

COMPAS Data Wrangling and Analysis

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The thesis body will have more in-depth descriptions of the data analysis as well as select output and results from this file. This file is intended for general preliminary analysis of the COMPAS data set. Note that the results can only be generalized to Broward County, Florida, but there are important findings about the United States judicial system nevertheless.

Reading in the Data

```
#read in the data
compas_path <- "/home/dasienga24/Statistics-Senior-Honors-Thesis/Data Sets/COMPAS/compas_data.csv"
compasdata <- read.csv(compas_path)
```

The Data Set

The COMPAS data set has 12160 observations of defendants that were evaluated for the risk of recidivism by the COMPAS tool. There are 29 variables of interest as described below:

- **id**: unique person identifier.
- **compas_person_id**: unique COMPAS case identifier.
- **name**: full name.
- **first**: first name.
- **last**: last name.
- **sex**: sex categorized as male or female.
- **race**: race categorized as African-American, Asian, Caucasian, Hispanic, Native American, or Other.
- **age**: numeric age, ranging from 18 to 96.
- **age_cat**: age categorized as Less than 25, 25 - 45, or Greater than 45.
- **marital_status**: marital status categorized as Single, Significant Other, Married, Widowed, Separated, Divorced, or Unknown.
- **custody_status**: custody status categorized as Jail Inmate, Prison Inmate, Pretrial Defendant, Parole, Residential Program, or Probation.
- **juv_fel_count**: number of prior juvenile felonies, ranging from 0 to 20.
- **juv_misd_count**: number of prior juvenile misdemeanors, ranging from 0 to 13.
- **juv_other_count**: number of other prior juvenile offenses, ranging from 0 to 17.
- **priors_count**: number of non-juvenile prior offenses, ranging from 0 to 43.
- **days_b_screening_arrest**: number of days between COMPAS screening and arrest.
- **c_days_from_compas**: the number of days since COMPAS screening.
- **c_charge_degree**: the charge degree according to the appropriate laws.
- **c_charge_desc**: the charge description in words.
- **type_of_assessment**: the type of assessment, in this case, the assessment is 'Risk of Recidivism'.
- **raw_score**: COMPAS tool raw score on risk of recidivism.
- **decile_score**: decile rank on a scale of 1 - 10 based on the COMPAS raw score.
- **score_text**: COMPAS risk of recidivism based on the decile scores and categorized as High, Medium, or Low.
- **is_violent_recid**: categorical variable recording whether a defendant was accused of a violent crime within 2 years (0 = N, 1 = Y).
- **num_vr_cases**: number of times a defendant was accused of a violent crime within 2 years.
- **is_recid**: categorical variable recording whether a defendant was accused of a crime within 2 years (0 = N, 1 = Y).
- **num_r_cases**: number of times a defendant was accused of a crime within 2 years.
- **days_in_jail**: number of days spent in jail before COMPAS screening.
- **days_in_prison**: number of days spent in prison before COMPAS screening.

```
colnames(compasdata)
```

```
## [1] "id"                "compas_person_id"
## [3] "name"              "first"
## [5] "last"              "sex"
## [7] "race"              "age"
```

## [9] "age_cat"	"marital_status"
## [11] "custody_status"	"juv_fel_count"
## [13] "juv_misd_count"	"juv_other_count"
## [15] "priors_count"	"days_b_screening_arrest"
## [17] "c_days_from_compas"	"c_charge_degree"
## [19] "c_charge_desc"	"type_of_assessment"
## [21] "raw_score"	"decile_score"
## [23] "score_text"	"is_violent_recid"
## [25] "num_vr_cases"	"is_recid"
## [27] "num_r_cases"	"days_in_jail"
## [29] "days_in_prison"	

Data Wrangling

Before proceeding with the data analysis, we first need to handle some data anomalies. We'll also only consider COMPAS cases within 30 days of arrest to improve the data quality. This resulted in 9683 total observations.

```
compasdata <- compasdata %>%  
  filter(decile_score > 0 & is_recid != -1 & days_b_screening_arrest >= -30 &  
         days_b_screening_arrest <= 30) %>%  
  mutate(days_b_screening_arrest = abs(days_b_screening_arrest))  
  
count(compasdata)  
  
##          n  
## 1  9683
```

Next, let's also make sure that there are no duplicate defendants.

```
clean_compasdata <- compasdata[-which(duplicated(compasdata$id)), ]
```

We'll proceed with this data set and 9387 observations total.

Descriptive Statistics

Now that the data is clean, let's generate some descriptive statistics to understand the distribution of the variables in the data set and their relationships with each other.

First, below is a glimpse of the data as described above. Notice that there is a lot of missing data for `num_vr_cases` and `num_r_cases` because that information is only recorded for defendants that recommit a crime in the next 2 years.

```
glimpse(clean_compasdata)
```

```
## Rows: 9,387
## Columns: 29
## $ id                <int> 1, 3, 4, 7, 8, 9, 10, 11, 12, 14, 15, 16, 17, ~
## $ compas_person_id  <int> 56418, 51601, 38864, 59301, 61330, 56890, 6199~
## $ name              <chr> "miguel hernandez", "kevon dixon", "ed philo", ~
## $ first             <chr> "miguel", "kevon", "ed", "marsha", "edward", "~
## $ last              <chr> "hernandez", "dixon", "philo", "miles", "riddl~
## $ sex               <chr> "Male", "Male", "Male", "Male", "Male", "Male"~
## $ race              <chr> "Other", "African-American", "African-American~
## $ age               <int> 69, 34, 24, 44, 41, 43, 39, 20, 26, 27, 23, 37~
## $ age_cat           <chr> "Greater than 45", "25 - 45", "Less than 25", ~
## $ marital_status    <chr> "Single", "Single", "Single", "Separated", "Si~
## $ custody_status    <chr> "Jail Inmate", "Jail Inmate", "Jail Inmate", "~
## $ juv_fel_count     <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0~
## $ juv_misd_count    <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0~
## $ juv_other_count   <int> 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0~
## $ priors_count      <int> 0, 0, 4, 0, 14, 3, 0, 0, 0, 0, 3, 0, 0, 0, 1, ~
## $ days_b_screening_arrest <int> 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 0, 0, 1, 20, ~
## $ c_days_from_compas <int> 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 0, 0, 1, 490,~
## $ c_charge_degree   <chr> "(F3)", "(F3)", "(F3)", "(M1)", "(F3)", "(F3)"~
## $ c_charge_desc     <chr> "Aggravated Assault w/Firearm", "Felony Batter~
## $ type_of_assessment <chr> "Risk of Recidivism", "Risk of Recidivism", "R~
## $ raw_score         <dbl> -2.78, -0.76, -0.66, -1.93, -0.16, -0.72, -1.7~
## $ decile_score      <int> 1, 3, 4, 1, 6, 4, 1, 10, 5, 4, 6, 1, 3, 4, 1, ~
## $ score_text        <chr> "Low", "Low", "Low", "Low", "Medium", "Low", "~
## $ is_violent_recid   <int> 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0~
## $ num_vr_cases      <lgl> NA, NA, NA, NA, NA, NA, NA, NA, NA, NA, NA, NA, NA~
## $ is_recid          <int> 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 1~
## $ num_r_cases       <int> NA, 3, 1, NA, 3, NA, NA, NA, NA, NA, 1, NA, NA~
## $ days_in_jail      <dbl> 1, 10, 1, NA, 6, 1, 3, 33, 1, 1, NA, NA, NA, 1~
## $ days_in_prison    <dbl> NA, NA, NA, NA, 1065, NA, NA, NA, NA, NA, NA, ~
```

Next, we will perform some univariate analysis for the variables in the data set before proceeding to conduct some bivariate and multivariate analysis.

Univariate Analysis

Univariate analysis will involve looking at some summary statistics and visualizations of the different variables in the data set.

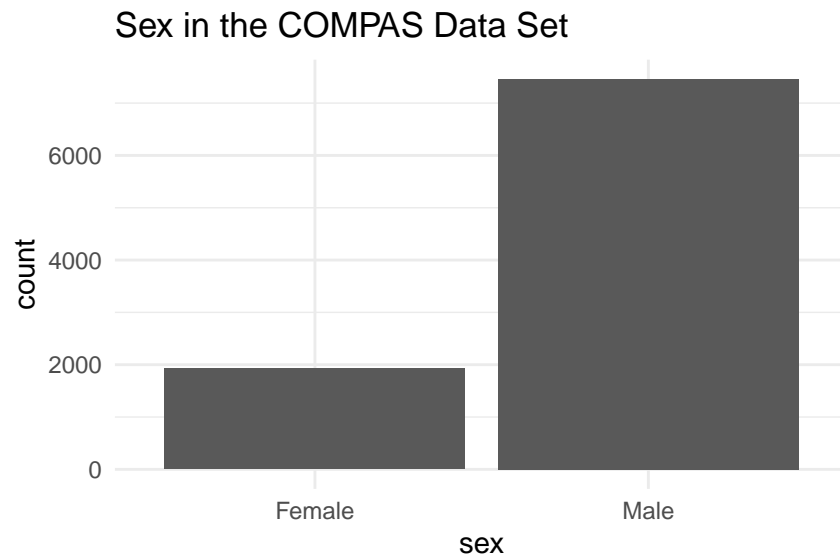
Categorical Variables

There 7457 males and 1930 females in the data set.

```
tally(clean_compasdata$sex)
```

```
## X
## Female    Male
##    1930    7457
```

```
ggplot(data = clean_compasdata, mapping = aes(x = sex)) +
  geom_bar() +
  theme_minimal() +
  labs(title = "Sex in the COMPAS Data Set")
```

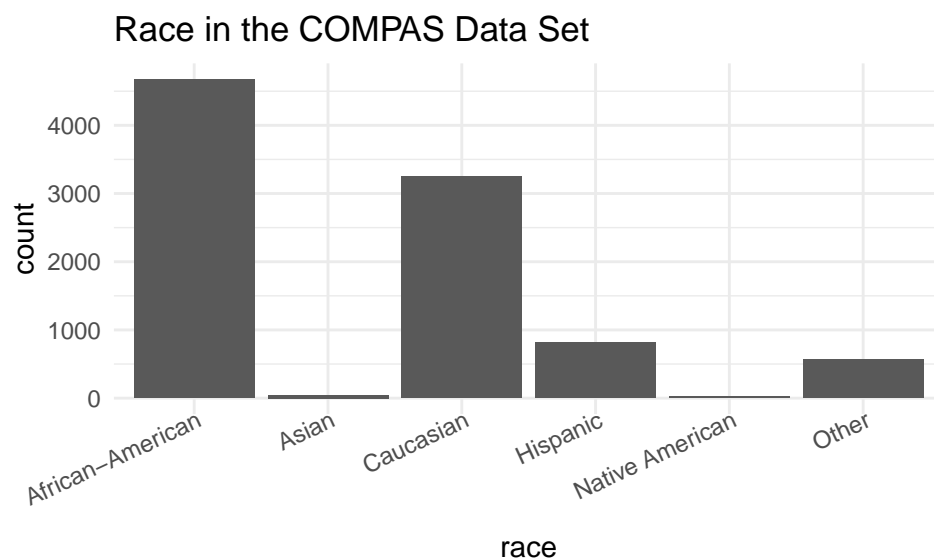


Most of the defendants are African-American and Caucasian, with only 27 Native Americans and 48 Asians.

```
tally(clean_compasdata$race)
```

```
## X
## African-American    Asian    Caucasian    Hispanic
##           4674           48           3250           818
## Native American    Other
##           27           570
```

```
ggplot(data = clean_compasdata, mapping = aes(x = race)) +
  geom_bar() +
  theme_minimal() +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1)) +
  labs(title = "Race in the COMPAS Data Set")
```



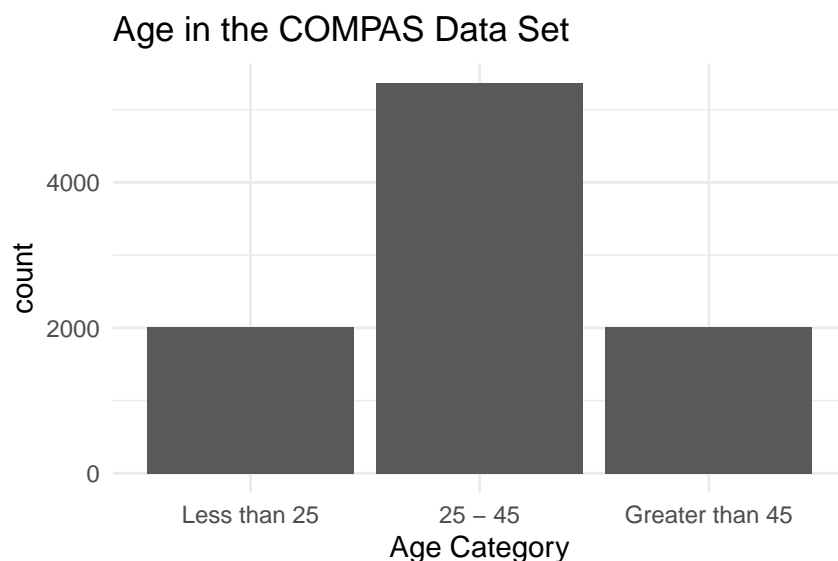
Majority of the defendants are between the age of 25 and 45, with about the same number of defendants less than 25 and greater than 25.

```
tally(clean_compasdata$age_cat)
```

```
## X
##      25 - 45 Greater than 45   Less than 25
##      5366      2012      2009

order <- c("Less than 25", "25 - 45", "Greater than 45")
```

```
ggplot(data = clean_compasdata, mapping = aes(x = age_cat)) +
  geom_bar() +
  theme_minimal() +
  scale_x_discrete(limits = order) +
  labs(x = "Age Category",
       title = "Age in the COMPAS Data Set")
```

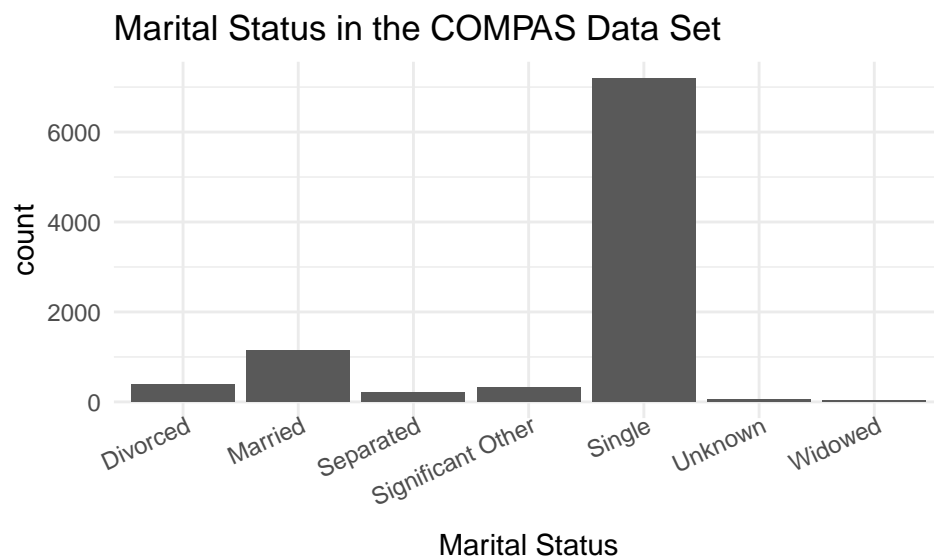


Most of the defendants are single, followed by married.

```
tally(clean_compasdata$marital_status)
```

```
## X
##      Divorced      Married      Separated Significant Other
##          398        1138          219             332
##      Single      Unknown      Widowed
##       7202         58          40
```

```
ggplot(data = clean_compasdata, mapping = aes(x = marital_status)) +
  geom_bar() +
  theme_minimal() +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1)) +
  labs(x = "Marital Status",
       title = "Marital Status in the COMPAS Data Set")
```

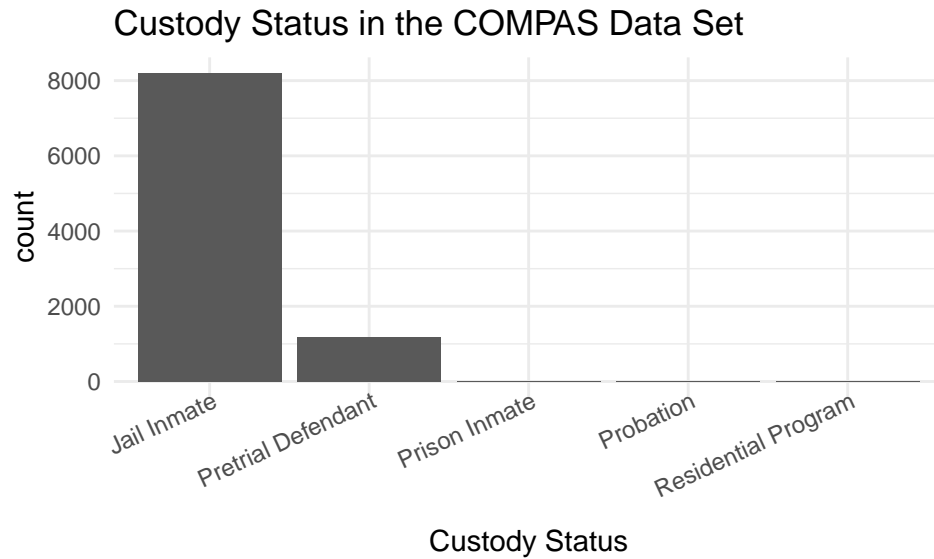


Most of the defendants are jail inmates, with only a handful of prison inmates, probationers, and defendants of the residential program.

```
tally(clean_compasdata$custody_status)
```

```
## X
##      Jail Inmate  Pretrial Defendant  Prison Inmate  Probation
##          8207        1171             4             3
## Residential Program
##              2
```

```
ggplot(data = clean_compasdata, mapping = aes(x = custody_status)) +
  geom_bar() +
  theme_minimal() +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1)) +
  labs(x = "Custody Status",
       title = "Custody Status in the COMPAS Data Set")
```

As a data check, all the assessments are for risk of recidivism.

```
tally(clean_compasdata$type_of_assessment)
```

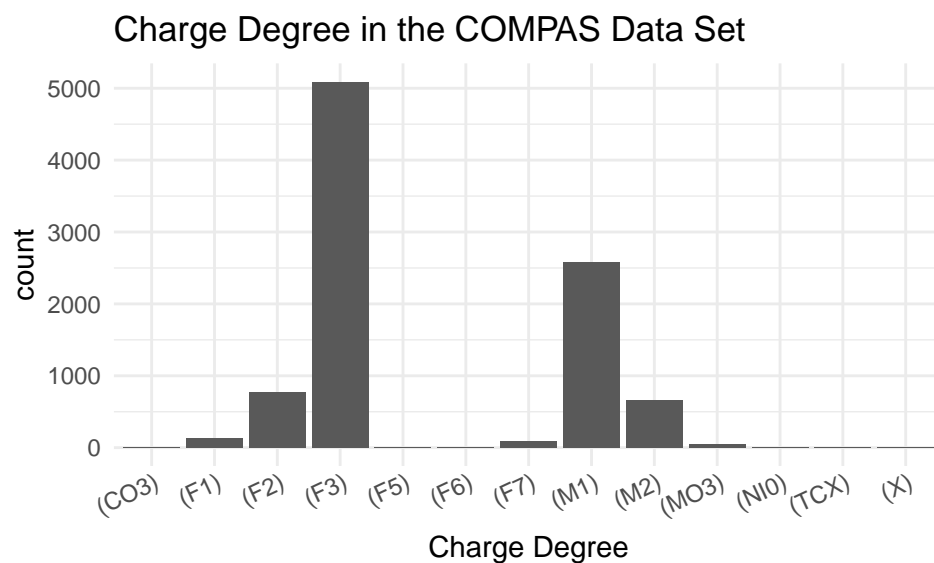
```
## X
## Risk of Recidivism
##          9387
```

There are 13 different charge degrees present in the data set. Most defendants were charged with (F3), which are felonies of the third degree. These are the least serious felonies in Florida and typically include crimes like breaking and entering, collecting and keeping stolen property, fraud, and petty theft. Many other defendants were also charged with (M1), which are a first-degree misdemeanors and can be punished by up to one year in jail. These include simple battery, disorderly conduct, DUI, indecent exposure, marijuana possession, shoplifting, prostitution, and vandalism, among others.

```
tally(clean_compasdata$c_charge_degree)
```

```
## X
## (C03) (F1) (F2) (F3) (F5) (F6) (F7) (M1) (M2) (M03) (N10) (TCX) (X)
##      1  129  774 5091      5    3   85 2584  658   51    4    1    1
```

```
ggplot(data = clean_compasdata, mapping = aes(x = c_charge_degree)) +
  geom_bar() +
  theme_minimal() +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1)) +
  labs(x = "Charge Degree",
       title = "Charge Degree in the COMPAS Data Set")
```

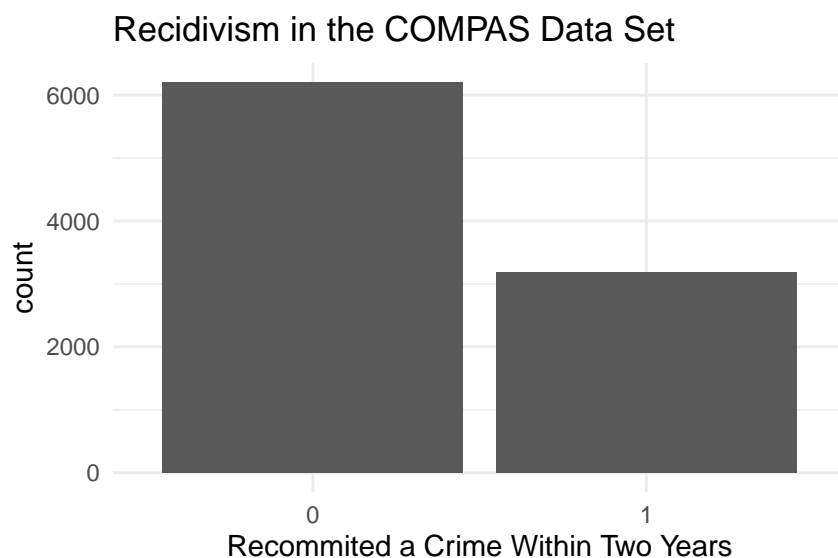


About two-thirds of the defendants did not recommit a crime within two years, while one-thirds did. This is our response variable and is indicative of class imbalance, which can affect the performance of machine learning classification algorithms. This is important to keep in mind when assessing model performance later on.

```
tally(clean_compasdata$is_recid)
```

```
## X
##   0   1
## 6199 3188
```

```
ggplot(data = clean_compasdata, mapping = aes(x = as.factor(is_recid))) +
  geom_bar() +
  theme_minimal() +
  labs(x = "Recommitted a Crime Within Two Years",
       title = "Recidivism in the COMPAS Data Set")
```



Only 745 defendants recommitted a violent crime.

```
tally(clean_compasdata$is_violent_recid)
```

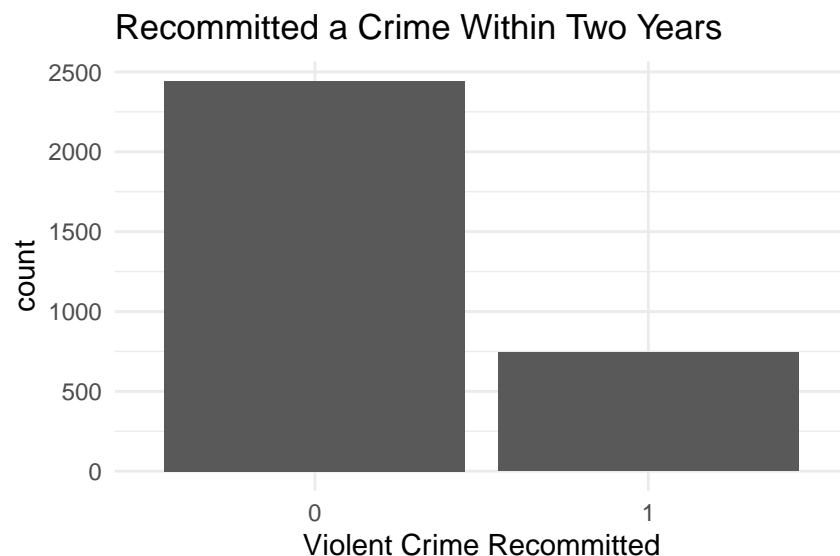
```
## X
##   0    1
## 8642  745
```

Out of the 3188 who recommitted a crime, 2443 re-committed a non-violent crime,

```
tally(clean_compasdata[clean_compasdata$is_recid == 1, ]$is_violent_recid,
      margins = TRUE)
```

```
## X
##   0    1 Total
## 2443  745 3188
```

```
ggplot(data = clean_compasdata[clean_compasdata$is_recid == 1, ],
       mapping = aes(x = as.factor(is_violent_recid))) +
  geom_bar() +
  theme_minimal() +
  labs(x = "Violent Crime Recommited",
       title = "Recommitted a Crime Within Two Years")
```



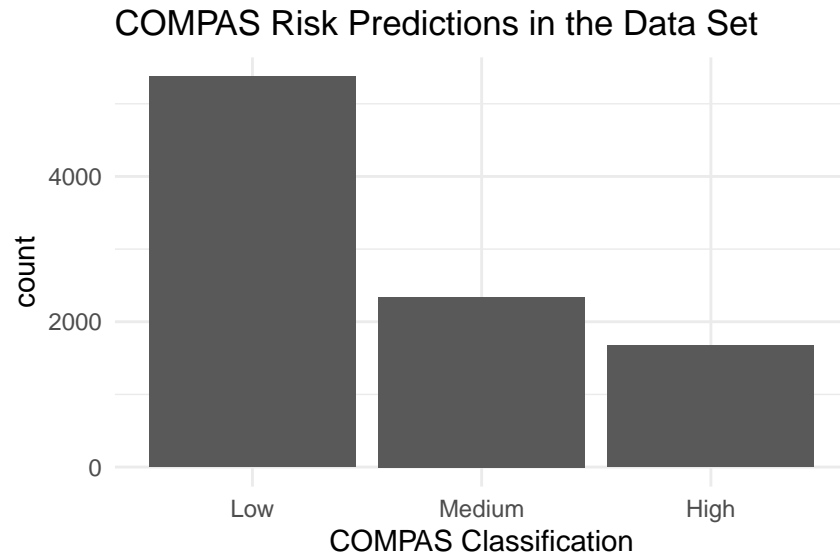
Finally, the COMPAS tool classified more than half of the defendants as low risk. In particular, 5370 were classified as low risk and 1677 as high risk, with the remaining 2340 as medium risk. This is expected since most of the defendants did not recommit a crime within the two year time window.

```
tally(clean_compasdata$score_text)
```

```
## X
##   High   Low Medium
##   1677  5370  2340
```

```
order <- c("Low", "Medium", "High")

ggplot(data = clean_compasdata, mapping = aes(x = score_text)) +
  geom_bar() +
  theme_minimal() +
  scale_x_discrete(limits = order) +
  labs(x = "COMPAS Classification",
       title = "COMPAS Risk Predictions in the Data Set")
```



This wraps up our univariate analysis of the categorical variables. Next, let's examine the univariate distribution of the continuous variables.

