

# ST3009: Statistical Methods for Computer Science

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## Week 3 Assignment - Senán d'Art - 17329580

### Question 1

**(a)**

The event  $(1, 1)$  is the only one that corresponds to  $Y = 2$ .

**(b)**

$\{(1, 2), (2, 1)\}$  correspond to  $Y = 3$

**(c)**

$\{(1, 3), (2, 2), (3, 1)\}$  correspond to  $Y = 4$

**(d)**

Number of total possible results: 36

Set size: 3

Probability of event:  $\frac{3}{36} = \frac{1}{12}$

### Question 2

$X = \text{Head} - \text{Tails}$

**(a)**

Possible values of X:  $\{-3, -1, 1, 3\}$

**(b)**

8 Total Combinations ( $2^3$ )

Only one way to roll  $-3$  :  $\{\text{Tails}, \text{Tails}, \text{Tails}\}$

Probability:  $\frac{1}{8}$

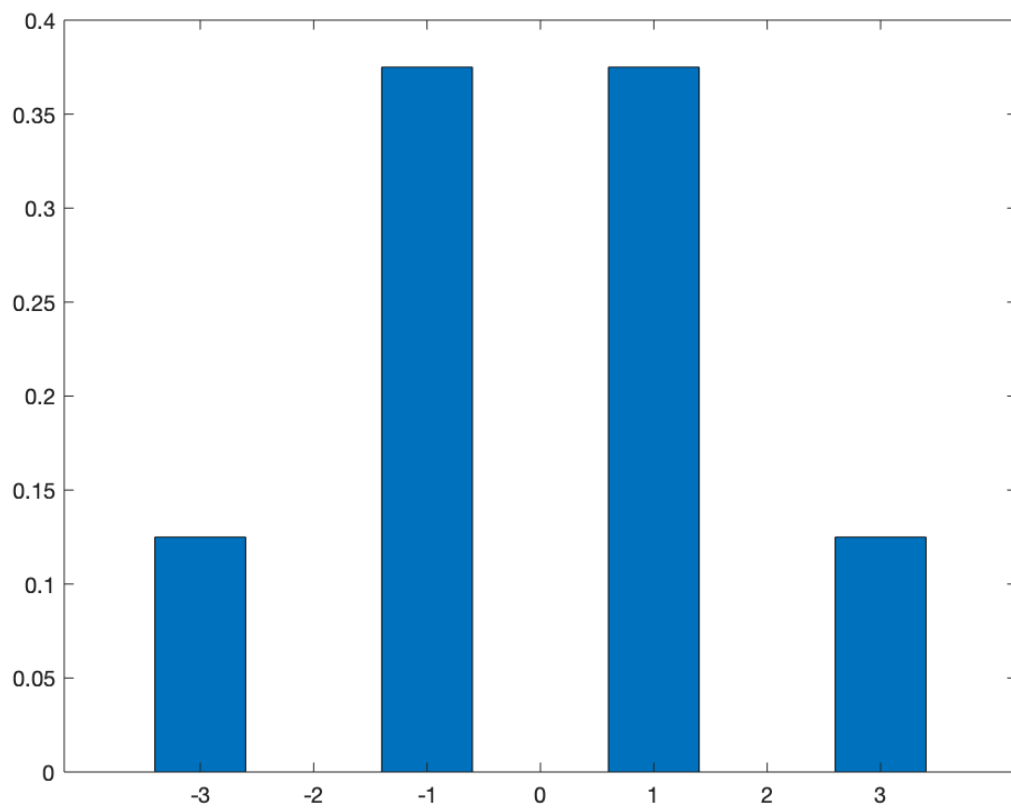
**(c)**

8 Total Combinations

