# Robot Teknolojisine Giriş BLM4830

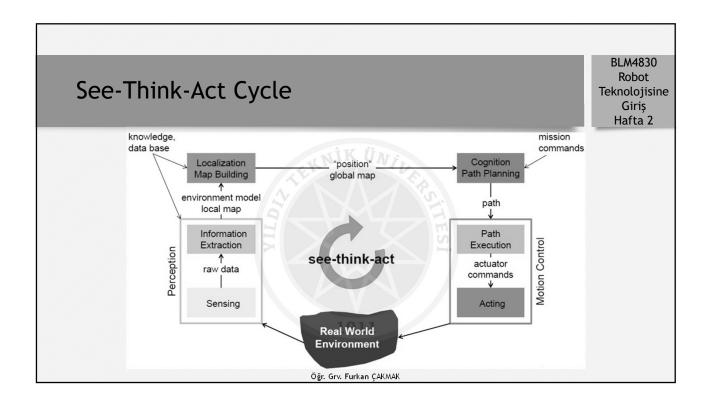


Öğr. Grv. Furkan ÇAKMAK

#### Ders Tanıtım Formu ve Konular

BLM4830 Robot Teknolojisine Giriş Hafta 2

		Tiaita Z						
Hafta	Tarih	Konular						
1	2.03.2022	Ders Tanıtımı, ROS ve Platform Tanıtımı, Robot Çeşitleri ve Robotik Konuları Başlangıcı						
2	9.03.2022	Kinematik - Genel Tanımlar - Diferansiyel Sürüşlü Robot İçin Hesaplama Örnekleri						
3	16.03.2022	Sensörler - Çeşitleri ve Çalışma Sistematikleri ve Uygulamaları						
4	23.03.2022	Odometri ve Lokalizasyon Kavramları						
5	30.03.2022	Uygulama 1 (Laboratuvar)						
6	6.04.2022	Haritalama Yöntemleri ve Uygulamaları						
7	13.04.2022	Navigasyon ve Keşif Yaklaşımları ve Uygulamaları (Ödev Teslimi)						
8	20.04.2022	Ara Sınav						
9	27.04.2022	Uygulama 2 (Laboratuvar)						
10	4.05.2022	Tatil - Ramazan Bayramı Arifesi						
11	11.05.2022	Robot Üzerinden Görüntü İşleme Teknikleri						
12	18.05.2022	Robot Üzerinden Görüntü İşleme Teknikleri (Devam)						
13	25.05.2022	3B Haritalama Yöntemleri						
14	1.06.2022	Proje Sunumları						
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#### Wheeled Mobile Robots

BLM4830 Robot Teknolojisine Giriş Hafta 2

- Combination of various physical (hardware) and computational (software) components
- A collection of subsystems:
  - Locomotion: How the robot moves through its environment.
  - Sensing: How the robot measures properties of itself and its environment.
  - · Control: How the robot generate physical actions.
  - Reasoning: How the robot maps measurements into actions.
  - **Communication**: How the robots communicate with each other or with an outside operator.

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# Wheeled Mobile Robots Wheeled Mobile Robots



#### Wheeled Mobile Robots

1

#### Contents

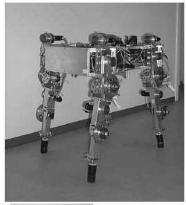
- Introduction
- Classification of wheels
  - Fixed wheel
  - Centered orientable wheel
  - Off-centered orientable wheel
  - Swedish wheel
- Mobile Robot Locomotion
  - Differential Drive
  - Tricycle
  - Synchronous Drive
  - Omni-directional
  - Ackerman Steering
- Kinematics models of WMR
- Summary

#### Locomotion











- Locomotion is the process of causing an autonomous robot to move
  - In order to produce motion, forces must be applied to the vehicle

# Wheeled Mobile Robots (WMR)



Yamabico



MagellanPro



Sojourner



ATRV-2



Hilare 2-Bis



Koy

3

#### Wheeled Mobile Robots

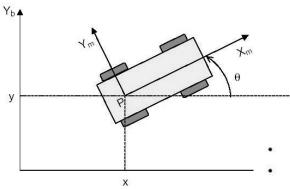
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  - Communication: how the robots communicate with each other or with an outside operator

5

#### Wheeled Mobile Robots

- Locomotion the process of causing an robot to move.
  - In order to produce motion, forces must be applied to the robot
  - Motor output, payload
- Kinematics study of the mathematics of motion without considering the forces that affect the motion.
  - Deals with the geometric relationships that govern the system
  - Deals with the relationship between control parameters and the behavior of a system.
- Dynamics study of motion in which these forces are modeled
  - Deals with the relationship between force and motions.