Continuous Variables

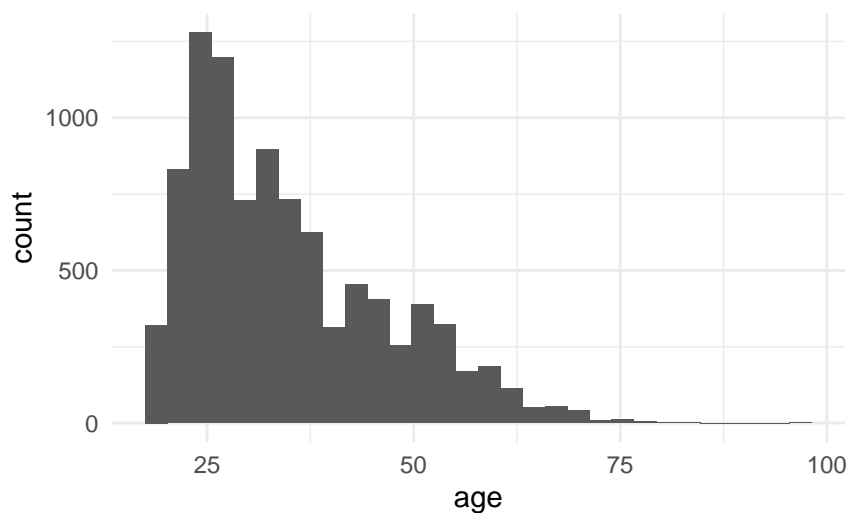
The age of the defendants ranges from 18 to 96 with a mean of 34 and a median of 32. There is no missing data. There's a right-skew in the distribution because of the few really old defendants.

```
favstats(clean_compasdata$age)
```

```
##  min Q1 median Q3 max    mean    sd    n missing
##   18  25     32  42  96 34.75413 11.80854 9387      0
```

```
ggplot(data = clean_compasdata, mapping = aes(x = age)) +
  geom_histogram() +
  theme_minimal() +
  labs(title = "Age in the COMPAS Data Set")
```

Age in the COMPAS Data Set



Most of the defendants had no juvenile felony accounts. The maximum juvenile felony count is 20. There is not enough variation in this variable.

```
favstats(clean_compasdata$juv_fel_count)
```

```
##  min Q1 median Q3 max      mean      sd    n missing
##    0  0      0  0  20 0.05837861 0.4518127 9387      0
```

Similarly, most defendants had no juvenile misdemeanor counts, which are less serious crimes than felonies. The maximum was 13, but there is not enough variation in this variable.

```
favstats(clean_compasdata$juv_misd_count)
```

```
##  min Q1 median Q3 max      mean      sd    n missing
##    0  0      0  0  13 0.0787259 0.4640061 9387      0
```

Similarly, most defendants had no other juvenile counts, excluding misdemeanors and felonies. The maximum was 11, but there is not enough variation in this variable.

```
favstats(clean_compasdata$juv_other_count)
```

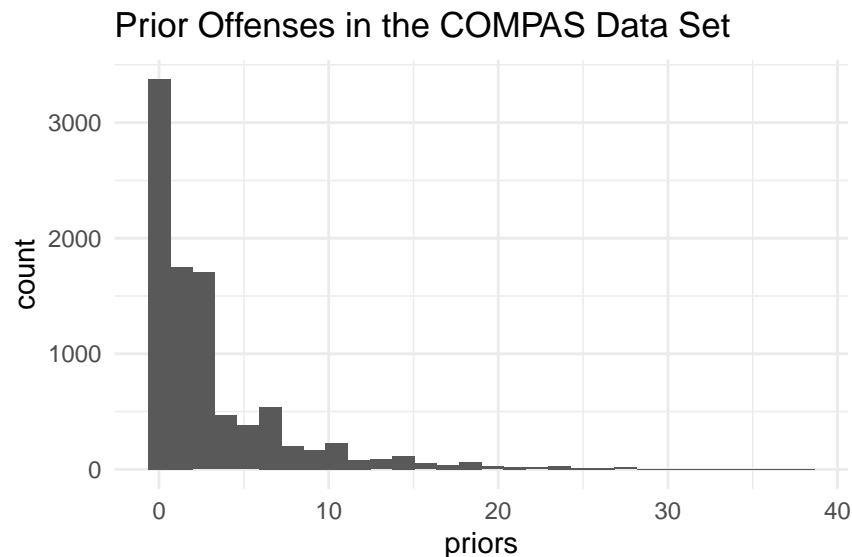
```
##  min Q1 median Q3 max      mean      sd    n missing
##    0  0      0  0  11 0.09917972 0.4683305 9387      0
```

There is slightly more variation in the `priors_count` variable which records the number of non-juvenile prior offenses for each defendant. It ranges from 0 to 38, with a median of 1 and a mean of 3.02, indicating a right skew as visualized in the histogram below. There is no missing data and the standard deviation is 4.586, suggesting that this may be a more informative variable when modeling.

```
favstats(clean_compasdata$priors_count)
```

```
## min Q1 median Q3 max      mean      sd    n missing
##   0  0       1  4  38 3.023863 4.586441 9387      0
```

```
ggplot(data = clean_compasdata, mapping = aes(x = priors_count)) +
  geom_histogram() +
  theme_minimal() +
  labs(x = "priors",
       title = "Prior Offenses in the COMPAS Data Set")
```



The `days_b_screening_arrest` variable indicates how many days passed between arrest and COMPAS screening. It may not be indicative of recidivism, however. We will evaluate this when performing bivariate analysis.

```
favstats(clean_compasdata$days_b_screening_arrest)
```

```
## min Q1 median Q3 max      mean      sd    n missing
##   0  1       1  1  30 2.140194 4.89312 9387      0
```

The interpretation of this variable is not clear – it seems to indicate the number of days since COMPAS screening to date. We will not include this in the analysis.

```
favstats(clean_compasdata$c_days_from_compas)
```

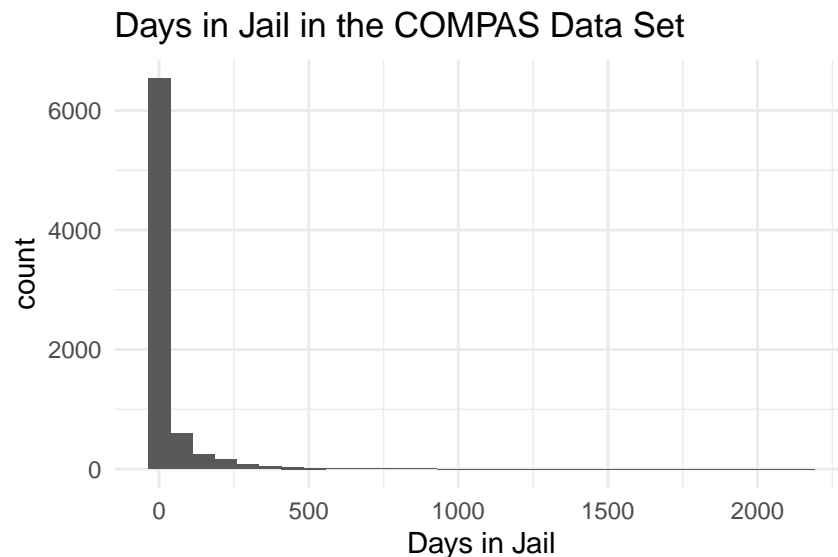
```
## min Q1 median Q3 max      mean      sd    n missing
##   0  1       1  1 9485 24.92436 263.4065 9387      0
```

Considering only the observations for which we have data, the number of days spent in jail ranges from 0 to 2154 days (5.9 years), with a median of 2 days and a mean of 29 days. This variable is extremely right skewed, as visualized in the histogram. The standard deviation is also 82.9, indicating a lot of variation that may potentially be useful for predicting the risk of recidivism.

```
favstats(clean_compasdata$days_in_jail)
```

```
## min Q1 median Q3 max mean sd n missing  
## 0 1 2 13 2154 28.96933 82.8563 7727 1660
```

```
ggplot(data = clean_compasdata, mapping = aes(x = days_in_jail)) +  
  geom_histogram() +  
  theme_minimal() +  
  labs(x = "Days in Jail",  
       title = "Days in Jail in the COMPAS Data Set")
```



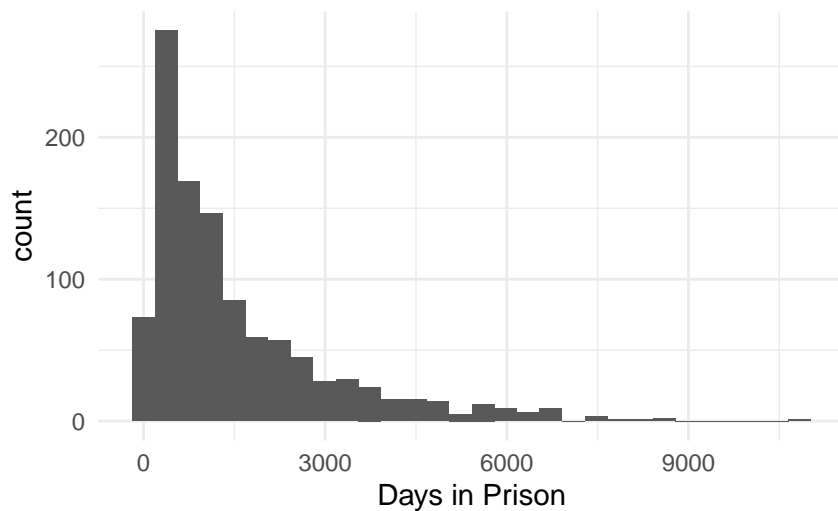
Considering only the observations for which we have data, the number of days spent in prison ranges from 0 to 10840 days (29.6 years), with a median of 1005 days (2.8 years) and a mean of 1534 days (4.2 years). This variable is quite right skewed, as visualized in the histogram. The standard deviation is also 1554.728, indicating a lot of variation that may potentially be useful for predicting the risk of recidivism.

```
favstats(clean_compasdata$days_in_prison)
```

```
## min Q1 median Q3 max mean sd n missing  
## 0 445.5 1005 2102.5 10840 1534.246 1554.728 1083 8304
```

```
ggplot(data = clean_compasdata, mapping = aes(x = days_in_prison)) +  
  geom_histogram() +  
  theme_minimal() +  
  labs(x = "Days in Prison",  
       title = "Days in Prison in the COMPAS Data Set")
```

Days in Prison in the COMPAS Data Set



Notice, however, that there is a lot of missing data for the `days_in_jail` and `days_in_prison` variables, with the former having 1660 missing observations and the latter having 8304 missing observations. Let's sum both columns up and create a new variable, `days_in_jail_or_prison`, to assess the impact on the amount of missing observations.

```
clean_compasdata <- clean_compasdata %>%
  rowwise() %>%
  mutate(days_in_jail_or_prison = sum(days_in_jail, days_in_prison, na.rm=TRUE)) %>%
  ungroup()
```

There are 1732 defendants with either no jail or prison history, or that spent less than half a day in jail or prison.

```
count(clean_compasdata$days_in_jail_or_prison == 0)
```

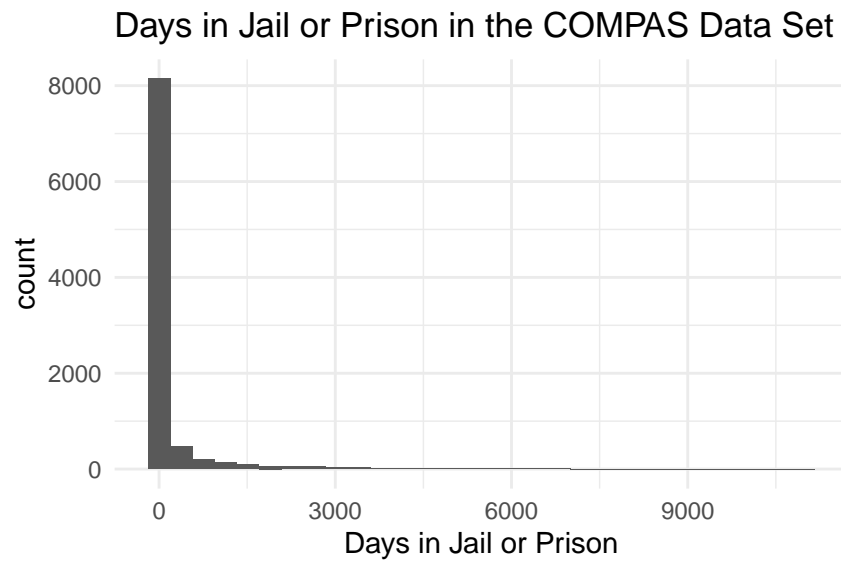
```
## n_TRUE
##    1732
```

The mean of this variable is now 200 days, with a median of 1 day, indicating an extreme right skew. There is no missing data, however.

```
favstats(clean_compasdata$days_in_jail_or_prison)
```

```
## min Q1 median Q3 max mean sd n missing
##    0  1      1 19 10973 200.8559 739.5814 9387 0
```

```
ggplot(data = clean_compasdata, mapping = aes(x = days_in_jail_or_prison)) +
  geom_histogram() +
  theme_minimal() +
  labs(x = "Days in Jail or Prison",
       title = "Days in Jail or Prison in the COMPAS Data Set")
```

The number of crimes recommitted by the defendants who re-committed a crime within two years ranges from 1 to 55, with a median of 1 and a mean of 1.73.

```
favstats(clean_compasdata$num_r_cases)
```

```
##   min  Q1 median  Q3 max    mean    sd    n missing
##    1   1     1   2  55  1.736512 1.629916 3188     6199
```

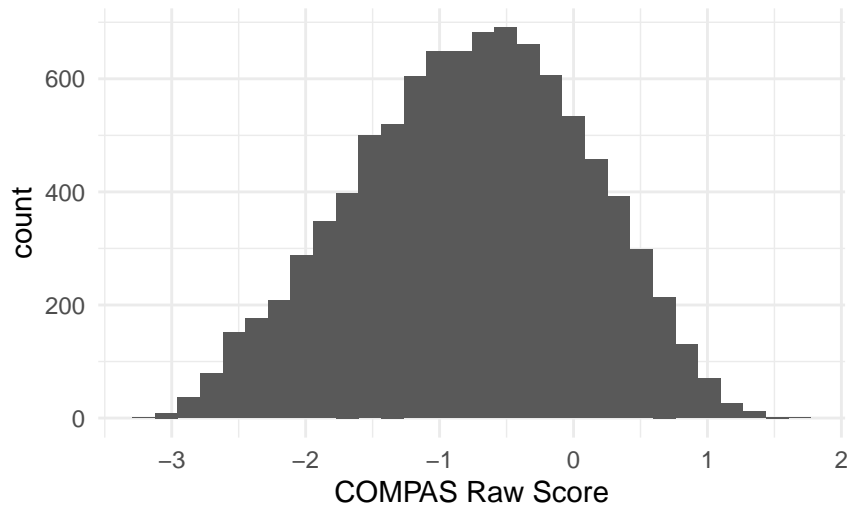
Finally, the COMPAS tool outputs a raw score for each defendant. The raw score ranges from -3.21 to 1.69 with a median of -0.74 and a mean of -0.78. The distribution of the raw scores is visualized on the histogram below. The distribution is unimodal and symmetric with a slight left skew.

```
favstats(clean_compasdata$raw_score)
```

```
##   min    Q1 median    Q3 max    mean    sd    n missing
## -3.21 -1.38 -0.74 -0.15 1.69 -0.7759146 0.8573394 9387      0
```

```
ggplot(data = clean_compasdata, mapping = aes(x = raw_score)) +
  geom_histogram() +
  theme_minimal() +
  labs(x = "COMPAS Raw Score",
       title = "Raw Scores in the COMPAS Data Set")
```

Raw Scores in the COMPAS Data Set



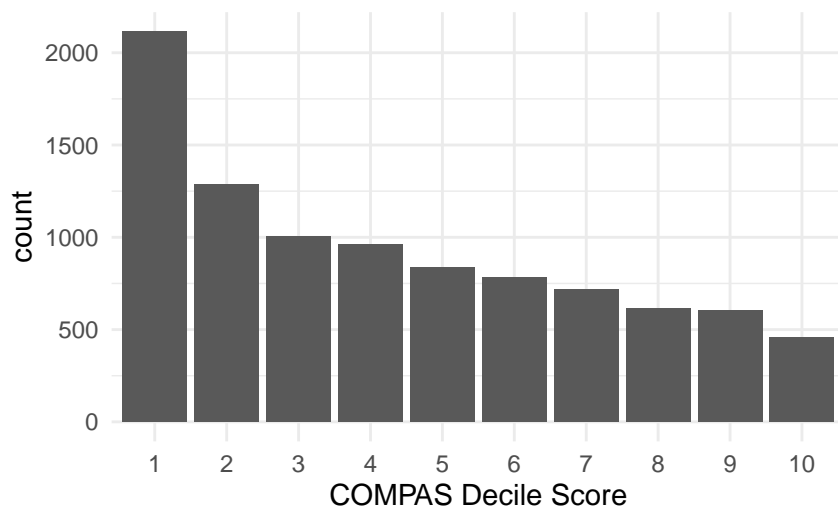
The raw scores are then converted into decile scores that determine the predicted risk of recidivism. The decile scores range from 1 to 10 with a median of 4 and a mean of 4.3. The histogram displays the distribution of the decile scores – it makes me wonder how, or whether, the decile scores are computed from the raw scores.

```
favstats(clean_compasdata$decile_score)
```

```
## min Q1 median Q3 max      mean      sd    n missing
##   1  2      4  7  10 4.305849 2.849011 9387      0
```

```
ggplot(data = clean_compasdata, mapping = aes(x = as.factor(decile_score))) +
  geom_bar() +
  theme_minimal() +
  labs(x = "COMPAS Decile Score",
       title = "Decile Scores in the COMPAS Data Set")
```

Decile Scores in the COMPAS Data Set



There is significant overlap between the decile scores and the raw scores. It's unclear how exactly these scores were mapped. However, because the decile score is what is handed to judges at court and what determines the risk of recidivism, we will proceed with that variable.

```
favstats(clean_compasdata$raw_score ~ clean_compasdata$decile_score)
```

```
##      clean_compasdata$decile_score  min    Q1 median    Q3    max      mean
## 1          1 -3.21 -2.21  -1.89 -1.6500 -1.39 -1.95135289
## 2          2 -1.65 -1.35  -1.23 -1.1100 -1.01 -1.24964286
## 3          3 -1.30 -1.00  -0.91 -0.8300 -0.75 -0.94058765
## 4          4 -1.02 -0.74  -0.66 -0.5800 -0.40 -0.69193983
## 5          5 -0.81 -0.51  -0.44 -0.3800 -0.32 -0.48439521
## 6          6 -0.58 -0.31  -0.25 -0.1900 -0.02 -0.28100637
## 7          7 -0.36 -0.11  -0.05  0.0125  0.19 -0.06243056
## 8          8 -0.13  0.11   0.17  0.2400  0.33  0.16462541
## 9          9  0.13  0.35   0.42  0.5200  0.65  0.42686469
## 10         10  0.44  0.68   0.78  0.9200  1.69  0.81579869
##              sd    n missing
## 1  0.38018237 2114         0
## 2  0.16522602 1288         0
## 3  0.14595631 1004         0
## 4  0.13642777  964         0
## 5  0.14094393  835         0
## 6  0.12481877  785         0
## 7  0.10487589  720         0
## 8  0.09722801  614         0
## 9  0.11202009  606         0
## 10 0.19736051  457         0
```

Note that the decile scores are mapped to 'low', 'medium', and 'high' risk as detailed in the table below.

```
clean_compasdata %>%
  dplyr::select(decile_score, score_text) %>%
  filter(score_text != 'N/A') %>%
  rename("Risk" = score_text) %>%
  group_by(Risk) %>%
  summarise("Min" = min(decile_score),
            "Max" = max(decile_score)) %>%
  arrange(Min) %>%
  kable(booktabs = TRUE)
```

Risk	Min	Max
Low	1	4
Medium	5	7
High	8	10

Adding Some New Variables

Based on the univariate analysis in this section, we will create 2 more columns:

- `juv_offense_count`, which is a continuous variable that records how many total prior juvenile offenses a defendant had.

- `juv_offense`, which is a binary variable that records whether or not a defendant had a juvenile offense (0 = 'No'; 1 = 'Yes').

Combining the information from multiple non-informative variables may create more informative variables.

```
clean_compasdata <- clean_compasdata %>%
  mutate(juv_offense_count = juv_fel_count + juv_misd_count + juv_other_count,
         juv_offense = ifelse(juv_offense_count == 0, 0, 1))
```

Let's assess the univariate distribution of these new variables.

`juv_offense_count` variable is still highly invariable, with at least $\frac{3}{4}$ of observations have no juvenile offenses.

```
favstats(clean_compasdata$juv_offense_count)
```

```
##  min Q1 median Q3 max      mean      sd    n missing
##    0  0      0  0  21 0.2362842 0.9082055 9387      0
```

We see the same trends for `juv_offense`, the categorical variable, with only 1133 defendants reporting a juvenile offense.

```
tally(clean_compasdata$juv_offense)
```

```
## X
##   0   1
## 8254 1133
```

We'll keep the continuous variable, which may have slightly more quantifiable information than the binary variable.

This concludes our univariate analysis of the variables in the COMPAS data set. Next, we will look at some of the bivariate relationships.

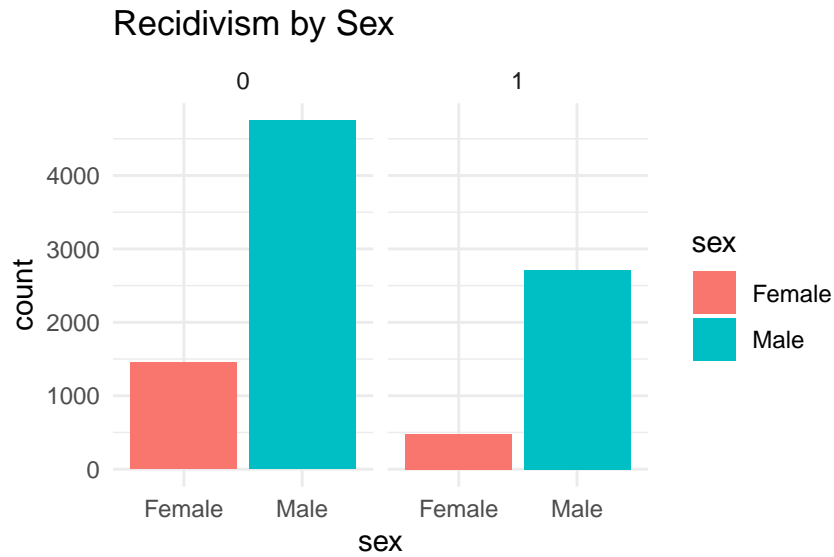
Bivariate Analysis

In this section, we will explore the relationships between our variables and the response variable, `is_recid`, which records whether or not a defendant recommitted a crime within 2 years.

Categorical Variables

It doesn't appear as though there is much evident relationship between sex and recidivism.

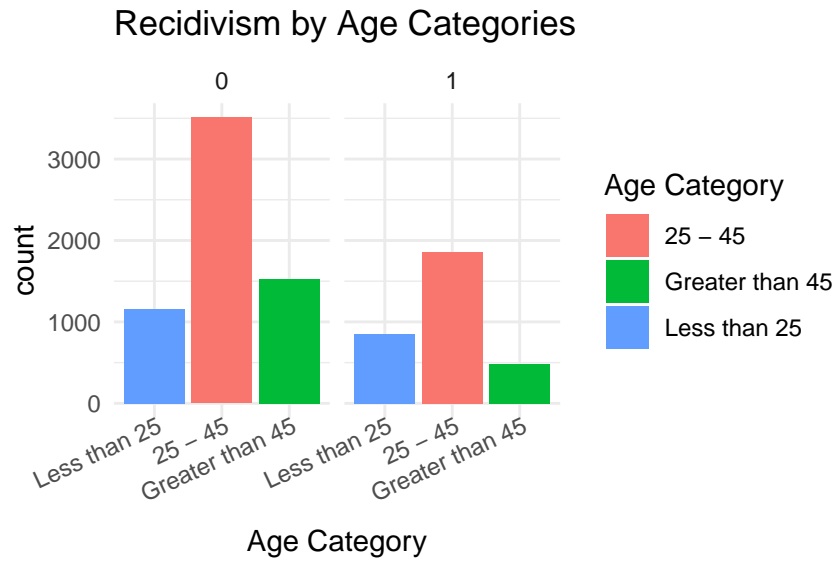
```
ggplot(data = clean_compasdata, mapping = aes(x = sex, fill = sex)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~is_recid) +
  labs(title = "Recidivism by Sex")
```



Among defendants who do not recidivate, there are more defendants that are aged 45 in comparison to those less than 25. However, among those that recidivated, there are more defendants that are less than 25 in comparison to those that are greater than 45. This indicates that age may hold some valuable information regarding a defendant's likelihood of recidivism.

