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INDIAN INSTITUTE OF TECHNOLOGY BOMBAY

उत्तर पुस्तिका/ Answer Book-12

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रोल नं./Roll No.

MM202

पाठ्यक्रम नाम/Course Name

MEMS

शाखा/प्रभाग/Branch/Div. शैक्षणिक बैच /Tutorial Batch

S2

अनुभाग/Section



प्र.सं./Q. No.	1	2	3	4	5	6	7	8	9	10	11	12	योग/Total
आरंभिक पृष्ठ Starting Page No.													
अंक/Marks													

प्र.सं./Q. No.	13	14	15	16	17	18	19	20	21	22	23	24	योग/Total
आरंभिक पृष्ठ Starting Page No.													
अंक/Marks													

परीक्षा में उपस्थित होने वाले अभ्यर्थियों से घोषणा पत्र	Declaration from the Candidate appearing in the Examination
1. मैं, इस परीक्षा के आयोजन संबंधी पाठ्यक्रम अनुदेशक द्वारा दिए गए सभी अनुदेशों का पालन करूंगा / करूंगी।	1. I will abide by all instructions given by the course instructor regarding the conduct of this examination.
2. मैं, संस्थान के नियम तथा विनियमों में दिए गए शैक्षिक कदाचार संबंधी नियम तथा विनियमों से अवगत हूँ।	2. I am aware of the rules and regulations regarding academic misconduct as given in rules and regulations of the institute.
3. मैं, इस परीक्षा के दौरान शैक्षिक सत्यनिष्ठा के सिद्धांतों पर दृढ़ रहूंगा / रहूंगी।	3. I will adhere to the principles of academic integrity during this examination.

हस्ताक्षर/ Signature :-

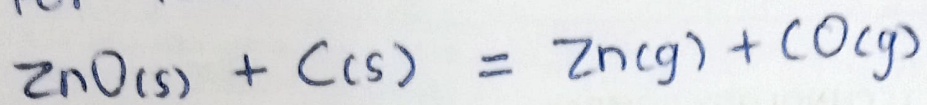
दिनांक/ Date

:-

16/9/22

Q. 17

(i) For 1200 K :-



$$\Delta S_{1200}^{\text{1200}} = (189.9 + 240.7) - (28.5 + 110.3) \\ = \underline{291.8 \text{ J/mol}\cdot\text{K}}$$

$$\Delta G_{1200} = \Delta H - T\Delta S \\ = (149165 - 82101) - (-306091 + 16241) \\ - 1200(291.8) \\ = \underline{6754 \text{ J/mol}}$$

\therefore At 1200 K the reaction is not spontaneous as ~~$\Delta G < 0$~~ $\Delta G > 0$.

(ii) For 1500 K

$$\Delta S_{1500} = (194.6 + 248.4) - (122.6 + 33.7) \\ = \underline{286.7 \text{ J/mol}\cdot\text{K}}$$

$$\Delta G_{1500} = \Delta H - T\Delta S \\ = (155401 - 71677) - (23257 - 289629) \\ - 1500(286.7) \\ = \underline{-79954 \text{ J/mol}}$$

\therefore At 1500 K the reaction is spontaneous as ~~$\Delta G < 0$~~ & $\Delta S > 0$.

Q.2] a) $F = KT \left(\frac{L}{L_0} - \frac{L_0^2}{L^2} \right)$

$$Y = \frac{L}{A} \left(\frac{dF}{dL} \right)$$

$$= \frac{L}{A} \left(KT \left(\frac{1}{L_0} + \frac{2L_0^2}{L^3} \right) \right)$$

$$= \frac{KT}{A} \left(\frac{L}{L_0} + \frac{2L_0^2}{L^2} \right)$$

$$= \frac{1}{A} \left[KT \left(\frac{L}{L_0} - \frac{L_0^2}{L^2} \right) + KT \left(\frac{3L_0^2}{L^2} \right) \right]$$

$$= \frac{1}{A} \left[F + \frac{3KT L_0^2}{L^2} \right]$$

$$\therefore \boxed{Y = \frac{F}{A} + \frac{3KT L_0^2}{A L^2}}$$

b) At zero tension $F=0$ & $L_0 = L$
Putting this in above Y eqn we get :-

$$Y = 0 + \frac{3KT L_0^2}{A L_0^2}$$

$$\therefore \boxed{Y = \frac{3KT}{A}}$$

c) Using the given values we get :-

$$F = KT \left(\frac{L}{L_0} - \frac{L_0^2}{L^2} \right)$$

$$= 1.333 \times 10^{-2} \times 300 \left(\frac{2L_0}{L_0} - \frac{L_0^2}{4L_0^2} \right)$$

$$= 1.333 \times 3 \times \frac{7}{4} = \boxed{6.998 \text{ N} \approx 7 \text{ N}}$$

$$\begin{aligned}
 \gamma &= \frac{F}{A} + \frac{3KTl_0^2}{Al^2} \\
 &= \frac{6.998}{10^{-6}} + \frac{3 \times 1.333 \times 10^{-2} \times 300 \times 10^2}{10^{-6} \times 4 \times 10^2} \\
 &= 10^6 (6.998 + 3 \times 1.333 \times 3)
 \end{aligned}$$

