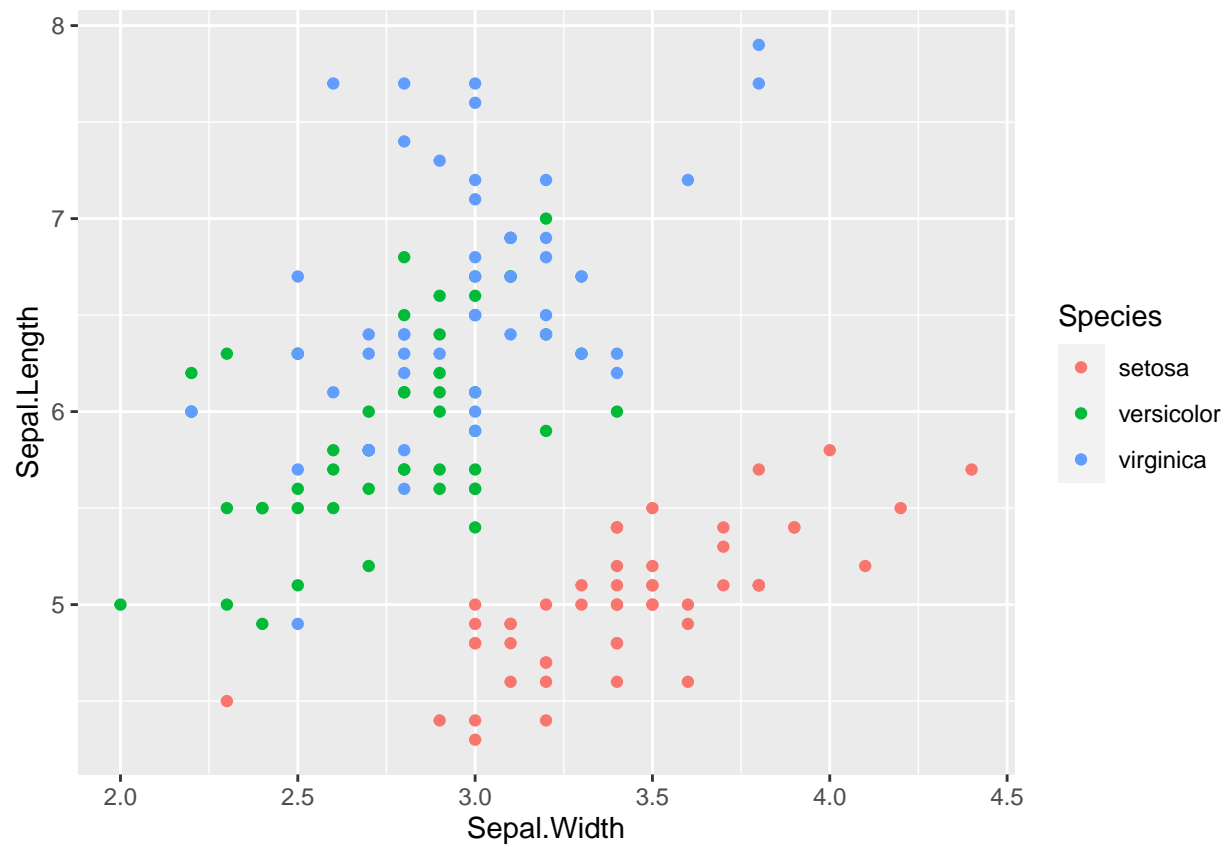


# LDA

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Scatter plot of Sepal length vs Sepal Width



Mean

Covariance

```
##           Sepal.Length Sepal.Width
## Sepal.Length 0.12424898 0.09921633
## Sepal.Width  0.09921633 0.14368980
```

```
##           Sepal.Length Sepal.Width
## Sepal.Length 0.40434286 0.09376327
## Sepal.Width  0.09376327 0.10400408
```

```
##           Sepal.Length Sepal.Width
## Sepal.Length  0.26643265  0.08518367
## Sepal.Width   0.08518367  0.09846939
```