#### **Notation**



Pose/Posture: position(x, y) and orientation  $\theta$ 

- $\{X_m, Y_m\}$  moving frame
- {X<sub>b</sub>, Y<sub>b</sub>} base frame

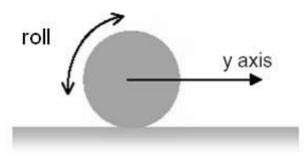
$$q = \begin{bmatrix} x \\ y \\ \theta \end{bmatrix}$$
 robot posture in base frame

$$R(\theta) = \begin{bmatrix} \cos \theta & \sin \theta & 0 \\ -\sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

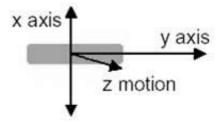
Rotation matrix expressing the orientation of the base frame with respect to the moving frame

7

#### Wheels



Rolling motion

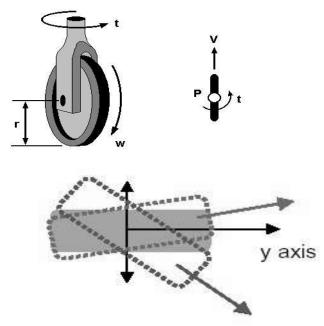


Lateral slip

#### Steered Wheel

#### Steered wheel

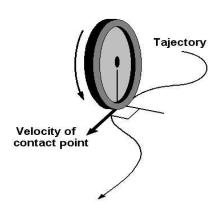
- The orientation of the rotation axis can be controlled



9

# Idealized Rolling Wheel

#### Assumptions



Non-slipping and pure rolling

- 1. The robot is built from rigid mechanisms.
- 2. No slip occurs in the orthogonal direction of rolling (non-slipping).
- 3. No translational slip occurs between the wheel and the floor (pure rolling).
- 4. The robot contains at most one steering link per wheel.
- 5. All steering axes are perpendicular to the floor.

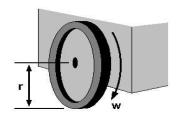
# Robot wheel parameters

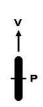
- For low velocities, rolling is a reasonable wheel model.
  - This is the model that will be considered in the kinematics models of WMR
- · Wheel parameters:
  - -r =wheel radius
  - v = wheel linear velocity
  - w = wheel angular velocity
  - t = steering velocity

11

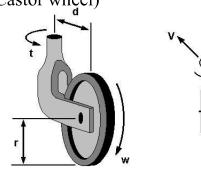
# Wheel Types

Fixed wheel

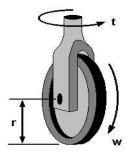




Off-centered orientable wheel (Castor wheel)

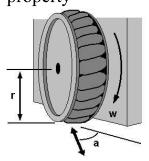


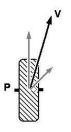
Centered orientable wheel





Swedish wheel:omnidirectional property





#### Fixed wheel

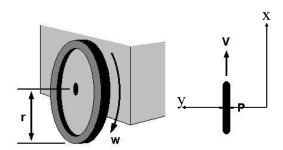
- Velocity of point **P** 

$$V = (r \times w)a_x$$

where, ax : A unit vector to X axis

Restriction to the robot mobility

Point **P** cannot move to the direction perpendicular to plane of the wheel.



