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ST3009: Statistical Methods for Computer Science

Week 1 Assignment - Senán d'Art - 17329580

Question 1

(a)

No restrictions so letters can be in any order. To generate all possible results: $\$\$ \binom{10}{1} \binom{9}{1} \binom{6}{1} \binom{6}{1} \binom{6}{1} \binom{4}{1} \binom{2}{1} \binom{2}{1} \binom{1}{1} \\$ As every time we choose a letter it is removed from the pool of available letters.

This becomes: \$\$ 1098765432*1 \$\$ Which is: \$\$ 10! = 3,628,800 \$\$

(b)

Restrictions of E and F being next to each other but in any order means we can treat it as a pool of 9 characters. \$\$ 9! \$\$ But since E and F can be in the order EF or FE we need to multiply this by 2. \$\$ 9! * 2 = 725,760 \$\$

(c)

Word 'BANANA' contains 6 letters but 'A' is repeated 3 times and 'N' 2 times. f(0){(3!)(2!)} = 60 \$\$

(d)

There are 5 letters to choose from. We must choose 3. \$ \binom{5}{3} = 10 \$\$

Question 2

(a)

(b)

(c)

To get all possible scenarios of at least two 3s:

- two 3s as above: \$\$ \binom{4}{2} * \binom{5}{1} * \binom{5}{1} = \binom{4}{2} * 5^2 = 150 \$\$
- three 3s similar to above but now 3 of 4 locations are 3s and only one can be 1,2,4,5,6: \$\$ \binom{4}{3}
 * \binom{5}{1} = \binom{4}{3} * 5 = 20 \$\$
- four 3s all 3s: \$\$ \binom{4}{4} = 1 \$\$ The sum of these options is: \$\$ 150 + 20 + 1 = 171 \$\$

Question 3

(a)

Similar to Q1(c). There are 8 total but each of the 4 distinct cards are repeated twice. $\$ \frac{8!}{2!*2!*2!*2!} = \frac{8!}{(2!)^4} = 2,520 \$$

(b)

Assuming order is important, the number of possible combinations is gotten by choosing 1 of 4 for the first card and 1 of the remaining 3 for the second. \$ \binom{4}{1}\binom{3}{1} \\$\$ But since the order is irrelevant this must be divided by 2: \\$\$ \frac{\binom{4}{3}\binom{3}{1}}{2} = 6 \\$\$

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(c)

Each card can have 2 values: $\$\$ 2^2 \$\$$ But one of these combinations is duplicated: {hearts,diamonds} = {diamonds, hearts} $\$\$ 2^2 -1 = 3 \$\$$