### Prior of classes

```
## [1] 0.3333333
```

```
## [1] 0.3333333
```

```
## [1] 0.3333333
```

### Pooled covariance

```
pooled_matrix <- (virginica_covariance*nrow(virginica)+(setosa_covariance*nrow(setosa))+versicolor_covariance*nrow(versicolor))
pooled_matrix
```

```
##           Sepal.Length Sepal.Width
## Sepal.Length  0.26500816  0.09272109
## Sepal.Width   0.09272109  0.11538776
```

### Underlying probabilistic model

$$x|y = C_i, \mu_i, \sum N(\mu_i, \sum)$$

$$y|\pi = Multinomial(\pi_1, \dots, \pi_k)$$

### Discriminant function

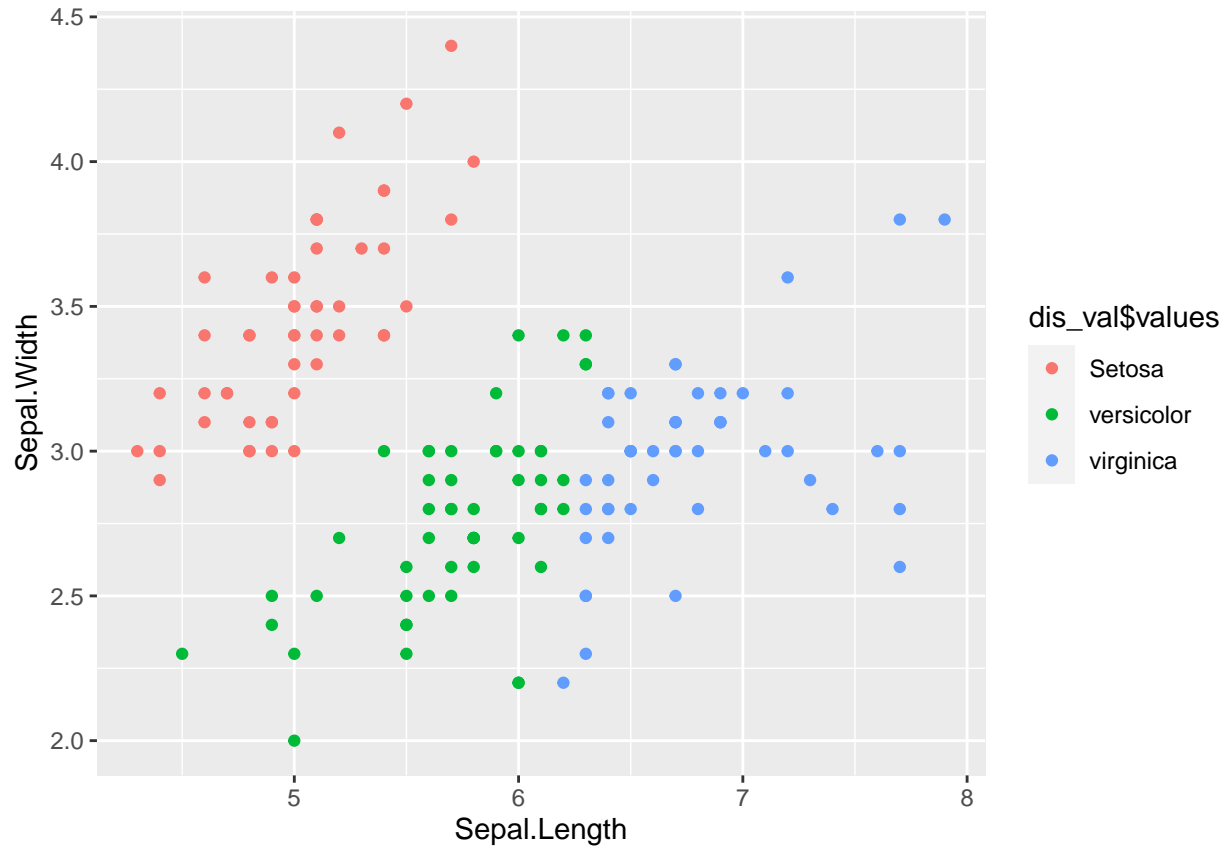
```
disc_function <- function(class_data, class_mean, class_prior, class_covariance)
{
  (as.matrix(class_data[1:2]) %*% solve(class_covariance) %*% class_mean) -
  rep((0.5*(class_mean[1:2] %*% solve(class_covariance) %*% class_mean)), nrow(class_data)) + rep(log(class_prior), nrow(class_data))
}

setosa_disc <- disc_function(data, setosa_mean, setosa_prior, pooled_matrix)
versicolor_disc <- disc_function(data, versicolor_mean, versicolor_prior, pooled_matrix)
virginica_disc <- disc_function(data, virginica_mean, virginica_prior, pooled_matrix)
```