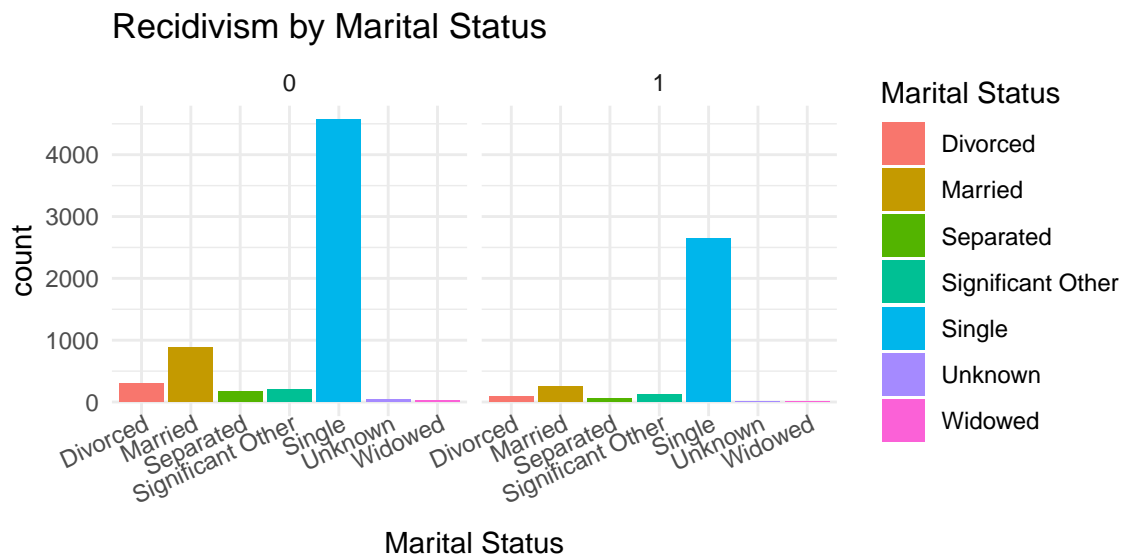
```
order <- c("Less than 25", "25 - 45", "Greater than 45")

ggplot(data = clean_compasdata,
       mapping = aes(x = age_cat, fill = age_cat)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~is_recid) +
  labs(title = "Recidivism by Age Categories",
       x = "Age Category",
       fill = "Age Category") +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1)) +
  scale_x_discrete(limits = order)
```



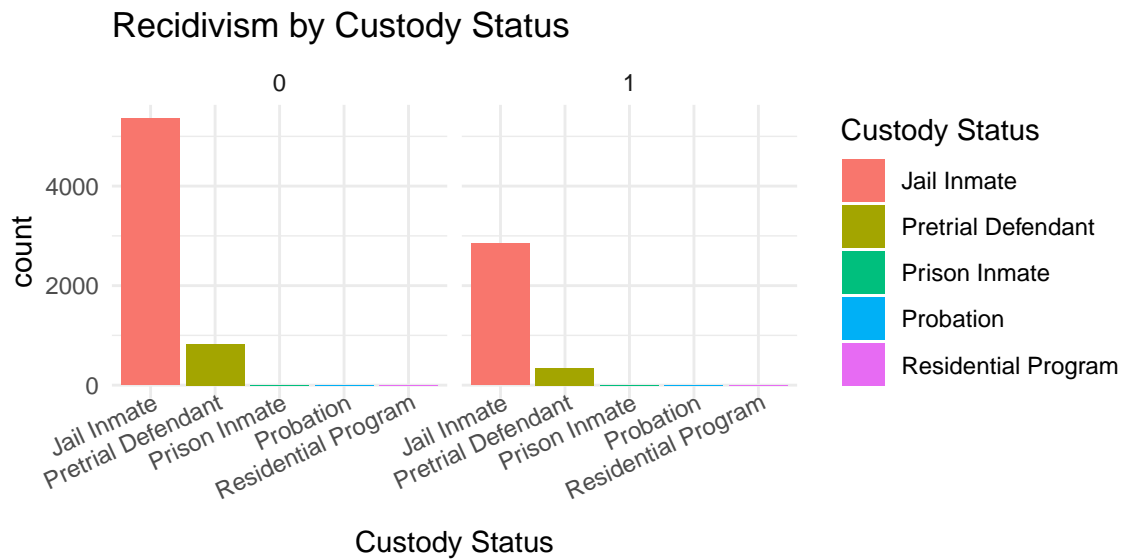
It doesn't appear as though there is much relationship between recidivism and marital status.

```
ggplot(data = clean_compasdata,
       mapping = aes(x = marital_status, fill = marital_status)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~is_recid) +
  labs(title = "Recidivism by Marital Status",
       x = "Marital Status",
       fill = "Marital Status") +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1))
```



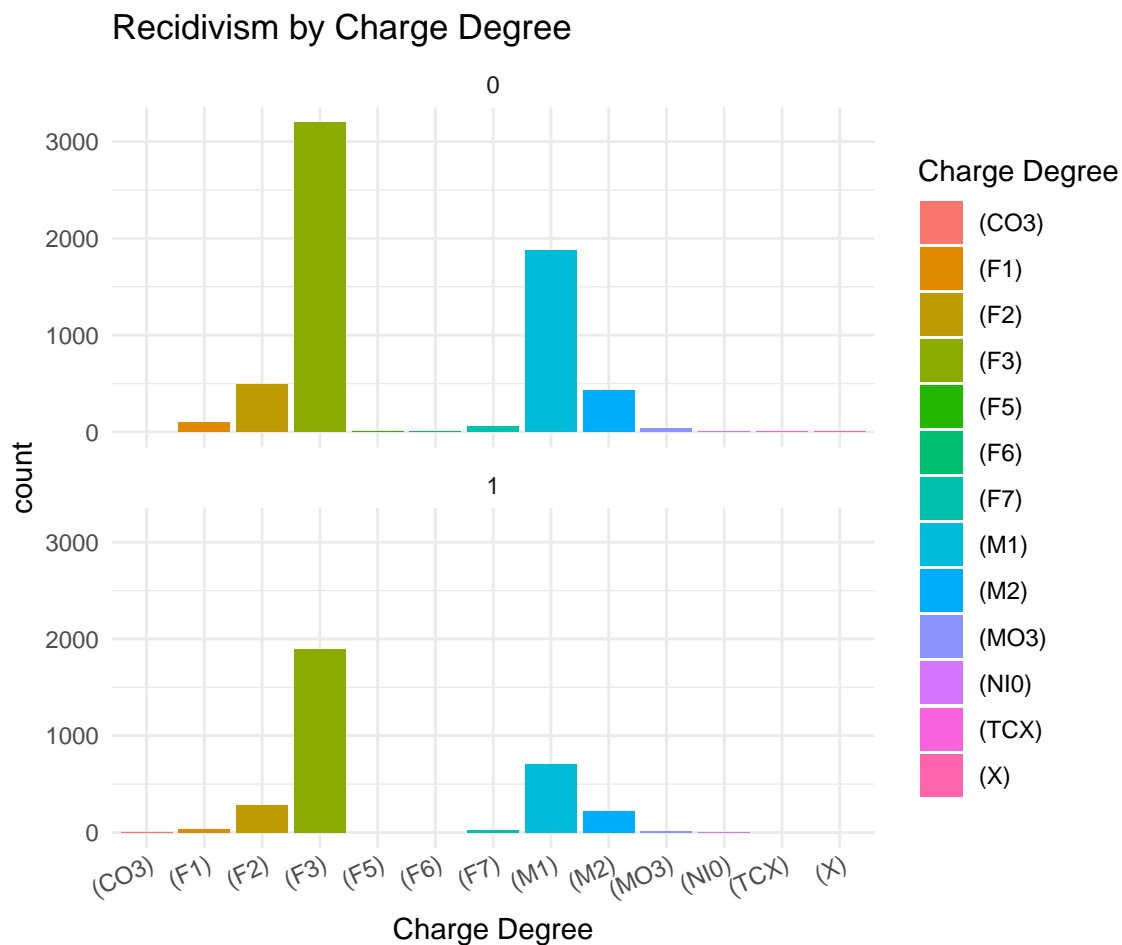
It doesn't appear as though there is much relationship between recidivism and custody status.

```
ggplot(data = clean_compasdata,
       mapping = aes(x = custody_status, fill = custody_status)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~is_recid) +
  labs(title = "Recidivism by Custody Status",
       x = "Custody Status",
       fill = "Custody Status") +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1))
```



It doesn't appear as though there is much relationship between recidivism and charge degree.

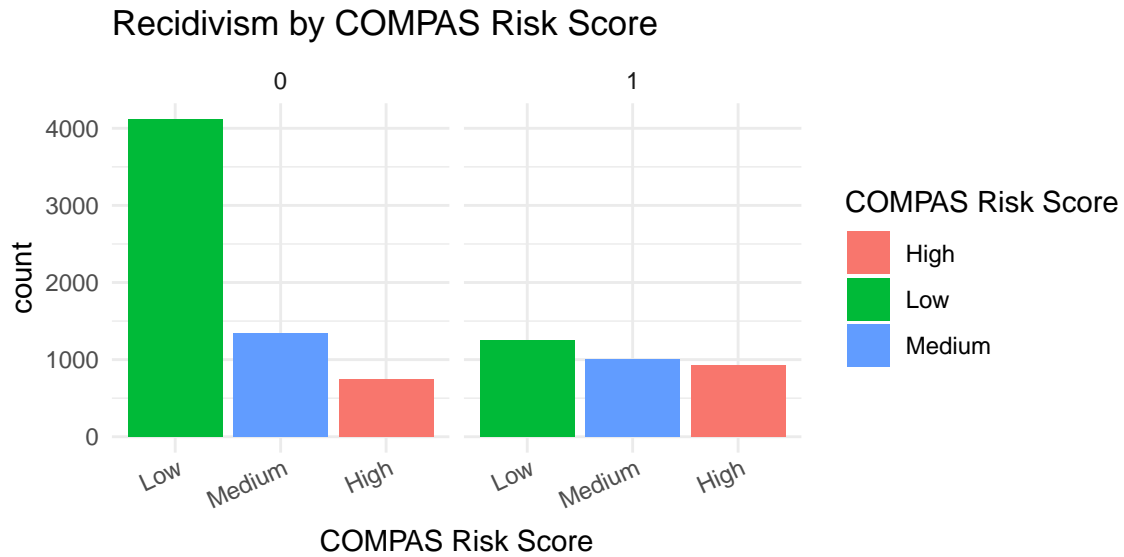
```
ggplot(data = clean_compasdata,
       mapping = aes(x = c_charge_degree, fill = c_charge_degree)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~is_recid, ncol = 1) +
  labs(title = "Recidivism by Charge Degree",
       x = "Charge Degree",
       fill = "Charge Degree") +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1))
```



However, it appears as though the COMPAS tool classifies defendants who recommit a crime as almost as equally risky of recidivism – there is no significant distinction between ‘low’, ‘medium’, and ‘high’ risk for these defendants. For the defendants that don’t recommit a crime, most are predicted as ‘low’ risk, followed by ‘medium’, and then ‘high’ risk. Note, however, that this variable will not be included as a predictor in the model as the purpose of this analysis is to assess COMPAS performance, or more generally, standard ML approaches, in comparison to the Seldonian framework.

```
order <- c("Low", "Medium", "High")

ggplot(data = clean_compasdata,
       mapping = aes(x = score_text, fill = score_text)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~is_recid) +
  labs(title = "Recidivism by COMPAS Risk Score",
       x = "COMPAS Risk Score",
       fill = "COMPAS Risk Score") +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1)) +
  scale_x_discrete(limits = order)
```

Next, let's perform a similar analysis for the continuous variables.

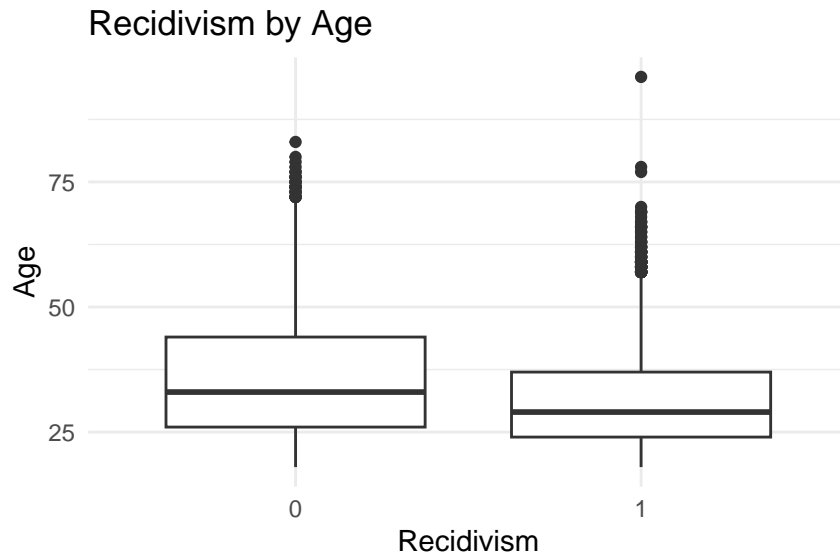
Continuous Variables

There is a difference in the mean and median ages for defendants who recommit a crime within two years versus those who don't. Those who recidivate tend to be younger than those who don't, indicating that this will be a useful variable in the model. This is in line with intuition from society.

```
favstats(data = clean_compasdata, age ~ is_recid)
```

	is_recid	min	Q1	median	Q3	max	mean	sd	n	missing
## 1	0	18	26	33	44	83	36.04646	12.17525	6199	0
## 2	1	18	24	29	37	96	32.24122	10.62147	3188	0

```
ggplot(data = clean_compasdata,
       mapping = aes(x = as.factor(is_recid), y = age)) +
  geom_boxplot() +
  theme_minimal() +
  labs(title = "Recidivism by Age",
       x = "Recidivism",
       y = "Age")
```



There is not much distributional difference in juvenile felony counts for defendants who recidivate versus those who don't.

```
favstats(data = clean_compasdata, juv_fel_count ~ is_recid)
```

##	is_recid	min	Q1	median	Q3	max	mean	sd	n	missing
## 1	0	0	0	0	0	13	0.03645749	0.3297061	6199	0
## 2	1	0	0	0	0	20	0.10100376	0.6221204	3188	0

There is not much distributional difference in juvenile misdemeanor counts for defendants who recidivate versus those who don't.

```
favstats(data = clean_compasdata, juv_misd_count ~ is_recid)
```

##	is_recid	min	Q1	median	Q3	max	mean	sd	n	missing
## 1	0	0	0	0	0	12	0.04387804	0.3356002	6199	0
## 2	1	0	0	0	0	13	0.14648683	0.6388211	3188	0

There is not much distributional difference in juvenile offenses for defendants who recidivate versus those who don't.

```
favstats(data = clean_compasdata, juv_other_count ~ is_recid)
```

##	is_recid	min	Q1	median	Q3	max	mean	sd	n	missing
## 1	0	0	0	0	0	11	0.06355864	0.3966132	6199	0
## 2	1	0	0	0	0	9	0.16844417	0.5768642	3188	0

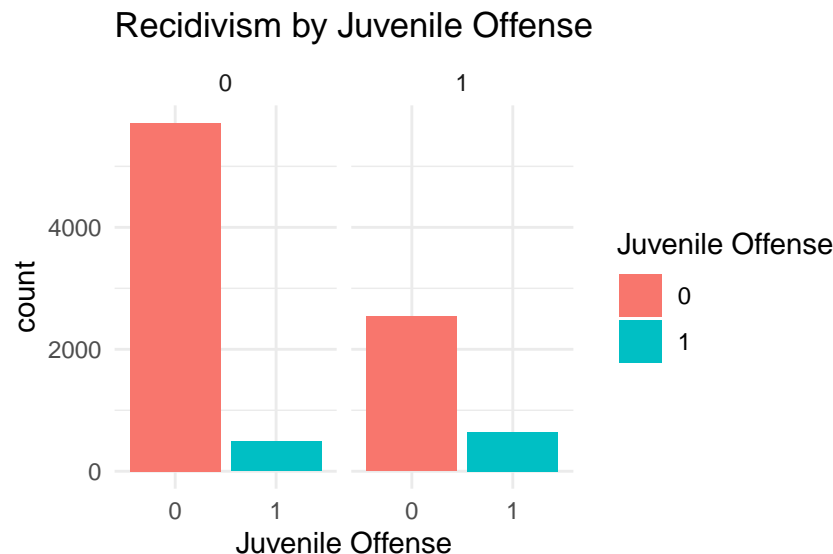
As expected, there is not much distributional difference in the number of juvenile offenses for defendants who do not recidivate versus those who do.

```
favstats(data = clean_compasdata, juv_offense_count ~ is_recid)
```

```
##   is_recid min Q1 median Q3 max      mean      sd    n missing
## 1         0  0  0      0  0  21 0.1438942 0.7044374 6199      0
## 2         1  0  0      0  0  20 0.4159348 1.1896519 3188      0
```

However, the bar plot below reveals that while most defendants don't have juvenile offenses, the proportion of those who don't to those who do is much smaller for defendants that re-offend in comparison to those that don't. This may be a useful variable to include in the model.

```
ggplot(data = clean_compasdata,
       mapping = aes(x = as.factor(juv_offense), fill = as.factor(juv_offense))) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~is_recid) +
  labs(title = "Recidivism by Juvenile Offense",
       x = "Juvenile Offense",
       fill = "Juvenile Offense")
```



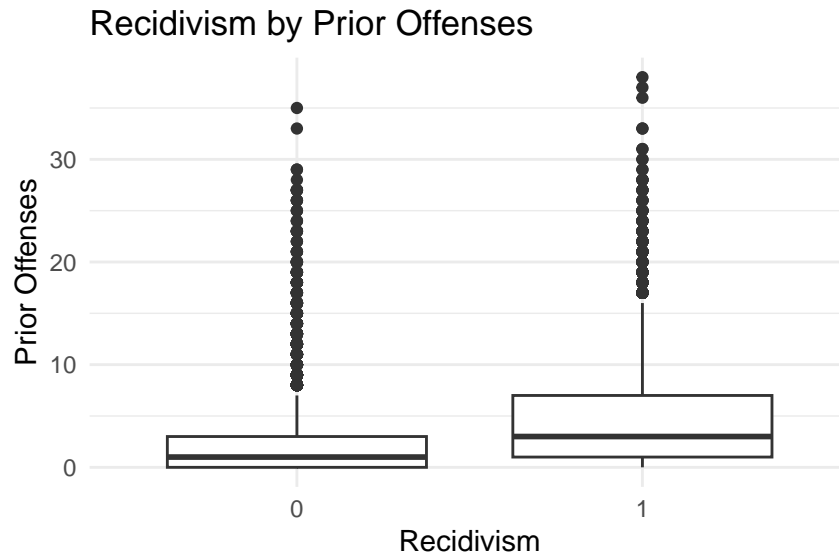
There is some distributional difference in non-juvenile prior offenses for defendants who recidivate versus those who don't, as is indicated by the different means and medians. Those who recommit a crime within two years tend to have more prior offenses. This will be a useful variable to include in the models.

```
favstats(data = clean_compasdata, priors_count ~ is_recid)
```

```
##   is_recid min Q1 median Q3 max      mean      sd    n missing
## 1         0  0  0      1  3  35 2.157283 3.684641 6199      0
## 2         1  0  1      3  7  38 4.708908 5.589893 3188      0
```

```
ggplot(data = clean_compasdata,
       mapping = aes(x = as.factor(is_recid), y = priors_count)) +
  geom_boxplot() +
  theme_minimal() +
```

```
labs(title = "Recidivism by Prior Offenses",
     x = "Recidivism",
     y = "Prior Offenses")
```



There doesn't appear to be any distributional difference in days between COMPAS screening and arrest for defendants who recidivate versus those who don't. This will not be a useful variable for modeling.

```
favstats(data = clean_compasdata, days_b_screening_arrest ~ is_recid)
```

##	is_recid	min	Q1	median	Q3	max	mean	sd	n	missing
## 1	0	0	1	1	1	30	2.149218	4.859912	6199	0
## 2	1	0	1	1	1	30	2.122647	4.957777	3188	0

While the means differ because of the right-skew nature of the data, there doesn't appear to be much distributional difference in days since COMPAS screening for defendants who recidivate versus those who don't. This will not be a useful variable for modeling.

```
favstats(data = clean_compasdata, c_days_from_compas ~ is_recid)
```

##	is_recid	min	Q1	median	Q3	max	mean	sd	n	missing
## 1	0	0	1	1	1	9485	31.21052	305.1847	6199	0
## 2	1	0	1	1	1	5450	12.70107	151.5946	3188	0

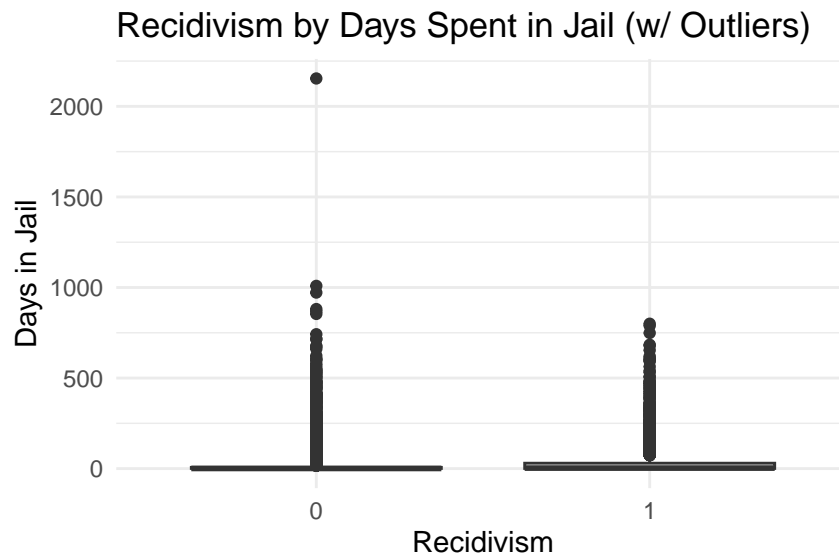
There is an evident difference in the distribution of the number of days spent in jail for participants who recommit a crime within two years versus those who don't. The mean and medians differ, with those who recommit spending more time in jail on average, indicating a distinction that may be useful in modeling. It's hard to visualize the boxplots with all the outliers, so the second boxplot trims the y-axis to better visualize this relationship.

```
favstats(data = clean_compasdata, days_in_jail ~ is_recid)
```

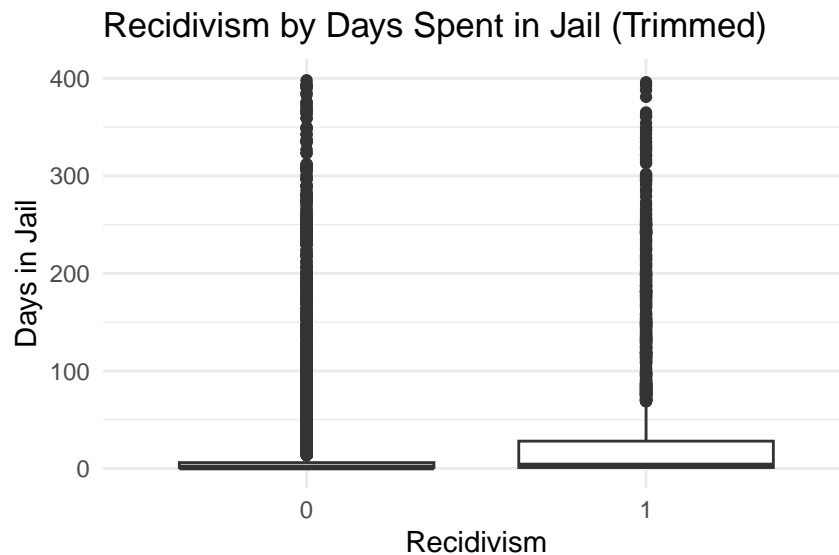
##	is_recid	min	Q1	median	Q3	max	mean	sd	n	missing
----	----------	-----	----	--------	----	-----	------	----	---	---------

```
## 1      0  0  1      1  7 2154 25.52887 83.46318 4988    1211
## 2      1  0  1      3 30  800 35.23476 81.38177 2739    449
```

```
ggplot(data = clean_compasdata,
       mapping = aes(x = as.factor(is_recid), y = days_in_jail)) +
  geom_boxplot() +
  theme_minimal() +
  labs(title = "Recidivism by Days Spent in Jail (w/ Outliers)",
       x = "Recidivism",
       y = "Days in Jail")
```



```
ggplot(data = clean_compasdata,
       mapping = aes(x = as.factor(is_recid), y = days_in_jail)) +
  geom_boxplot() +
  theme_minimal() +
  labs(title = "Recidivism by Days Spent in Jail (Trimmed)",
       x = "Recidivism",
       y = "Days in Jail") +
  ylim(0,400)
```



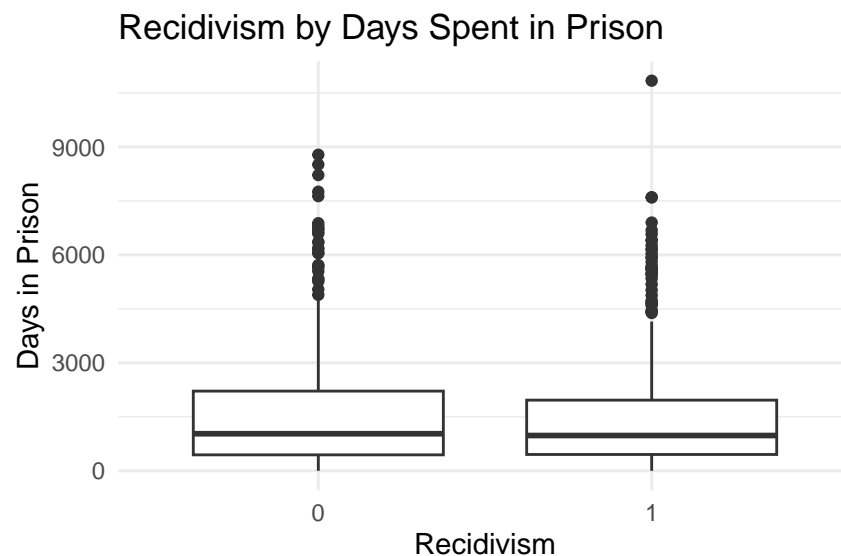
Similarly, there is some distributional difference in the days spent in prison, although in the opposite direction that might be expected and not as extreme as for the days spent in jail. Defendants who don't re-offend spend more days in prison, on average.

