

Exercise 5b

Question 1.

If $A = \begin{bmatrix} 2 & -3 & 5 \\ -1 & 0 & 3 \end{bmatrix}$ and $B = \begin{bmatrix} 3 & 2 & -2 \\ 4 & -3 & 1 \end{bmatrix}$, verify that $(A + B) = (B + A)$.

Answer:

$$A + B = \begin{bmatrix} 2 & -3 & 5 \\ -1 & 0 & 3 \end{bmatrix} + \begin{bmatrix} 3 & 2 & -2 \\ 4 & -3 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 5 & -1 & 3 \\ 3 & -3 & 4 \end{bmatrix}$$

$$B + A = \begin{bmatrix} 3 & 2 & -2 \\ 4 & -3 & 1 \end{bmatrix} + \begin{bmatrix} 2 & -3 & 5 \\ -1 & 0 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 5 & -1 & 3 \\ 3 & -3 & 4 \end{bmatrix} = B + A$$

Therefore, $A + B = B + A$

This is true for any matrix

Conclusion: $A + B = B + A$

Question 2.

If $A = \begin{bmatrix} 3 & 5 \\ -2 & 0 \\ 6 & -1 \end{bmatrix}$, $B = \begin{bmatrix} -1 & -3 \\ 4 & 2 \\ -2 & 3 \end{bmatrix}$ and $C = \begin{bmatrix} 0 & 2 \\ 3 & -4 \\ 1 & 6 \end{bmatrix}$, verify that $(A + B) + C = A + (B + C)$.

Answer:

$$(A+B)+C = \left(\begin{bmatrix} 3 & 5 \\ -2 & 0 \\ 6 & -1 \end{bmatrix} + \begin{bmatrix} -1 & -3 \\ 4 & 2 \\ -2 & 3 \end{bmatrix} \right) + \begin{bmatrix} 0 & 2 \\ 3 & -4 \\ 1 & 6 \end{bmatrix}$$

$$= \left(\begin{bmatrix} 2 & 2 \\ 2 & 2 \\ 4 & 2 \end{bmatrix} \right) + \begin{bmatrix} 0 & 2 \\ 3 & -4 \\ 1 & 6 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & 4 \\ 5 & -2 \\ 5 & 8 \end{bmatrix}$$

$$A+(B+C) = \begin{bmatrix} 3 & 5 \\ -2 & 0 \\ 6 & -1 \end{bmatrix} + \left(\begin{bmatrix} -1 & -3 \\ 4 & 2 \\ -2 & 3 \end{bmatrix} + \begin{bmatrix} 0 & 2 \\ 3 & -4 \\ 1 & 6 \end{bmatrix} \right)$$

$$= \begin{bmatrix} 3 & 5 \\ -2 & 0 \\ 6 & -1 \end{bmatrix} + \left(\begin{bmatrix} -1 & -1 \\ 7 & -2 \\ -1 & 9 \end{bmatrix} \right)$$

$$= \begin{bmatrix} 2 & 4 \\ 5 & -2 \\ 5 & 8 \end{bmatrix}$$

Therefore, $(A+B)+C = A+(B+C)$

It is true for any matrix

Conclusion: $(A+B)+C = A+(B+C)$

Question 3.

If $A = \begin{bmatrix} 3 & 1 & 2 \\ 1 & 2 & -3 \end{bmatrix}$ and $B = \begin{bmatrix} -2 & 0 & 4 \\ 5 & -3 & 2 \end{bmatrix}$, find $(2A - B)$.

Answer:

$$2A = 2 \left(\begin{bmatrix} 3 & 1 & 2 \\ 1 & 2 & -3 \end{bmatrix} \right)$$

$$= \begin{bmatrix} 6 & 2 & 4 \\ 2 & 4 & -6 \end{bmatrix}$$

$$(2A-B) = \begin{bmatrix} 6 & 2 & 4 \\ 2 & 4 & -6 \end{bmatrix} - \begin{bmatrix} -2 & 0 & 4 \\ 5 & -3 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 8 & 2 & 0 \\ -3 & 7 & -8 \end{bmatrix}$$

$$\text{Conclusion: } (2A-B) = \begin{bmatrix} 8 & 2 & 0 \\ -3 & 7 & -8 \end{bmatrix}$$

Question 4.

