# Predict 2028 Olympics Medal Table: Hierarchical Adaptive Prediction Framework with LSTM-Attention Mechanism

### **Summary**

In this study, we explored the dynamics of Olympic medal predictions and the specific manifestations of the great coach effect. By leveraging historical data and advanced modeling techniques, we developed two key models: one for predicting the gold medal and overall medal counts for the 2028 Los Angeles Summer Olympics which is called **HAPF-LSTM**, and another for quantifying the impact of exceptional coaches on medal outcomes. Our analysis not only provided insights into potential medal distributions, aiding each nation's Olympic Committee in strategic adjustments but also offering investment recommendations in **great coach effect** for three countries.

The first model provided a detailed **hierarchical adaptive** forecast for the 2028 Olympics, identifying medal distribution patterns and performance trends among nations. By integrating historical data and **feature engineering**, we quantified characteristics like dominance, and fierceness of competitions, which came from either nation's and certain Olympic year's aspects. The model **progressively** uses the main data group by going through **random-forests-classifier** for predictions of whether will achieve a medal and then going through the regressor powered by **MLP**, with the collaboration of additional important data group. Differences in going through **various branches** mainly depend on a **timely judgment** of whether a country is competitive enough. **LSTM-Attention mechanism** is introduced to the model to drive the training and evaluation. The model offered insights into countries that are steadily competitive and those hardly having achieved any medals. These predictions not only informed audience expectations but also provided strategic guidance to national Olympic committees for refining their sports development strategies.

The second model, leveraging a data-driven approach, confirmed the existence of the **great coach effect** and quantified its influence on medal counts. The study highlighted the significant role that top-level coaches play in enhancing medal performance. Furthermore, it identified three additional factors, **Sports Powerhouse**, **Stable Athlete Pool** and **Historical Success** which are based on insights from relevant research, that can help determine which sporting events would benefit most from the investment in a great coach. This **quantitative analysis** highlighted the significant impact of exceptional coaching on athletic success, specifically identifying Sailing in Great Britain, Boxing in the United States, and Trampoline Gymnastics in China as key areas for improvement.

By integrating various methods and incorporating diverse variables, our model demonstrates robustness and stability, ensuring reliable performance even with noisy or incomplete data. Future research could build on these findings by incorporating additional variables, such as athlete development programs, technological advancements, and socio-economic factors, to further refine predictions and deepen insights.

**Keywords:** Olympics, medal estimation, hybrid model, Random Forest, LSTM, Attention, MLP, great coach effect

# **Contents**

1		roduction	1
	1.1	Problem Background	1
	1.2 1.3	Restatement of the Problem	7
	1.3	Literature Review	2
	1.4	Our work	-
2		neral Assumptions and Notations	3
	2.1	Assumptions	3
	2.2	Notations	4
3	Data	a Preprocessing and Analysis	4
	3.1	Data Preprocessing	4
	3.2		5
4	HAI	PF-LSTM: Hierarchical Adaptive Prediction Framework Driven by LSTM-Attention	
-		chanism	8
	4.1	Feature Selection	8
		4.1.1 Feature for Participating Nation	8
		4.1.2 Feature for certain Olympic year	ç
			10
	4.2	Main body of HAPF-LSTM	11
		4.2.1 Overview	11
		4.2.2 Data Grouping and engineering	11
		4.2.3 Core Inner Structure: Hierarchical Adaptive Prediction Framework	12
		4.2.4 Temporal prediction: LSTM-Attention Driven mechanism	14
	4.3	Result	14
5	Gre	at Coach Effect Analysis	14
	5.1	Great Coach Effect Quantification	
	5.2	Investment Suggestions	16
6	Oth	er Insight and Suggestions	18
7	Mod	del Evaluation	19
	7.1	Sensitivity Analysis	
	7.2	Robustness Analysis	
8	Stre	engths and Weaknesses	20
U	8.1	Strengths	
	8.2	Weaknesses	
9			21
J	COII	Cusion	<b>4</b> ]
R	feren	nces	2.2

## Team 2502406

A	Prediction medal table for 2028 Los Angeles, USA summer Olympics	23
В	Additional Code	25
C	Report on Use of AI	88

## 1 Introduction

## 1.1 Problem Background

The Olympic Games represent a unique global spectacle, featuring athletes from more than 200 countries competing in more than 400 events in both the Summer and Winter Games. This prestigious multi-sport event not only showcases competition but also fosters inspiration and unity among participants and spectators worldwide [5].