The difference between jail and prison is still not clear, however.

```
favstats(data = clean_compasdata, days_in_prison ~ is_recid)
```

```
##   is_recid min      Q1 median      Q3   max      mean      sd   n missing
## 1         0  0 444.00  1031 2216.00  8783 1583.826 1590.026 535    5664
## 2         1  0 454.75   981 1964.75 10840 1485.841 1519.368 548    2640
```

```
ggplot(data = clean_compasdata,
       mapping = aes(x = as.factor(is_recid), y = days_in_prison)) +
  geom_boxplot() +
  theme_minimal() +
  labs(title = "Recidivism by Days Spent in Prison",
       x = "Recidivism",
       y = "Days in Prison")
```



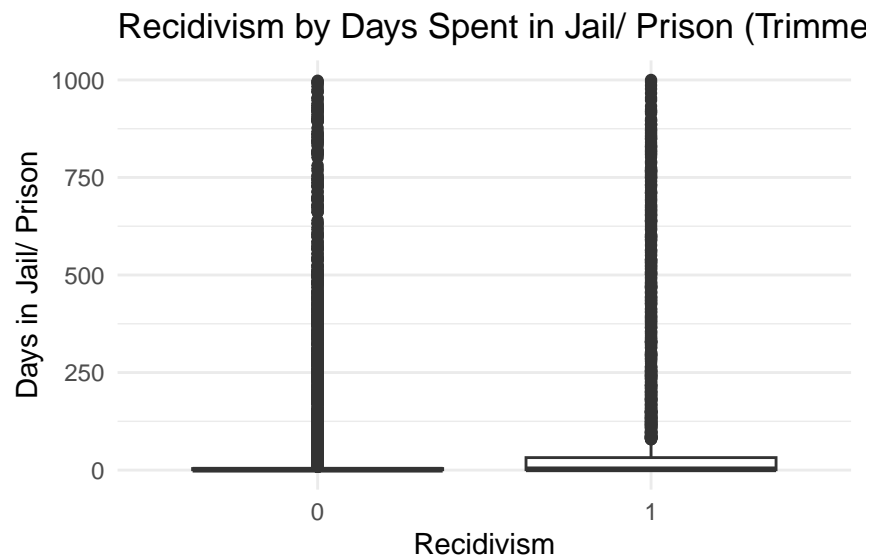
Using the new variable we created, we observe that defendants who reoffend spend, on average, more days in jail or prison. This is a useful variable that may aid our analysis. The boxplot below visualizes the distributional difference, although it is quite difficult to visually assess.

```
favstats(data = clean_compasdata, days_in_jail_or_prison ~ is_recid)
```

```
##   is_recid min Q1 median      Q3   max      mean      sd   n missing
## 1         0  0  1      1  6.00  8956 157.2326 668.0901 6199      0
## 2         1  0  1      3 66.25 10973 285.6804 855.5516 3188      0
```

```
ggplot(data = clean_compasdata,
       mapping = aes(x = as.factor(is_recid), y = days_in_jail_or_prison)) +
  geom_boxplot() +
  theme_minimal() +
```

```
labs(title = "Recidivism by Days Spent in Jail/ Prison (Trimmed)",
     x = "Recidivism",
     y = "Days in Jail/ Prison") +
ylim(0, 1000)
```

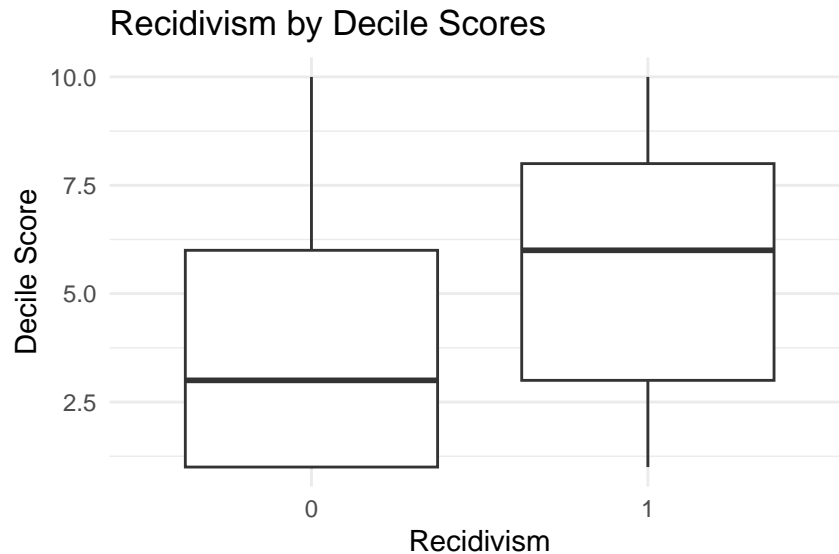


Finally, let's assess the COMPAS decile scores. The median and mean decile scores differ for defendants who recommit a crime within 2 years versus those who don't. The median score for those who don't is 3, which is mapped to low risk. The median score for those who do is 6, which is mapped to medium risk. This indicates that the COMPAS tool has some predictive accuracy. However, the range of scores is the same for both defendants who recidivate versus those who do not, suggesting that the tool is not entirely accurate in its predictions.

```
favstats(data = clean_compasdata, decile_score ~ is_recid)
```

```
##   is_recid min Q1 median Q3 max    mean    sd    n missing
## 1         0  1  1      3  6  10 3.694467 2.667049 6199      0
## 2         1  1  3      6  8  10 5.494668 2.816137 3188      0
```

```
ggplot(data = clean_compasdata,
       mapping = aes(x = as.factor(is_recid), y = decile_score)) +
  geom_boxplot() +
  theme_minimal() +
  labs(title = "Recidivism by Decile Scores",
       x = "Recidivism",
       y = "Decile Score")
```



This wraps up our analysis of the bivariate relationships between the continuous variables in the data set and the response variable: `is_recid`.

Multivariate Analysis

Based on the univariate and bivariate analysis, the 9 most informative predictive variables for modeling will be:

- sex
- age
- age category
- marital status
- custody status
- juvenile offense (binary)
- prior offenses
- charge degree
- days in jail or prison

We will also include `race` in the modeling data set as our demographic variable, though it will not be included in the models themselves. Finally, `is_recid`, the response variable, will also be selected in the data set.

For further analysis, we will also include the COMPAS decile scores to assess which of these variables may have been used to model the COMPAS risk assessment tool.

Now, let's create a new data set with these 12 variables. Below is a glimpse of the data set.

```
compas_final <- clean_compasdata %>%
  dplyr::select(c(race, sex, age, age_cat, marital_status,
                  custody_status, juv_offense, priors_count, c_charge_degree,
                  days_in_jail_or_prison, decile_score, is_recid))

glimpse(compas_final)

## Rows: 9,387
## Columns: 12
## $ race      <chr> "Other", "African-American", "African-American"~
## $ sex       <chr> "Male", "Male", "Male", "Male", "Male", "Male",~
```



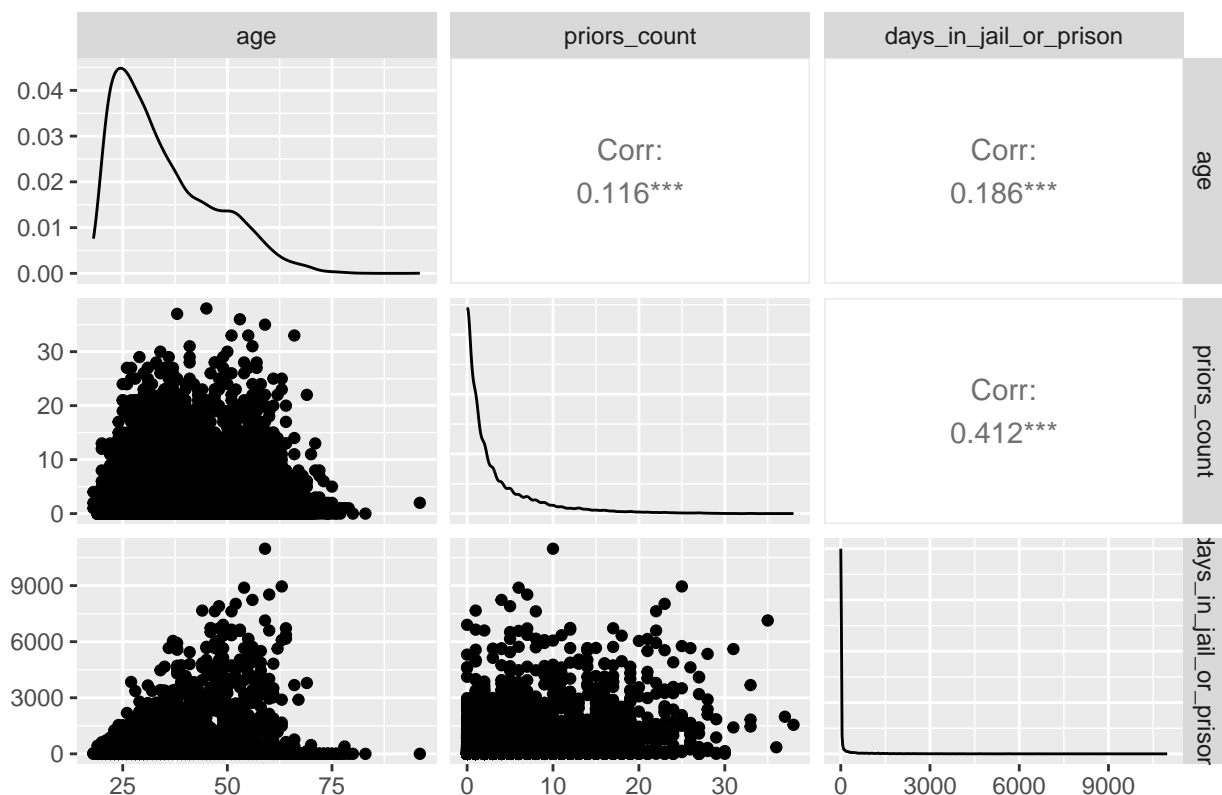
```
## $ age                <int> 69, 34, 24, 44, 41, 43, 39, 20, 26, 27, 23, 37, ~
## $ age_cat            <chr> "Greater than 45", "25 - 45", "Less than 25", "~
## $ marital_status     <chr> "Single", "Single", "Single", "Separated", "Sin~
## $ custody_status     <chr> "Jail Inmate", "Jail Inmate", "Jail Inmate", "J~
## $ juv_offense        <dbl> 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, ~
## $ priors_count       <int> 0, 0, 4, 0, 14, 3, 0, 0, 0, 0, 3, 0, 0, 0, 1, 7~
## $ c_charge_degree    <chr> "(F3)", "(F3)", "(F3)", "(M1)", "(F3)", "(F3)", ~
## $ days_in_jail_or_prison <dbl> 1, 10, 1, 0, 1071, 1, 3, 33, 1, 1, 0, 0, 0, 1, ~
## $ decile_score       <int> 1, 3, 4, 1, 6, 4, 1, 10, 5, 4, 6, 1, 3, 4, 1, 3~
## $ is_recid          <int> 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 1, ~
```

Scatterplot Matrix

First, a scatterplot matrix with just the 3 continuous predictive variables in the final data set, `age`, `prior offenses`, and `days in jail or prison`, will help to elucidate the covariate relationships between the variables. All the variables have moderate to weak correlations, with the strongest correlation of 0.412 being between the number of prior offenses and the number of days spent in jail. All correlations are significant. There are no major concerns for multicollinearity.

```
ggpairs(data = compas_final,
        columns = c("age", "priors_count", "days_in_jail_or_prison"),
        title = "Scatterplot Matrix of the COMPAS Continuous Variables")
```

Scatterplot Matrix of the COMPAS Continuous Variables



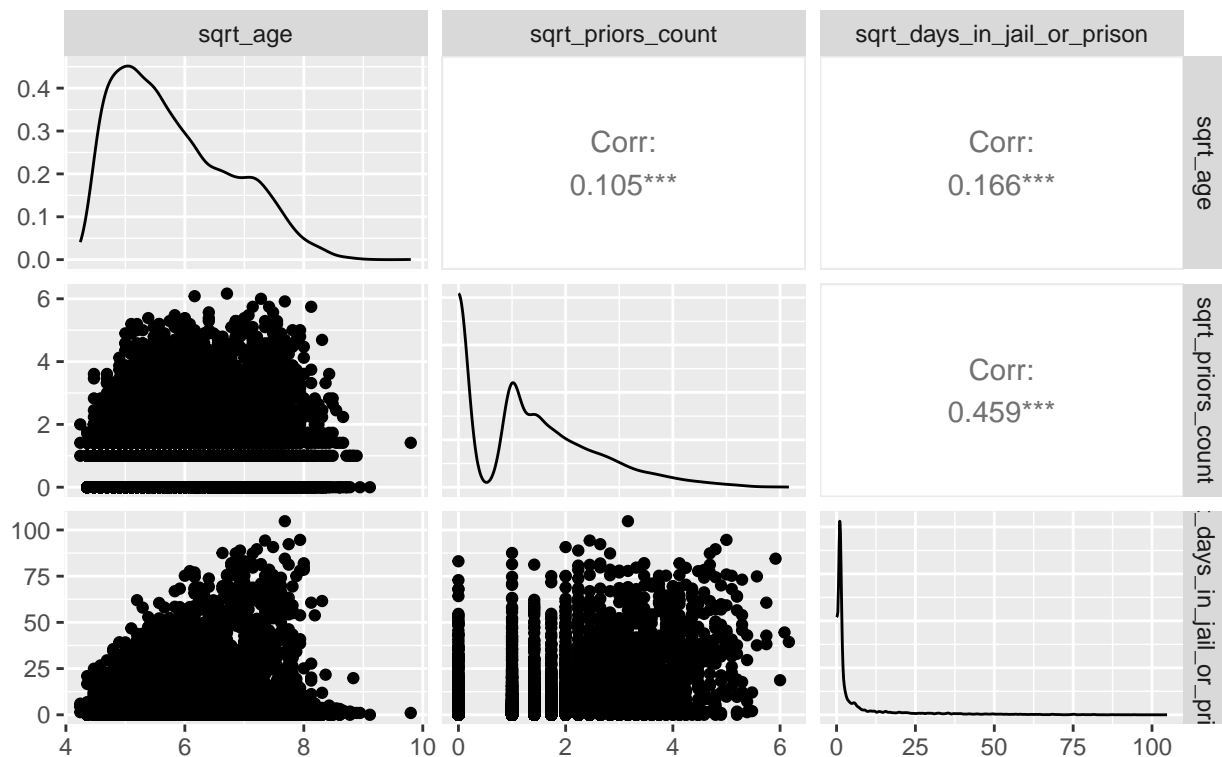
As observed, the variables have a significant right skew and the relationship is non-linear. Let's explore what effect different transformations may have on the covariate relationships. The log transformation resulted in many non-finite values because of the present of zeros, so we will look at a square root transformation instead.

```
compas_final <- compas_final %>%
  mutate(sqrt_age = sqrt(age),
         sqrt_priors_count = sqrt(priors_count),
         sqrt_days_in_jail_or_prison = sqrt(days_in_jail_or_prison))
```

While this transformation strengthened the relationship between the number of prior offenses and the number of days spent in jail or prison ($r = 0.459$), it weakened the other correlations slightly. Next, we'll assess how much this affects the relationship with the COMPAS decile scores.

```
ggpairs(data = compas_final,
       columns = c("sqrt_age", "sqrt_priors_count", "sqrt_days_in_jail_or_prison"),
       title = "Scatterplot Matrix of the COMPAS Continuous Variables  
(Square Root)")
```

Scatterplot Matrix of the COMPAS Continuous Variables
(Square Root)



Pearson's Correlation Matrix

Decile scores has a moderate relationship with age, prior offenses, and number of days spent in jail or prison – this suggests that these variables may indeed be useful for modeling recidivism.

```
mycordata1 <- compas_final %>%
  dplyr::rename("Age" = age,
               "Priors" = priors_count,
               "Days in Jail or Prison" = days_in_jail_or_prison,
```

```

    "Decile Scores" = decile_score) %>%
  dplyr::select("Age", "Priors", "Days in Jail or Prison", "Decile Scores")

cor(mycordata1) %>%
  kable(digits = 2,
        booktabs = TRUE)

```

	Age	Priors	Days in Jail or Prison	Decile Scores
Age	1.00	0.12	0.19	-0.39
Priors	0.12	1.00	0.41	0.45
Days in Jail or Prison	0.19	0.41	1.00	0.26
Decile Scores	-0.39	0.45	0.26	1.00

The square root transformation of the predictor variables actually slightly strengthens the relationship with decile scores – this suggests that the square root transformation of these variables may be better for modeling recidivism.

```

mycordata2 <- compas_final %>%
  dplyr::rename("Square Root Age" = sqrt_age,
               "Priors" = sqrt_priors_count,
               "Days in Jail or Prison" = sqrt_days_in_jail_or_prison,
               "Decile Scores" = decile_score) %>%
  dplyr::select("Square Root Age", "Priors", "Days in Jail or Prison", "Decile Scores")

cor(mycordata2) %>%
  kable(digits = 2,
        booktabs = TRUE)

```

	Square Root Age	Priors	Days in Jail or Prison	Decile Scores
Square Root Age	1.00	0.11	0.17	-0.39
Priors	0.11	1.00	0.46	0.46
Days in Jail or Prison	0.17	0.46	1.00	0.38
Decile Scores	-0.39	0.46	0.38	1.00

Spearman's Correlation Matrix

Spearman's Correlation is better at capturing non-linear relationships. Using Spearman correlations reveals slightly stronger correlations between the variables and the COMPAS decile scores, especially the days spent in jail or prison.

There is no observable difference when calculating Spearman's correlation with the square-root transformed variables versus the original variables.

```

mycordata3 <- compas_final %>%
  dplyr::rename("Age" = age,
               "Priors" = priors_count,
               "Days in Jail or Prison" = days_in_jail_or_prison,
               "Decile Scores" = decile_score) %>%
  dplyr::select("Age", "Priors", "Days in Jail or Prison", "Decile Scores")

cor(mycordata3, method = "spearman") %>%

```

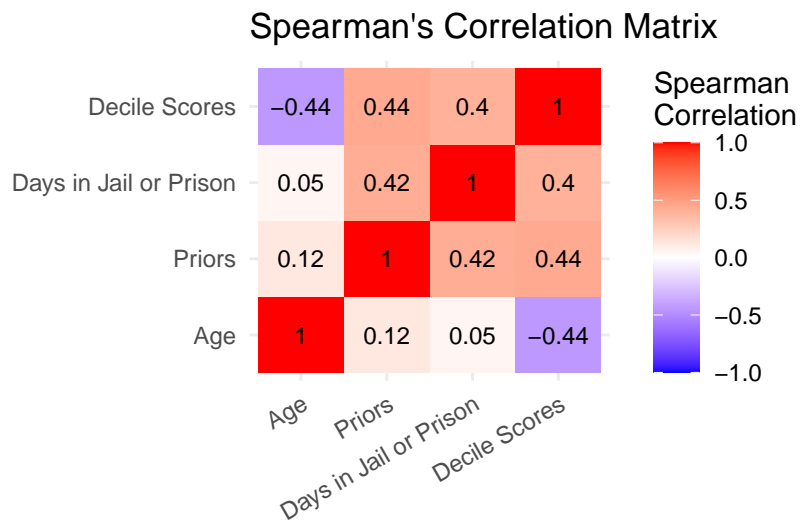
```
kable(digits = 2,
       booktabs = TRUE)
```

	Age	Priors	Days in Jail or Prison	Decile Scores
Age	1.00	0.12	0.05	-0.44
Priors	0.12	1.00	0.42	0.44
Days in Jail or Prison	0.05	0.42	1.00	0.40
Decile Scores	-0.44	0.44	0.40	1.00

Finally, let's visualize these correlations.

```
mycors <- round(cor(mycordata3, method = "spearman"), 2)
mycorplot <- melt(mycors)

ggplot(data = mycorplot, aes(x = Var1, y = Var2, fill = value)) +
  geom_tile() +
  labs(x = "",
       y = "",
       title = "Spearman's Correlation Matrix") +
  scale_fill_gradient2(
    low = "blue",
    high = "red",
    mid = "white",
    midpoint = 0,
    limit = c(-1, 1),
    space = "Lab",
    name = "Spearman\nCorrelation"
  ) +
  geom_text(aes(Var2, Var1, label = value),
            color = "black",
            size = 3) +
  theme_minimal() +
  theme(axis.text.x = element_text(angle = 30, vjust = 1, hjust = 1))
```



Now that we have a thorough understanding of the make-up of the data set, we will perform a demographic analysis next to get a better understanding of the racial discrepancies that may be present before, finally, proceeding with the recidivism risk modeling.

Demographic Group Analysis

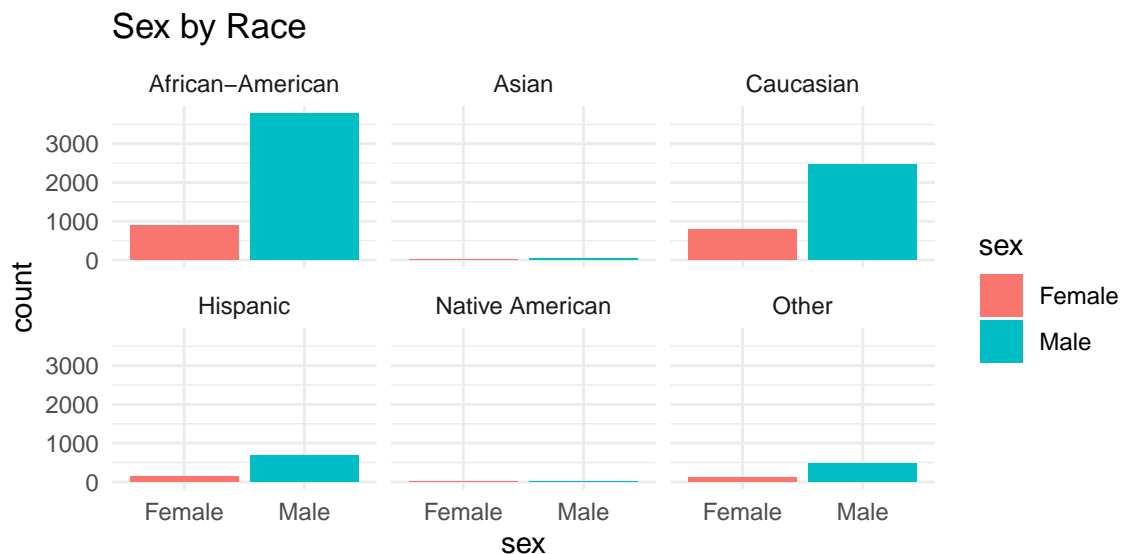
Bivariate Analysis by Race

The demographic variable of interest for this analysis is **race**, and we will employ the Seldonian algorithm in a hope to achieve fairer recidivism risk predictions. With that goal in mind, it's important to perform a demographic group analysis along the defendants' races to better understand any underlying or proxy relationships with the variables.

First, let's analyze the bivariate relationships of some of the most important variables with race.

For all the races, with the exception of native Americans for who there are not many data points available, there are more male defendants than female defendants.

```
ggplot(data = compas_final, mapping = aes(x = sex, fill = sex)) +  
  geom_bar() +  
  theme_minimal() +  
  facet_wrap(~race) +  
  labs(title = "Sex by Race")
```



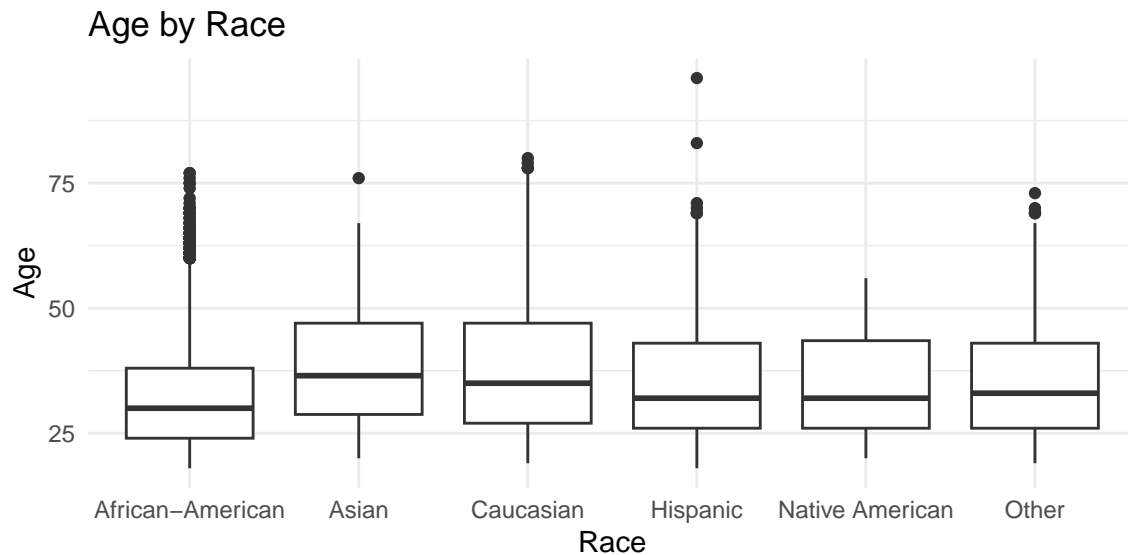
African-American defendants tend to be, on average, the youngest compared to all the other races. Asian defendants, followed by Caucasian defendants, tend to be the oldest. However, there is considerable overlap among all the races, and the relationships is visualized in the boxplot below.

```
favstats(data = compas_final, age ~ race)
```

##	race	min	Q1	median	Q3	max	mean	sd	n	missing
## 1	African-American	18	24.00	30.0	38.0	77	32.60312	10.77213	4674	0
## 2	Asian	20	28.75	36.5	47.0	76	38.20833	12.21607	48	0
## 3	Caucasian	19	27.00	35.0	47.0	80	37.51969	12.60537	3250	0
## 4	Hispanic	18	26.00	32.0	43.0	96	35.22494	11.86236	818	0
## 5	Native American	20	26.00	32.0	43.5	56	34.29630	10.57870	27	0
## 6	Other	19	26.00	33.0	43.0	73	35.67895	11.68420	570	0

```
ggplot(data = compas_final,  
  mapping = aes(x = as.factor(race), y = age)) +  
  geom_boxplot() +
```

```
theme_minimal() +
labs(title = "Age by Race",
     x = "Race",
     y = "Age")
```

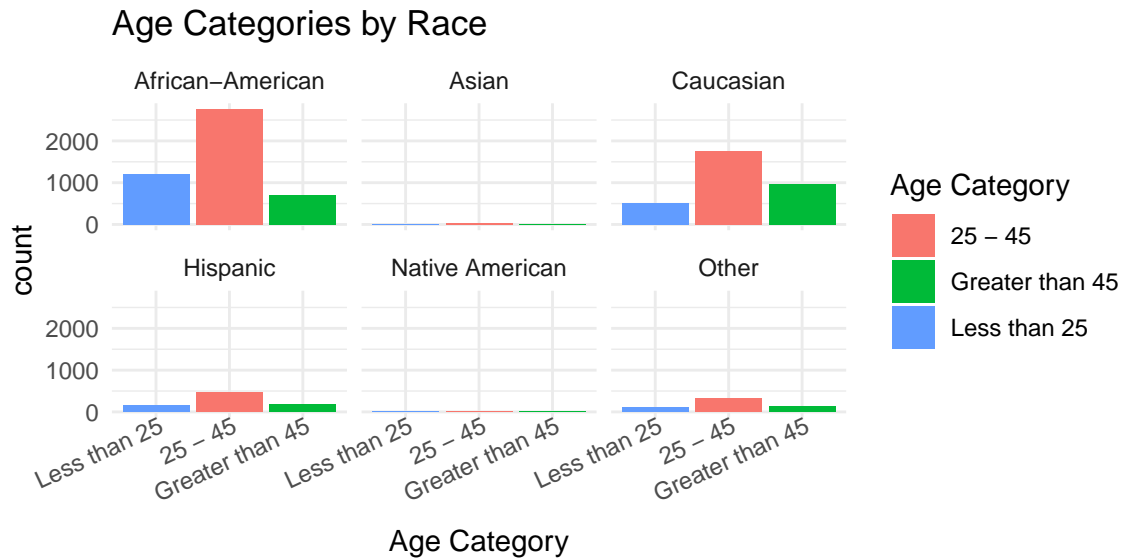


The bar plot below illustrates that for all races, most defendants fall between the ages of 25 and 45. Notice, however, that for African-American defendants, there are more defendants that are less than 25 than those that are greater than 45. The converse is true for Caucasians, with more defendants that are greater than 45 in comparison to those less than 25.