Let $A = \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix}$, $B = \begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix}$ and $C = \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix}$. Find:

i. $A + 2B$

ii. $B - 4C$

iii. $A - 2B + 3C$

Answer:

$$A + 2B = \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} + 2\left(\begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix}\right)$$

$$= \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} + \begin{bmatrix} 2 & 6 \\ -4 & 10 \end{bmatrix}$$

$$= \begin{bmatrix} 4 & 10 \\ -1 & 12 \end{bmatrix}$$

$$\text{Conclusion: } (A+2B) = \begin{bmatrix} 4 & 10 \\ -1 & 12 \end{bmatrix}$$

ii. $B - 4C$

$$B - 4C = \begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix} - 4\left(\begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix}\right)$$

$$= \begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix} - \begin{bmatrix} -8 & 20 \\ 12 & 16 \end{bmatrix}$$

$$= \begin{bmatrix} 9 & -17 \\ -14 & -11 \end{bmatrix}$$

$$\text{Conclusion: } B - 4C = \begin{bmatrix} 9 & -17 \\ -14 & -11 \end{bmatrix}$$

iii. $A - 2B + 3C$

$$A - 2B + 3C = \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} - 2\left(\begin{bmatrix} 1 & 3 \\ -2 & 5 \end{bmatrix}\right) + 3\left(\begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix}\right)$$

$$= \begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} - \begin{bmatrix} 2 & 6 \\ -4 & 10 \end{bmatrix} + \begin{bmatrix} -6 & 15 \\ 9 & 12 \end{bmatrix}$$

$$= \begin{bmatrix} -6 & 13 \\ 16 & 4 \end{bmatrix}$$

$$\text{Conclusion: } A - 2B + 3C = \begin{bmatrix} -6 & 13 \\ 16 & 4 \end{bmatrix}$$

Question 5.

$$\text{Let } A = \begin{bmatrix} 0 & 1 & -2 \\ 5 & -1 & -4 \end{bmatrix}, B = \begin{bmatrix} 1 & -3 & -1 \\ 0 & -2 & 5 \end{bmatrix} \text{ and } C = \begin{bmatrix} 2 & -5 & 1 \\ -4 & 0 & 6 \end{bmatrix}. \text{ Compute } 5A - 3B + 4C.$$

Answer:

$$5A - 3B + 4C = 5\left(\begin{bmatrix} 0 & 1 & -2 \\ 5 & -1 & -4 \end{bmatrix}\right) - 3\left(\begin{bmatrix} 1 & -3 & -1 \\ 0 & -2 & 5 \end{bmatrix}\right) + 4\left(\begin{bmatrix} 2 & -5 & 1 \\ -4 & 0 & 6 \end{bmatrix}\right)$$

$$= \left(\begin{bmatrix} 0 & 5 & -10 \\ 25 & -5 & -20 \end{bmatrix}\right) - \left(\begin{bmatrix} 3 & -9 & -3 \\ 0 & -6 & 15 \end{bmatrix}\right) + \left(\begin{bmatrix} 8 & -20 & 4 \\ -16 & 0 & 24 \end{bmatrix}\right)$$

$$= \begin{bmatrix} -3 & 14 & -7 \\ 25 & 1 & -35 \end{bmatrix} + \begin{bmatrix} 8 & -20 & 4 \\ -16 & 0 & 24 \end{bmatrix}$$

$$= \begin{bmatrix} 5 & -6 & -3 \\ 9 & 1 & -11 \end{bmatrix}$$

$$\text{Conclusion: } 5A - 3B + 4C = \begin{bmatrix} 5 & -6 & -3 \\ 9 & 1 & -11 \end{bmatrix}$$

Question 6.

$$\text{If } 5A = \begin{bmatrix} 5 & 10 & -15 \\ 2 & 3 & 4 \\ 1 & 0 & -5 \end{bmatrix}, \text{ find } A.$$