During the 2024 Summer Olympics, Paris became the center of sport enthusiasts around the world. Spectators focused not only on the outcomes of individual events but also on the national rankings in the medal tally. The United States and China performed notably, each securing an equal number of gold medals, demonstrating their formidable prowess in global sports. Meanwhile, the host nation France, although ranked fifth in gold medals, secured the fourth position in total medals, suggesting that the home advantage may have positively influenced their performance. Additionally, this Olympics witnessed breakthroughs by smaller nations such as Saint Lucia and Albania, which not only won Olympic medals for the first time but also captured gold, marking significant progress in their sporting achievements. This phenomenon indicates that the Olympics not only serve as a competitive arena for sports powerhouses but also provide a platform for smaller nations to showcase their developmental strides.

With the progression of globalization and the rise of social media, there is an increasing focus on sports events, especially massive competitions like the Olympics [3]. Medal predictions for the Olympics not only satisfy the curiosity of the audience but also offer substantive guidance to national Olympic committees to improve their countries' standings on the medal table. Predictions are typically based on the athletes' capabilities and past performances, yet the outcomes of the Games are often filled with uncertainties. This unpredictability not only enhances the spectacle of the competitions but also makes forecasting a challenging task.

#### 1.2 Restatement of the Problem

#### • Question 1:

The first question can be divided into three sub-questions. The first sub-question involves predicting the medal tally for the 2028 Los Angeles Summer Olympics, including all result intervals, and analyzing which countries are likely to perform better or worse compared to 2024. The second sub-question estimates the number of countries that might win their first Olympic medals in 2028 and discusses the likelihood of these predictions. The final sub-question explores how the number and type of events influence the distribution of medals among competing nations, identifies key sports crucial to different countries and the reasons why, and assesses how the selection of events by the host nation might impact the outcomes of the games.

#### • Question 2:

Through data analysis, investigate whether there are performance changes that can be attributed to the influence of great coaches. Please evaluate the extent of this impact on medal count. Subsequently, select three countries and analyze which sports could benefit from investing in

top-level coaches, and estimate the potential effectiveness of this strategy.

#### • Question 3:

Analyze the Olympic medal counts predicted by the existing model and provide unique insights to inform the national Olympic committees.

#### 1.3 Literature Review

With the rapid development of social media and the growing aspiration of people for a higher quality of life, the Olympic Games, an ancient and prestigious sporting event, have captured unprecedented levels of global attention in the 21st century [5]. As a result, predicting the Olympic medal counts each year has also become a focal point for audiences.

For each Olympic Games, a significant amount of literature provides predictions. For example, Sanchez-Fernandez et al. describe the process of predicting the distribution of Olympic medals. By analyzing the accuracy of predictions made for the 2012 London Olympics, it further predicts the medal distribution for the 2016 Rio Olympics and provides the medal rankings for each country [8]. There is another study that aimed to predict the success of countries participating in the Tokyo 2020 Olympics using smart methods, including the PEST+S model and neural network modeling [4]. Nagpal's team mainly discusses the status of the Olympics as a top international sporting event and uses data from the 2020 Tokyo Olympics to predict the medal counts for the 2024 Paris Olympics [7]. The above studies focused on predicting medal counts for the 2016 Rio Olympics, the 2020 Tokyo Olympics, and the 2024 Paris Olympics. From this, we can observe that forecasting the distribution of gold medals for each edition of the Olympic Games has become a consistent and enduring tradition. This practice reflects not only the audience's fascination with the competitive outcomes but also the broader interest in analyzing patterns, trends, and factors that influence athletic success on the global stage [5]. Such predictions serve as a bridge between historical performance and future expectations, enriching the Olympic experience for fans, researchers, and stakeholders alike.