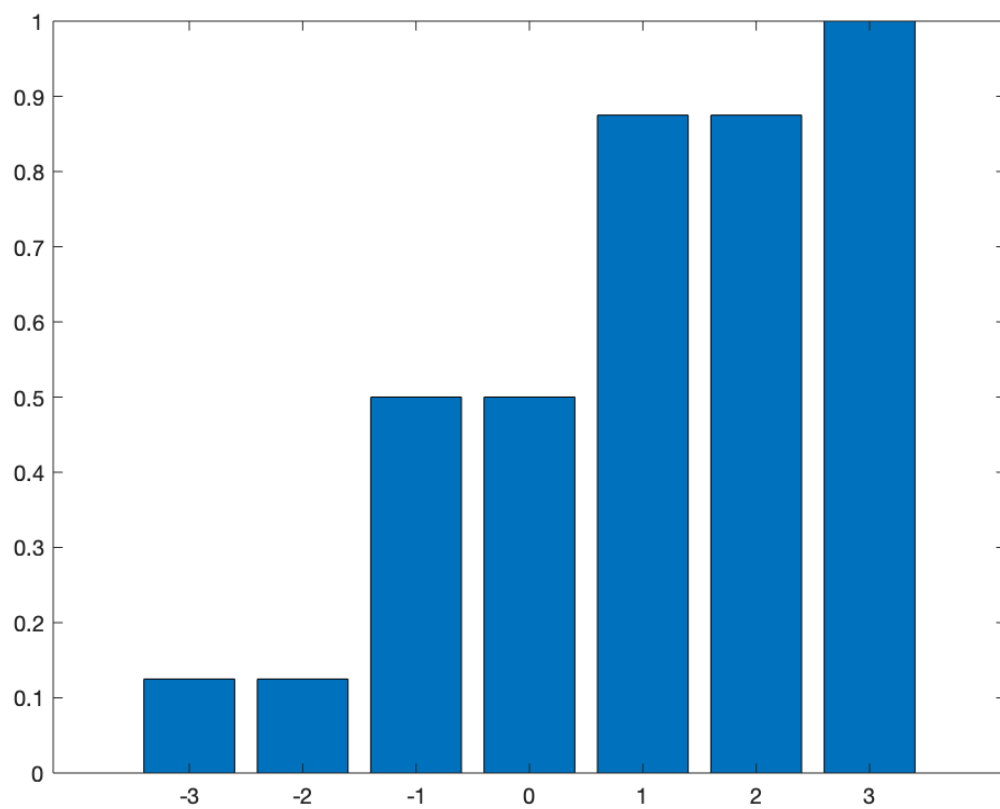
Three ways to roll  $-1$  :  $\{[H, T, T], [T, H, T], [T, T, H]\}$

Probability:  $\frac{3}{8}$

**(d)**



**PMF of X**



**CDF of X**

Question 3

(a)

Possible values for X are {1,2,3,4,5,6}.

X will always be  $\geq 1$ .

Probability is 1.

(b)

For  $X \geq 2$ , no ones must be rolled.

$$\frac{5}{6} * \frac{5}{6} * \frac{5}{6} * \frac{5}{6} = 0.4823$$

(c)

$$X \leq 1, K = 1 - \left(\frac{5}{6}\right)^4 = 0.5177$$

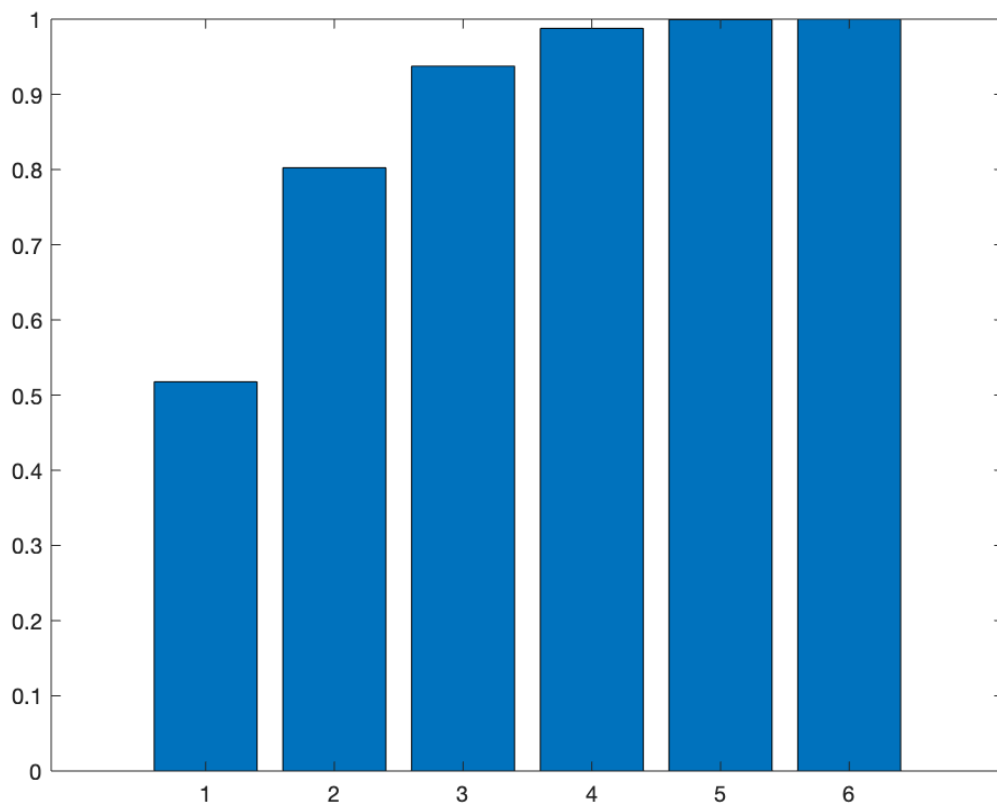
$$X \leq 2, K = 1 - \left(\frac{4}{6}\right)^4 = 0.8024$$

$$X \leq 3, K = 1 - \left(\frac{3}{6}\right)^4 = 0.9375$$

$$X \leq 4, K = 1 - \left(\frac{2}{6}\right)^4 = 0.9877$$

$$X \leq 5, K = 1 - \left(\frac{1}{6}\right)^4 = 0.9992$$

$$X \leq 6, K = 1$$



CDF of X