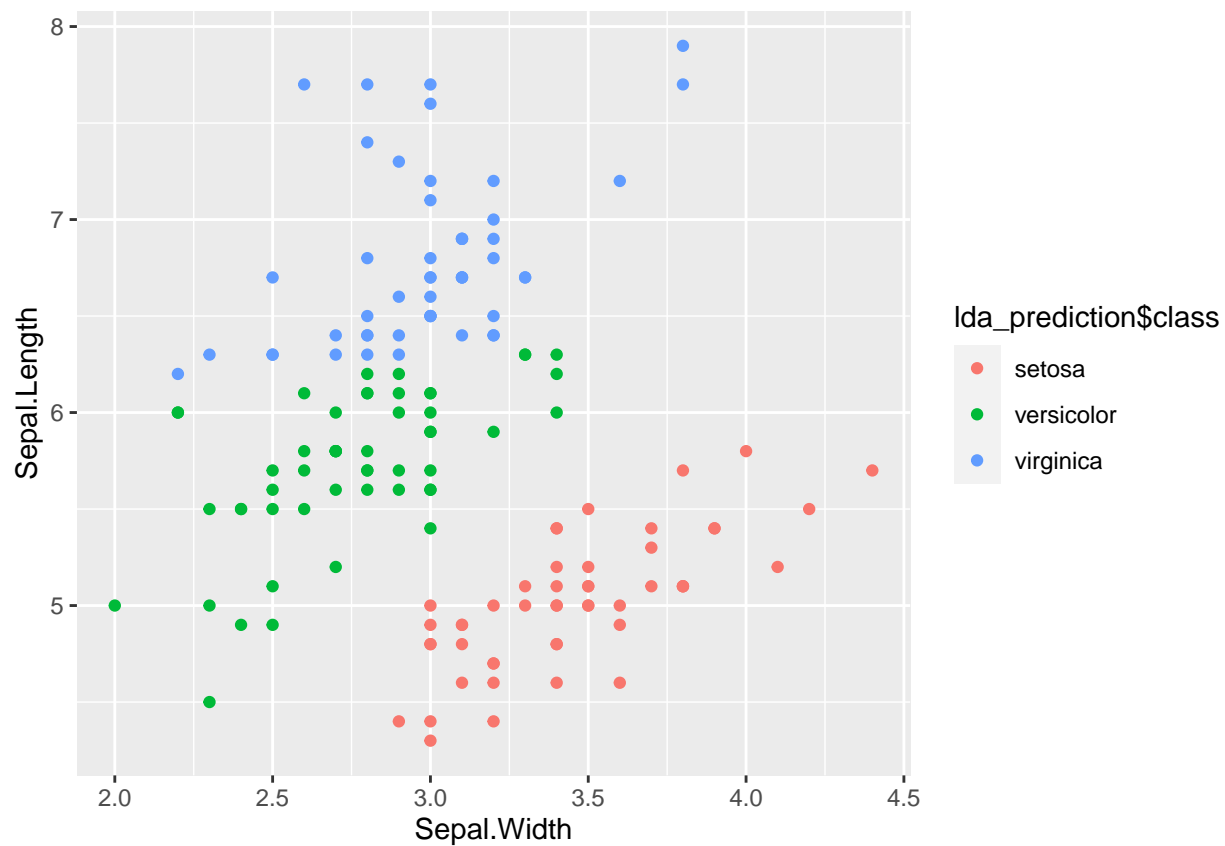
### Decision boundaries

$$\text{Log}(\pi_l/\pi_k) - 1/2(\mu_k + \mu_l)^T \sum (\mu_k - \mu_l) + x^T \sum_{l=1}^{-1} (\mu_k - \mu_l)$$