13

#### Centered orientable wheels

- Velocity of point P

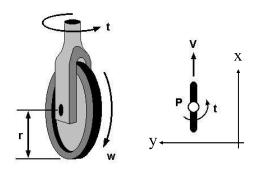
$$V = (r \times w)a_x$$

where,

**ax**: A unit vector of x axis

ay: A unit vector of y axis

Restriction to the robot mobility



#### Off-Centered Orientable Wheels

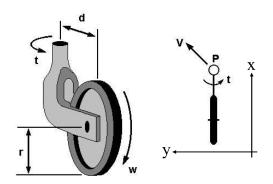
Velocity of point P

$$v = (r \times w)a_x + (d \times t)a_y$$

where,  $a_x$ : A unit vector of x axis

ay: A unit vector of y axis

Restriction to the robot mobility



15

#### Swedish wheel

Velocity of point P

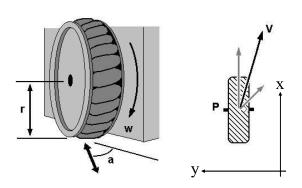
$$v = (r \times w)a_x + Ua_s$$

where,

**ax**: A unit vector of x axis

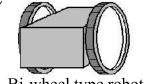
**as**: A unit vector to the motion of roller

- Omnidirectional property

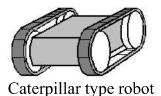


# Examples of WMR

#### Example



Bi-wheel type robot



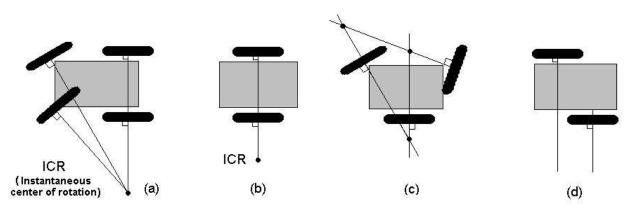
Omnidirectional robot

- Smooth motion
- Risk of slipping
- Some times use roller-ball to make balance
- Exact straight motion
- Robust to slipping
- Inexact modeling of turning
- Free motion
- Complex structure
- Weakness of the frame

17

#### Mobile Robot Locomotion

- Instantaneous center of rotation (ICR) or Instantaneous center of curvature (ICC)
  - A cross point of all axes of the wheels

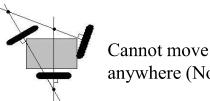


We talk about the instantaneous center, because we'll analyze this at each instant- the curve may, and probably will, change in the next moment.

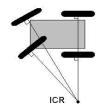
# Degree of Mobility

#### **Degree of mobility**

The degree of freedom of the robot motion

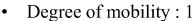


anywhere (No ICR)



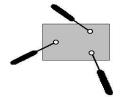
Fixed arc motion (Only one ICR)

Degree of mobility: 0





Variable arc motion (line of ICRs)



Fully free motion

(ICR can be located at any position)

19

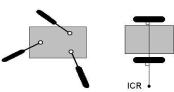
Degree of mobility: 2

Degree of mobility: 3

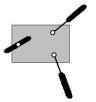
Degree of Steerability

**Degree of steerability** 

The number of centered orientable wheels that can be steered independently in order to steer the robot



No centered orientable wheels

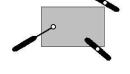


Degree of steerability: 0

One centered orientable wheel



Two mutually dependent centered orientable wheels



Two mutually independent centered orientable wheels

Degree of steerability: 1

Degree of steerability: 2

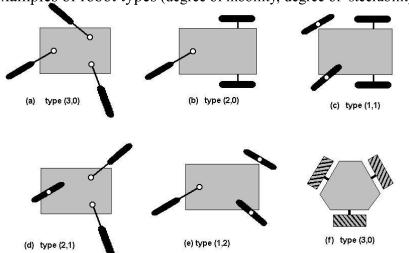
20

# Degree of Maneuverability

• The overall degrees of freedom that a robot can manipulate:

$\delta_{M} = \delta_{m} + \delta_{s}$								
Degree of Mobility	3	2	2	1	1			
Degree of Steerability	0	0	1	1	2			

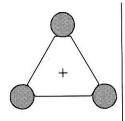
• Examples of robot types (degree of mobility, degree of steerability)



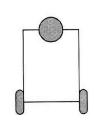
21

# Degree of Maneuverability

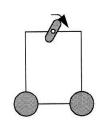
$$\delta_{\scriptscriptstyle M} = \delta_{\scriptscriptstyle m} + \delta_{\scriptscriptstyle S}$$



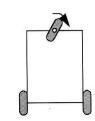
Omnidirectional  $\delta_{M} = 3$   $\delta_{m} = 3$   $\delta_{m} = 0$ 