This illustrates that there is some relationship between age and race in this data set, particularly for African-Americans versus Caucasians.

```
order <- c("Less than 25", "25 - 45", "Greater than 45")

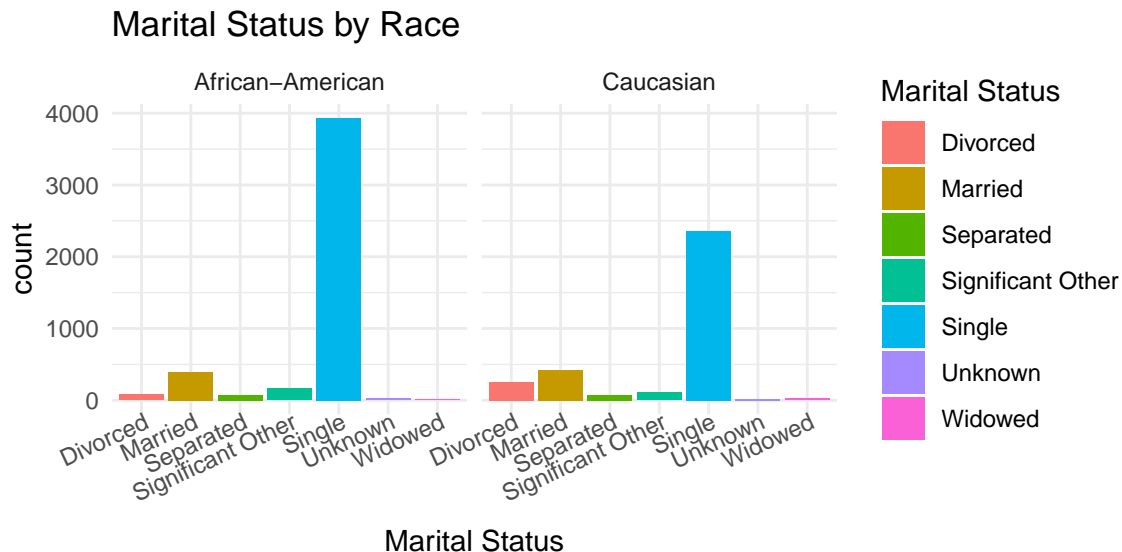
ggplot(data = compas_final,
       mapping = aes(x = age_cat, fill = age_cat)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~race) +
  labs(title = "Age Categories by Race",
       x = "Age Category",
       fill = "Age Category") +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1)) +
  scale_x_discrete(limits = order)
```



For simpler visualization, let's assess the marital status just for Black and White defendants. For both races, most defendants are single. There are no distinct distributional differences.

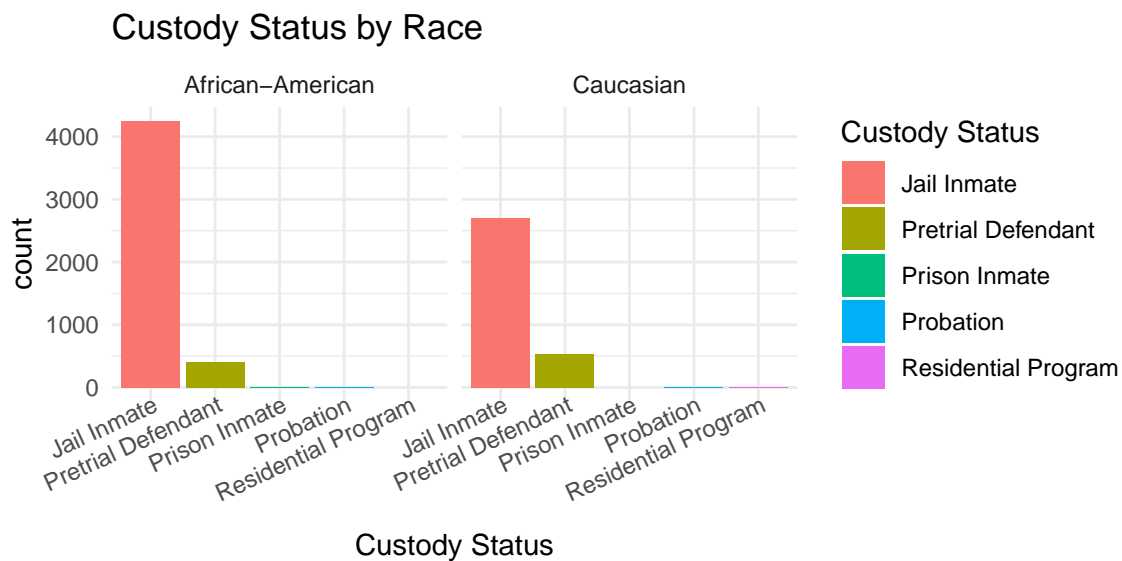
```
compas_final_bw <- compas_final %>%
  filter(race %in% c("African-American", "Caucasian"))

ggplot(data = compas_final_bw,
  mapping = aes(x = marital_status, fill = marital_status)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~race) +
  labs(title = "Marital Status by Race",
    x = "Marital Status",
    fill = "Marital Status") +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1))
```



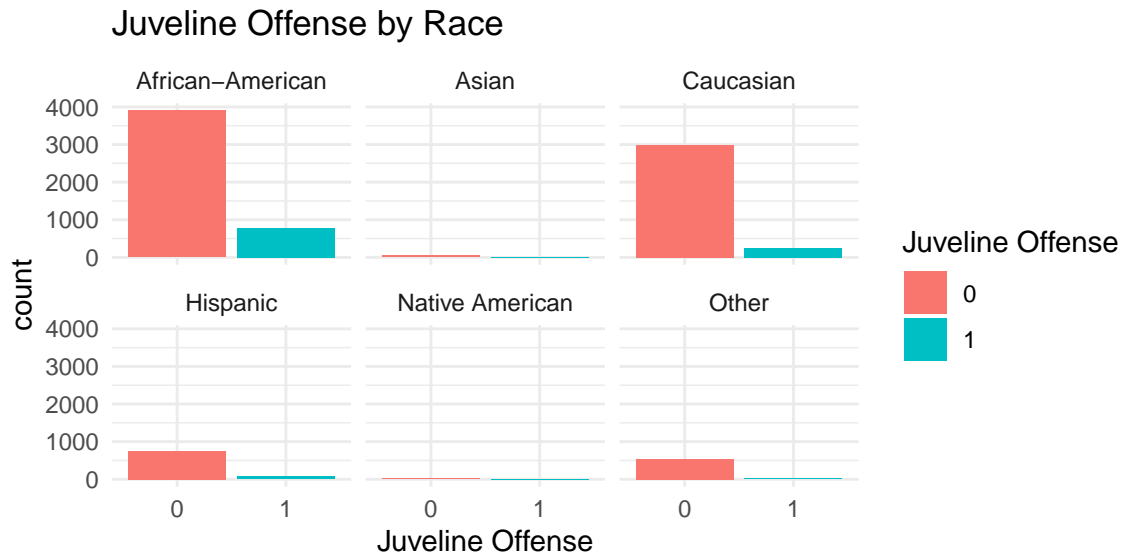
Similarly, there is no observable distribution difference in custody status by race. However, as much as there are less Caucasian defendants overall in comparison to African-American defendants, there are slightly more Caucasian prison defendants.

```
ggplot(data = compas_final_bw,
       mapping = aes(x = custody_status, fill = custody_status)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~race) +
  labs(title = "Custody Status by Race",
       x = "Custody Status",
       fill = "Custody Status") +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1))
```



There does not appear to be much distributional difference in juvenile offense by race.

```
ggplot(data = compas_final,
       mapping = aes(x = as.factor(juv_offense), fill = as.factor(juv_offense))) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~race) +
  labs(title = "Juvenile Offense by Race",
       x = "Juvenile Offense",
       fill = "Juvenile Offense")
```

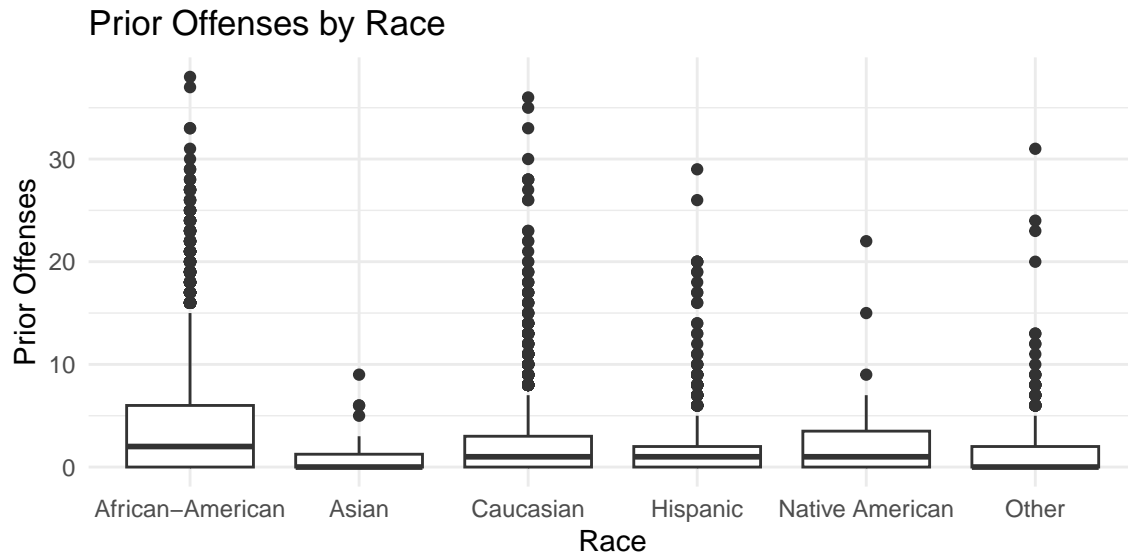


Notably, African-Americans have the most prior offenses, on average, followed by Native Americans. When comparing with Caucasian defendants, African-Americans have almost twice as many prior offenses, suggesting a strong proxy relationship between race and prior offenses. Asian defendants have the least prior offenses. This is an important result and illustrates how a system that pre-disposes certain races to prison can perpetuate that discriminatory trend by using those same variables to predict risk of recommitting another crime. The boxplot helps to visualize this relationship more clearly.

```
favstats(data = compas_final, priors_count ~ race)
```

##	1	2	3	4	5	6
race	African-American	Asian	Caucasian	Hispanic	Native American	Other
min	0	0	0	0	0	0
Q1	0	0	0	0	0	0
median	2	0	1	1	1	0
Q3	6.00	1.25	3.00	2.00	3.50	2.00
max	38	9	36	29	22	31
mean	4.042576	1.083333	2.146462	1.806846	3.185185	1.575439
sd	5.345310	1.888750	3.472545	3.321139	5.076621	2.949861
n	4674	48	3250	818	27	570
missing	0	0	0	0	0	0

```
ggplot(data = compas_final,
  mapping = aes(x = as.factor(race), y = priors_count)) +
  geom_boxplot() +
  theme_minimal() +
  labs(title = "Prior Offenses by Race",
    x = "Race",
    y = "Prior Offenses")
```

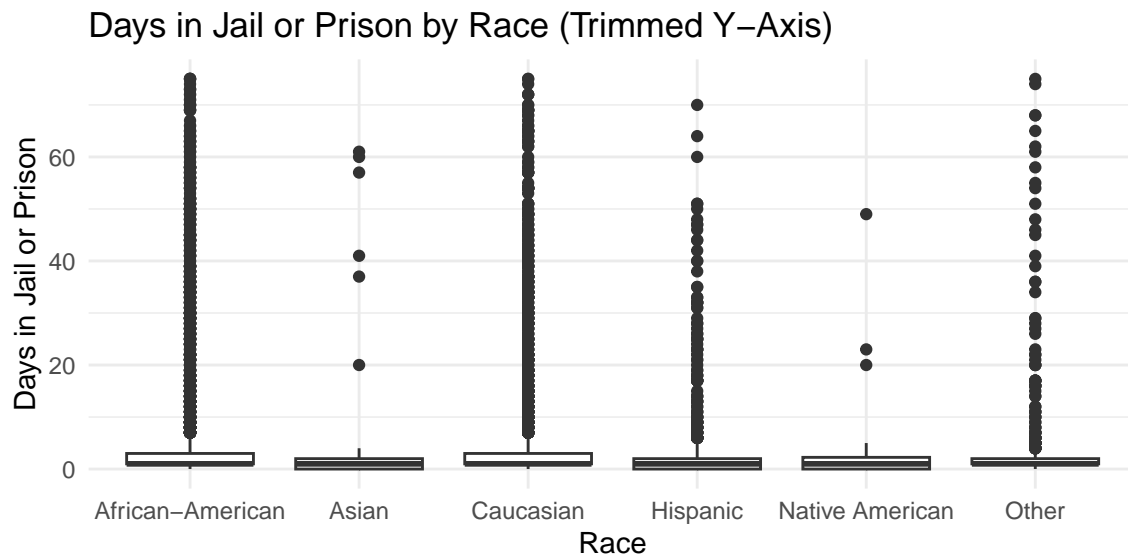


The same trend is observed when observing the difference in the days spent in jail. On average, Native Americans and African-Americans spend the most time in jail or prison. In fact, their average jail/ prison time is more than quadruple and triple, respectively, that of Caucasian defendants. Asian defendants spend the least time on average. When looking at the medians, 50% of the African-American defendants spent 2 days or more days in jail, as compared to only 1 or more days for 50% of the all other defendants. The relationship is hard to visualize on a boxplot because of the presence of many outlying observations.

```
favstats(data = compas_final, days_in_jail_or_prison ~ race)
```

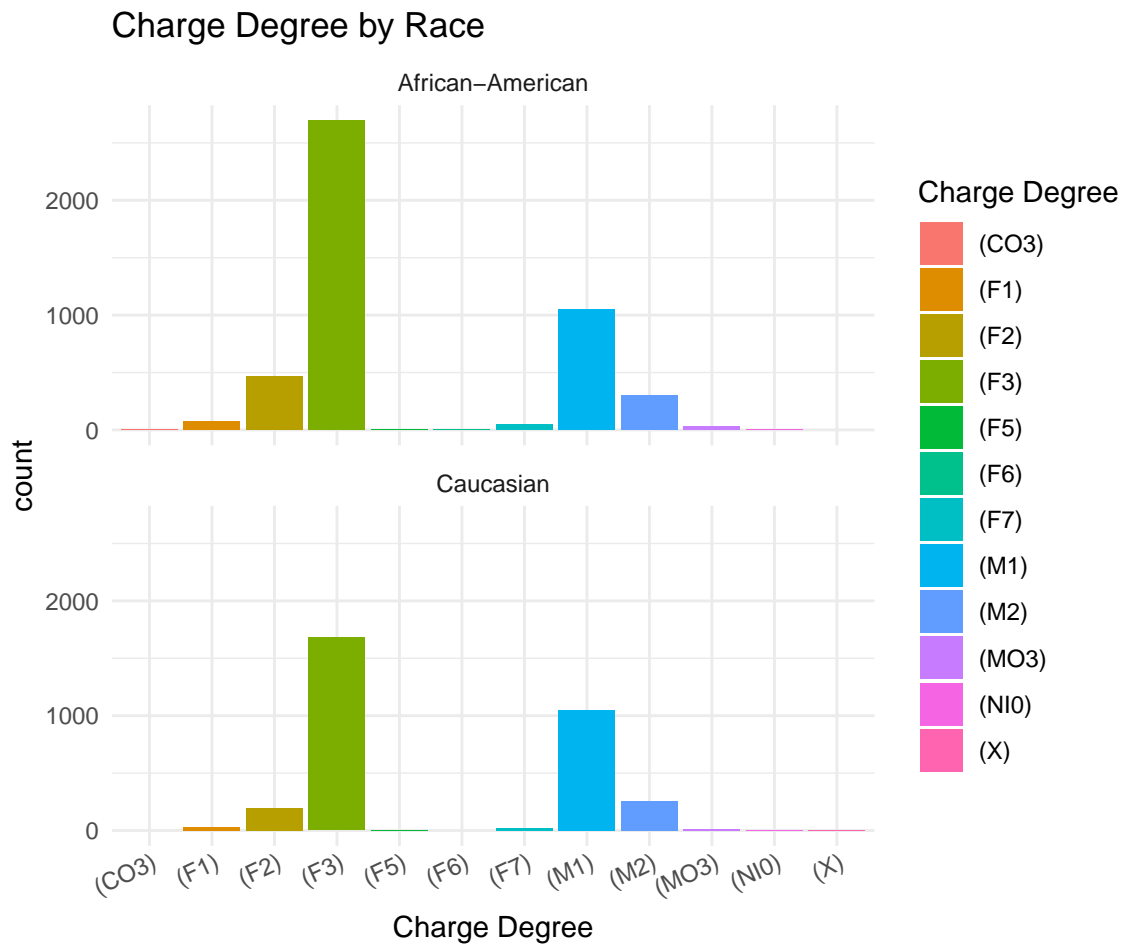
##	race	min	Q1	median	Q3	max	mean	sd	n	missing
## 1	African-American	0	1	2	57.75	10973	307.07018	927.29956	4674	0
## 2	Asian	0	1	1	24.25	388	33.95833	77.45883	48	0
## 3	Caucasian	0	1	1	7.00	7136	98.39908	464.94108	3250	0
## 4	Hispanic	0	0	1	5.00	5608	106.21027	483.40377	818	0
## 5	Native American	0	0	1	4.50	7630	421.25926	1528.72022	27	0
## 6	Other	0	1	1	3.00	3844	53.52105	302.96923	570	0

```
ggplot(data = compas_final,
  mapping = aes(x = as.factor(race), y = days_in_jail_or_prison)) +
  geom_boxplot() +
  theme_minimal() +
  labs(title = "Days in Jail or Prison by Race (Trimmed Y-Axis)",
    x = "Race",
    y = "Days in Jail or Prison") +
  ylim(0,75)
```



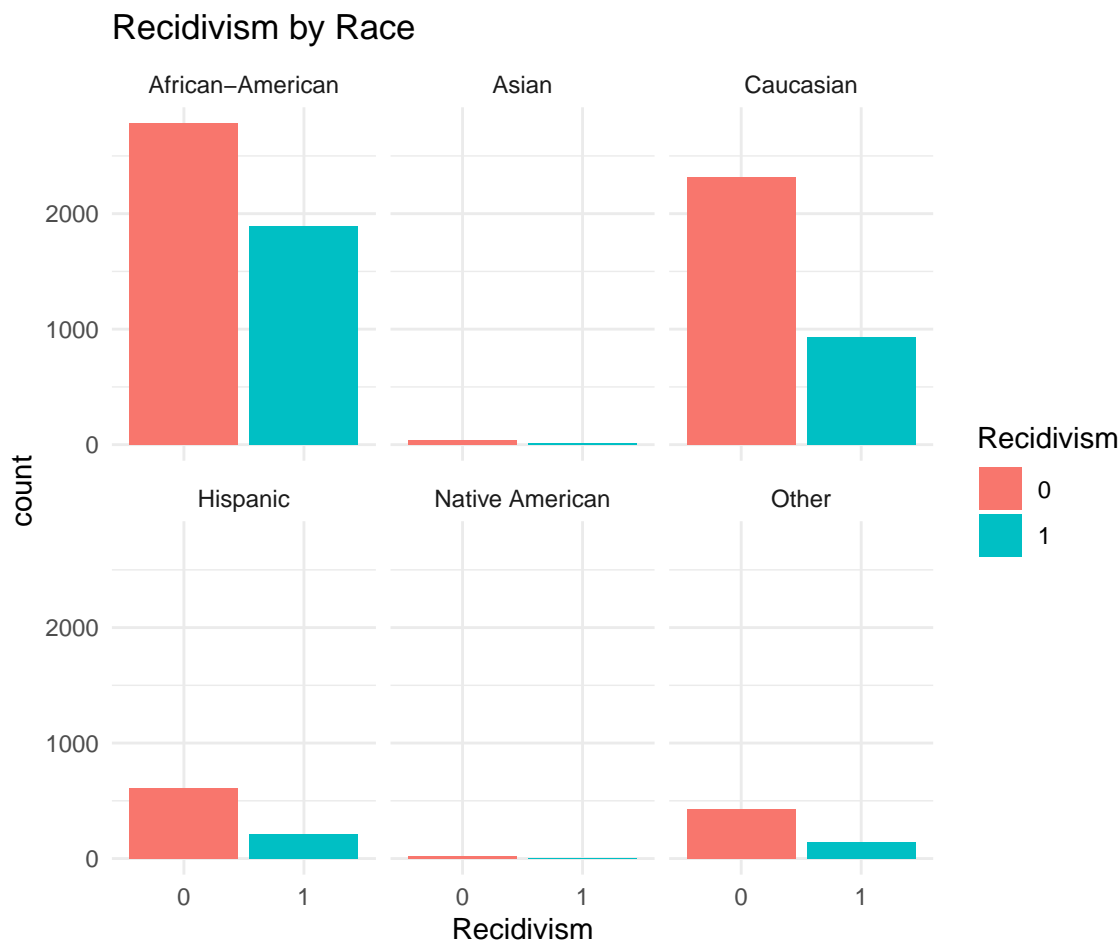
Next, let's look at the distribution of the charge degrees just for Black and White defendants. There are no notable distributional differences.

```
ggplot(data = compas_final_bw,
       mapping = aes(x = c_charge_degree, fill = c_charge_degree)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~race, ncol = 1) +
  labs(title = "Charge Degree by Race",
       x = "Charge Degree",
       fill = "Charge Degree") +
  theme(axis.text.x = element_text(angle = 25, vjust = 1.2, hjust=1))
```



Finally, let's look at the response variable: `is_recid`. Most defendants do not re-commit a crime, although the ratio of those who don't against those who do appears to be larger for African-American defendants than for Caucasian defendants. Nevertheless, of important note is that the class imbalance is in the same direction.

```
ggplot(data = compas_final,
       mapping = aes(x = as.factor(is_recid), fill = as.factor(is_recid))) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~race) +
  labs(title = "Recidivism by Race",
       x = "Recidivism",
       fill = "Recidivism")
```



In conclusion, our demographic variable, **race** (A), has proxy relationships with some of the predictor variables (X). Even a group-blind classifier will not be entirely blind to race because of the correlations present and the information that can be gained from the proxy variables.

Additionally, we've learned that the distribution of those who recommit a crime within 2 years versus those who don't is not drastically different for Black v White defendants – the class imbalance is in the same direction, so ideally, the model should not misclassify defendants in different directions on the basis of race.

Next, let's see how the COMPAS tool actually performs with regard to race and whether it is in line with these expectations.

COMPAS Analysis

Before we can analyze the COMPAS performance, recall that that the decile scores are mapped to 3 different risk levels – low, medium, or high – yet the response variable only has 2 levels – 0 or 1. Let's recreate this mapping such that there are only 2 risk levels to line up with the 2 levels of the response variable. Instead, decile scores of 1 to 5 will be associated with lower risk of recidivism and decile scores of 6 to 10 will be associated with higher risk as displayed in the table below.

```
compas <- compas_final %>%
  mutate(risk = ifelse(decile_score %in% c(1, 2, 3, 4, 5), 'Lower', 'Higher'))
```

```

compas %>%
  dplyr::select(decile_score, risk) %>%
  rename("Risk" = risk) %>%
  group_by(Risk) %>%
  summarise("Min" = min(decile_score),
            "Max" = max(decile_score)) %>%
  arrange(Min) %>%
  kable(booktabs = TRUE)

```

Risk	Min	Max
Lower	1	5
Higher	6	10

Now, let's recreate the table from Chapter 1 using this data set to assess the false positive and false negative rates for Black v White defendants.

While the numbers are different, which could likely be due to a host of reasons such as different subsets of the data set, the same trends are evident. 16.34% of White defendants who did not re-offend are labelled as higher risk, compared to more than twice as many Black defendants (37.71%). Similarly, 62.26% of White defendants who do re-offend are labelled as lower risk, compared to 39.01% of Black defendants. This is in line with ProPublica's findings, and is alarming given that race was not included in the model.

```

compas_table <- compas %>%
  filter(race %in% c("African-American", "Caucasian")) %>%
  dplyr::select(race, risk, is_recid) %>%
  rename("Risk" = risk,
         "Race" = race) %>%
  group_by(Race, is_recid) %>%
  mutate(Total = n()) %>%
  group_by(Risk, Race, Total) %>%
  summarise("Reoffended" = count(is_recid == 1),
            "Did Not Reoffend" = count(is_recid == 0)) %>%
  pivot_longer(cols = c("Reoffended", "Did Not Reoffend"),
               names_to = "Recidivism") %>%
  pivot_wider(
    id_cols = c("Risk", "Recidivism", "Total"),
    names_from = "Race",
    values_from = value
  ) %>%
  rename("Black" = `African-American`,
         "White" = `Caucasian`) %>%
  mutate(Black = round(100 * Black / Total, 2),
         White = round(100 * White / Total, 2)) %>%
  dplyr::select(-Total) %>%
  group_by(Risk, Recidivism) %>%
  summarize(Black = max(Black, na.rm = TRUE),
            White = max(White, na.rm = TRUE)) %>%
  filter((Risk == "Higher" & Recidivism == "Did Not Reoffend") |
         (Risk == "Lower" & Recidivism == "Reoffended"))
)

compas_table %>%
  kable(booktabs = TRUE)

```

Risk	Recidivism	Black	White
Higher	Did Not Reoffend	37.71	16.34
Lower	Reoffended	39.01	62.26

The results in this section also show that the model is more wrong in predicting whether defendants will re-offend versus predicting defendants who do not re-offend. This is expected because of the class imbalance we observed when performing exploratory data analysis – there are more defendants that don’t re-offend, so the model maximizes performance for those defendants.

However, it also raises a question of what type of prediction is more important: the risk of recidivism or the risk of non-recidivism. Is wrongly attributing a defendant as higher risk may cause or wrongly attributing a defendant as lower risk worse?

The table below shows the confusion matrix of the COMPAS model as a whole, including all races. As observed, a larger proportion (49.25%) of defendants who re-offended are incorrectly labelled as lower risk in comparison to the proportion (25.23%) that did not re-offend but are incorrectly labelled as higher risk.

