

# Hash Table

A hash table is a **data structure** that allows efficient lookup, insertion, and deletion of key-value pairs. It works by mapping each key to a unique index in it.

## Why we need a Hash Table?

Suppose we have an array/linked list. If we want to get a certain value, we must traverse the it.

0	1	2		...	500,000	...	...	1M
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If the array/linked list is very long, the traversal will generate huge overhead.

Can we find this value in constant time without traversal?

**Hash Table!**

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## Direct Address Table

The keys are used as their indexes in the array to store the record by Direct Addressing

If we want to store the values {0, 1, 2, 3, 100001}

Create an array with the size of 100002, each value is stored under its corresponding index

0	1	2	3	...	100001
0	1	2	3		100001

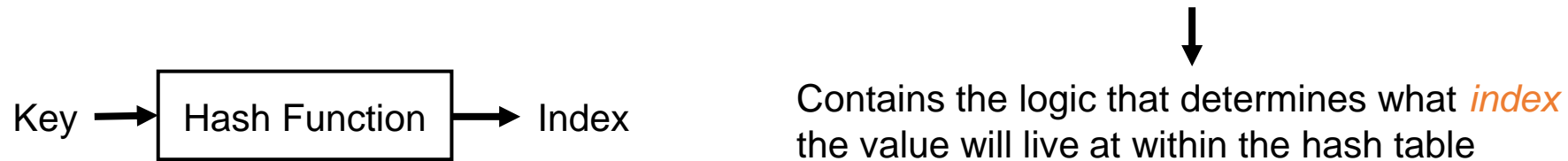
Now, to find the value 1001, we don't need to traverse the array. Since arrays support **random access**, we can simply retrieve it using its index:  $A[1001] = 1001$ .

Operations take  $O(1)$  time, but waste too much space → **Hash Function** Map the universe of all keys into a hash table slots space efficiently

# Hash Table

## Hash Function

Determine how the table should store the data ---- Requires both key and the value



- Modulo Arithmetic:  $H(k) = k \bmod h$
- Folding:  $H(abc) \rightarrow (a + b + c) \bmod h$
- Mid-square:  $H(k) = k^2 \bmod h$ , the middle part of the result is used as the hash address
- Multiplicative Congruential Method:  $H(k) = (a \times k) \bmod h$ ,  $a$  is a pseudo-random number

## Collision

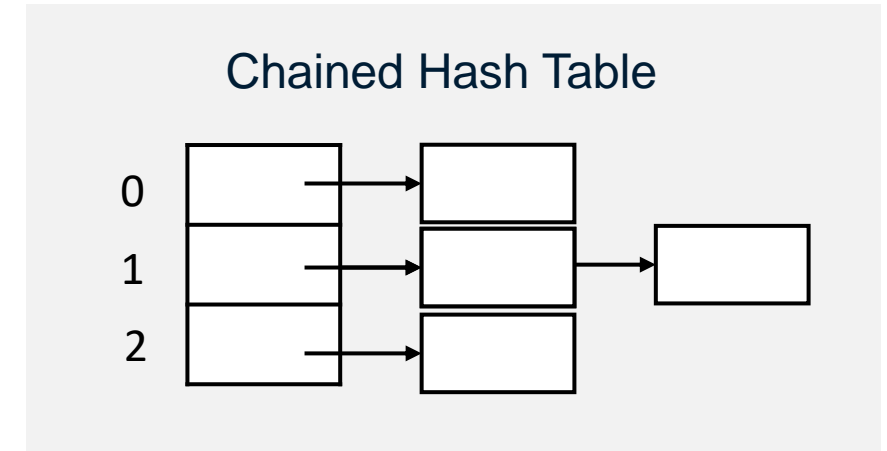
Ensure each possible key can find its index in the table, but multiple keys may be mapped to the same slots

- Closed Address Hashing
- Open Address Hashing

# Hash Table

## Closed Address Hashing (Chained Hashing)

- The address is **closed** (fixed). Each key has a corresponding fixed address
- If there are  $n$  records to store in the hash table, then  $\alpha = \frac{n}{h}$  is the **load factor** of the hash table.



