```
Counting:
P(A) = |A| | Equially likely outcome
     the number
      of elements
Coffe example SML in how many ways can you order your coffee?
   7 F:1 Em
                  3x7= 9 mays
   - Perot
   Vlight
Multipli cation Principle (Prensiti)
(r deregini japtigimizi varsagalim)
Suppose that we perform r experiments. There are n possible outcomer
for each axperiment
                              12 KZr

1-2 n1

2-2 n2

1-2 n1

Possible outcomes

K-2 n2
  ( se < ne)
  Choosing a password
-> begin with 2 lower case letters followed by
     (biyok harf
-> 1 capital letter followed by
 -> 4 digits
 HOP total passwords
-> mul Elplication principle
  \frac{e}{l} \quad \frac{e}{l} \quad \frac{c}{l} \quad \frac{1}{l} \quad \frac{1}{l} \quad \frac{1}{l} \quad \frac{1}{l}
  26 × 26 × 26 × 17 × 10 × 15 × 10 -> 26.15
 Sampling
 - Sampling from a set random ly choosing an element from a sex.
                         ( corbasu geri atiliser)
                         with replacement; put the sampled element back
  Replacement
 without replacement - don't put the sampled element back
 Ordering If ordering matters (a1) a2,03) $ (as, a2,04) Ismal, secim
unordored sampling - order is not important (01/2) 9] = (a), d, a)
        don't matter - zören i değil
                       Expes of sampling
   Ordered sampling with replecement.
   ex A = {1,2,3} draw k=2 samples
  inflow many ways the sampling can be done?
   (1,2), (1,3), (2,3), (4,1), (2,2), (3,1), (2,1), (3,2), (3,1)
    3×3-59 son Kis number of sampling
 -- number of subsets=? A= {...} n eloments. What is the number of diffrent
 Mul Kiplication principle
 Ordered sampling without raplacement
                                      L) Permotation
   -No repetition
  0x : A = { 1, 3, 1 }
   (1)2), (1)7), (3,1), (2,1), (2,3), (3,2) -> 3 × 2 = 6
  Ex: k people in a class what is the probability
         of them have same bhirthday
                      1 person = 1
  A= event that 2 preople have same bhilt day
  A= 10 2 people have the same bhirtday.
     K 2 365 = at least -> Peagerhole principle
     Unordered sampling without replecament
   ex A= {1,2,13} K=2 nordered

Sampling with replecement
   (1,2), (1,3) (2,3) \rightarrow combination \binom{n}{k} = \frac{n!}{k!(n-k)!}
       \binom{3}{2} = \frac{3!}{2!(1)!} = 3
P = \binom{2}{k}!
 ex: Choose I cards from a deck (52 cards)
  What is the probability that these cards contain at least one ACE
   hA(E in a deck
   P(A°)= Nono of ] conds with contain A(E=(52-4)
   P(\Lambda) = \begin{pmatrix} 52 \\ 3 \end{pmatrix}
   P(A) = 1 - \frac{\binom{48}{3}}{\binom{52}{1}} - 1 - \frac{18.47.46}{52.51.50} = 1 - \frac{12.23.47}{51.13.27}
   Binomial ( be fficient (Bison agilini)
      Dividing sets into two is like in choose k"
                                         \binom{n}{k} = \binom{n}{n-k}
    EX. Onfair coin P(H)=P 0 < P < 1 P(T)=1-P
    wa toss the coin 5 times.
    @ What is the prob. that the output is H H T H +)
      Lamaj Eipilication rule
P.P. (1-P).P.P = Ph. (1-P)
    O Prob 4 heads 1 fail
       \rightarrow \left(\frac{5}{4}\right), P^{4}(1-P)
    3 If I toss the com n times, what is the prob. that I observe
     k head and n-k tails.
      P \cdot (1-P) \cdot (P)
  ex10 people ... to a resturnate
            5 a main Lish.
            3 <- drinks
             2 a dessert In how many ways can these people be selected?
             \binom{10}{5}\binom{5}{1}\binom{2}{2} = \frac{10!}{5!5!} \cdot \frac{5!}{3!2!} \cdot \frac{2!}{2!0!}
          Unordered sampling with Keplacement
          A = {1/2,33
           (1,1), (1,2) (1,1) (2,1) (2,1) (2,1) 6 possible lists

C>2 kining not site 1000 (1,1) = ×1 + ×2+1 = 2 0 0
                  un ondered
                  with neplace
                     \begin{pmatrix} 1 + 1 & 1 \\ 1 & 1 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 1 \\ 2 & 1 \end{pmatrix} = \frac{4 \cdot 3}{2} = 6
            ati lo passengers get on an airport shuttle. The shuttle noute includes
            5 hotels and each passengers gets off his hotel. The driver
           records how many pussengers leave the shuttle at each hotel. How
                  different possible lists.
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 $\left(\begin{array}{c} 5 \times 10^{-1} \\ 10 \end{array}\right) = \frac{14!}{4! \cdot 10!}$