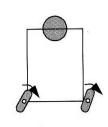
Differential  $\delta_{\rm M} = 2$   $\delta_{\rm m} = 2$   $\delta_{\rm s} = 0$ 



Omni-Steer  $\delta_{M} = 3$   $\delta_{m} = 2$   $\delta_{s} = 1$ 



Tricycle  $\delta_{M} = 2$   $\delta_{m} = 1$   $\delta_{s} = 1$ 



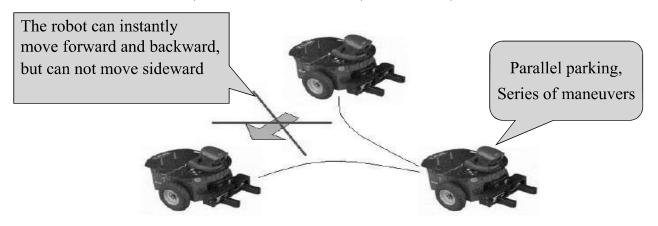
Two-Steer  $\delta_{\rm M} = 3$   $\delta_{\rm m} = 1$   $\delta_{\rm s} = 2$ 

#### Non-holonomic constraint

A non-holonomic constraint is a constraint on the feasible velocities of a body

So what does that mean?

Your robot can move in some directions (forward and backward), but not others (sideward).

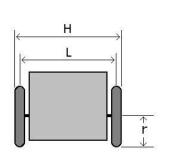


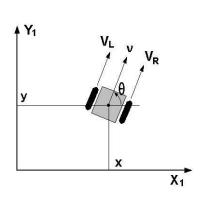
23

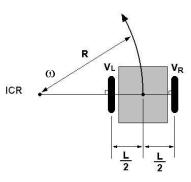
#### Mobile Robot Locomotion

- Differential Drive
  - two driving wheels (plus roller-ball for balance)
  - simplest drive mechanism
  - sensitive to the relative velocity of the two wheels (small error result in different trajectories, not just speed)
- Steered wheels (tricycle, bicycles, wagon)
  - Steering wheel + rear wheels
  - cannot turn ±90°
  - limited radius of curvature
- Synchronous Drive
- Omni-directional
- Car Drive (Ackerman Steering)

#### **Differential Drive**







- Posture of the robot
- $P = \begin{pmatrix} x \\ y \\ \theta \end{pmatrix}$  (x,y) : Position of the robot  $\theta$  : Orientation of the robot
- Control input

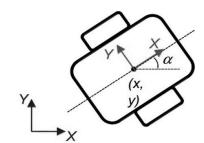
$$U = \begin{pmatrix} v \\ w \end{pmatrix}$$

 $U = \begin{pmatrix} v \\ w \end{pmatrix}$  v: Linear velocity of the **robot** w: Angular velocity of the **robot** (notice: not for each wheel)

25

#### **Differential Drive**

· Two wheels, either side of the robot driven independently

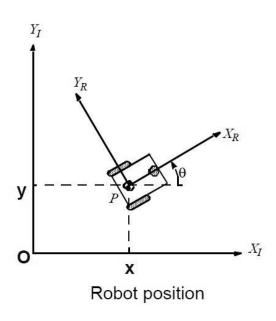


 Steering is achieved by driving the wheels at different speeds



• Two degrees of freedom -> 2 controllable values:  $(V_1, V_r)$ 

#### Robot Reference Frame

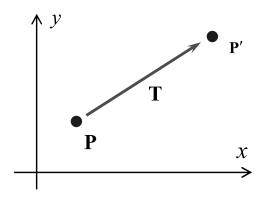


- The robot's reference frame is three dimensional including position on the plane and the orientation, {X<sub>R</sub>, Y<sub>R</sub>,θ}
- The axes {X<sub>I</sub>, Y<sub>I</sub>}, define inertial global reference frame with origin, O
- The angular difference between the global and reference frames is θ
- Point P on the robot chassis in the global reference frame is specified by coordinates (x, y)