Observe that while the overall FPR is 25.23%, it’s much higher for Black defendants (37.71%) and much lower for White defendants (16.34%). Similarly, while the overall FNR is 49.25%, it’s much higher for White defendants (62.26%) and much lower for Black defendants (39.01%).

```
compas %>%
  dplyr::select(risk, is_recid) %>%
  rename("Risk" = risk) %>%
  group_by(is_recid) %>%
  mutate(Total = n()) %>%
  group_by(Risk, Total) %>%
  summarise("Reoffended" = count(is_recid == 1),
            "Did Not Reoffend" = count(is_recid == 0)) %>%
  mutate(Reoffended = round(100 * Reoffended / Total, 2),
         `Did Not Reoffend` = round(100 * `Did Not Reoffend` / Total, 2)) %>%
  dplyr::select(-Total) %>%
  group_by(Risk) %>%
  summarize(Reoffended = max(Reoffended, na.rm = TRUE),
            `Did Not Reoffend` = max(`Did Not Reoffend`, na.rm = TRUE)) %>%
  kable()
```

Risk	Reoffended	Did Not Reoffend
Higher	50.75	25.23
Lower	49.25	74.77

The table below replicates the above table with raw numbers instead of proportions. This reveals that the model has an overall accuracy of 66.61%, but the analysis above reveals the discrepancies (and unfairness) in the model results for Black v White defendants.

However, if we classified every observation in the majority class (no recidivism), we’d expect an accuracy of 66.04%. The COMPAS model, thus, is not useful in a predictive sense, and on the contrary, introduces more bias into the judicial system.

```
compas %>%
  dplyr::select(risk, is_recid) %>%
  rename("Risk" = risk) %>%
```



```
group_by(Risk) %>%
  summarise("Reoffended" = count(is_recid == 1),
            "Did Not Reoffend" = count(is_recid == 0)) %>%
  kable()
```

Risk	Reoffended	Did Not Reoffend
Higher	1618	1564
Lower	1570	4635

```
(1618 + 4635) / 9387
```

```
## [1] 0.666134
```

```
count(compas$is_recid == 0) / 9387
```

```
##      n_TRUE
```

```
## 0.6603814
```

Now that we've recreated the table from Chapter 1, let's examine the false negative and false positive rates for all the races in the data set.

Asian defendants who did not re-offend were the least likely to be labelled as higher risk – Black defendants were the most likely. Conversely, excluding the “Other” group, White defendants who re-offended were the most likely to be labelled as lower risk – Native Americans were the least likely. This, and previous analysis, suggest disparities with favorable outcomes for white and Asian defendants, and unfavorable outcomes for Black and Native American defendants.

```
compas %>%
  dplyr::select(race, risk, is_recid) %>%
  rename("Risk" = risk,
         "Race" = race) %>%
  group_by(Race, is_recid) %>%
  mutate(Total = n()) %>%
  group_by(Risk, Race, Total) %>%
  summarise("Reoffended" = count(is_recid == 1),
            "Did Not Reoffend" = count(is_recid == 0)) %>%
  pivot_longer(cols = c("Reoffended", "Did Not Reoffend"),
               names_to = "Recidivism") %>%
  pivot_wider(
    id_cols = c("Risk", "Recidivism", "Total"),
    names_from = "Race",
    values_from = value
  ) %>%
  rename("Black" = `African-American`,
         "White" = `Caucasian`) %>%
  mutate(Black = round(100 * Black / Total, 2),
         White = round(100 * White / Total, 2),
         Hispanic = round(100 * Hispanic / Total, 2),
         Asian = round(100 * Asian / Total, 2),
         `Native American` = round(100 * `Native American` / Total, 2),
         Other = round(100 * Other / Total, 2)) %>%
  dplyr::select(-Total) %>%
  group_by(Risk, Recidivism) %>%
  summarize(Black = max(Black, na.rm = TRUE),
```

```

White = max(White, na.rm = TRUE),
Hispanic = max(Hispanic, na.rm = TRUE),
Asian = max(Asian, na.rm = TRUE),
`Native American` = max(`Native American`, na.rm = TRUE),
Other = max(Other, na.rm = TRUE)) %>%
filter((Risk == "Higher" & Recidivism == "Did Not Reoffend") |
(Risk == "Lower" & Recidivism == "Reoffended"))
) %>%
kable(booktabs = TRUE)

```

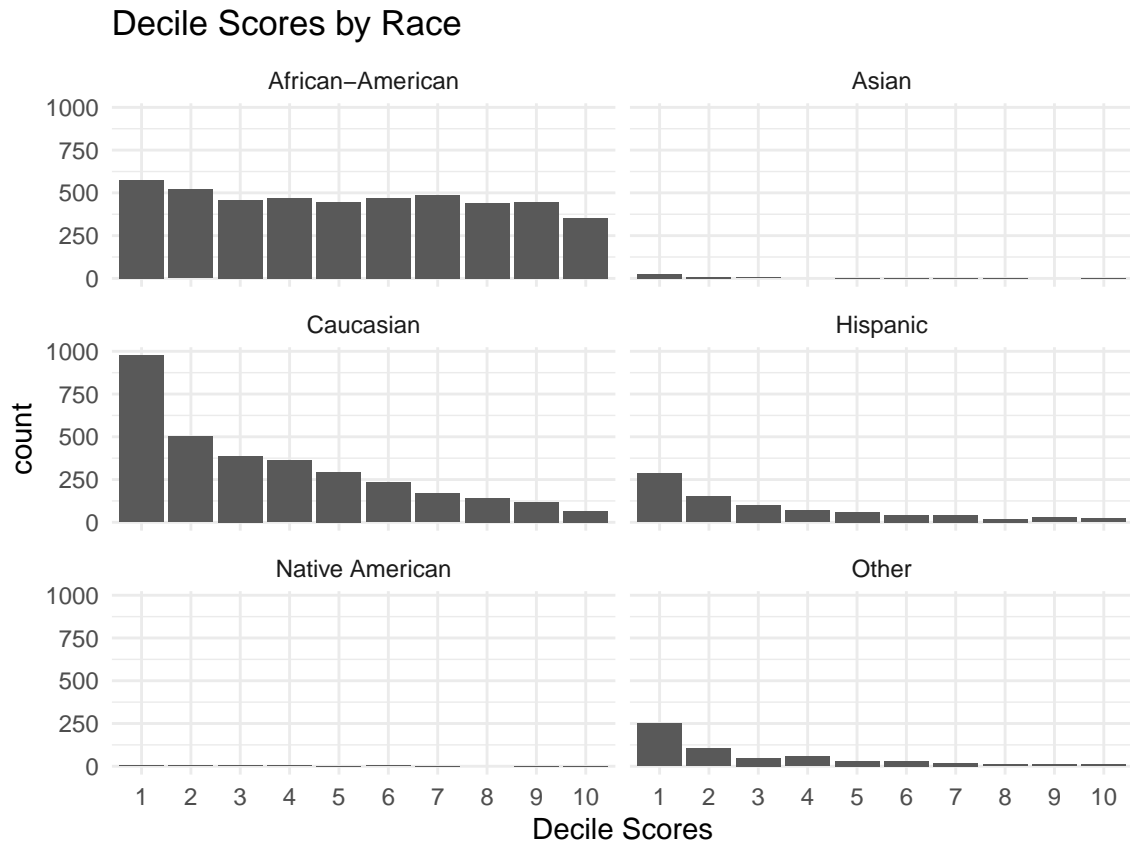
Risk	Recidivism	Black	White	Hispanic	Asian	Native American	Other
Higher	Did Not Reoffend	37.71	16.34	14.26	7.89	21.05	9.77
Lower	Reoffended	39.01	62.26	68.27	50.00	25.00	74.29

Finally, to visualize these results better, let's plot the distribution of the decile scores by race. Observe that while we observed a similar distribution of recidivism for all races, the African-American decile scores are distributed differently from the Caucasian decile scores. The decile scores for the Caucasian defendants is quite right-skewed in comparison to that of the African-Americans which appears to be more evenly distributed, further emphasizing the racial disparity in the risk scores.

```

ggplot(data = compas,
       mapping = aes(x = as.factor(decile_score))) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~race, ncol = 2) +
  labs(title = "Decile Scores by Race",
       x = "Decile Scores")

```



We have a thorough understanding of the data set now and the results we would expect from the COMPAS tool.

We're ready to proceed with modeling now. First, we will fit a logistic regression, which uses the standard ML approach discussed in Chapter 2. We expect it to behave similarly to the COMPAS tool. Then, we will define a fairness metric and fit a Seldonian classification algorithm on this data set. We expect to observe less disparities along racial lines, but perhaps with a slight trade-off in overall accuracy.

Logistic Regression

Logistic regression is a statistical generalized linear model (GLM) that is particularly designed for predicting dichotomous/ binary outcomes such as ours. We will use logistic regression to model the probability of a defendant re-committing a crime within two years in Broward County, Florida. We'll then set cutoffs to divide the probabilities into 2 bins: 0 for 'no' and 1 for 'yes' based on the probability predictions. This will also allow us to analyze which features may be most important in predicting recidivism.

Recall that if we classified every observation in the majority class, we'd expect an accuracy 66%. This serves as a benchmark for the race-blind logistic regression model we will implement. Note that logistic regression follows the standard ML process [will describe in more detail in the thesis body] and is one of the most widely used classification algorithms – this will allow us to assess how we might expect state-of-the-art traditional algorithms that do not take fairness guarantees into account to perform.

Check for Missing Data

Linear models do not handle missing observations well. Let's ensure that there are no missing observations. There were no missing observations!

```
compas <- tidyr::drop_na(compas)
count(compas)
```

```
## # A tibble: 1 x 1
##       n
##   <int>
## 1  9387
```

Train and Test Split

Before we proceed to fitting the models, we need to perform a train/ test split. The reason for this is to be able to test how our model would perform on unseen data and to avoid over-fitting. Therefore, we will train our models using the **train** data, and then assess performance on “new” data, that is, the **test** set. Let's partition 70% of the data into the train set and 30% into the test set. We will use randomization without replacement for this.

```
set.seed(123)
n <- nrow(compas)
train_index <- sample(1:n, 0.70 * n)
test_index <- setdiff(1:n, train_index)
train <- compas[train_index, ]
test <- compas[test_index, ]
```

There are now 6570 observations in the train set and 2817 observations in the test set. Let's ensure that the distribution of the response variable is preserved in each set. There split appears to be stratified so there is no concern.

```
tally(train$is_recid)
```

```
## X
##   0   1
## 4333 2237
```

```
tally(test$is_recid)
```

```
## X
```

```
##      0      1
## 1866  951
```

Finally, let's also make sure that there are enough observations in each race category for both the train and test splits. There is concern for the Native American and Asian race categories, which have very few observations. We may fit a separate model with just the Caucasian and African-American offenders if this poses a challenge.

```
tally(train$race)
```

```
## X
## African-American      Asian      Caucasian      Hispanic
##           3270           34           2280           573
## Native American      Other
##           18           395
```

```
tally(test$race)
```

```
## X
## African-American      Asian      Caucasian      Hispanic
##           1404           14           970           245
## Native American      Other
##           9           175
```

We're ready for model fitting!

Modeling

First, let's fit a kitchen sink model without transformations. This means that we'll include all the variables in the initial model. Notice that race will not be used as a predictor in this model.

```
glm1 <- glm(is_recid ~ sex + age + age_cat + marital_status + custody_status +
             juv_offense + priors_count + c_charge_degree +
             days_in_jail_or_prison,
             data = train,
             family = binomial(logit))
```

```
msummary(glm1)
```

```
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)    1.487e+01  5.354e+02   0.028 0.977839
## sexMale        3.790e-01  7.428e-02   5.103 3.35e-07 ***
## age          -4.954e-02  6.150e-03  -8.054 8.00e-16 ***
## age_catGreater than 45  4.943e-01  1.446e-01   3.417 0.000633 ***
## age_catLess than 25    8.701e-02  8.949e-02   0.972 0.330914
## marital_statusMarried -1.077e-01  1.846e-01  -0.584 0.559505
## marital_statusSeparated -3.515e-02  2.575e-01  -0.136 0.891454
## marital_statusSignificant Other  4.999e-01  2.193e-01   2.279 0.022676 *
## marital_statusSingle   1.398e-01  1.670e-01   0.837 0.402593
## marital_statusUnknown  2.335e-01  3.981e-01   0.586 0.557575
## marital_statusWidowed   1.115e+00  4.781e-01   2.331 0.019734 *
```

```
## custody_statusPretrial Defendant -8.774e-02 8.779e-02 -0.999 0.317580
## custody_statusPrison Inmate -8.414e-01 1.238e+00 -0.680 0.496762
## custody_statusProbation -1.261e+01 5.354e+02 -0.024 0.981216
## custody_statusResidential Program 4.276e-01 1.455e+00 0.294 0.768862
## juv_offense 3.881e-01 8.830e-02 4.396 1.10e-05 ***
## priors_count 1.349e-01 7.740e-03 17.430 < 2e-16 ***
## c_charge_degree(F1) -1.520e+01 5.354e+02 -0.028 0.977355
## c_charge_degree(F2) -1.497e+01 5.354e+02 -0.028 0.977698
## c_charge_degree(F3) -1.480e+01 5.354e+02 -0.028 0.977941
## c_charge_degree(F5) -2.780e+01 5.851e+02 -0.048 0.962099
## c_charge_degree(F6) -2.859e+01 6.512e+02 -0.044 0.964987
## c_charge_degree(F7) -1.501e+01 5.354e+02 -0.028 0.977633
## c_charge_degree(M1) -1.501e+01 5.354e+02 -0.028 0.977636
## c_charge_degree(M2) -1.478e+01 5.354e+02 -0.028 0.977980
## c_charge_degree(M03) -1.480e+01 5.354e+02 -0.028 0.977944
## c_charge_degree(NI0) -1.379e+01 5.354e+02 -0.026 0.979450
## c_charge_degree(X) -2.755e+01 7.572e+02 -0.036 0.970977
## days_in_jail_or_prison -9.274e-07 4.427e-05 -0.021 0.983287
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 8427.4 on 6569 degrees of freedom
## Residual deviance: 7549.8 on 6541 degrees of freedom
## AIC: 7607.8
##
## Number of Fisher Scoring iterations: 12
```

Let's calculate the overall accuracy of this model on the train set, which tends to be overconfident.

The values in the diagonal are correct predictions while those in the off-diagonal are misclassifications using a probability cutoff of 0.5.

```
glm1augment <- glm1 %>%
  broom::augment(type.predict = "response")
glm1augment <- mutate(glm1augment, binprediction = round(.fitted, 0))
with(glm1augment, table(is_recid, binprediction))

##          binprediction
## is_recid    0      1
##          0 3938  395
##          1 1564  673
```

This kitchen-sink model has an accuracy of 70.2%, slightly better than the COMPAS tool accuracy of 66%.

```
(3938 + 673) / count(train)

##          n
## 1 0.7018265
```

Using a probability cutoff of 0.34, which is the probability of being in the positive class given the class imbalance in the COMPAS data set, the accuracy is the same as the COMPAS tool: 66.7%.

```

glm1augment_2 <- glm1 %>%
  broom::augment(type.predict = "response")
glm1augment_2 <- mutate(glm1augment_2, binprediction = ifelse(.fitted >= 0.34, 1, 0))
with(glm1augment_2, table(is_recid, binprediction))

```

```

##          binprediction
## is_recid    0      1
##          0 2905 1428
##          1  761 1476

```

```

(2905+1476)/count(train)

```

```

##          n
## 1 0.6668189

```

Using a stricter probability results in an accuracy of 68.2%

```

glm1augment_2 <- glm1 %>%
  broom::augment(type.predict = "response")
glm1augment_2 <- mutate(glm1augment_2, binprediction = ifelse(.fitted >= 0.66, 1, 0))
with(glm1augment_2, table(is_recid, binprediction))

```

```

##          binprediction
## is_recid    0      1
##          0 4229  104
##          1 1988  249

```

```

(4229+249)/count(train)

```

```

##          n
## 1 0.681583

```

The probability of 0.5 is an appropriate cutoff. Notice, however, that the only significant variables in the kitchen-sink model are sex, age, age_category, marital_status, juv_offense, and priors_count. Let's fit another model with just these predictors.

```

glm2 <- glm(is_recid ~ sex + age + age_cat + marital_status +
  juv_offense + priors_count,
  data = train,
  family = binomial(logit))

```

```

msummary(glm2)

```

```

## Coefficients:
##
##          Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -0.009828   0.273046  -0.036 0.971287
## sexMale         0.390681   0.073758   5.297 1.18e-07 ***
## age           -0.050222   0.006087  -8.251 < 2e-16 ***
## age_catGreater than 45  0.508380   0.144297   3.523 0.000426 ***
## age_catLess than 25    0.089960   0.089052   1.010 0.312403
## marital_statusMarried  -0.136133   0.184174  -0.739 0.459813
## marital_statusSeparated -0.023786   0.257143  -0.093 0.926301
## marital_statusSignificant Other  0.493876   0.219082   2.254 0.024178 *

```

```
## marital_statusSingle      0.141861  0.166802  0.850 0.395062
## marital_statusUnknown     0.255089  0.396522  0.643 0.520019
## marital_statusWidowed     1.139997  0.475660  2.397 0.016545 *
## juv_offense                0.382606  0.087645  4.365 1.27e-05 ***
## priors_count               0.137055  0.007249 18.908 < 2e-16 ***
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 8427.4 on 6569 degrees of freedom
## Residual deviance: 7576.6 on 6557 degrees of freedom
## AIC: 7602.6
##
## Number of Fisher Scoring iterations: 4
```

```
glm2augment <- glm2 %>%
  broom::augment(type.predict = "response")
glm2augment <- mutate(glm2augment, binprediction = round(.fitted, 0))
with(glm2augment, table(is_recid, binprediction))
```

```
##      binprediction
## is_recid    0    1
##      0 3956  377
##      1 1581  656
```

There is no effect on predictive accuracy by reducing the number of variables: 70.2%.

```
(3956 + 656) / count(train)
```

```
##      n
## 1 0.7019787
```

Finally, let's assess performance when we use the square-root transformed variables. The same variables are significant.

```
glm3 <- glm(is_recid ~ sex + sqrt_age + age_cat + marital_status + custody_status +
  juv_offense + sqrt_priors_count + c_charge_degree +
  sqrt_days_in_jail_or_prison,
  data = train,
  family = binomial(logit))
msummary(glm3)
```

```
## Coefficients:
##      Estimate Std. Error z value Pr(>|z|)
## (Intercept) 16.313306 535.411403  0.030 0.975693
## sexMale      0.339417  0.075246  4.511 6.46e-06 ***
## sqrt_age     -0.632307  0.074644 -8.471 < 2e-16 ***
## age_catGreater than 45 0.487163  0.139432  3.494 0.000476 ***
## age_catLess than 25   0.112351  0.096475  1.165 0.244195
## marital_statusMarried -0.067026  0.185160 -0.362 0.717361
## marital_statusSeparated -0.032919  0.258771 -0.127 0.898772
## marital_statusSignificant Other 0.475337  0.220975  2.151 0.031469 *
```



```
## marital_statusSingle          0.097231  0.167383  0.581 0.561313
## marital_statusUnknown         0.301756  0.404084  0.747 0.455205
## marital_statusWidowed         0.997625  0.486060  2.052 0.040124 *
## custody_statusPretrial Defendant -0.138916  0.088326 -1.573 0.115775
## custody_statusPrison Inmate    -1.018251  1.237448 -0.823 0.410586
## custody_statusProbation       -12.834477 535.411175 -0.024 0.980876
## custody_statusResidential Program 0.585953  1.505249  0.389 0.697074
## juv_offense                   0.261143  0.088817  2.940 0.003280 **
## sqrt_priors_count             0.566413  0.028799 19.668 < 2e-16 ***
## c_charge_degree(F1)          -15.010178 535.411237 -0.028 0.977634
## c_charge_degree(F2)          -14.767817 535.411181 -0.028 0.977995
## c_charge_degree(F3)          -14.584335 535.411173 -0.027 0.978269
## c_charge_degree(F5)          -27.778103 584.539153 -0.048 0.962098
## c_charge_degree(F6)          -28.630853 652.924899 -0.044 0.965024
## c_charge_degree(F7)          -14.846965 535.411251 -0.028 0.977877
## c_charge_degree(M1)          -14.720471 535.411175 -0.027 0.978066
## c_charge_degree(M2)          -14.540801 535.411183 -0.027 0.978334
## c_charge_degree(M03)         -14.582420 535.411278 -0.027 0.978272
## c_charge_degree(NI0)         -13.486319 535.412727 -0.025 0.979904
## c_charge_degree(X)           -27.202623 757.185745 -0.036 0.971341
## sqrt_days_in_jail_or_prison   0.003900  0.002495  1.563 0.118072
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 8427.4 on 6569 degrees of freedom
## Residual deviance: 7434.0 on 6541 degrees of freedom
## AIC: 7492
##
## Number of Fisher Scoring iterations: 12
```

A reduced model yields the same overall accuracy observed in the other models: 70.2%.

```
glm4 <- glm(is_recid ~ sex + age + age_cat + marital_status +
            juv_offense + priors_count,
            data = train,
            family = binomial(logit))

glm4augment <- glm4 %>%
  broom::augment(type.predict = "response")
glm4augment <- mutate(glm4augment, binprediction = round(.fitted, 0))
with(glm4augment, table(is_recid, binprediction))

##           binprediction
## is_recid    0      1
##           0 3956  377
##           1 1581  656

(3956 + 656) / count(train)

##           n
## 1 0.7019787
```

Based on the modeling results, we will proceed with glm2, which fits the most important non-transformed variables.

Evaluating Test Set Performance

It's important to assess performance on unseen data as that serves as a better indicator for model generalization performance and rules out over-fitting.

The performance on the test set is comparable with the training set at 70.1% accuracy.

```
preds <- predict(glm2, newdata=test, type="response")
```

```
test2 <- test %>%  
  mutate(preds = preds,  
         prediction = round(preds, 0))
```

```
with(test2, table(is_recid, prediction))
```

```
##           prediction  
## is_recid    0     1  
##           0 1699  167  
##           1  675  276
```

```
(1699 + 276) / count(test)
```

```
##           n  
## 1 0.7011005
```

The ROC curve is a graph that also helps us assess the performance of a classification model. The diagonal line shows how the model would perform with random predictions. We prefer curves that budge out closer to the top left because those types of curves maximize the area under the curve (AUC) and the sensitivity and specificity of the model is closer to 100%.

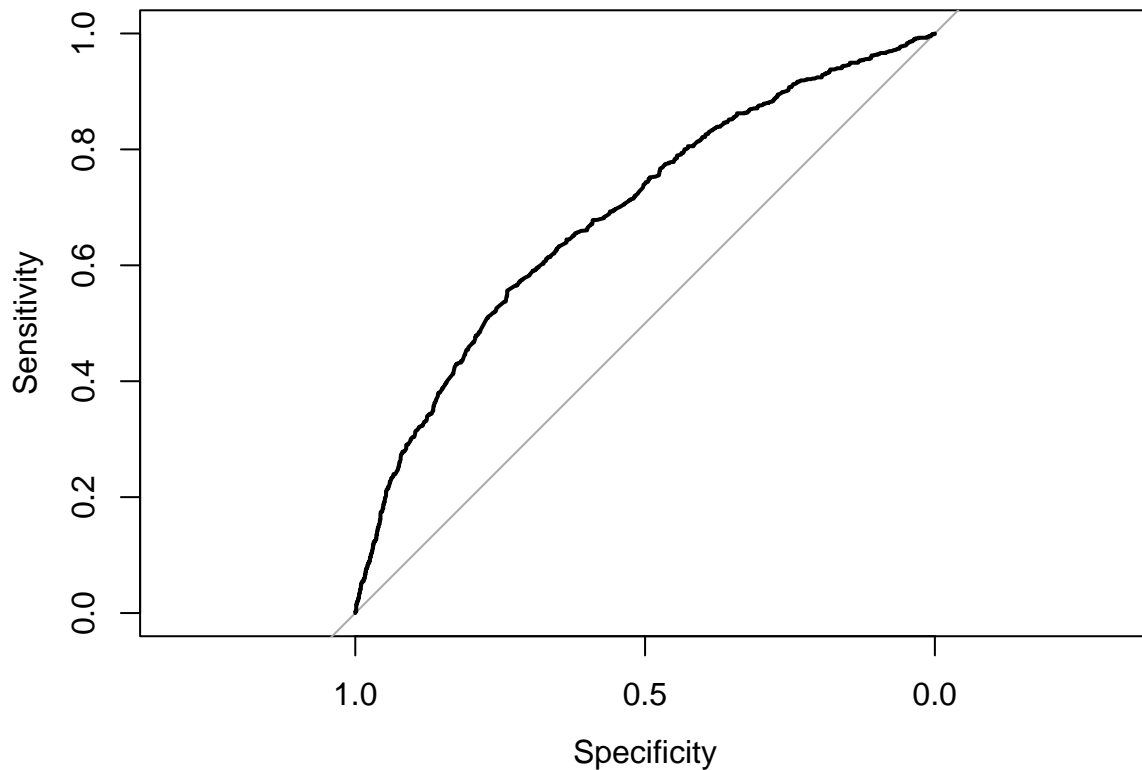
This curve has an AUC of 0.68 and it doesn't exhibit the best shape. This raises overall concerns about the model's performance.

```
predlm <- predict(glm2, type=c("response"), newdata = test)  
roccurve1 <- with(test, roc(is_recid ~ predlm))
```

```
## Setting levels: control = 0, case = 1
```

```
## Setting direction: controls < cases
```

```
plot(roccurve1)
```



```
print(roccurve1)
```

```
##
## Call:
## roc.formula(formula = is_recid ~ predlm)
##
## Data: predlm in 1866 controls (is_recid 0) < 951 cases (is_recid 1).
## Area under the curve: 0.688
```

In conclusion, the final logistic regression model has the following 6 variables:

- age
- sex
- age category
- marital status
- whether a defendant committed a binary offense or not
- number of prior offenses

The accuracy on the test set is 70.1%, comparable to the COMPAS test set. This means that ~30% of defendants are misclassified in the incorrect recidivism prediction.

However, the ROC curve indicated some problems with the performance of this model, particularly with regard to sensitivity (1 - FNR) and specificity (1 - FPR). Next, let's assess the direction of these misclassifications and perform a demographic analysis by race in an attempt to assess the model's 'fairness' along racial lines.

Demographic and 'Fairness' Analysis

First, let's re-examine the confusion matrix using the test set to determine whether the model makes more false negative or more false positive results.

The first table depicts the raw numbers and the second table interprets that in terms of proportions in order to better understand the magnitude.