Answer:

$$5A = \begin{bmatrix} 5 & 10 & -15 \\ 2 & 3 & 4 \\ 1 & 0 & -5 \end{bmatrix}$$

$$A = \begin{bmatrix} \frac{5}{5} & \frac{10}{5} & \frac{-15}{5} \\ \frac{2}{5} & \frac{3}{5} & \frac{4}{5} \\ \frac{1}{5} & \frac{0}{5} & \frac{-5}{5} \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 2 & -3 \\ \frac{2}{5} & \frac{3}{5} & \frac{4}{5} \\ \frac{1}{5} & 0 & -1 \end{bmatrix}$$

$$\text{Conclusion: } A = \begin{bmatrix} 1 & 2 & -3 \\ \frac{2}{5} & \frac{3}{5} & \frac{4}{5} \\ \frac{1}{5} & 0 & -1 \end{bmatrix}$$

Question 7.

$$\text{Find matrices A and B, if } A + B = \begin{bmatrix} 1 & 0 & 2 \\ 5 & 4 & -6 \\ 7 & 3 & 8 \end{bmatrix} \text{ and } A - B = \begin{bmatrix} -5 & -4 & 8 \\ 11 & 2 & 0 \\ -1 & 7 & 4 \end{bmatrix}.$$

Answer:

Add (A+B) and (A-B)

$$\text{We get } (A+B) + (A-B) = \begin{bmatrix} 1 & 0 & 2 \\ 5 & 4 & -6 \\ 7 & 3 & 8 \end{bmatrix} + \begin{bmatrix} -5 & -4 & 8 \\ 11 & 2 & 0 \\ -1 & 7 & 4 \end{bmatrix}$$

$$2A = \begin{bmatrix} -4 & -4 & 10 \\ 16 & 6 & -6 \\ 6 & 10 & 12 \end{bmatrix}$$

$$A = \begin{bmatrix} -2 & -2 & 5 \\ 8 & 3 & -3 \\ 3 & 5 & 6 \end{bmatrix}$$

Now Subtract (A-B) from (A+B)

$$(A+B) - (A-B) = \begin{bmatrix} 1 & 0 & 2 \\ 5 & 4 & -6 \\ 7 & 3 & 8 \end{bmatrix} - \begin{bmatrix} -5 & -4 & 8 \\ 11 & 2 & 0 \\ -1 & 7 & 4 \end{bmatrix}$$

$$(2B) = \begin{bmatrix} 6 & 4 & -6 \\ -6 & 2 & -6 \\ 8 & -4 & 4 \end{bmatrix}$$

$$B = \begin{bmatrix} 3 & 2 & -3 \\ -3 & 1 & -3 \\ 4 & -2 & 2 \end{bmatrix}$$

$$\text{Conclusion: } A = \begin{bmatrix} -2 & -2 & 5 \\ 8 & 3 & -3 \\ 3 & 5 & 6 \end{bmatrix}, B = \begin{bmatrix} 3 & 2 & -3 \\ -3 & 1 & -3 \\ 4 & -2 & 2 \end{bmatrix}$$

Question 8.

$$\text{Find matrices A and B, if } 2A - B = \begin{bmatrix} 6 & -6 & 0 \\ -4 & 2 & 1 \end{bmatrix} \text{ and } 2B + A = \begin{bmatrix} 3 & 2 & 5 \\ -2 & 1 & -7 \end{bmatrix}$$

Answer:

Add 2(2A-B) and (2B+A)

$$2(2A-B) + (2B+A) = 2 \left(\begin{bmatrix} 6 & -6 & 0 \\ -4 & 2 & 1 \end{bmatrix} \right) + \begin{bmatrix} 3 & 2 & 5 \\ -2 & 1 & -7 \end{bmatrix}$$

$$5A = \left(\begin{bmatrix} 12 & -12 & 0 \\ -8 & 4 & 2 \end{bmatrix} \right) + \begin{bmatrix} 3 & 2 & 5 \\ -2 & 1 & -7 \end{bmatrix}$$

$$5A = \begin{bmatrix} 15 & -10 & 5 \\ -10 & 5 & -5 \end{bmatrix}$$

$$A = \begin{bmatrix} 3 & -2 & 1 \\ -2 & 1 & -1 \end{bmatrix}$$

$$B = 2 \left(\begin{bmatrix} 3 & -2 & 1 \\ -2 & 1 & -1 \end{bmatrix} \right) - \begin{bmatrix} 6 & -6 & 0 \\ -4 & 2 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 6 & -4 & 2 \\ -4 & 2 & -2 \end{bmatrix} - \begin{bmatrix} 6 & -6 & 0 \\ -4 & 2 & 1 \end{bmatrix}$$

$$B = \begin{bmatrix} 0 & 2 & 2 \\ 0 & 0 & -3 \end{bmatrix}$$

$$\text{Conclusion: } A = \begin{bmatrix} 3 & -2 & 1 \\ -2 & 1 & -1 \end{bmatrix}, B = \begin{bmatrix} 0 & 2 & 2 \\ 0 & 0 & -3 \end{bmatrix}$$