Scelles et al. provide a wealth of recommendations on feature selection for predicting the gold medal tally in his paper. Including the population size of a country four years prior to the Olympic Games, the country's economic development, the host country effect, country regions, medal totals four years earlier and so on [9]. For prediction model selection, Varagiri Shailaja's team experimented with some common algorithm including Decision Tree, KNN, Linear Regression, Random Forest Algorithm and Bayesian Ridge Algorithm [11]. Moreover, Edward M. Condon built linear regression models and neural network models and afterwards compared them, indicating the neural network model outperformed the regression model [3]. Christoph Schlembach proposed a socioeconomic machine learning model including Tobit model and Hurdle modeel [10]. The Tobit model is a type of regression model designed to handle censored dependent variables, where the observed values are either partially or entirely limited by a threshold (e.g., non-negative variables like income or scores) [1]. It is commonly used in cases where the dependent variable is restricted in range, allowing for the estimation of relationships while accounting for the censoring effect, providing more accurate and meaningful results than standard linear regression [6]. The above literature on variable selection and model choice provides a solid foundation for our work.

#### 1.4 Our Work

We began by collecting relevant literature on the topic, learning from previous research on medal prediction. We are initiating the processes of data pre-processing and data analysis. After that, we proceeded to build our models.

The first model, Hierarchical Adaptive Prediction Framework Driven by LSTM-Attention Mechanism (HAPF-LSTM), is designed to predict the gold and overall medals for 2028 Olympics. We analyzed data from two perspectives: the characteristics of participating countries and the features of events in each Olympic year. Participating-nation-factors such as host nation status, athlete quality, and event dominance, as well as certain-Olympic-year-features like the competition intensity and the number of events, were integrated into different parts of the model for prediction. This approach achieved strong predictive performance. To account for differences between countries, we designed specialized model branches for those with low medal prospects and consistently top-ranked nations, allowing for tailored prediction strategies. Additionally, we applied the 'LSTM + Attention' mechanism to capture temporal features and fine-tuned the model with the Adam optimizer, leading to satisfactory results.

The second model is capable of accurately reflecting the great coach effect on the medal standings. We identified three additional great coaches and analyzed the changes in medal counts before and after the five coaches began coaching and the local highest value in medal count during the coaching period. These data allowed us to assess the impact of these exceptional coaches on specific events across various countries. Additionally, by examining relevant research, we identified three other critical factors that significantly influence the effectiveness and value of investing in a coach for a particular sport: Sports Powerhouse, Stable Athlete Pool and Historical Success. Using the three features we filtered the most suitable sports of coach investment.

Evaluation, strengths and weaknesses of the proposed model are discussed afterward. All source codes and the prediction medal table for 2028 Los Angeles, USA summer Olympics are attached to the Appendix.

## 2 General Assumptions and Notations

## 2.1 Assumptions

- 1. It is assumed that the collected data is authentic and reliable, with no instances of fabrication.
- 2. It is assumed that athletes from all countries compete with integrity, without resorting to substances such as doping or high-tech aids beyond the rules (such as specially designed clothing or sports equipment), and that no cheating occurs.
- 3. For sports involving referees, it is assumed that referees are fair and impartial, and there will be no intentional misjudgments, omissions, or favoritism.
- 4. The possibility of major sporting nations refusing to participate in the Olympics for various reasons is not considered, nor is the absence of athletes due to injuries or other reasons.

5. The impact of the International Olympic Committee's temporary changes to the competition rules on the performance of athletes is not considered.

#### 2.2 Notations

Symbol	Description
$TS_{i,j}$	Total score of the $i^{th}$ country in the $j^{th}$ sport.
$S_{i,j}$	Score rate of the $i^{th}$ country in the $j^{th}$ sport.
$a_{i,j}$	Number of athlete of the $i^{th}$ country in the $j^{th}$ sport.
$Q_{i,j}$	Athlete quality of the $i^{th}$ country in the $j^{th}$ sport.
$m_{j}$	Number of events in the $j^{th}$ sport
$n_{Gold}$	Number of gold medals
$n_{Silver}$	Number of silver medals
$n_{Bronze}$	Number of bronze medals
$P_{1s}$	Score achieved by the team under the coach's leadership during Period 1
$\Delta_{pre1}$	Difference in score compared to the previous term
$\Delta_{max1}$	Difference in score compared to the best performance among the previous three terms
$P_{2s}$	Score achieved by the team under the coach's leadership during Period 2
$\Delta_{pre2}$	Difference in score compared to the previous term
$\Delta_{max2}$	Difference in score compared to the best performance among the previous three terms
δ	If it is a team event

## 3 Data Preprocessing and Analysis

## 3.1 Data Preprocessing

After reviewing the provided dataset, we find that only one file which is called summerOly\_programs.csv contains some missing or anomalous data points. First, we address the missing values by replacing all of them with a question mark. Following that, we handle outliers, which includes removing irrelevant information, deleting columns related to competitions outside the Olympic cycle, and eliminating rows with incomplete data. In the 'Sports Governing Body' column, replace question marks with NULL, and then substitute any other occurrences of question mark with the number 0. After completing these operations, we recalculate the totals for events, disciplines, and sports and correct the data accordingly.

