $r \leq \mu g / \omega^2$. The condition is satisfied by the nearer coin (4 cm from the centre).

5.38 At the uppermost point, $N + mg = \frac{mv^2}{R}$, where N is the normal force (downwards) on the motorcyclist by the ceiling of the chamber. The minimum possible speed at the uppermost point corresponds to $N = 0$.

$$\text{i.e. } v_{\min} = \sqrt{Rg} = \sqrt{25 \times 10} = 16 \text{ m s}^{-1}$$

5.39 The horizontal force N by the wall on the man provides the needed centripetal force : $N = mR\omega^2$. The frictional force f (vertically upwards) opposes the weight mg . The man remains stuck to the wall after the floor is removed if $mg = f < \mu N$ i.e. $mg < \mu mR\omega^2$. The minimum angular speed of rotation of the cylinder is $\omega_{\min} = \sqrt{g / \mu R} = 5 \text{ s}^{-1}$

5.40 Consider the free-body diagram of the bead when the radius vector joining the centre of the wire makes an angle θ with the vertical downward direction. We have $mg = N \cos \theta$ and $mR \sin \theta \omega^2 = N \sin \theta$. These equations give $\cos \theta = g / R\omega^2$. Since $\cos \theta \leq 1$,

the bead remains at its lowermost point for $\omega \leq \sqrt{\frac{g}{R}}$.

$$\text{For } \omega = \sqrt{\frac{2g}{R}}, \quad \cos \theta = \frac{1}{2} \quad \text{i.e. } \theta = 60^\circ.$$

Chapter 6

6.1 (a) +ve (b) -ve (c) -ve (d) +ve (e) -ve

6.2 (a) 882 J ; (b) -247 J; (c) 635 J ; (d) 635 J;
Work done by the net force on a body equals change in its kinetic energy.

6.3 (a) $x > a$; 0 (c) $x < a$, $x > b$; $-V_1$
(b) $-\infty < x < \infty$; V_1 (d) $-b/2 < x < -a/2$, $a/2 < x < b/2$; $-V_1$

6.5 (a) rocket; (b) For a conservative force work done over a path is minus of change in potential energy. Over a complete orbit, there is no change in potential energy; (c) K.E. increases, but P.E. decreases, and the sum decreases due to dissipation against friction; (d) in the second case.

6.6 (a) decrease; (b) kinetic energy; (c) external force; (d) total linear momentum, and also total energy (if the system of two bodies is isolated).

6.7 (a) F ; (b) F ; (c) F ; (d) F (true usually but not always, why?)

6.8 (a) No
(b) Yes
(c) Linear momentum is conserved during an inelastic collision, kinetic energy is, of course, not conserved even after the collision is over.
(d) elastic.

6.9 (b) t

- 6.10** (c) $t^{3/2}$
- 6.11** 12 J
- 6.12** The electron is faster, $v_e / v_p = 13.5$
- 6.13** 0.082 J in each half; -0.163 J
- 6.14** Yes, momentum of the molecule + wall system is conserved. The wall has a recoil momentum such that the momentum of the wall + momentum of the outgoing molecule equals momentum of the incoming molecule, assuming the wall to be stationary initially. However, the recoil momentum produces negligible velocity because of the large mass of the wall. Since kinetic energy is also conserved, the collision is elastic.
- 6.15** 43.6 kW
- 6.16** (b)
- 6.17** It transfers its entire momentum to the ball on the table, and does not rise at all.
- 6.18** 5.3 m s^{-1}
- 6.19** 27 km h^{-1} (no change in speed)
- 6.20** 50 J
- 6.21** (a) $m = \rho A v t$ (b) $K = \rho A v^3 t / 2$ (c) $P = 4.5 \text{ kW}$
- 6.22** (a) 49,000 J (b) $6.45 \times 10^{-3} \text{ kg}$
- 6.23** (a) 200 m^2 (b) comparable to the roof of a large house of dimension $14 \text{ m} \times 14 \text{ m}$.
- 6.24** 21.2 cm, 28.5 J
- 6.25** No, the stone on the steep plane reaches the bottom earlier; yes, they reach with the same speed v , [since $mgh = (1/2) m v^2$]
 $v_B = v_C = 14.1 \text{ m s}^{-1}$, $t_B = 2\sqrt{2} \text{ s}$, $t_C = 2\sqrt{2} \text{ s}$
- 6.26** 0.125
- 6.27** 8.82 J for both cases.
- 6.28** The child gives an impulse to the trolley at the start and then runs with a constant relative velocity of 4 m s^{-1} with respect to the trolley's new velocity. Apply momentum conservation for an observer outside. 10.36 m s^{-1} , 25.9 m.
- 6.29** All except (V) are impossible.

Chapter 7

- 7.1** The geometrical centre of each. No, the CM may lie outside the body, as in case of a ring, a hollow sphere, a hollow cylinder, a hollow cube etc.
- 7.2** Located on the line joining H and C1 nuclei at a distance of 1.24 \AA from the H end.
- 7.3** The speed of the CM of the (trolley + child) system remains unchanged (equal to v) because no external force acts on the system. The forces involved in running on the trolley are internal to this system.
- 7.6** $l_z = x p_y - y p_x$, $l_x = y p_z - z p_y$, $l_y = z p_x - x p_z$
- 7.8** 72 cm
- 7.9** 3675 N on each front wheel, 5145 N on each back wheel.
- 7.10** (a) $7/5 MR^2$ (b) $3/2 MR^2$

