

# Assessing the Predictive Performance of Seldonian Algorithms: A Simulation Study

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## MOTIVATION

Using the standard machine learning (ML) approach for real-life applications can result in algorithmic bias: a situation where an algorithm's predictions systematically discriminate against a demographic group. Seldonian algorithms offer a way to address this problem by incorporating probabilistic constraints on undesirable behavior (mathematically defined) in the search for an optimal solution.

## OBJECTIVES

The primary objective of the simulation study is to investigate the efficacy and applicability of Seldonian algorithms in practical classification settings along three key performance measures:

- convergence (probability of a solution)
- fairer (less discriminatory) outcomes
- predictive accuracy

## METHODS

**Data Generation:** this study is a proof of concept, so the data-generation mechanism follows a realistic design. The COMPAS recidivism data set (collected in Broward County, Florida, 2013-2014) is used nationwide to predict recidivism by defendants, but it exhibits racial discrepancies. The response variable in this study is modeled as a linear combination of the COMPAS variables such that the complex social relationships that may be expected in the real world are retained.

**Methodology:** 1 logistic regression and 4 Seldonian algorithms (with different fairness constraints  $\epsilon$  as an upper bound of the total absolute difference in error rates between Black and White defendants:  $\epsilon = 0.2, 0.1, 0.05, 0.01$ ) are fit on 250 simulated data sets of size  $n = 500, 1000, 2500, 5000$  [1000 total data sets] and results compared.  $\delta = 0.05$  to ensure 95% confidence that the Seldonian solution will satisfy the specified fairness constraint.

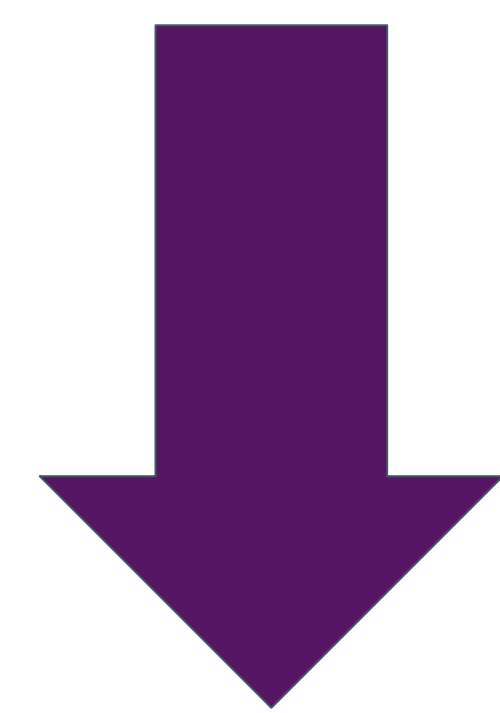
## RESULTS



## HPC CLUSTER USE

### DATA GENERATION

Generate 1000 simulated data sets



### MODEL FITTING (5000 models)

In an *sbatch* file, loop through all 1000 data sets, running a *Python* script on each set and appending results to a global data frame as a row

```
for file in $files; do  
  srun ./seldonian_sim.py "$folder$file" &  
done
```

## CONCLUSIONS

1. There is an accuracy-fairness trade-off.
2. Seldonian solutions are not guaranteed and may still yield unfair results, though it's less probable.