## Syntax

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egin{aligned} i \in \operatorname{Int} \ b \in \operatorname{Bool} \ x,y \in \operatorname{Var} \ op \in \operatorname{Prim} &::= + |-| * | < \ &	au \in \operatorname{Types} &::= \operatorname{bool} | \operatorname{int} | &	au \to 	au | &	au \operatorname{list} \ &\Gamma \in \operatorname{Env} &::= \bullet | &\Gamma, x : 	au \ &e \in \operatorname{Exp} &::= i & |b| & x | e \ op \ e \ | & \operatorname{if} \ e \ \operatorname{then} \ e \ \operatorname{else} \ e \ | \operatorname{let} \ x = e \ \operatorname{in} \ e \ | & | \| \| e :: e \ | \ \operatorname{match} \ e \ \operatorname{with} \ \| \| \to e \ | \ x :: y \to e \end{aligned}
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## **Derivation Rules**

$$\frac{\Gamma \vdash i : \operatorname{int}}{\Gamma \vdash i : \operatorname{int}} (\text{T-Int}) \qquad \frac{\Gamma \vdash b : \operatorname{bool}}{\Gamma \vdash b : \operatorname{bool}} (\text{T-Bool}) \qquad \frac{(\Gamma(x) = \tau)}{\Gamma \vdash x : \tau} (\text{T-Var})$$
 
$$\frac{\Gamma \vdash e_1 : \operatorname{bool}}{\Gamma \vdash i : \operatorname{int}} \frac{\Gamma \vdash e_2 : \tau}{\Gamma \vdash i : \operatorname{int}} \frac{\Gamma \vdash e_2 : \tau}{\Gamma \vdash e_1 : \operatorname{then}} e_2 \text{ else } e_3 : \tau$$
 
$$\frac{\Gamma \vdash e_1 : \operatorname{int}}{\Gamma \vdash e_1 + e_2 : \operatorname{int}} (\text{T-PLUS}) \qquad \frac{\Gamma \vdash e_1 : \operatorname{int}}{\Gamma \vdash e_1 - e_2 : \operatorname{int}} (\text{T-Minus})$$
 
$$\frac{\Gamma \vdash e_1 : \operatorname{int}}{\Gamma \vdash e_1 : \operatorname{int}} \frac{\Gamma \vdash e_2 : \operatorname{int}}{\Gamma \vdash e_1 : \operatorname{ep} : \operatorname{int}} (\text{T-LT})$$
 
$$\frac{\Gamma \vdash e_1 : \operatorname{int}}{\Gamma \vdash e_1 : e_2 : \operatorname{int}} (\text{T-LT})$$
 
$$\frac{\Gamma \vdash e_1 : \tau_1 \vdash e_2 : \tau_2}{\Gamma \vdash \operatorname{fun}} (\text{T-Var})$$
 
$$\frac{\Gamma \vdash e_1 : \tau_1 \to \tau_2}{\Gamma \vdash e_1 : e_2 : \tau_2} (\text{T-App})$$
 
$$\frac{\Gamma \vdash e_1 : \tau_1 \to \tau_2}{\Gamma \vdash \operatorname{let}} x = e_1 : \operatorname{in} e_2 : \tau_2} (\text{T-Let})$$
 
$$\frac{\Gamma \vdash e_1 : \tau_1 \to \tau_2, y : \tau_1 \vdash e_1 : \tau_2}{\Gamma \vdash \operatorname{let}} \frac{\Gamma, x : \tau_1 \to \tau_2 \vdash e_2 : \tau}{\Gamma \vdash \operatorname{let}} (\text{T-Cons})$$
 
$$\frac{\Gamma \vdash e_1 : \tau}{\Gamma \vdash e_1 : \tau} \underset{\Gamma \vdash e_1 : \tau}{\operatorname{Iist}} (\text{T-Nil})$$
 
$$\frac{\Gamma \vdash e_1 : \tau}{\Gamma \vdash e_1 : e_2 : \tau} \underset{\Gamma \vdash e_1 : \tau}{\operatorname{Iist}} (\text{T-Cons})$$
 
$$\frac{\Gamma \vdash e_1 : \tau' : \tau' : \operatorname{Iist}}{\Gamma \vdash e_1 : \tau'} \underset{\Gamma \vdash e_2 : \tau}{\Gamma \vdash e_2 : \tau} \underset{\Gamma \vdash e_3 : \tau}{\operatorname{Iist}} (\text{T-Match})$$