

2024秋物理化学I第三次测验

1. 偏摩尔量: 广度函数 \times 固定 p, T .

化学势: 对自然变量

$$dU = TdS - pdV + \mu dn$$

$$dA = -SdT - pdV + \mu dn \Rightarrow C.$$

2.

$$\mu = \cancel{\mu^0} \mu^* + RT \ln \pi \Rightarrow D.$$

3.

$$\pi \sim cRT, \text{ glucose: 几乎全部分子 } C = 0.01$$

$$NaCl: Na^+, Cl^- \quad C = 0.02.$$

$$\Rightarrow C.$$

4.

$$\text{混合后, 液相作用力比纯态减小} \Rightarrow p_A > p_A^* \pi_A.$$

$$\text{液相体积增大} \Rightarrow A.$$

5.

$$\text{不同相分配定律} \Rightarrow A.$$

都有挥发性, 可能沸点降低.

6.

$$\mu^0[C^0] = \mu^0[m^0] + RT \ln \frac{m[C^0]}{m^0} \Rightarrow B.$$

$$m[C^0] = \frac{1 \text{ mol}}{m[1 \text{ L}]} \quad \text{其未必是 } 1 \text{ kg}.$$

7.

$$\Delta T = 546 - 273 = T.$$

$$\Delta H = C_p \Delta T = \frac{5}{2} nRT.$$

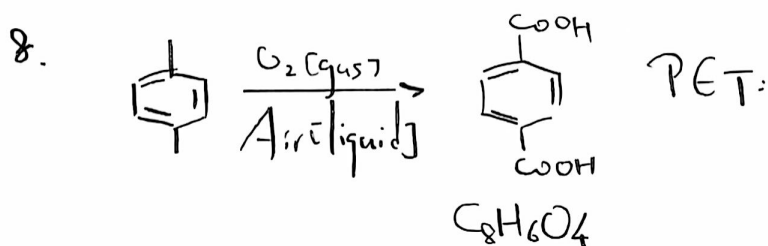
$$dH = TdS + Vdp \Rightarrow dS = \frac{C_p dT}{T} - \frac{V}{T} dp = \frac{C_p}{T} dT - \frac{nR}{p} dp$$



$$\begin{aligned} \Delta S &= C_p \ln \frac{T_2}{T_1} - nR \ln \frac{P_2}{P_1} \\ &= \frac{5}{2} nR \ln 2 - nR \ln \frac{1}{2} \\ &= \frac{7}{2} nR \ln 2. \quad S_2 = S_1 + \Delta S = \frac{9}{2} nR \ln 2 \end{aligned}$$

$$\begin{aligned} \Delta G &= \Delta H - \Delta(TS) \\ &= \frac{5}{2} nRT - (2T \cdot \frac{9}{2} nR \ln 2 - T \cdot nR \ln 2) \\ &= \frac{5}{2} nRT - 8 nRT \ln 2, \\ \Delta \mu &= \Delta G / n = (\frac{5}{2} - 8 \ln 2) RT, \end{aligned}$$

$$\begin{aligned} \Delta A &= \Delta G - \Delta(pV) = \Delta G - nR\Delta T \\ &= (\frac{3}{2} - 8 \ln 2) nRT. \Rightarrow C. \end{aligned}$$



$$\mu = 166.128.$$

$$\text{理论 } n = m / \mu = 0.6862 \text{ mol.}$$

$$\text{实际 } n = \frac{\Delta T}{k_b} \cdot 1 \text{ kg} = 0.1977 \text{ mol}$$

$$\text{平均聚合度} = 3.47 > 3 \Rightarrow D.$$

9. $P_B = P(1 - 0.89) = 5.2503 \text{ kPa} = k_{A,B} \lambda \Rightarrow$

$$k = 35.002 \text{ kPa} \Rightarrow B.$$



10. 化学势平衡:

$$\mu_- + \mu_+ = 2\mu_r = 0$$

体系热力学势判据:

$$dA = -SdT - pdV + \mu_+ dn_+ + \cancel{\mu_- dn_-} \quad \mu_- dn_-$$

$$n_+ \rightarrow \delta n_+$$

$$\begin{aligned} \delta A &= \mu_+ \delta n_+ + \mu_- \delta n_- \\ &= \mu_+ \delta n_+ + \mu_- \frac{\partial n_-}{\partial n_+} \delta n_+ \end{aligned}$$

$$\text{粒子数守恒: } \left(\frac{\partial n_-}{\partial n_+} \right)_{n_- - n_+} = 1 \Rightarrow$$

$$\delta A = (\mu_+ + \mu_-) \delta n_+ = 0, \quad \text{i.e. 化学势平衡}$$

$$\begin{aligned} \left(\frac{\partial A}{\partial n_+} \right)_{n_- - n_+} &= \left(\frac{\partial A}{\partial n_+} \right)_{n_-} \left(\frac{\partial n_+}{\partial n_+} \right)_{n_- - n_+} + \left(\frac{\partial A}{\partial n_-} \right)_{n_+} \left(\frac{\partial n_-}{\partial n_+} \right)_{n_- - n_+} \\ &= \mu_+ + \mu_- \Rightarrow A \end{aligned}$$

$$dn_- - dn_+ = 0 \Rightarrow B.$$

11.