After addressing outliers and missing values, we further consolidated the data. First, we removed the years from the summerOly\_hosts.csv file for which the Olympic Games were not successfully held. Next, we delete the contents within parentheses to standardize the format of the host location names and use regular expressions to extract text and ensure there are no extra spaces. Finally, we used pandas to split the city and country names, then linked these with the summerOly\_medal\_counts.csv and summerOly\_athletes.csv tables to obtain the final clean and usable data.

Furthermore, there are 18 kinds of sports events that have not occurred in the past 10 years which are then deemed outdated and are therefore all removed. For example, Art competition, Alpinism, Aeronautics and so on. The naming convention of the 'sport' column in the 'athletes' table should be consistent with that in the 'programs' table.

## 3.2 Data Analysis

Through data analysis and visualization, we have created the two charts above to illustrate the trends in event count changes in sports over the years. We removed events with a count of 0, indicating that these sports were not successfully held.

Figure 1 offers a macro view of how the number of events for various sports at the Summer Olympics has evolved from 1896 to 2024. It is evident that certain events experienced significant growth in specific years, particularly newly introduced or developing sports, which reflect a more diversified trend. The scattered points and line segments signify that these events were short-lived and did not continue to appear in subsequent Olympic Games.

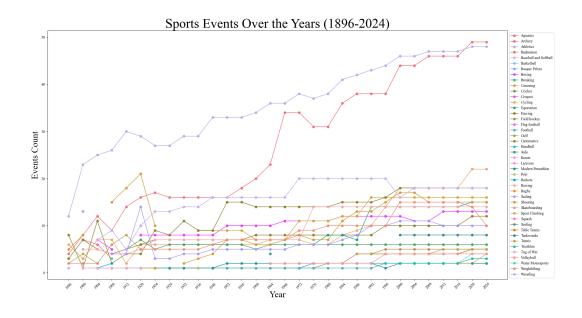


Figure 1: Sports Events Overview for The Last 30 Summer Olympic Games

Figure 2 compares the event count changes from the first 15 editions of the Olympics (1896-1964) with those from 1968 to 2024. It is clear that the first 15 editions showed more fluctuation in event

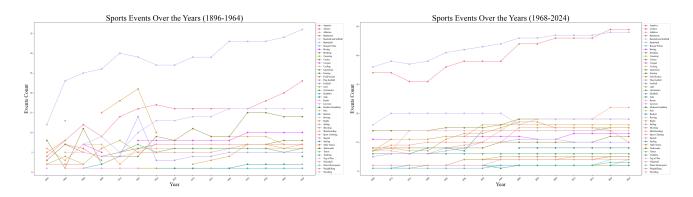


Figure 2: Comparison of Sports Events Count between 1896-1964 and 1968-2024

numbers, suggesting that the selection of sports was still in development. In contrast, the number of events in the subsequent 15 editions became more stable, indicating that the Olympic Games had reached a more mature stage. So, we brought only the second half of the Olympic years into analysis and prediction.

To explore the hosting effect, we examined changes in the event list based on different hosts and whether these align with the host's dominant sports. We also analyzed performance fluctuations when a country is the host, considering current, past, and future hosting scenarios. We subsequently randomly selected a year and the corresponding host country (1908, UK) and conducted a data visualization analysis of the host effect. Finally, we obtained the following bar chart.