$$\xi_I = \begin{bmatrix} x & y & \theta \end{bmatrix}^T$$

27

#### 2D Translation

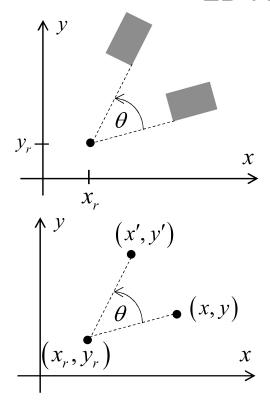


$$x' = x + t_{x}, \quad y' = y + t_{y}$$

$$\mathbf{P} = \begin{bmatrix} x \\ y \end{bmatrix}, \quad \mathbf{P}' = \begin{bmatrix} x' \\ y' \end{bmatrix}, \quad \mathbf{T} = \begin{bmatrix} t_{x} \\ t_{y} \end{bmatrix}$$

$$\mathbf{P}' = \mathbf{P} + \mathbf{T}$$

#### 2D Rotation



Rotation in angle  $\theta$  about a pivot (rotation) point  $(x_r, y_r)$ .

$$x' = x_r + (x - x_r)\cos\theta - (y - y_r)\sin\theta$$

$$y' = y_r + (x - x_r)\sin\theta + (y - y_r)\cos\theta$$

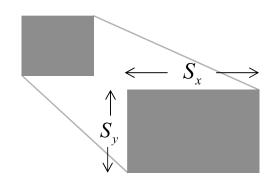
$$\mathbf{P}' = \mathbf{P}_r + \mathbf{R} \cdot (\mathbf{P} - \mathbf{P}_r)$$

$$\mathbf{R} = \begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix}$$

$$\mathbf{R} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

29 April 2010

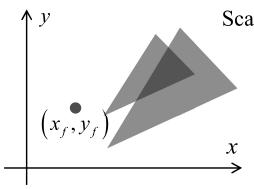
#### 2D Scaling



$$x' = x \cdot s_x, \quad y' = y \cdot s_y$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$\mathbf{P}' = \mathbf{S} \cdot \mathbf{P}$$



Scaling about a fixed point  $(x_f, y_f)$ 

$$x' = x \cdot s_x + x_f \left( 1 - s_x \right)$$

$$y' = y \cdot s_y + y_f \left( 1 - s_y \right)$$

$$\mathbf{P}' = \mathbf{P} \cdot \mathbf{S} + \mathbf{P}_f \cdot (\mathbf{1} - \mathbf{S})$$

#### Homogeneous Coordinates

Rotate and then displace a point  $P: P' = M_1 \cdot P + M_2$ 

 $\mathbf{M}_1$ : 2×2 rotation matrix.  $\mathbf{M}_2$ : 2×1 displacement vector.

Displacement is unfortunately a non linear operation.

Make displacement linear with Homoheneous Coordinates.

 $(x, y) \Rightarrow (x, y, 1)$ . Transformations turn into  $3 \times 3$  matrices.

Very big advantage. All transformations are concatenated by matrix multiplication.

31 April 2010

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}, \quad \mathbf{P}' = \mathbf{T}(t_x, t_y) \cdot \mathbf{P}$$

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}, \quad \mathbf{P}' = \mathbf{R}(\theta) \cdot \mathbf{P}$$

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} S_x & 0 & 0 \\ 0 & S_y & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}, \quad \mathbf{P'} = \mathbf{S}(S_x, S_y) \cdot \mathbf{P}$$

# **Orthogonal Rotation Matrix**

The **orthogonal rotation matrix** is used to map motion in the global reference  $\{X_l, Y_l\}$  frame to motion in the robot's local reference frame  $\{X_R, Y_R\}$ 

$$R(\theta) = \begin{bmatrix} \cos \theta & \sin \theta & 0 \\ -\sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

The orthogonal rotation matrix is used to convert robot velocity in the global reference frame to components of motion along the robot's local axes  $\{X_R, Y_R\}$ 

$$\dot{\xi}_{R} = R(\theta)\dot{\xi}_{I} = R(\theta)\cdot\begin{bmatrix} \dot{x} & \dot{y} & \dot{\theta} \end{bmatrix}^{T}$$

33

# How to convert Degrees to Radians

- One degree is equal 0.01745329252 radians:  $1^{\circ} = \pi/180^{\circ} = 0.005555556\pi = 0.01745329252$  rad
- The angle α in radians is equal to the angle α in degrees times pi constant divided by 180 degrees:

$$\alpha(\text{radians}) = \alpha(\text{degrees}) \times \pi / 180^{\circ}$$

• or radians = degrees × π / 180°