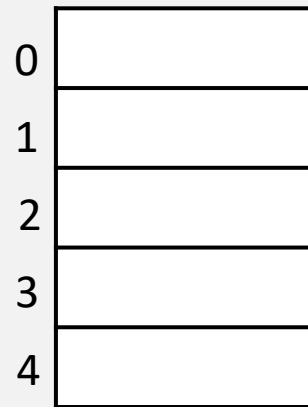
Collision: When multiple keys hash to the same index, they are stored in the linked list at that index.

## Open Address Hashing

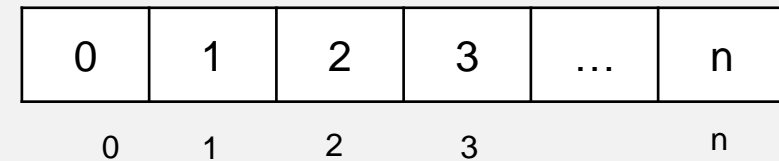
The address is open (not fixed)

- Linear Probing
- Quadratic Probing
- Double Hashing

The load factor is never greater than 1



## Linear Hash Table



Collision: If a collision occurs, the algorithm "probes" the next available slot until an empty one is found

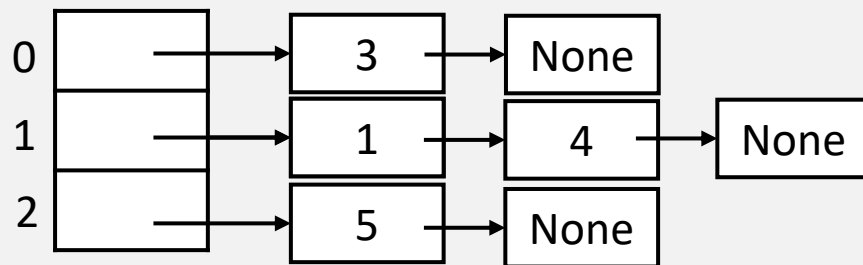
# Q1 Closed Address Hashing

Implement a closed addressing hash table to perform insertion and key searching. The insertion may not have to insert at the end of the linklist. The function prototype is given below:

```
def hash_search(self, key):  
def hash_insert(self, key):
```

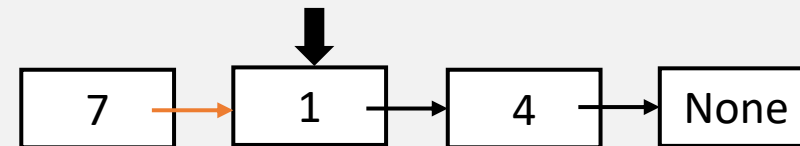
The default load factor is 3. The number of hash slots of the created hash table depends on the provided amount of data.

Insert {1, 3, 4, 5, 7}

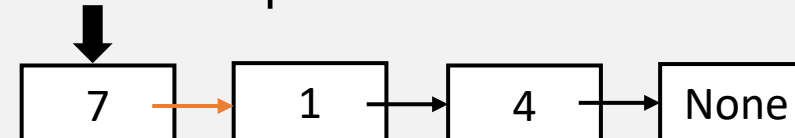


self.table[1] → 1

- Create a new node “7”
- Link “7”’s next to the linklist



- Update the head pointer to “7”



## Q2 Open Address Hashing with Linear Probing

Implement an open addressing hash table with linear probing to perform insertion, deletion, and key searching. The function prototype is given below:

```
def hash_search(self, key):  
def hash_insert(self, key):  
def hash_delete(self, key):
```

$$H(k, i) = (H'(k) + i) \bmod h, \text{ where } H'(k) = k \bmod h$$

0	5
1	1
2	2
3	3
4	8

$$\text{size} = h = 5 \quad H(k, i) = (H'(k) + i) \bmod h$$

Insert "8",  $i = 0$ ,  $H(8, 0) = (8 + 0) \bmod 5 = 3$

Use linear probing,  $i += 1$ ,  $H(8, 1) = (8 + 1) \bmod 5 = 4$

If `self.table[4] == None`: `self.table[4] = Node(8)`

- Boundary of  $i$
- Deleted or not?