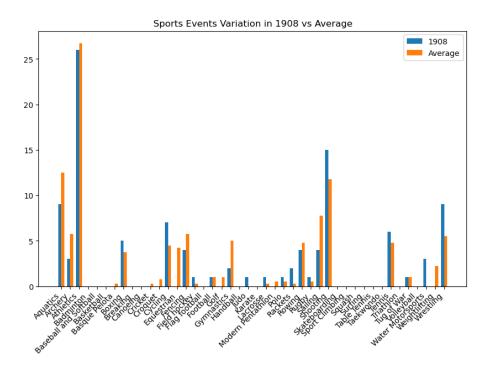


Figure 3: Visualization of the Hosting-Effect

The chart shows a comparison between the number of sports events in 1908 and the average number. The horizontal axis lists different sports, and the vertical axis represents the number of events. The blue bars represent the data from 1908, while the orange bars represent the average. From the chart, it can be seen that the number of events for certain sports in 1908 was significantly higher than the average, such as athletics and cycling, while for other sports it was lower than the average, such as baseball and basketball. This chart explains the distribution of sports events when the UK was the host in 1908, and the differences in the distribution of sports events on average when other countries were hosts. Upon further observation, we find that the host country does have some influence on the selection of sports events.

The Fourier Transform Distance is a metric method based on Fourier transformation to measure the similarity or difference between two images. The Shape Based Distance, on the other hand, assesses the similarity or difference between two objects or shapes by comparing their geometric structures. As shown in the table, we can observe the Fourier Transform Distance and Shape Based Distance data for each Olympic host country from 1896 to 2032. By analyzing these data, we can derive a coefficient table of change to reflect the trends of variation for each year. For instance, when Belgium (BEL) was the host in 1920, its Fourier Transform Distance was 117.1523775, and its Shape Based Distance was 18.13025706, indicating a significant change in the distribution of sports events compared to the average. Similarly, when Japan (JPN) was the host in 2020, its Fourier Transform Distance was 72.37198119, and its Shape Based Distance was 11.45689952, also showing a marked difference compared to the average. These data can help us understand the impact of different countries as hosts on the distribution of Olympic sports events and the trends of change between different years.

Table 1: Table of Fourier Transforms and Shape-Based Distances for Different Years and Countries

Year	NOC	Fourier Transform	<b>Shape Based Distance</b>
1896	GRE	12.44897663	2.551577259
1900	FRA	83.26921768	13.05903229
1904	USA	73.66071638	11.67650102
1908	GBR	41.39282408	6.841051889
1912	SWE	51.4455513	8.341526382
1920	BEL	117.1523775	18.13025706
1924	FRA	30.2210292	5.095189278
1928	NED	3.015353154	0.931077955
1932	USA	11.33551053	3.295729732
1936	GER	27.45071305	4.452446289
1948	GBR	17.64138247	2.98867595
1952	FIN	23.70182931	4.133668247
1956	AUS	13.7343408	2.582847666
1960	ITA	2.542094369	0.872093177
1964	JPN	14.84975411	2.667966737
1968	MEX	42.7871375	7.042558737
1972	FRG	34.78965986	5.577291953
1976	CAN	21.88883168	3.855519899
1980	URS	11.6411997	2.222258114

Year	NOC	Fourier Transform	<b>Shape Based Distance</b>
1984	USA	10.98803475	2.21474652
1988	KOR	23.57418575	4.11547974
1992	ESP	26.77025262	4.347124447
1996	USA	18.67467862	3.142705704
2000	AUS	41.075838	6.519716669
2004	GRE	17.4431855	2.960624485
2008	CHN	7.51287561	1.742737543
2012	GBR	4.764737058	1.290237613
2016	BRA	10.51872984	1.968057019
2020	JPN	72.37198119	11.45689952
2024	FRA	30.59058187	5.222303253
2028	USA		
2032	AUS		

## 4 HAPF-LSTM: Hierarchical Adaptive Prediction Framework Driven by LSTM-Attention Mechanism

#### 4.1 Feature Selection

According to the requirements, only the provided data sets are available for our training and estimation. Due to the lack of consecutive data and the limited amount of resources, we had to make great efforts on characteristic selection and engineering. In our work, we investigated these data sets in two aspects, participating nations and the Olympic year itself. Both obvious and strenuous features are included.