$$\boxed{\gamma = 18.995 \times 10^6 \text{ N/m}^2}$$

$$\therefore \boxed{
 \begin{aligned}
 F &= 6.998 \approx 7 \text{ N} \\
 \gamma &= 18.995 \times 10^6 \approx 19 \times 10^6 \text{ N/m}^2
 \end{aligned}
 }$$

$$\text{Q.3] } \cancel{x} \Delta H_f = \cancel{n} n C_{p(s)} \Delta T$$

$$\therefore x \times 11240 = 1 \times 30.5 \times 61$$

$$\therefore x = \frac{30.5 \times 61}{11240}$$

$$= 0.165 \text{ mol.}$$

\therefore 0.165 moles of silver solidifies

$$\text{Heat released} = 1 \times 30.5 \times 61 = 1860.5 \text{ J}$$

$$\therefore \Delta S = \frac{\delta Q}{T} = \frac{1860.5}{(900+273)} = \frac{1860.5}{1173}$$

$$= \underline{\underline{1.586 \text{ J/K}}}$$

\therefore The entropy change is 1.586 J/K

Q.4] Two aluminas: A & B

$$n_A = 1, T_A = 273 \text{ K} \quad n_B = 1, T_B = 473 \text{ K}$$

$$C_p(\text{Al}_2\text{O}_3(s)) = 106.6 + 17.78 \times 10^{-3} T$$

$$\int_{273}^T n_A C_p dT = - \int_{473}^T n_B C_p dT$$

$$\therefore \int_{273}^T 1 \times (106.6 + 17.78 \times 10^{-3} T) dT = \int_T^{473} 1 \times (106.6 + 17.78 \times 10^{-3} T) dT$$

$$\therefore 106.6(T - 273) + \frac{17.78 \times 10^{-3}}{2} (T^2 - 273^2)$$

$$= 106.6(473 - T) + \frac{17.78 \times 10^{-3}}{2} (473^2 - T^2)$$

$$\therefore 106.6T + \frac{17.78 \times 10^{-3}}{2} T^2 - \left(106.6 \times 273 + \frac{17.78 \times 10^{-3}}{2} \times 273^2 \right)$$

$$= -106.6 \times T - \frac{17.78 \times 10^{-3}}{2} T^2$$

$$+ \left(106.6 \times 473 + \frac{17.78 \times 10^{-3}}{2} \times 473^2 \right)$$

$$\therefore 213.2T + 17.78 \times 10^{-3} T^2 = 79523.6 + 6.632$$

$$\therefore 213.2T + 17.78 \times 10^{-3} T^2 = 86,155.54$$

$$\therefore T^2 +$$

P.T.O.

$$\therefore 213.2T + 17.78 \times 10^3 T^2 = 79523.6 + 2651.5$$

$$\therefore 213.2T + 17.78 \times 10^3 T^2 = 82175.11$$

$$\therefore T^2 + 11991T - 4621772.21 = 0$$

$$\therefore T = \frac{-11991 + \sqrt{(11991)^2 + 4 \times (4621772.21)}}{2}$$

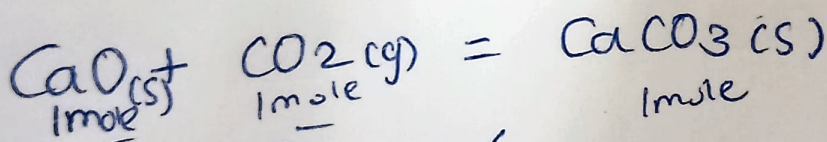
$$\boxed{T = 373.785 \text{ K}}$$

$$\approx \underline{\underline{100.785^\circ \text{C}}}$$

The common uniform Temperature is not exactly 100°C because some heat is lost in the surroundings.

Q.5]

Bonus Question :



$$\cancel{\Delta H_{\text{rxn}}} = \cancel{\Delta H^\circ} + \cancel{\Delta G}$$

1 mole of CaO reacts with 1 mole of CO₂
to form 1 mole CaCO₃

$\therefore \cancel{\Delta H_{\text{CaO}}}$

$$\Delta H = -168000 + (-123 \times (1183 - 298))$$

$$+ 52.8 (1183 - 298)$$

$$+ 51.6 (1183 - 298)$$

$$= \cancel{-124989} - 184,461 \text{ J}$$

$$\Delta G = \Delta G^\circ + \Delta n_g R T$$

$$= 0 - 1 \times 8.314 \times \cancel{1183} 298$$

$$= \cancel{-9835.462} \text{ J}$$

$$= -2477.572 \text{ J}$$

P.T.O.

$$\Delta G = \Delta H - T\Delta S$$

$$\therefore \rightarrow \cancel{9835.462} = \cancel{-124989} -$$

$$\therefore -2477.5720 = -184461 - 298 \Delta S$$

$$\therefore \Delta S = \frac{-181983.428}{298}$$

$$\boxed{\Delta S_{\text{sys.}} = -610.682 \text{ J/K}}$$

$$\underline{\underline{\Delta S_{\text{sur}} = 610.682 \text{ J/K}}} \quad \underline{\underline{\Delta S_{\text{total}} = 0}}$$