(GIVEN ANSWER IS WRONG for question 8)

Question 9.

Find matrix X, if $\begin{bmatrix} 3 & 5 & -9 \\ -1 & 4 & -7 \end{bmatrix} + X = \begin{bmatrix} 6 & 2 & 3 \\ 4 & 8 & 6 \end{bmatrix}$.

Answer:

Given $\begin{bmatrix} 3 & 5 & -9 \\ -1 & 4 & -7 \end{bmatrix} + x = \begin{bmatrix} 6 & 2 & 3 \\ 4 & 8 & 6 \end{bmatrix}$

$$x = \begin{bmatrix} 6 & 2 & 3 \\ 4 & 8 & 6 \end{bmatrix} - \begin{bmatrix} 3 & 5 & -9 \\ -1 & 4 & -7 \end{bmatrix}$$

$$= \begin{bmatrix} 3 & -3 & 12 \\ 5 & 4 & 13 \end{bmatrix}$$

Conclusion : $x = \begin{bmatrix} 3 & -3 & 12 \\ 5 & 4 & 13 \end{bmatrix}$

Question 10.

If $A = \begin{bmatrix} -2 & 3 \\ 4 & 5 \\ 1 & -6 \end{bmatrix}$ and $B = \begin{bmatrix} 5 & 2 \\ -7 & 3 \\ 6 & 4 \end{bmatrix}$, find a matrix C such that $A + B - C = O$.

Answer:

Given $A + B - C = O$

$$\begin{bmatrix} -2 & 3 \\ 4 & 5 \\ 1 & -6 \end{bmatrix} + \begin{bmatrix} 5 & 2 \\ -7 & 3 \\ 6 & 4 \end{bmatrix} - C = 0$$

$$C = \begin{bmatrix} -2 & 3 \\ 4 & 5 \\ 1 & -6 \end{bmatrix} + \begin{bmatrix} 5 & 2 \\ -7 & 3 \\ 6 & 4 \end{bmatrix}$$

$$C = \begin{bmatrix} 3 & 5 \\ -3 & 8 \\ 7 & -2 \end{bmatrix}$$

Conclusion: $C = \begin{bmatrix} 3 & 5 \\ -3 & 8 \\ 7 & -2 \end{bmatrix}$

Question 11.

Find the matrix X such that $2A - B + X = O$,

$$\text{where } A = \begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix} \text{ and } B = \begin{bmatrix} -2 & 1 \\ 0 & 3 \end{bmatrix}.$$

Answer:

Given $2A - B + X = 0$

$$2\left(\begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix}\right) - \begin{bmatrix} -2 & 1 \\ 0 & 3 \end{bmatrix} + X = 0$$

$$X = \begin{bmatrix} -2 & 1 \\ 0 & 3 \end{bmatrix} - 2\left(\begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix}\right)$$

$$= \begin{bmatrix} -2 & 1 \\ 0 & 3 \end{bmatrix} - \begin{bmatrix} 6 & 2 \\ 0 & 4 \end{bmatrix}$$

$$= \begin{bmatrix} -8 & -1 \\ 0 & -1 \end{bmatrix}$$

$$\text{Conclusion: } X = \begin{bmatrix} -8 & -1 \\ 0 & -1 \end{bmatrix}$$

Question 12.

If $A = \begin{bmatrix} 1 & -3 & 2 \\ 2 & 0 & 2 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & -1 & -1 \\ 1 & 0 & -1 \end{bmatrix}$, find a matrix C such that $(A + B + C)$ is a zero matrix.