#### **4.1.1** Feature for Participating Nation

#### A) Typical-strenuous-feature: Total Score, Score Rate and Athlete Quality

The total score  $TS_{i,j}$  for  $i^{th}$  country in  $j^{th}$  sport event is determined by the number of medals there, with gold medals worth 3 points, silver medals worth 2 points, bronze medals worth 1 point, and no medal earns 0 points. One special sport event is expressed by the following equation:

$$TS_j = \sum_{i} 3 \times n_{Gold,i,j} + 2 \times n_{Silver,i,j} + n_{Bronze,i,j}$$
 (1)

The score rate  $S_{i,j}$  for a country in such a specific kind of sport is calculated by dividing the total score  $TS_{i,j}$  by the total number of events under such  $j^{th}$  sport  $m_j$  that the country participated in during the year. This score is then multiplied by 6 to standardize the score to a range that reflects the relative dominance level of the country. The formula is as follows:

$$S_{i,j} = \frac{TS_{i,j}}{m_j \times 6} \tag{2}$$

This score rate provides an effective metric to assess the country's overall performance in such a specific sport over the year. It normalizes the performance, accounting for the number of events participated in, and gives an insight into how well the country performed relative to others. Similarly, the athlete quality  $Q_{i,j}$  for a certain country is quantified as the total score achieved by  $i^{th}$  country and their amount of athletes  $a_{i,j}$  participating in that  $j^{th}$  sport, with the equation:

$$Q_{i,j} = \frac{TS_{i,j}}{a_{i,j}} \tag{3}$$

#### B) Typical-obvious-feature: Host-nation Status

First, we observed that there is a certain degree of overlap between the additional events over the years and the host country's advantageous events (taking 1920 as an example). We speculate that the host nation's advantageous events may have some correlation with the prediction of the number of competition events. By calculating the Score\_Rated\_Sum and then expressing it as a weighted average of the Score\_Rated\_Sum for the country in the two previous Olympic Games, we represent the host country's advantageous events.

Next, when determining the coefficient of a country relative to its most recent host year, the relationship between the current year and the year when the country last hosted the Olympics must be considered. The specific rules are as follows:

- If the current year is the year when the country hosted the Olympics, the coefficient is 3.
- If the current year is the year immediately preceding or following the year when the country hosted the Olympics, for example, one year before or after the host year, the coefficient is 2.
- If the current year is two years before or after the year when the country hosted the Olympics, for example, two years before or after the host year, the coefficient is 1.
- If the current year does not fall into any of the above categories, the coefficient is 0.

This coefficient system is designed to reflect the unique advantages and preparation levels associated with hosting the Olympic Games. Hosting the Olympics provides a country with significant benefits, including enhanced infrastructure, improved training facilities, and increased public support for sports. These factors contribute to better performance in the years surrounding the host year. The coefficient system acknowledges these advantages by assigning larger values to years closer to the host year, thereby providing a more accurate representation of a country's competitive level during these periods.

#### 4.1.2 Feature for certain Olympic year

Similarly, a certain Olympic year always has its special attributes. As demonstrated above, we can notice that there always exists a relationship between the host's dominating sports and the increment in the number of corresponding sports events. We specially picked out features like the increment of participating countries  $w_1$ , athlete  $w_2$ , number of events  $w_3$ . And then quantified  $w_4$ , which indicates the Intensity of competition to some extent, by the following formula:

$$w_4 = \frac{0.2 \times w_1 + 0.8 \times w_2}{w_3} \tag{4}$$

#### **4.1.3** Features Overview

We divide the countries into those with strong sports capabilities and those with weak sports capabilities. A country is considered to have strong sports capabilities if its score\_rate\_sum is in the top 10% of all countries, while a country is considered to have weak sports capabilities if its cumulative number of participants ranks in the bottom 20% of all countries.