The model correctly classifies 276 defendants as reoffenders and 1699 defendants as non-reoffenders. 675 defendants who reoffend are classified as low risk, whereas 167 defendants who did not reoffend are classified as high risk. The model does a better job at classifying those who do not reoffend, as is expected because there is more data for that group. In general, this is consistent with what we observed in the COMPAS tool's results.

```
test2 <- test2 %>%
  mutate(pred_risk = ifelse(prediction == 0, 'Low', 'High'))
```

```
test2 %>%
  dplyr::select(pred_risk, is_recid) %>%
  rename("Risk" = pred_risk) %>%
  group_by(Risk) %>%
  summarise("Reoffended" = count(is_recid == 1),
            "Did Not Reoffend" = count(is_recid == 0)) %>%
  kable()
```

Risk	Reoffended	Did Not Reoffend
High	276	167
Low	675	1699

When looking at the proportions, 91% of participants who did not reoffend are correctly classified as low risk. This means only 9% of participants who do not reoffend are classified as high risk. This is a lower FPR than COMPAS.

On the flip side, only 29% of defendants who reoffended are correctly classified as high risk. This means 71% of defendants who reoffended are classified as low risk. This is a higher FNR than COMPAS.

The model, overall, has worse false negative rates than false positive rates. While this is the same general trend observed in the COMPAS tool, the discrepancy is much larger.

```
test2 %>%
  dplyr::select(pred_risk, is_recid) %>%
  rename("Risk" = pred_risk) %>%
  group_by(is_recid) %>%
  mutate(Total = n()) %>%
  group_by(Risk, Total) %>%
  summarise("Reoffended" = count(is_recid == 1),
            "Did Not Reoffend" = count(is_recid == 0)) %>%
  mutate(Reoffended = round(100 * Reoffended / Total, 2),
         `Did Not Reoffend` = round(100 * `Did Not Reoffend` / Total, 2)) %>%
  dplyr::select(-Total) %>%
  group_by(Risk) %>%
  summarize(Reoffended = max(Reoffended, na.rm = TRUE),
            `Did Not Reoffend` = max(`Did Not Reoffend`, na.rm = TRUE)) %>%
  kable()
```

Risk	Reoffended	Did Not Reoffend
High	29.02	8.95
Low	70.98	91.05

Now, let's examine these false positive and false negative rates along racial lines. First, we'll compare Black v White defendants.

Recall that the overall FPR rate for the model is 8.95%. However, notice that the FPR for Black defendants is 13.93%, compared to only 5.09% for White defendants. Just like in the COMPAS tool, Black defendants who do not reoffend are incorrectly misclassified as high risk at twice the rate of White defendants.

Recall that the overall FNR rate for the model is 70.98%. However, notice that the FNR for Black defendants is 60.82%, compared to 86.17%. Just like in the COMPAS tool, the logistic regression makes the opposite mistake in predicting recidivism for Black v White defendants, with White defendants being more likely to be incorrectly classified as low risk.

This serves to highlight the real danger with using standard ML procedures, even when the sensitive variable itself is not included. It has potential to perpetuate, and even introduce, harmful and discriminatory practices as we have observed. The COMPAS tool likely employs a similar standard approach.

```
test2 %>%
  filter(race %in% c("African-American", "Caucasian")) %>%
  dplyr::select(race, pred_risk, is_recid) %>%
  rename("Risk" = pred_risk,
         "Race" = race) %>%
  group_by(Race, is_recid) %>%
  mutate(Total = n()) %>%
  group_by(Risk, Race, Total) %>%
  summarise("Reoffended" = count(is_recid == 1),
            "Did Not Reoffend" = count(is_recid == 0)) %>%
  pivot_longer(cols = c("Reoffended", "Did Not Reoffend"),
               names_to = "Recidivism") %>%
  pivot_wider(
    id_cols = c("Risk", "Recidivism", "Total"),
    names_from = "Race",
    values_from = value
  ) %>%
  rename("Black" = `African-American`,
         "White" = `Caucasian`) %>%
  mutate(Black = round(100 * Black / Total, 2),
         White = round(100 * White / Total, 2)) %>%
  dplyr::select(-Total) %>%
  group_by(Risk, Recidivism) %>%
  summarise(Black = max(Black, na.rm = TRUE),
            White = max(White, na.rm = TRUE)) %>%
  filter((Risk == "High" & Recidivism == "Did Not Reoffend") |
         (Risk == "Low" & Recidivism == "Reoffended"))
  ) %>%
  kable(booktabs = TRUE)
```

Risk	Recidivism	Black	White
High	Did Not Reoffend	13.93	5.09
Low	Reoffended	60.82	86.17

Now, let's examine the false negative and false positive rates for all the races in the data set.

Due to the low amount of data on Asian and Native American defendants, their FPR was 0. Regardless, Black defendants had the highest FPR – more than double that of all other races.

Conversely, excluding the “Other” group, White defendants who re-offended were the most likely to be labelled as lower risk (highest FNR) – Native Americans were the least likely, followed by Black defendants.

This, and previous analysis, suggest disparities with favorable outcomes for white and Asian defendants, and unfavorable outcomes for Black and Native American defendants.

These outcomes are quite similar to the COMPAS tool.

```
test2 %>%
  dplyr::select(race, pred_risk, is_recid) %>%
  rename("Risk" = pred_risk,
         "Race" = race) %>%
  group_by(Race, is_recid) %>%
  mutate(Total = n()) %>%
  group_by(Risk, Race, Total) %>%
  summarise("Reoffended" = count(is_recid == 1),
            "Did Not Reoffend" = count(is_recid == 0)) %>%
  pivot_longer(cols = c("Reoffended", "Did Not Reoffend"),
               names_to = "Recidivism") %>%
  pivot_wider(
    id_cols = c("Risk", "Recidivism", "Total"),
    names_from = "Race",
    values_from = value
  ) %>%
  rename("Black" = `African-American`,
         "White" = `Caucasian`) %>%
  mutate(Black = round(100 * Black / Total, 2),
         White = round(100 * White / Total, 2),
         Hispanic = round(100 * Hispanic / Total, 2),
         Asian = round(100 * Asian / Total, 2),
         `Native American` = round(100 * `Native American` / Total, 2),
         Other = round(100 * Other / Total, 2)) %>%
  dplyr::select(-Total) %>%
  group_by(Risk, Recidivism) %>%
  summarize(Black = max(Black, na.rm = TRUE),
            White = max(White, na.rm = TRUE),
            Hispanic = max(Hispanic, na.rm = TRUE),
            Asian = max(Asian, na.rm = TRUE),
            `Native American` = max(`Native American`, na.rm = TRUE),
            Other = max(Other, na.rm = TRUE)) %>%
  filter((Risk == "High" & Recidivism == "Did Not Reoffend") |
         (Risk == "Low" & Recidivism == "Reoffended"))
  ) %>%
  kable(booktabs = TRUE)
```

Risk	Recidivism	Black	White	Hispanic	Asian	Native American	Other
High	Did Not Reoffend	13.93	5.09	4.89	0	0	4.29
Low	Reoffended	60.82	86.17	83.61	80	50	91.43

Finally, let’s examine how close to the COMPAS tool the logistic regression performed.

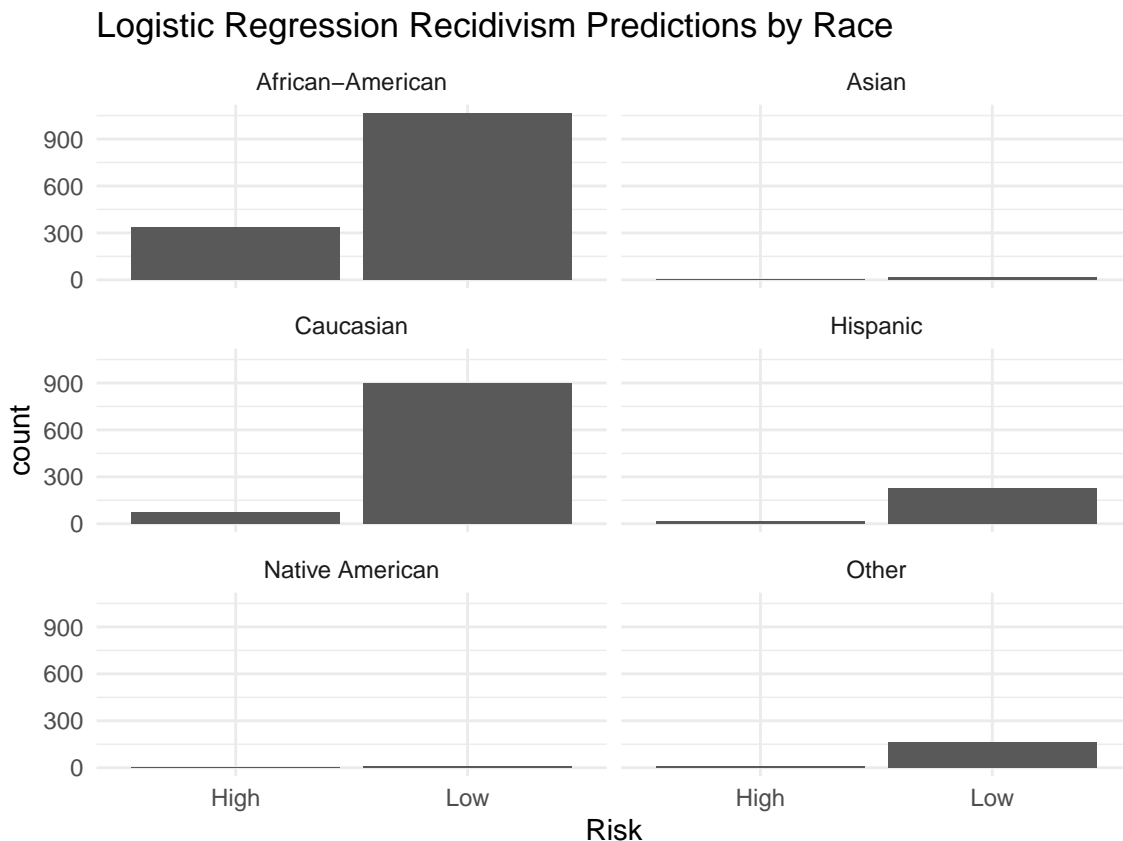
There is some overlap between our risk predictions and the COMPAS decile scores. However, the mean and median of the ‘High’ risk group is significantly larger than that of the ‘Low’ risk group. There is some predictive similarity between both models.

```
favstats(test2$decile_score ~ test2$pred_risk)
```

```
## test2$pred_risk min Q1 median Q3 max mean sd n missing
## 1 High 1 6 8 9 10 7.494357 2.188377 443 0
## 2 Low 1 1 3 5 10 3.627211 2.554512 2374 0
```

There is no alarming discrepancy in the risk distributions.

```
ggplot(data = test2,
       mapping = aes(x = pred_risk)) +
  geom_bar() +
  theme_minimal() +
  facet_wrap(~race, ncol = 2) +
  labs(title = "Logistic Regression Recidivism Predictions by Race",
       x = "Risk")
```



In conclusion, the logistic regression performed comparably to the COMPAS tool. When assessed on the test set, the overall accuracy is 70.1% with majority of the errors being false negatives. However, there are notably higher FPR rates for Black defendants and notably higher FNR rates for White defendants.

The logistic regression, which employs the standard ML approach, thus, produces unfair outcomes with regard to race.

Next, let's test the Seldonian framework on this data set in an aim to achieve more equitable results by

enforcing fairness constraints.

Seldonian Algorithm

Recall that Seldonian algorithms allow us to enforce probabilistic fairness constraints on traditional ML algorithms. First, let's create a data set for the Seldonian algorithm with only the most significant variables from the logistic regression. This is because the Seldonian algorithm will use the logistic regression solution as a starting point to its solution.

We'll limit the analysis to just Black and White defendants. We may consider other races in future analysis.

Set Up the Python Environment

Let's ensure we have all the packages and libraries needed to run the Seldonian algorithm on the COMPAS data set.

```
# set up Python environment
library(reticulate)
use_python("/cm/shared/apps/amh-Rstudio/python-3.11.4/bin/python3",
           required = TRUE)

# import necessary libraries
import numpy as np
import os

import pandas as pd
import json

from sklearn.preprocessing import LabelEncoder
from sklearn.preprocessing import OneHotEncoder
from sklearn.preprocessing import StandardScaler
from sklearn.compose import ColumnTransformer

from seldonian.utils.io_utils import save_json
from seldonian.parse_tree.parse_tree import (ParseTree,
                                             make_parse_trees_from_constraints)
from seldonian.dataset import DataSetLoader
from seldonian.utils.io_utils import (load_json, save_pickle)
from seldonian.spec import SupervisedSpec
from seldonian.models.models import (
    BinaryLogisticRegressionModel as LogisticRegressionModel)
from seldonian.models import objectives

import matplotlib.pyplot as plt
```

Pre-Process the Data

Let's ensure our data is in the correct format.

First, we'll read it in and make sure it looks alright.

```
# point to the data file
f_orig = "/home/dasienga24/Statistics-Senior-Honors-Thesis/Data Sets/COMPAS/compas_seldonian_bw.csv"

# list the column names that were most important
columns_orig = [
    "race", "sex", "age",
    "age_cat", "marital_status", "juv_offense",
    "priors_count", "is_recid"]
```

```
df = pd.read_csv(f_orig, header=1, names=columns_orig)
df.head()
```

```
##           race      sex  age  ...  juv_offense  priors_count  is_recid
## 0  African-American   Male   24  ...           1           4           1
## 1      Caucasian     Male   41  ...           0          14           1
## 2      Caucasian  Female   39  ...           0           0           0
## 3      Caucasian     Male   20  ...           1           0           0
## 4      Caucasian  Female   26  ...           0           0           0
##
## [5 rows x 8 columns]
```

```
df.dtypes
```

```
## race           object
## sex            object
## age            int64
## age_cat        object
## marital_status object
## juv_offense     int64
## priors_count    int64
## is_recid        int64
## dtype: object
```

Next, we'll separate the predictor variables from the response variable.

```
# split into inputs and outputs
X = df.drop(columns=["is_recid"])
y = df["is_recid"]
```

```
X
```

```
##           race      sex  age  ...  marital_status  juv_offense  priors_count
## 0  African-American   Male   24  ...           Single           1           4
## 1      Caucasian     Male   41  ...           Single           0          14
## 2      Caucasian  Female   39  ...           Single           0           0
## 3      Caucasian     Male   20  ...           Single           1           0
## 4      Caucasian  Female   26  ...          Married           0           0
## ...           ...      ...  ...  ...           ...           ...           ...
## 7918      Caucasian   Male   24  ...           Single           0           0
## 7919      Caucasian   Male   23  ...           Single           0           0
## 7920  African-American   Male   56  ...          Divorced           0           0
## 7921  African-American   Male   63  ...           Single           0           5
## 7922      Caucasian   Male   22  ...           Single           1           3
##
## [7923 rows x 7 columns]
```

```
y
```

```
## 0      1
## 1      1
## 2      0
## 3      0
## 4      0
```

```
##      ..
## 7918  0
## 7919  0
## 7920  0
## 7921  1
## 7922  1
## Name: is_recid, Length: 7923, dtype: int64
```

We'll one-hot encode all the categorical variables to make sure everything is numerically encoded. We will also scale all the numerical variables on a Standard N(0,1) scale.

```
# one hot encode cat features only, scale numerical features using standard scaler
ct = ColumnTransformer([('c',OneHotEncoder()),('race', 'sex', 'age_cat', 'marital_status')], ('n',StandardScaler))

# apply transformation
X_transformed = ct.fit_transform(X)

# get names after one-hot encoding
output_columns = ct.get_feature_names_out(ct.feature_names_in_)

# make an output dataframe to save transformed X and y
outdf = pd.DataFrame(X_transformed,columns=output_columns)
```

```
outdf
```

```
##      c__race_African-American  c__race_Caucasian  ...  n__age  n__priors_count
## 0                1.0                0.0  ... -0.899307      0.154321
## 1                0.0                1.0  ...  0.540301      2.254798
## 2                0.0                1.0  ...  0.370935     -0.685869
## 3                0.0                1.0  ... -1.238039     -0.685869
## 4                0.0                1.0  ... -0.729942     -0.685869
## ...                ...                ...  ...  ...      ...
## 7918              0.0                1.0  ... -0.899307     -0.685869
## 7919              0.0                1.0  ... -0.983990     -0.685869
## 7920              1.0                0.0  ...  1.810543     -0.685869
## 7921              1.0                0.0  ...  2.403322      0.364369
## 7922              0.0                1.0  ... -1.068673     -0.055726
##
## [7923 rows x 16 columns]
```

```
outdf.columns
```

```
## Index(['c__race_African-American', 'c__race_Caucasian', 'c__sex_Female',
##       'c__sex_Male', 'c__age_cat_25 - 45', 'c__age_cat_Greater than 45',
##       'c__age_cat_Less than 25', 'c__marital_status_Divorced',
##       'c__marital_status_Married', 'c__marital_status_Separated',
##       'c__marital_status_Significant Other', 'c__marital_status_Single',
##       'c__marital_status_Unknown', 'c__marital_status_Widowed', 'n__age',
##       'n__priors_count'],
##       dtype='object')
```

Let's rename the columns for easier interpretation.

```
# change names of columns
outdf.rename(columns={'c__race_African-American':'Black', 'c__race_Caucasian':'White', 'c__sex_Female':
inplace=True)

# add label column and `juv_offense` into final dataframe
outdf['juv_offense'] = df['juv_offense']
outdf['is_recid'] = y
```

```
outdf.columns
```

```
## Index(['Black', 'White', 'Female', 'Male', '25_45', 'Greater_than_45',
##       'Less_than_25', 'Divorced', 'Married', 'Separated', 'Significant_Other',
##       'Single', 'marital_status_Unknown', 'Widowed', 'age', 'priors_count',
##       'juv_offense', 'is_recid'],
##       dtype='object')
```

```
outdf.head()
```

```
##   Black  White  Female  Male  ...      age  priors_count  juv_offense  is_recid
## 0    1.0    0.0     0.0    1.0  ... -0.899307     0.154321           1         1
## 1    0.0    1.0     0.0    1.0  ...  0.540301     2.254798           0         1
## 2    0.0    1.0     1.0    0.0  ...  0.370935    -0.685869           0         0
## 3    0.0    1.0     0.0    1.0  ... -1.238039    -0.685869           1         0
## 4    0.0    1.0     1.0    0.0  ... -0.729942    -0.685869           0         0
##
## [5 rows x 18 columns]
```

Finally, we'll save the final data set for easier retrieval later.

```
# save final dataframe
output_path_data="/home/dasienga24/Statistics-Senior-Honors-Thesis/Data Sets/COMPAS/compas_seldonian_nu

outdf.to_csv(output_path_data,index=False,header=False)
print(f"Saved data file to: {output_path_data}")
```

```
## Saved data file to: /home/dasienga24/Statistics-Senior-Honors-Thesis/Data Sets/COMPAS/compas_seldonian_nu
```

Similarly, we'll save a JSON metadata file that describes the seldonian compas data set, as well specify the sensitive columns, the response variable, and the ML problem, which in our case is classification.

```
# save metadata json file
output_path_metadata="/home/dasienga24/Statistics-Senior-Honors-Thesis/Data Sets/COMPAS/metadata_compas.

metadata_dict = {
    "regime":"supervised_learning",
    "sub_regime":"classification",
    "all_col_names":list(outdf.columns),
    "label_col_names":"is_recid",
    "sensitive_col_names":["Black", "White"]
}
```

```
with open(output_path_metadata, 'w') as outfile:
    json.dump(metadata_dict, outfile, indent=2)
print(f"Saved metadata file to: {output_path_metadata}")
```

```
## Saved metadata file to: /home/dasienga24/Statistics-Senior-Honors-Thesis/Data Sets/COMPAS/metadata_c
```

We've pre-processed the data into the right format! Next, let's formulate the Seldonian ML problem before actually fitting the Seldonian algorithm.

Formulate the Seldonian ML Problem

As in Chapter 2, we first need to define the standard machine learning problem in the absence of constraints. The decision of whether to deem a defendant as being a high or low recidivism risk is a binary classification problem, where the label `is_recid` is 0 if the person is low risk and 1 if the person is high risk. We could use logistic regression and minimize an objective function, for example the logistic loss, via gradient descent to solve this standard machine learning problem as we did in the previous section. However, we observed the the logistic regression resulted in some undesirable results.

Based on the COMPAS analysis, 3 fairness definitions are most applicable:

1. Equalized odds: $\text{abs}((\text{FNR} \mid [\text{Black}]) - (\text{FNR} \mid [\text{White}])) + \text{abs}((\text{FPR} \mid [\text{Black}]) - (\text{FPR} \mid [\text{White}])) \leq \epsilon$
2. Equal opportunity: $\text{abs}((\text{FNR} \mid [\text{Black}]) - (\text{FNR} \mid [\text{White}])) \leq \epsilon$
3. Predictive equality: $\text{abs}((\text{FPR} \mid [\text{Black}]) - (\text{FPR} \mid [\text{White}])) \leq \epsilon$

The cutoffs are arbitrary, and it may be worthwhile to investigate how tight the constraint can be. In essence, these fairness constraints ensure that the FNR and FPR between Black and White defendants does not each differ by more than 0.1. The equalized odds combines these 2 constraints by ensuring the difference in FNR and the difference in FPR do not jointly differ by more than 0.2. We will take $\delta = 0.05$ to ensure 0.95 confidence.

Therefore, the Seldonian ML problem can be formulated as: using gradient descent on a logistic regression model, minimize the logistic loss, subject to either g_1 , g_2 , g_3 , or both g_2 and g_3 , with $\delta_1, \delta_2, \delta_3 = 0.05$. We'll start with g_1 and adjust as necessary.

Create the Specification Object

A complete script for reading the data and metadata files created above and creating the spec object for our Seldonian ML problem is shown below. This script will save the spec object as a pickle file called `spec.pkl` in the appropriate directory. That directory is currently set to `/home/dasienga24/Statistics-Senior-Honors-Thesis/Python/COMPAS Application/`.

```
import autograd.numpy as np

data_pth = output_path_data
metadata_pth = output_path_metadata
save_dir = "/home/dasienga24/Statistics-Senior-Honors-Thesis/Python/COMPAS Application/"
os.makedirs(save_dir, exist_ok=True)

# create dataset from data and metadata file
regime='supervised_learning'
sub_regime='classification'

loader = DataSetLoader(regime=regime)
```

```

dataset = loader.load_supervised_dataset(
    filename=data_pth,
    metadata_filename=metadata_pth,
    file_type='csv')

sensitive_col_names = dataset.meta.sensitive_col_names

# use logistic regression model
model = LogisticRegressionModel()

# set the primary objective to be log loss
primary_objective = objectives.binary_logistic_loss

```

We'll start with $\epsilon = 0.2$.

```

from seldonian.spec import createSupervisedSpec

# define behavioral constraints
epsilon = 0.2
constraint_name = "equalized_odds"
if constraint_name == "equalized_odds":
    constraint_strs = [f'abs((FNR | [Black]) - (FNR | [White])) + abs((FPR | [Black]) - (FPR | [White])) < {epsilon}']
    deltas = [0.05]

# create spec file
save_dir = "/home/dasienga24/Statistics-Senior-Honors-Thesis/Python/COMPAS Application/equalized_odds_0.2"

createSupervisedSpec(
    dataset=dataset,
    metadata_pth=metadata_pth,
    constraint_strs=constraint_strs,
    deltas=deltas,
    save_dir=save_dir,
    save=True,
    verbose=False)

```

```
## <seldonian.spec.SupervisedSpec object at 0x7ffe84779a10>
```

Next, we'll do $\epsilon = 0.1$.

```

from seldonian.spec import createSupervisedSpec

# define behavioral constraints
epsilon = 0.1
constraint_name = "equalized_odds"
if constraint_name == "equalized_odds":
    constraint_strs = [f'abs((FNR | [Black]) - (FNR | [White])) + abs((FPR | [Black]) - (FPR | [White])) < {epsilon}']
    deltas = [0.05]

# create spec file

```

```

save_dir = "/home/dasienga24/Statistics-Senior-Honors-Thesis/Python/COMPAS Application/equalized_odds_0

createSupervisedSpec(
    dataset=dataset,
    metadata_pth=metadata_pth,
    constraint_strs=constraint_strs,
    deltas=deltas,
    save_dir=save_dir,
    save=True,
    verbose=False)

## <seldonian.spec.SupervisedSpec object at 0x7ffe83e21490>

```

Next, we'll do $\epsilon = 0.05$.

```

from seldonian.spec import createSupervisedSpec

# define behavioral constraints
epsilon = 0.05
constraint_name = "equalized_odds"
if constraint_name == "equalized_odds":
    constraint_strs = [f'abs((FNR | [Black]) - (FNR | [White])) + abs((FPR | [Black]) - (FPR | [White]))'
    deltas = [0.05]

# create spec file
save_dir = "/home/dasienga24/Statistics-Senior-Honors-Thesis/Python/COMPAS Application/equalized_odds_0

createSupervisedSpec(
    dataset=dataset,
    metadata_pth=metadata_pth,
    constraint_strs=constraint_strs,
    deltas=deltas,
    save_dir=save_dir,
    save=True,
    verbose=False)

## <seldonian.spec.SupervisedSpec object at 0x7ffe84cabdd0>

```

Finally, we'll do $\epsilon = 0.01$.

```

from seldonian.spec import createSupervisedSpec

# define behavioral constraints
epsilon = 0.01
constraint_name = "equalized_odds"
if constraint_name == "equalized_odds":
    constraint_strs = [f'abs((FNR | [Black]) - (FNR | [White])) + abs((FPR | [Black]) - (FPR | [White]))'
    deltas = [0.05]

# create spec file
save_dir = "/home/dasienga24/Statistics-Senior-Honors-Thesis/Python/COMPAS Application/equalized_odds_0

```

```
createSupervisedSpec(
    dataset=dataset,
    metadata_pth=metadata_pth,
    constraint_strs=constraint_strs,
    deltas=deltas,
    save_dir=save_dir,
    save=True,
    verbose=False)
```

```
## <seldonian.spec.SupervisedSpec object at 0x7ffe86aeb690>
```

The code chunk below illustrates another way to create a spec file. This way did not work well for us.

```
spec = SupervisedSpec(
    dataset=dataset,
    model=model,
    parse_trees=parse_trees,
    sub_regime=sub_regime,
    frac_data_in_safety=0.6,
    primary_objective=primary_objective,
    initial_solution_fn=initial_solution_fn,
    use_builtin_primary_gradient_fn=True,
    optimization_technique='gradient_descent',
    optimizer='adam',
    optimization_hyperparams={
        'lambda_init' : np.array([0.5]),
        'alpha_theta' : 0.01,
        'alpha_lamb' : 0.01,
        'beta_velocity' : 0.9,
        'beta_rmsprop' : 0.95,
        'use_batches' : False,
        'num_iters' : 1500,
        'gradient_library': "autograd",
        'hyper_search' : None,
        'verbose' : True,
    }
)
```

First, the spec object takes the `dataset` and `model` objects as arguments. Next, we pass the `parse_trees` list that we defined above in the script. In our case, we only have one parse tree (because there is one parse tree per constraint), but it still must be passed as a list. We also need to pass the `sub_regime` to indicate the type of supervised ML problem, which is classification for this case. Then, we set `frac_data_in_safety=0.4`, which specifies that 60% of the data points in our data set will be used for the safety test. The remaining 40% of the points will be used for candidate selection. Next, we specify the `primary_objective` function, followed by the `initial_solution_fn`, which specifies the function we will use to provide the initial solution to candidate selection. Here, we set `initial_solution_fn=model.fit`. Because `model` refers to our `LogisticRegressionModel()` object, `model.fit` refers to that object's fit method. This method is just a wrapper for scikit-learn's `LogisticRegression` fit method. The reason we use this method to create an initial solution is so that we start gradient descent with model weights that minimize the primary objective (in the absence of constraints), that is, the logistic loss. Because we have constraints, this initial solution is not necessarily the true optimum of our optimization problem, but it can help us find the true optimum much more efficiently in some cases.