Answer:

Given $A+B+C$ is zero matrix i.e $A+B+C = 0$

$$\begin{bmatrix} 1 & -3 & 2 \\ 2 & 0 & 2 \end{bmatrix} + \begin{bmatrix} 2 & -1 & -1 \\ 1 & 0 & -1 \end{bmatrix} + C = 0$$

$$C = -\begin{bmatrix} 1 & -3 & 2 \\ 2 & 0 & 2 \end{bmatrix} - \begin{bmatrix} 2 & -1 & -1 \\ 1 & 0 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} -3 & 4 & -1 \\ -3 & 0 & -1 \end{bmatrix}$$

$$\text{Conclusion: } C = \begin{bmatrix} -3 & 4 & -1 \\ -3 & 0 & -1 \end{bmatrix}$$

Question 13.

If $A = \text{diag}[2, -5, 9]$, $B = \text{diag}[-3, 7, 14]$ and $C = \text{diag}[4, -6, 3]$, find:

(i) $A + 2B$

(ii) $B + C - A$

Answer:

If $Z = \text{diag}[a, b, c]$, then we can write it as

$$Z = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & c \end{bmatrix}$$

$$\text{So, } A + 2B = \begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & 9 \end{bmatrix} + 2\left(\begin{bmatrix} -3 & 0 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 14 \end{bmatrix}\right)$$

$$= \begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & 9 \end{bmatrix} + \begin{bmatrix} -6 & 0 & 0 \\ 0 & 14 & 0 \\ 0 & 0 & 28 \end{bmatrix}$$

$$= \begin{bmatrix} 4 & 0 & 0 \\ 0 & 9 & 0 \\ 0 & 0 & 37 \end{bmatrix}$$

$$= \text{diag}[4, 9, 37]$$

$$\text{Conclusion: } A + 2B = \text{diag}[4, 9, 37]$$

(Given answer is wrong)

ii. $B + C - A$

If $Z = \text{diag}[a, b, c]$, then we can write it as

$$Z = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & c \end{bmatrix}$$

$$B + C - A = \begin{bmatrix} -3 & 0 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 14 \end{bmatrix} + \begin{bmatrix} 4 & 0 & 0 \\ 0 & -6 & 0 \\ 0 & 0 & 3 \end{bmatrix} - \begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & 9 \end{bmatrix}$$

$$= \begin{bmatrix} -1 & 0 & 0 \\ 0 & 6 & 0 \\ 0 & 0 & 8 \end{bmatrix}$$

$$= \text{diag}[-1,6,8]$$

Conclusion: $B+C-A = \text{diag}[-1,6,8]$

iii. $2A + B - 5C$

If $Z = \text{diag}[a,b,c]$, then we can write it as

$$Z = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & c \end{bmatrix}$$

$$2A+B-5C = 2\left(\begin{bmatrix} 2 & 0 & 0 \\ 0 & -5 & 0 \\ 0 & 0 & 9 \end{bmatrix}\right) + \begin{bmatrix} -3 & 0 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 14 \end{bmatrix} - 5\left(\begin{bmatrix} 4 & 0 & 0 \\ 0 & -6 & 0 \\ 0 & 0 & 3 \end{bmatrix}\right)$$

$$= \begin{bmatrix} 4 & 0 & 0 \\ 0 & -10 & 0 \\ 0 & 0 & 18 \end{bmatrix} + \begin{bmatrix} -3 & 0 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 14 \end{bmatrix} - \begin{bmatrix} 20 & 0 & 0 \\ 0 & -30 & 0 \\ 0 & 0 & 15 \end{bmatrix}$$

$$= \begin{bmatrix} -19 & 0 & 0 \\ 0 & 27 & 0 \\ 0 & 0 & 17 \end{bmatrix}$$

$$= \text{diag}[-19,27,17]$$

Conclusion: $2A + B - 5C = \text{diag}[-19,27,17]$

(Given answer is wrong)

Question 14.