### Predicting using dicriminant function



### Prediction using LDA



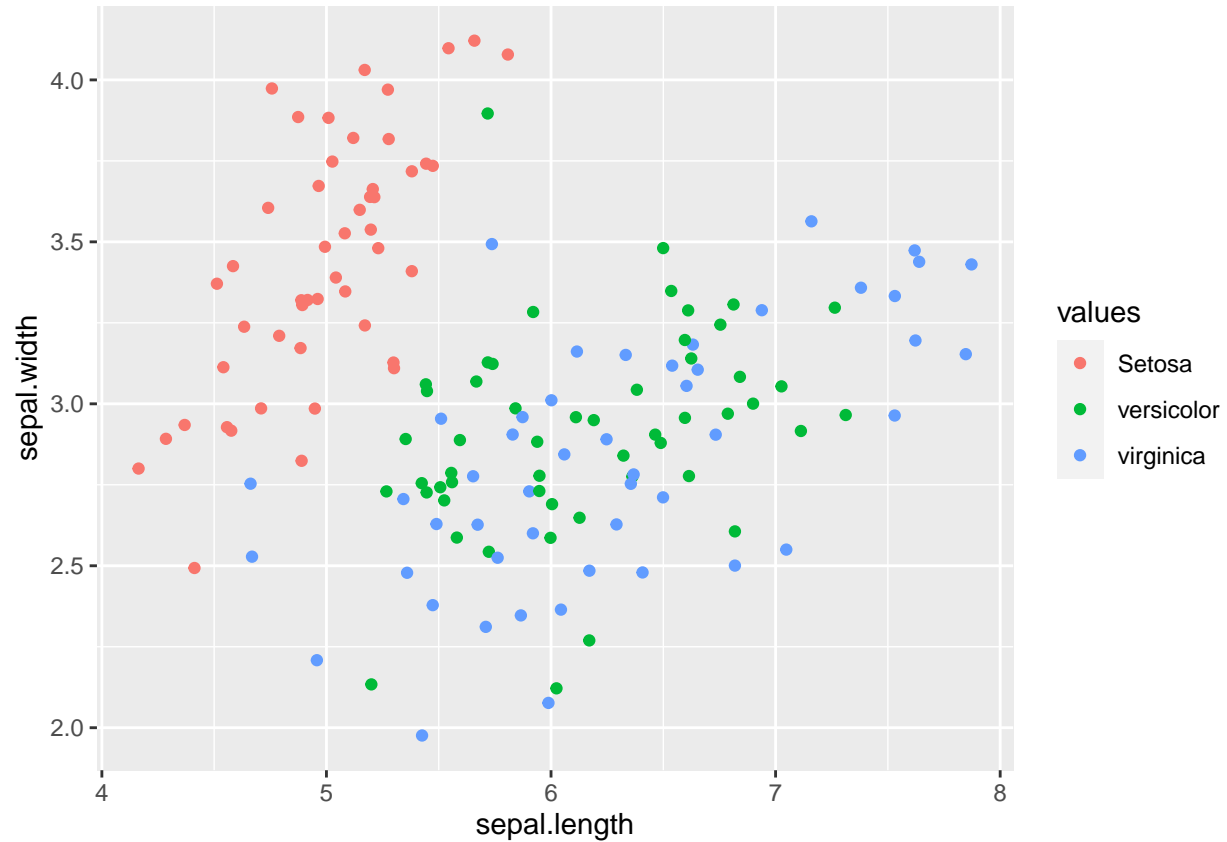
### Confusion matrix using LDA function

```
##
##           setosa versicolor virginica
## setosa         49           0         0
## versicolor      1          36        15
## virginica       0          14        35
```

### Misclassification error using LDA function

```
## [1] 0.2
```

## Generatin new data with discriminant function



```
## versicolor      0      38      13
## virginica       0      12      37
```

**Misclassification error**

```
## [1] 0.1666667
```