(1) 353K时蒸汽压下降: $p = p^* x \Rightarrow x = \frac{89330}{101325} = 0.88162,$

凝固点降低: $d\mu^l = d\mu^s \Leftrightarrow$

同相 $x \equiv 1$

$$\left(\frac{\partial \mu^l}{\partial T} \right)_x dT + \left(\frac{\partial \mu^l}{\partial x} \right)_T dx = \left(\frac{\partial \mu^s}{\partial T} \right)_x dT + \left(\frac{\partial \mu^s}{\partial x} \right)_T dx \Rightarrow$$

$$-S_m^l dT + RT/x dx = -S_m^s dT \Rightarrow$$

$$d \ln x = \frac{S_m^l - S_m^s}{RT} dT = \frac{\Delta_{\text{fus}} H_m}{RT^2} dT,$$



$$\ln x = -\frac{\Delta_{\text{fus}} H_m^\circ}{R} \left(\frac{1}{T_f} - \frac{1}{T_f^*} \right) \Rightarrow T_f = 271.08. \quad 3'$$

(2)

$$x_{\text{苯}} = 1 - x = 0.11838 \Rightarrow n_{\text{苯}} = \frac{0.1}{x_{\text{苯}}} = 0.8447 \text{ mol}$$

$$n_{\text{苯}} = 0.7447 \Rightarrow \Delta n = 0.1553 \text{ mol}. \quad 2'$$

12.

寻找状态 p, V 方程.

$$\text{gas: } p_i = p^* + p_i^{\text{Air}} \quad 3'$$

$$\text{Henry: } p_i^{\text{Air}} = k a_i^{\text{Air}} = k \frac{n_i^{\text{Air}, l}}{V} \equiv k' n_i^{\text{Air}, l} \quad 2'$$

$$\begin{aligned} \text{Air 物料守恒: } n_i^{\text{Air}, l} &= n_0 - n_i^{\text{Air}, g} \quad 3' \\ &= n_0 - \frac{p_i^{\text{Air}} V_i}{RT} \quad 2' \end{aligned}$$

$$\text{故 } p_i - p^* = k' \left(n_0 - \frac{(p_i - p^*) V_i}{RT} \right) \quad 4'$$

$i=1,2,3 \Rightarrow 3 \text{ equations, denote (1), (2), (3)}$

$p^*, k', n_0 \Rightarrow 3 \text{ variables.}$

$$(1)-(2): p_1 - p_2 = \frac{k'(p_2 - p^*) V_2}{RT} - \frac{k'(p_1 - p^*) V_1}{RT} \quad 3' \quad (4)$$

$$(1)-(3): p_1 - p_3 = \frac{k'(p_3 - p^*) V_3}{RT} - \frac{k'(p_1 - p^*) V_1}{RT} \quad 3' \quad (5)$$

$$(4)/(5): \frac{p_1 - p_2}{p_1 - p_3} = \frac{(p_2 - p^*) V_2 - (p_1 - p^*) V_1}{(p_3 - p^*) V_3 - (p_1 - p^*) V_1} \quad 3' \Rightarrow$$

$$p^* = 16.0998 \sim 16.10 \text{ kPa}. \quad 2'$$



13. 仅 CaCO_3 发生分解.

$$\text{分解 } 3.98 \text{ mmol} \Rightarrow n_{\text{CaCO}_3}' = 11.10 - 3.98 = 7.12 \quad 3'$$

$$(1) \gamma_{\text{CaCO}_3} = 0.55887 \quad 2'$$

$$(2) K^\ominus = \frac{p_{\text{CO}_2}/p^\ominus \cdot a_{\text{CaO}}}{a_{\text{CaCO}_3}} = \frac{1.01 \times 10^{-5} \cdot 1}{1 \times 10^{-5}} \Rightarrow \quad 3'$$

$$a_{\text{CaCO}_3} = 0.28857 \quad 3' = \gamma_{\text{CaCO}_3} \Rightarrow$$

$$\gamma = 0.51635 \quad 2'$$

14.

$$(1) \Phi = -pV \Leftrightarrow -pV = A - \mu_B n_B \Leftrightarrow \mu_B n_B = A + pV = G \quad 4'$$

$$(2) dU = +T dS - p dV + \mu_B d n_B \quad 4'$$

$$(3) U[S, V, n_B]$$

$$U \rightarrow \lambda U[S, V, n_B] = U[\lambda S, \lambda V, \lambda n_B] \Rightarrow$$

$$U[S, V, n_B] = \frac{\partial U[\lambda S, \lambda V, \lambda n_B]}{\partial (\lambda S)} \frac{\partial (\lambda S)}{\partial \lambda} + \frac{\partial U}{\partial (\lambda V)} \frac{\partial (\lambda V)}{\partial \lambda} + \frac{\partial U}{\partial (\lambda n_B)} \frac{\partial (\lambda n_B)}{\partial \lambda}$$

$$= TS - pV + \mu_B n_B \Rightarrow$$

$$G = U + pV - TS = \mu_B n_B \quad 2'$$