- 7.11** Sphere
- 7.12** Kinetic Energy = 3125 J; Angular Momentum = 62.5 J s
- 7.13** (a) 100 rev/min (use angular momentum conservation).
(b) The new kinetic energy is 2.5 times the initial kinetic energy of rotation. The child uses his internal energy to increase his rotational kinetic energy.
- 7.14** 25 s^{-2} ; 10 m s^{-2}
- 7.15** 36 kW
- 7.16** at $R/6$ from the center of original disc opposite to the center of cut portion.
- 7.17** 66.0 g
- 7.18** (a) Yes; (b) Yes, (c) the plane with smaller inclination ($\because a \propto \sin \theta$)
- 7.19** 4J
- 7.20** $6.75 \times 10^{12} \text{ rad s}^{-1}$
- 7.21** (a) 3.8 m (b) 3.0 s
- 7.22** Tension = 98 N, $N_B = 245 \text{ N}$, $N_C = 147 \text{ N}$.
- 7.23** (a) 59 rev/min, (b) No, the K.E. is increased and it comes from work done by man in the process.
- 7.24** 0.625 rad s^{-1}
- 7.27** (a) By angular momentum conservation, the common angular speed

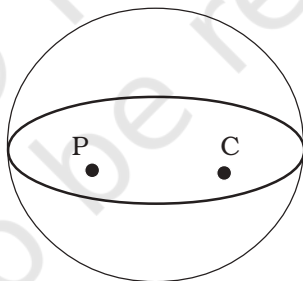
$$\omega = (I_1 \omega_1 + I_2 \omega_2) / (I_1 + I_2)$$

 (b) The loss is due to energy dissipation in frictional contact which brings the two discs to a common angular speed ω . However, since frictional torques are internal to the system, angular momentum is unaltered.
- 7.28** Velocity of A = $\omega_o R$ in the same direction as the arrow; velocity of B = $\omega_o R$ in the opposite direction to the arrow; velocity of C = $\omega_o R/2$ in the same direction as the arrow. The disc will not roll on a frictionless plane.
- 7.29** (a) Frictional force at B opposes velocity of B. Therefore, frictional force is in the same direction as the arrow. The sense of frictional torque is such as to oppose angular motion. ω_o and τ are both normal to the paper, the first into the paper, and the second coming out of the paper.
 (b) Frictional force decreases the velocity of the point of contact B. Perfect rolling ensues when this velocity is zero. Once this is so, the force of friction is zero.
- 7.30** Frictional force causes the CM to accelerate from its initial zero velocity. Frictional torque causes retardation in the initial angular speed ω_o . The equations of motion are : $\mu_k mg = ma$ and $\mu_k mgR = -I\alpha$, which yield $v = \mu_k g t$, $\omega = \omega_o - \mu_k mgRt / I$. Rolling begins when $v = R\omega$. For a ring, $I = mR^2$, and rolling begins at $t = \omega_o R / 2\mu_k g$. For a disc, $I = \frac{1}{2} mR^2$ and rolling starts at break line $t = R\omega_o / 3\mu_k g$. Thus, the disc begins to roll earlier than the ring, for the same R and ω_o . The actual times can be obtained for $R = 10 \text{ cm}$, $\omega_o = 10 \pi \text{ rad s}^{-1}$, $\mu_k = 0.2$

- 7.31** (a) 16.4 N
 (b) Zero
 (c) 37° approx.

Chapter 8

- 8.1** (a) No.
 (b) Yes, if the size of the space ship is large enough for him to detect the variation in g .
 (c) Tidal effect depends inversely on the cube of the distance unlike force, which depends inversely on the square of the distance.
- 8.2** (a) decreases; (b) decreases; (c) mass of the body; (d) more.
- 8.3** Smaller by a factor of 0.63.
- 8.5** 3.54×10^8 years.
- 8.6** (a) Kinetic energy, (b) less,
- 8.7** (a) No, (b) No, (c) No, (d) Yes
 [The escape velocity is independent of mass of the body and the direction of projection. It depends upon the gravitational potential at the point from where the body is launched. Since this potential depends (slightly) on the latitude and height of the point, the escape velocity (speed) depends (slightly) on these factors.]
- 8.8** All quantities vary over an orbit except angular momentum and total energy.
- 8.9** (b), (c) and (d)
- 8.10** and **8.11** For these two problems, complete the hemisphere to sphere. At both P, and C, potential is constant and hence intensity = 0. Therefore, for the hemisphere, (c) and (e) are correct.



- 8.12** 2.6×10^8 m
8.13 2.0×10^{30} kg
8.14 1.43×10^{12} m
8.15 28 N
8.16 125 N
8.17 8.0×10^6 m from the earth's centre
8.18 31.7 km/s
8.19 5.9×10^9 J

- 8.20** $2.6 \times 10^6 \text{ m/s}$
- 8.21** $0, 2.7 \times 10^{-8} \text{ J/kg}$; an object placed at the mid point is in an unstable equilibrium
- 8.22** $-9.4 \times 10^6 \text{ J/kg}$
- 8.23** $GM/R^2 = 2.3 \times 10^{12} \text{ m s}^{-2}$, $\omega^2 R = 1.1 \times 10^6 \text{ m s}^{-2}$; here ω is the angular speed of rotation. Thus in the rotating frame of the star, the inward force is much greater than the outward centrifugal force at its equator. The object will remain stuck (and not fly off due to centrifugal force). Note, if angular speed of rotation increases say by a factor of 2000, the object will fly off.
- 8.24** $3 \times 10^{11} \text{ J}$
- 8.25** 495 km

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