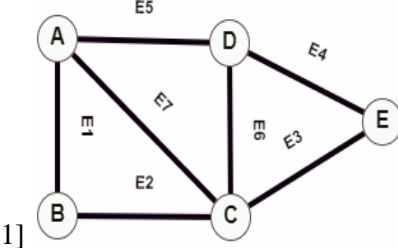
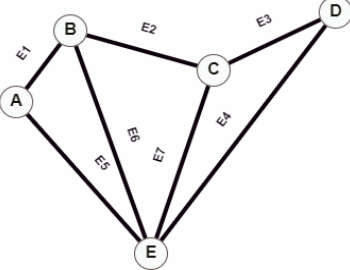
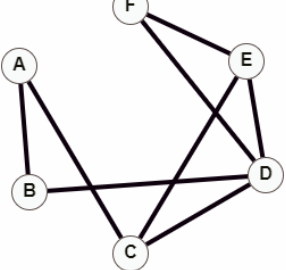
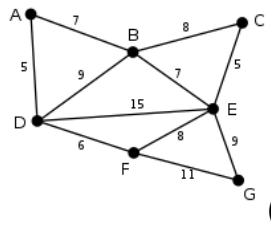
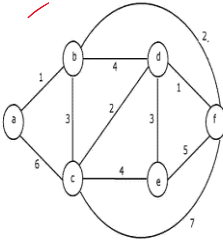


**Subject: DM**

**SEM: 04**

**AY: 2024-25**

**Tutorial 3**  
**Unit: Graphs & Trees**

1	<p>Prove that the following are equivalent for an <math>n</math>-vertex graph <math>T</math>.</p> <ol style="list-style-type: none"> <li><math>T</math> is a tree.</li> <li><math>T</math> is connected and has no cycles.</li> <li>For <math>u, v \in V(T)</math>, <math>T</math> has exactly one path between <math>u</math> to <math>v</math>.</li> <li><math>T</math> is connected and has exactly <math>n - 1</math> edges.</li> </ol>	Understanding
2	<p>Explain the spanning tree. Consider the following graph and draw its possible spanning tree.</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;">  <p>1]</p> </div> <div style="text-align: center;">  <p>2]</p> </div> <div style="text-align: center;">  <p>3]</p> </div> </div>	Evaluate
3	<p>A tree <math>T</math> has 4 vertices of degree 2, 4 vertices of degree 3, 2 vertices of degree 4. Find the number of pendant vertices in <math>T</math>.</p>	
4	<p>How many spanning trees does <math>K_4</math> have? why?</p>	Understanding
5	<p>Derive the minimum weighted spanning tree of following graph.</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;">  <p>(1)</p> </div> <div style="text-align: center;">  <p>(2)</p> </div> </div>	Evaluate