The next argument is `use_builtin_primary_gradient_fn=True`. This instructs the engine to use a function that is already part of the library to calculate the gradient of the primary objective. Recall that earlier in the script we set the primary objective to be the logistic loss with the line: `primary_objective = objectives.binary_logistic_loss`. Built-in gradients exist for some common objective functions (see <https://github.com/seldonian-toolkit/Engine/blob/main/seldonian/models/objectives.py>), including the binary logistic loss. Setting `use_builtin_primary_gradient_fn=False` will cause the engine to use automatic differentiation to calculate the gradient of the primary objective instead. While automatic differentiation will work, using a built-in function for the gradient can speed up execution in some cases.

The next argument is `optimization_technique='gradient_descent'`, which specifies how we will search for a candidate solution during candidate selection. The other option for this argument is `'barrier_function'`. The argument `optimizer='adam'` instructs the code to use the Adam optimizer during gradient descent. The final argument, `optimization_hyperparams`, is for setting the parameters of gradient descent, which include:

- `'lambda_init'`: the initial value of the Lagrange multiplier(s).
- `'alpha_theta'`: the initial learning rate for the model parameters.
- `'alpha_lamb'`: the initial learning rate for the Lagrange multiplier(s).
- `'beta_velocity'`: the decay rate of the velocity (also called momentum) term.
- `'beta_rmsprop'`: the decay rate of the rmsprop term (adaptive learning rate optimization algorithm).
- `'use_batches'`: whether to use mini batches for gradient descent.
- `'num_iters'`: the number of iterations of gradient descent to run. This is only used if `'use_batches'` is False. Otherwise, the batch size and number of epochs determine the number of iterations.
- `'gradient_library'`: the library to use for calculating gradients automatically. Currently “autograd” is the only option.
- `'hyper_search'`: how to conduct search over hyper-parameters. Set to None which does not perform a search.
- `'verbose'`: whether to print out iteration progress during gradient descent.

Running the Seldonian Engine

We are now ready to run the Seldonian algorithm using the spec files generated in the previous step. The code below modifies some defaults of the spec object that we created and then runs the Seldonian algorithm using the modified spec object.

For $\epsilon = 0.2$:

```
from seldonian.seldonian_algorithm import SeldonianAlgorithm
from seldonian.utils.io_utils import load_pickle

# load the spec file
specfile = '/home/dasienga24/Statistics-Senior-Honors-Thesis/Python/COMPAS Application/equalized_odds_0
spec = load_pickle(specfile)
SA_02 = SeldonianAlgorithm(spec)
passed_safety, solution = SA_02.run(write_cs_logfile=True)
if passed_safety:
    print("Passed safety test!")
else:
    print("Failed safety test")

## Passed safety test!

print()
```

```

print("Primary objective (log loss) evaluated on safety dataset:")

## Primary objective (log loss) evaluated on safety dataset:
print(SA_02.evaluate_primary_objective(branch='safety_test',theta=solution))

## 0.610179143199577

```

We got a solution! Therefore, we are 95% confident that the equalized odds – ‘abs((FNR | [Black]) - (FNR | [White])) + abs((FPR | [Black]) - (FPR | [White])) – <= 0.2’.

For $\epsilon = 0.1$:

```

from seldonian.seldonian_algorithm import SeldonianAlgorithm
from seldonian.utils.io_utils import load_pickle

# load the spec file
specfile = '/home/dasienga24/Statistics-Senior-Honors-Thesis/Python/COMPAS Application/equalized_odds_0
spec = load_pickle(specfile)
SA_01 = SeldonianAlgorithm(spec)
passed_safety, solution = SA_01.run(write_cs_logfile=True)
if passed_safety:
    print("Passed safety test!")
else:
    print("Failed safety test")

## Passed safety test!
print()

print("Primary objective (log loss) evaluated on safety dataset:")

## Primary objective (log loss) evaluated on safety dataset:
print(SA_01.evaluate_primary_objective(branch='safety_test',theta=solution))

## 0.6269724706856237

```

We got a solution! Therefore, we are 95% confident that the equalized odds – ‘abs((FNR | [Black]) - (FNR | [White])) + abs((FPR | [Black]) - (FPR | [White])) – <= 0.1’. Notice that the log odds is larger than before.

For $\epsilon = 0.01$:

```

from seldonian.seldonian_algorithm import SeldonianAlgorithm
from seldonian.utils.io_utils import load_pickle

# load the spec file
specfile = '/home/dasienga24/Statistics-Senior-Honors-Thesis/Python/COMPAS Application/equalized_odds_0
spec = load_pickle(specfile)

```

```

SA_001 = SeldonianAlgorithm(spec)
passed_safety, solution = SA_001.run(write_cs_logfile=True)
if passed_safety:
    print("Passed safety test!")
else:
    print("Failed safety test")

## Passed safety test!
print()

print("Primary objective (log loss) evaluated on safety dataset:")

## Primary objective (log loss) evaluated on safety dataset:
print(SA_001.evaluate_primary_objective(branch='safety_test',theta=solution))

## 0.6540658292185901

```

We got a solution! Therefore, we are 95% confident that the equalized odds – ‘ $\text{abs}((\text{FNR} \mid [\text{Black}]) - (\text{FNR} \mid [\text{White}])) + \text{abs}((\text{FPR} \mid [\text{Black}]) - (\text{FPR} \mid [\text{White}])) - \leq 0.01$ ’. Notice that the log odds is larger than before.

Finally, for $\epsilon = 0.05$:

```

from seldonian.seldonian_algorithm import SeldonianAlgorithm
from seldonian.utils.io_utils import load_pickle

# load the spec file
specfile = '/home/dasienga24/Statistics-Senior-Honors-Thesis/Python/COMPAS Application/equalized_odds_0
spec = load_pickle(specfile)
SA_005 = SeldonianAlgorithm(spec)
passed_safety, solution = SA_005.run(write_cs_logfile=True)
if passed_safety:
    print("Passed safety test!")
else:
    print("Failed safety test")

## Passed safety test!
print()

print("Primary objective (log loss) evaluated on safety dataset:")

## Primary objective (log loss) evaluated on safety dataset:
print(SA_005.evaluate_primary_objective(branch='safety_test',theta=solution))

## 0.6440689557895964

```

We got a solution! Therefore, we are 95% confident that the equalized odds – ‘ $\text{abs}((\text{FNR} \mid [\text{Black}]) - (\text{FNR} \mid [\text{White}])) + \text{abs}((\text{FPR} \mid [\text{Black}]) - (\text{FPR} \mid [\text{White}])) - \leq 0.05$ ’.

We've obtained our solutions, but let's match the predictions to individual defendants.

Obtain the Predictive Values

For $\epsilon = 0.2$:

```
# get the solution
SA_02.cs_result["candidate_solution"]

## array([-0.52696066, -0.33697273,  0.16595447, -0.270598   ,  0.41665413,
##        -0.38267721,  0.09327715, -0.25506438, -0.67330972,  0.25834798,
##        -0.07264601,  0.31410687,  0.1522012  , -0.51927429,  0.42354113,
##        0.26008067])

# store the coefficients
coefficients = SA_02.cs_result["candidate_solution"]

# get the intercept
intercept = coefficients[0]

# separate the predictor variables from the sensitive variable and the response variable
X_outdf = outdf.drop(columns = ['is_recid', 'Black', 'White'])
X_sens = outdf[['Black', 'White']]
y_outdf = outdf['is_recid']

# compute the predictive values
linear_combination = np.dot(X_outdf, coefficients[1:]) + intercept
pred_probs_02 = 1 / (1 + np.exp(-linear_combination))
```

For $\epsilon = 0.1$:

```
# get the solution
SA_01.cs_result["candidate_solution"]

## array([-0.53854853, -0.22828825,  0.12810261, -0.20926012,  0.17240756,
##        -0.24766205,  0.23502088, -0.24273309, -0.43752558,  0.14241691,
##        -0.11293855,  0.07772611,  0.15926157, -0.2363721  ,  0.19387598,
##        0.23217029])

# store the coefficients
coefficients = SA_01.cs_result["candidate_solution"]

# get the intercept
intercept = coefficients[0]

# compute the predictive values
linear_combination = np.dot(X_outdf, coefficients[1:]) + intercept
pred_probs_01 = 1 / (1 + np.exp(-linear_combination))
```

For $\epsilon = 0.05$:

```
# get the solution
SA_005.cs_result["candidate_solution"]

## array([-0.52428854, -0.05963897,  0.10246825, -0.2647602 ,  0.52344601,
##        -0.47007818,  0.29167096, -0.10431779, -0.31209392,  0.06480644,
##        -0.13715609,  0.1578141 ,  0.29616349, -0.35833974,  0.11026368,
##        0.0842359 ])
```

```
# store the coefficients
coefficients = SA_005.cs_result["candidate_solution"]

# get the intercept
intercept = coefficients[0]

# compute the predictive values
linear_combination = np.dot(X_outdf, coefficients[1:]) + intercept
pred_probs_005 = 1 / (1 + np.exp(-linear_combination))
```

For $\epsilon = 0.01$:

```
# get the solution
SA_001.cs_result["candidate_solution"]

## array([-0.60996182, -0.00859643,  0.03027057, -0.05611803,  0.12347005,
##        -0.12732562,  0.04983803, -0.05994502, -0.0958877 ,  0.00491368,
##        -0.05200155, -0.0498986 , -0.00169219, -0.08723298,  0.00974704,
##        0.03265784])
```

```
# store the coefficients
coefficients = SA_001.cs_result["candidate_solution"]

# get the intercept
intercept = coefficients[0]

# compute the predictive values
linear_combination = np.dot(X_outdf, coefficients[1:]) + intercept
pred_probs_001 = 1 / (1 + np.exp(-linear_combination))
```

Now, let's store all of these results.

```
seldonian_results = pd.DataFrame({'is_recid': y_outdf, 'pred_0.2': pred_probs_02, 'pred_0.1': pred_probs_01, 'pred_0.05': pred_probs_005, 'pred_0.01': pred_probs_001})
seldonian_results = pd.concat([X_outdf, X_sens, seldonian_results], axis = 1)
```

```
seldonian_results.head()
```

```
##   Female  Male  25_45  ...  pred_0.1  pred_0.05  pred_0.01
## 0     0.0   1.0   0.0  ...   0.426441   0.353076   0.343800
## 1     0.0   1.0   1.0  ...   0.395750   0.316755   0.328944
## 2     1.0   0.0   1.0  ...   0.212539   0.232475   0.317406
## 3     0.0   1.0   0.0  ...   0.406317   0.359668   0.348634
```

```
## 4      1.0    0.0    1.0    ...  0.235184    0.317114    0.336790
##
## [5 rows x 22 columns]
```

Finally, let's obtain binary risk predictions.

```
# define threshold
threshold = 0.5

# create risk columns
risk_02 = np.where(pred_probs_02 >= threshold, 1, 0)
risk_01 = np.where(pred_probs_01 >= threshold, 1, 0)
risk_005 = np.where(pred_probs_005 >= threshold, 1, 0)
risk_001 = np.where(pred_probs_001 >= threshold, 1, 0)

# add risk columns to dataframe
seldonian_results['risk_0.2'] = risk_02
seldonian_results['risk_0.1'] = risk_01
seldonian_results['risk_0.05'] = risk_005
seldonian_results['risk_0.01'] = risk_001

seldonian_results.head()
```

```
##      Female  Male  25_45  ...  risk_0.1  risk_0.05  risk_0.01
## 0      0.0    1.0    0.0  ...          0          0          0
## 1      0.0    1.0    1.0  ...          0          0          0
## 2      1.0    0.0    1.0  ...          0          0          0
## 3      0.0    1.0    0.0  ...          0          0          0
## 4      1.0    0.0    1.0  ...          0          0          0
##
## [5 rows x 26 columns]
```

Evaluating Performance

We will evaluate performance on the entire data set for simplicity, even though only 40% was used to train the model.

Before that, let's switch back to R!

```
# write the dataframe to a CSV file
seldonian_results.to_csv("/home/dasienga24/Statistics-Senior-Honors-Thesis/Data Sets/COMPAS/compas_seld
```

Now, let's get the confusion matrices.

```
# read in the data
seldonian_results <- read.csv("/home/dasienga24/Statistics-Senior-Honors-Thesis/Data Sets/COMPAS/compas
```

```
epsilon = 0.2
```

```
tally(data = seldonian_results, risk_0.2 ~ is_recid)
```

```
##      is_recid
```

```
## risk_0.2    0    1
##           0 4803 2222
##           1  299  599
```

This model performs comparably to the logistic regression, with 68.2% accuracy.

```
(599 + 4803) / 7923
```

```
## [1] 0.6818124
```

This means that ~32% of defendants are misclassified in the incorrect recidivism prediction. ### epsilon = 0.1

```
tally(data = seldonian_results, risk_0.1 ~ is_recid)
```

```
##           is_recid
## risk_0.1    0    1
##           0 5043 2667
##           1   59  154
```

This model has an accuracy of 65.59%.

```
(154 + 5043) / 7923
```

```
## [1] 0.6559384
```

epsilon = 0.05

```
tally(data = seldonian_results, risk_0.05 ~ is_recid)
```

```
##           is_recid
## risk_0.05    0    1
##           0 5085 2780
##           1   17   41
```

This model has an accuracy of 64.7%.

```
(41 + 5085) / 7923
```

```
## [1] 0.6469772
```

epsilon = 0.01

```
tally(data = seldonian_results, risk_0.01 ~ is_recid)
```

```
##           is_recid
## risk_0.01    0    1
##           0 5102 2821
```

This model has an accuracy of 64.4%.

```
(5102)/ 7923
```

```
## [1] 0.643948
```

Notice that as the constraint gets tighter, the accuracy drops. The models also get worse and worse at making positive predictions, with the final model classifying everything in the negative class and resulting in an accuracy of 64.4%.

The accuracy differences are not drastic. However, the real determinant of this models' performances is the difference in FPR v FNR for Black v White defendants since that is our fairness constraint. We are 95% confident that our conditions are met. Let's actually observe what we obtain as our results.

Demographic and 'Fairness' Analysis

Before we perform the demographic analysis, let's reconstruct the `race` column.

```
seldonian_results <- seldonian_results %>%
  mutate(race = ifelse(Black == 1, 'Black', 'White'),
         pred_risk_0.2 = ifelse(risk_0.2 == 0, 'Low', 'High'),
         pred_risk_0.1 = ifelse(risk_0.1 == 0, 'Low', 'High'),
         pred_risk_0.05 = ifelse(risk_0.05 == 0, 'Low', 'High'),
         pred_risk_0.01 = ifelse(risk_0.01 == 0, 'Low', 'High'))

head(seldonian_results)
```

	Female	Male	X25_45	Greater_than_45	Less_than_25	Divorced	Married	Separated
## 1	0	1	0	0	1	0	0	0
## 2	0	1	1	0	0	0	0	0
## 3	1	0	1	0	0	0	0	0
## 4	0	1	0	0	1	0	0	0
## 5	1	0	1	0	0	0	1	0
## 6	0	1	1	0	0	0	0	0

	Significant_Other	Single	marital_status_Unknown	Widowed	age
## 1		0	1	0	-0.8993073
## 2		0	1	0	0.5403005
## 3		0	1	0	0.3709349
## 4		0	1	0	-1.2380386
## 5		0	0	0	-0.7299417
## 6		0	1	0	-0.6452589

	priors_count	juv_offense	Black	White	is_recid	pred_0.2	pred_0.1	pred_0.05	
## 1	0.1543213		1	1	0	1	0.4940252	0.4264412	0.3530761
## 2	2.2547979		0	0	1	1	0.4925469	0.3957500	0.3167549
## 3	-0.6858694		0	0	1	0	0.1557379	0.2125391	0.2324745
## 4	-0.6858694		1	0	1	0	0.4492105	0.4063170	0.3596677
## 5	-0.6858694		0	0	1	0	0.2139884	0.2351842	0.3171144
## 6	-0.6858694		0	0	1	0	0.3408120	0.3289149	0.3389132

	pred_0.01	risk_0.2	risk_0.1	risk_0.05	risk_0.01	race	pred_risk_0.2
## 1	0.3437996	0	0	0	0	Black	Low
## 2	0.3289440	0	0	0	0	White	Low
## 3	0.3174055	0	0	0	0	White	Low


```
## 4 0.3486342      0      0      0      0 White      Low
## 5 0.3367901      0      0      0      0 White      Low
## 6 0.3456517      0      0      0      0 White      Low
##   pred_risk_0.1 pred_risk_0.05 pred_risk_0.01
## 1           Low           Low           Low
## 2           Low           Low           Low
## 3           Low           Low           Low
## 4           Low           Low           Low
## 5           Low           Low           Low
## 6           Low           Low           Low
```

We can now reconstruct the tables.

epsilon = 0.2

First, let's re-examine the confusion matrix to determine whether the model makes more false negative or more false positive results.

The first table depicts the raw numbers and the second table interprets that in terms of proportions in order to better understand the magnitude.

The model correctly classifies 599 defendants as reoffenders and 4803 defendants as non-reoffenders. 2222 defendants who reoffend are classified as low risk, whereas 299 defendants who did not reoffend are classified as high risk. The model does a better job at classifying those who do not reoffend, as is expected because there is more data for that group. In general, the trends are consistent with what we observed in the COMPAS tool's results.

```
seldonian_results %>%
  dplyr::select(pred_risk_0.2, is_recid) %>%
  rename("Risk" = pred_risk_0.2) %>%
  group_by(Risk) %>%
  summarise("Reoffended" = count(is_recid == 1),
            "Did Not Reoffend" = count(is_recid == 0)) %>%
  kable()
```

Risk	Reoffended	Did Not Reoffend
High	599	299
Low	2222	4803

When looking at the proportions, 94% of participants who did not reoffend are correctly classified as low risk. This means only 6% of participants who do not reoffend are classified as high risk. This is a lower FPR than the logistic regression and COMPAS tool.

On the flip side, only 21% of defendants who reoffended are correctly classified as high risk. This means 79% of defendants who reoffended are classified as low risk. This is a higher FNR than the logistic regression and COMPAS.

The model, overall, has worse false negative rates than false positive rates. While this is the same general trend observed in the logistic regression and the COMPAS tool, the discrepancy is much larger.

Because of the imbalanced data, such models are prone to higher FNR rates than FPR rates.

```
seldonian_results %>%
  dplyr::select(pred_risk_0.2, is_recid) %>%
  rename("Risk" = pred_risk_0.2) %>%
```

```

group_by(is_recid) %>%
mutate(Total = n()) %>%
group_by(Risk, Total) %>%
summarise("Reoffended" = count(is_recid == 1),
          "Did Not Reoffend" = count(is_recid == 0)) %>%
mutate(Reoffended = round(100 * Reoffended / Total, 2),
       `Did Not Reoffend` = round(100 * `Did Not Reoffend` / Total, 2)) %>%
dplyr::select(-Total) %>%
group_by(Risk) %>%
summarize(Reoffended = max(Reoffended, na.rm = TRUE),
          `Did Not Reoffend` = max(`Did Not Reoffend`, na.rm = TRUE)) %>%
kable()

```

Risk	Reoffended	Did Not Reoffend
High	21.23	5.86
Low	78.77	94.14

Now, let's examine these false positive and false negative rates along racial lines for Black v White defendants.

Recall that the overall FPR rate for the model is 5.86%. We still observe similar trends to the logistic regression model. The FPR for Black defendants is still higher than that of White defendants. Observe that the FPR for Black defendants is now 8.88%, lower than the previous 13.93%. On the flip side, the FPR for White defendants is 2.24%, lower than the previous 5.09%. There is still a discrepancy, but there was a decrease in FPR for both races.

Recall that the overall FNR rate for the model is 78.77%. We still observe similar trends to the logistic regression model. The FNR for Black defendants is still lower than that of White defendants. Observe that the FNR for Black defendants is now 73.82%, much higher than the previous 60.82%. On the flip side, the FNR for White defendants is 88.82%, only slightly higher than the previous 86.17%. There is still a discrepancy, but there was an increase in FNR for both races, significantly higher for Black defendants.

```

seldonian_results %>%
dplyr::select(race, pred_risk_0.2, is_recid) %>%
rename("Risk" = pred_risk_0.2,
       "Race" = race) %>%
group_by(Race, is_recid) %>%
mutate(Total = n()) %>%
group_by(Risk, Race, Total) %>%
summarise("Reoffended" = count(is_recid == 1),
          "Did Not Reoffend" = count(is_recid == 0)) %>%
pivot_longer(cols = c("Reoffended", "Did Not Reoffend"),
             names_to = "Recidivism") %>%
pivot_wider(
  id_cols = c("Risk", "Recidivism", "Total"),
  names_from = "Race",
  values_from = value
) %>%
mutate(Black = round(100 * Black / Total, 2),
       White = round(100 * White / Total, 2)) %>%
dplyr::select(-Total) %>%
group_by(Risk, Recidivism) %>%
summarize(Black = max(Black, na.rm = TRUE),
          White = max(White, na.rm = TRUE)) %>%
filter((Risk == "High" & Recidivism == "Did Not Reoffend") |

```

```

      (Risk == "Low" & Recidivism == "Reoffended")
    ) %>%
    kable(booktabs = TRUE)

```

Risk	Recidivism	Black	White
High	Did Not Reoffend	8.88	2.24
Low	Reoffended	73.82	88.82

We'll only reconstruct this final table, which is the most important for us, for the remaining epsilon values.

epsilon = 0.1

```

seldonian_results %>%
  dplyr::select(race, pred_risk_0.1, is_recid) %>%
  rename("Risk" = pred_risk_0.1,
         "Race" = race) %>%
  group_by(Race, is_recid) %>%
  mutate(Total = n()) %>%
  group_by(Risk, Race, Total) %>%
  summarise("Reoffended" = count(is_recid == 1),
            "Did Not Reoffend" = count(is_recid == 0)) %>%
  pivot_longer(cols = c("Reoffended", "Did Not Reoffend"),
               names_to = "Recidivism") %>%
  pivot_wider(
    id_cols = c("Risk", "Recidivism", "Total"),
    names_from = "Race",
    values_from = value
  ) %>%
  mutate(Black = round(100 * Black / Total, 2),
         White = round(100 * White / Total, 2)) %>%
  dplyr::select(-Total) %>%
  group_by(Risk, Recidivism) %>%
  summarise(Black = max(Black, na.rm = TRUE),
            White = max(White, na.rm = TRUE)) %>%
  filter((Risk == "High" & Recidivism == "Did Not Reoffend") |
         (Risk == "Low" & Recidivism == "Reoffended"))
  ) %>%
  kable(booktabs = TRUE)

```

Risk	Recidivism	Black	White
High	Did Not Reoffend	1.87	0.30
Low	Reoffended	93.13	97.42

epsilon = 0.05

```

seldonian_results %>%
  dplyr::select(race, pred_risk_0.05, is_recid) %>%
  rename("Risk" = pred_risk_0.05,
         "Race" = race) %>%
  group_by(Race, is_recid) %>%
  mutate(Total = n()) %>%

```

```

group_by(Risk, Race, Total) %>%
summarise("Reoffended" = count(is_recid == 1),
          "Did Not Reoffend" = count(is_recid == 0)) %>%
pivot_longer(cols = c("Reoffended", "Did Not Reoffend"),
              names_to = "Recidivism") %>%
pivot_wider(
  id_cols = c("Risk", "Recidivism", "Total"),
  names_from = "Race",
  values_from = value
) %>%
mutate(Black = round(100 * Black / Total, 2),
       White = round(100 * White / Total, 2)) %>%
dplyr::select(-Total) %>%
group_by(Risk, Recidivism) %>%
summarize(Black = max(Black, na.rm = TRUE),
          White = max(White, na.rm = TRUE)) %>%
filter((Risk == "High" & Recidivism == "Did Not Reoffend") |
       (Risk == "Low" & Recidivism == "Reoffended"))
) %>%
kable(booktabs = TRUE)

```

Risk	Recidivism	Black	White
High	Did Not Reoffend	0.29	0.39
Low	Reoffended	98.73	98.17

epsilon = 0.01

```

seldonian_results %>%
dplyr::select(race, pred_risk_0.01, is_recid) %>%
rename("Risk" = pred_risk_0.01,
       "Race" = race) %>%
group_by(Race, is_recid) %>%
mutate(Total = n()) %>%
group_by(Risk, Race, Total) %>%
summarise("Reoffended" = count(is_recid == 1),
          "Did Not Reoffend" = count(is_recid == 0)) %>%
pivot_longer(cols = c("Reoffended", "Did Not Reoffend"),
              names_to = "Recidivism") %>%
pivot_wider(
  id_cols = c("Risk", "Recidivism", "Total"),
  names_from = "Race",
  values_from = value
) %>%
mutate(Black = round(100 * Black / Total, 2),
       White = round(100 * White / Total, 2)) %>%
dplyr::select(-Total) %>%
group_by(Risk, Recidivism) %>%
summarize(Black = max(Black, na.rm = TRUE),
          White = max(White, na.rm = TRUE)) %>%
filter((Risk == "High" & Recidivism == "Did Not Reoffend") |
       (Risk == "Low" & Recidivism == "Reoffended"))
) %>%
kable(booktabs = TRUE)

```

Risk	Recidivism	Black	White
Low	Reoffended	100	100

Results

The false positive rates gain more parity as we tighten ϵ , but we lose model accuracy! The key question this brings up is: how do we balance these trade-offs?

In conclusion, when $\epsilon = 0.2$, the Seldonian algorithm still exhibits discrepancies between the FPR and FNR for Black v White defendants, which perhaps is unavoidable because of the role that race plays in proxy variables. However, there was barely any accuracy trade-off, and we saw an increase in FNR for both races, accompanied by a decrease in FPR for both races. There is still inequality, although less than before, and everyone is just a little bit happier.

However, as we tighten ϵ , this discrepancy begins to disappear and we get fairer results at the cost of the FNR. At a certain threshold, the model just classifies everything into the negative class.