Find the value of x and y , when

$$\text{i. } \begin{bmatrix} x+y \\ x-y \end{bmatrix} = \begin{bmatrix} 8 \\ 4 \end{bmatrix}$$

Answer:

$$\text{If } \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} e & f \\ g & h \end{bmatrix},$$

Then $a=e$, $b=f$, $c=g$, $d=h$

$$\text{Given } \begin{bmatrix} x+y \\ x-y \end{bmatrix} = \begin{bmatrix} 8 \\ 4 \end{bmatrix}$$

So, $x+y=8$ and $x-y=4$

Adding these two gives $2x=12$

$$\Rightarrow x=6$$

$$y=2$$

Conclusion : $x=6$ and $y=2$

$$\text{ii. } \begin{bmatrix} 2x+5 & 7 \\ 0 & 3y-7 \end{bmatrix} = \begin{bmatrix} x-3 & 7 \\ 0 & -5 \end{bmatrix}$$

$$\text{Given, } \begin{bmatrix} 2x+5 & 7 \\ 0 & 3y-7 \end{bmatrix} = \begin{bmatrix} x-3 & 7 \\ 0 & -5 \end{bmatrix}$$

So, $2x+5=x-3$ and $3y-7=-5$

$$\Rightarrow 3y=2 \Rightarrow y=\frac{2}{3}$$

$$\Rightarrow 2x+5=x-3 \Rightarrow x=-8$$

Conclusion : $x=-8$ and $y=\frac{2}{3}$

$$\text{iii. } 2 \begin{bmatrix} x & 5 \\ 7 & y-3 \end{bmatrix} + \begin{bmatrix} 3 & -4 \\ 1 & 2 \end{bmatrix} = \begin{bmatrix} 7 & 6 \\ 15 & 14 \end{bmatrix}$$

$$2 \begin{bmatrix} x & 5 \\ 7 & y-3 \end{bmatrix} + \begin{bmatrix} 3 & -4 \\ 1 & 2 \end{bmatrix} = \begin{bmatrix} 7 & 6 \\ 15 & 14 \end{bmatrix}$$

$$\begin{bmatrix} 2x+3 & 6 \\ 15 & 2y-4 \end{bmatrix} = \begin{bmatrix} 7 & 6 \\ 15 & 14 \end{bmatrix}$$

$$2x+3 = 7 \Rightarrow x = 2$$

$$2y-4 = 14 \Rightarrow y = 9$$

Conclusion : $x = 2$ and $y = 9$

(Given answer is wrong)

Question 15.

Find the value of $(x + y)$ from the following equation :

$$2 \begin{bmatrix} 1 & 3 \\ 0 & x \end{bmatrix} + \begin{bmatrix} y & 0 \\ 1 & 2 \end{bmatrix} = \begin{bmatrix} 5 & 6 \\ 1 & 8 \end{bmatrix}$$

Answer:

Given

$$2 \begin{bmatrix} 1 & 3 \\ 0 & x \end{bmatrix} + \begin{bmatrix} y & 0 \\ 1 & 2 \end{bmatrix} = \begin{bmatrix} 5 & 6 \\ 1 & 8 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 6 \\ 0 & 2x \end{bmatrix} + \begin{bmatrix} y & 0 \\ 1 & 2 \end{bmatrix} = \begin{bmatrix} 5 & 6 \\ 1 & 8 \end{bmatrix}$$

$$\begin{bmatrix} 2+y & 6 \\ 1 & 2x+2 \end{bmatrix} = \begin{bmatrix} 5 & 6 \\ 1 & 8 \end{bmatrix}$$

So, $2+y = 5$ and $2x+2 = 8$

i.e $y = 3$ and $x = 3$

Therefore, $x+y=6$

Conclusion: Therefore $x+y = 6$

Question 16.

If $\begin{bmatrix} x-y & 2y \\ 2y+z & x+y \end{bmatrix} = \begin{bmatrix} 1 & 4 \\ 9 & 5 \end{bmatrix}$ then write the value of $(x + y)$.

Answer:

$$\text{If } \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} e & f \\ g & h \end{bmatrix},$$

Then $a=e$, $b=f$, $c=g$, $d=h$

$$\text{Given, } \begin{bmatrix} x-y & 2y \\ 2y+z & x+y \end{bmatrix} = \begin{bmatrix} 1 & 4 \\ 9 & 5 \end{bmatrix},$$

So, $x-y = 1$, $x+y = 5$, $2y = 4$ and $2y+z = 9$

Therefore, $x+y = 5$

Conclusion: $x+y = 5$

(Given answer is wrong)