Table 2: Variable Descriptions in Model 1

Variable	Type	Description
$\overline{v_1}$	INT	Whether be host country
$v_2$	LIST	Predicted number of gold medals in this edition
<i>v</i> <sub>3</sub>	LIST	Total Score, $[TS_{i,1}, TS_{i,2},, TS_{i,j},]$
$v_4$	LIST	Score Rate, $[S_{i,1}, S_{i,2},, S_{i,j},]$
<i>v</i> <sub>5</sub>	LIST	Number of participating athletes $[a_{i,1}, a_{i,2},, a_{i,j},]$
$v_6$	INT	Number of gold medals in the last edition
<i>v</i> <sub>7</sub>	INT	Coefficient of a country relative to its most recent host year
$v_8$	LIST	Athlete quality $[Q_{i,1}, Q_{i,2},, Q_{i,j},]$
$v_3^{sum}$	INT	Sum of v3
$v_4^{sum}$	INT	Sum of v4
$v_5^{sum}$	INT	Sum of v5
v <sub>5</sub> sum v <sub>8</sub> sum	INT	Sum of v8
$\overline{w_1}$	LIST	Increase in participating countries $[w_{1,1}, w_{1,2},, w_{1,j},]$
$w_2$	LIST	Increase in participating athletes $[w_{2,1}, w_{2,2},, w_{2,j},]$
$W_3$	LIST	Increase in events $[w_{3,1}, w_{3,2},, w_{3,j},]$
$w_4$	LIST	$\frac{0.2w_1+0.8w_2}{w_3}$
$W_3^{sum}$	INT	Sum of w3
$w_4^{sum}$	INT	Sum of w4
$\overline{\lambda}$	INT	Small country coefficient
$\mu$	INT	Large country coefficient

The table shows all the variables we have considered, some of which were not ultimately included in the model training for various reasons. For example, the utilization of gold medal counts (a principle that applies analogously to other types of medal) for the direct prediction of current gold medal totals may engender overfitting, thereby leading to an excessive reliance on the extrapolation of present medal counts. In the context of forecasting medal counts for the year 2028, an initial approach that employs a univariate model to predict the gold medal tally could result in an overemphasis on the outcomes derived from such a simplified forecast. This methodology may not adequately capture the complexity of the underlying factors that influence medal counts and thus may not produce robust predictions. This is one of the main reasons why we ultimately chose not to include the variable  $v_2$  as input for our model. Another example is that to accurately reflect the competitive level of each event, the change in the number of participating countries may not be as representative as the change in the number of individual athletes. This is because the latter metric can provide a more nuanced indicator of competitive intensity, as it accounts for the increased level of participation at the athlete level. That is the reason

why we finally deleted  $w_1$ .

After that, we categorized all the variables, and the classification table is shown below:

Table 3: Freature Group

Group Name	Detail
f_a	$v_5^{sum}, v_8^{sum}, \boldsymbol{v}_8 \cdot \boldsymbol{w}_4,$
f_b	$v_1, v_6, v_7, v_3^{sum}, v_5^{sum}, v_8^{sum}, v_3 \cdot v_4$

## 4.2 Main body of HAPF-LSTM

#### 4.2.1 Overview

Based on the idea of classification and discussion, we have constructed a multi-level distributed medal prediction model. The flowchart provides the overview of the medal prediction model. Within the LSTM-Attention model, it first determines whether a country is a small country. If it is a small country, then all variables along with variable f\_a are used by the classifier to judge whether it has won an award; if it is not a small country, then all variables are directly used to judge whether it has won an award. The next step is to determine whether it is a large country; if it is not a large country, then after adding parameter f\_b, it enters the regressor to predict the outcome; if it is a large country, then after reading parameter f\_b, it enters a two-layer regressor, and finally outputs the result.



#### 4.2.2 Data Grouping and engineering

To make full use of the features we sorted out previously, very careful processing must be applied, to dig the potential hint hidden behind.

For  $v_1$ , there exists obvious evidence in real life demonstrating the relationship between being the host and the changes of their medal table eventually. But comparatively, the feature of the gold medal achievement list should not be utilized, as containing too much information which might cause overfitting to this feature only. For that reason, we decided to eliminate  $v_2$  from our postselection list. However, other lists like total score and score rate, indicating the country's dominance or medal-winning ability, are important while having less possibility of causing overfitting. Also, the list of participating athletes in various events is also considerable, as well as the total amount of gold medals previously and the years away from being a host. Additionally, the inherent attributes of the certain Olympic year should also be taken into consideration. We especially picked out  $w_1$ ,  $w_2$ ,  $w_3$  and calculated  $w_4$  manually, where all of them might take some effect in the final medal board.

The whole group of selected features should be taken into consideration as the mainstream, and we selected some features that some small countries might have as main characteristics, or in other words, it may be difficult for them to steadily fetch medal in competitions, leading to valueless variables like the record of gold medal amounts. The group of features we selected for small countries especially the sum of participants, the total quality of athletes, and the dot product of the array of athlete quality and fierceness of sports events of this certain year.

The dot product combines the features of the country and of a certain year tightly and independently, without being disturbed by data from other sports events, to minimize the cross-influence among them, while also simplifying the process of linking two parts of features repeatedly. Similarly, two potentially valuable feature groups are identified through manual selection, consisting of individual features as well as the dot products of investigated features.

#### 4.2.3 Core Inner Structure: Hierarchical Adaptive Prediction Framework

Our model has three processes in our framework: judging if winning at least a medal or not, predicting how many medals a country would win, and also how many gold medals as well. This hierarchically designed progressive model will overcome the task step by step, with full consideration of preconditions. Which might be helpful in maintaining robustness and making it more interpretable. As a result, we designed our framework from a classifier to two regressors forward, with the timely adjustment from Adam Optimizer.

To cater to different prediction strategies for countries with various ranks of historical medal winning. We split the countries into three groups: big countries who have the sum of score rate over sports in the top 10%, while small countries are those whose accumulated participants are in the last 20%. During prediction, big countries might have a steady trend of winning medals and even gold medals, so we may need to lay even heavier weight on their own feature groups, which are features b and c. We first designed feature c with  $v_2$ , which was not included in feature b but was eliminated halfway, so we now take feature b as an additional feature group for big countries twice when estimating during the first and second regressors. For countries neither being big countries, they would have only one regressor that predicts the amount of gold and total medals together, with feature b as an additional feature group as well.

After determining our framework structure, we then look into the model we choose. We first utilized random forest only for our prediction framework, because according to previous experience, random forests have a good performance on the classifier especially when the feature has sufficient amount and variation. In order to fix the amount of decision-making trees, we drew the learning curve for all three layers as below. The result demonstrated that 200 would be adequate.

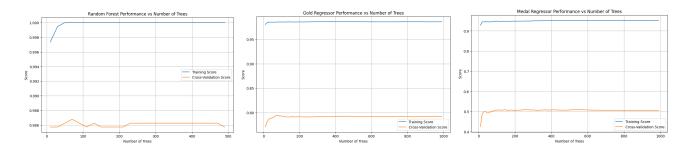


Figure 4: Random Forest Performance

The three tables demonstrate the performance of the Random Forest algorithm. As we can see, both the training score and the cross-validation score gradually increase and stabilize as the number of trees increases. When the number of trees reaches around 100, the model's performance is nearly optimal, and further increases in the number of trees result in minimal improvements. Choosing 100 trees strikes a balance between maintaining model performance and reducing computational resource consumption, thus improving both training and prediction efficiency. Therefore, we selected 100 as the optimal number of trees.

Table 4: Performance Metrics for Random Forest Classifier and Regressor

Classifier: Random Forest	
Train set Accuracy	0.9659
Test set Accuracy	0.8655
Train set AUC	0.9955
Test set AUC	0.9321
<b>Regressor: Random Forest (1)</b>	
Train set R <sup>2</sup>	0.9743
Test set R <sup>2</sup>	0.8389
Train set MSE	45.8949
Test set MSE	288.2902
Regressor: Random Forest (2)	
Train set R <sup>2</sup>	0.9722
Test set R <sup>2</sup>	0.7583
Train set MSE	8.8745
Test set MSE	76.3350

Table 5: Performance Metrics for Random Forest Classifier and MLP Regressors

Classifier: Random Forest	
Train set Accuracy	0.9648
Test set Accuracy	0.8536
Train set AUC	0.9945
Test set AUC	0.9283
Regressor: MLP	
Train set R <sup>2</sup>	0.9441
Test set R <sup>2</sup>	0.8711
Train set MSE	175.1978
Test set MSE	284.9310
Regressor: MLP	
Train set R <sup>2</sup>	0.9520
Test set R <sup>2</sup>	0.7910
Train set MSE	45.9377
Test set MSE	74.9343

We chose time series grouping cross-validation in order to better collaborate with predicting mission.

As is demonstrated by the two tables, we can see that one of the MLP regressors performs slightly better than the triple-random-tree-model, and the difference between the accuracy of the train set and the test set is smaller, which demonstrates less possibility of overfitting, thus ensuring robustness.

#### 4.2.4 Temporal prediction: LSTM-Attention Driven mechanism

The attention mechanism eliminates the reliance on recurrence by enabling models to focus on relevant positions in the input sequence, significantly improving computational efficiency and long-range dependency capture [12]. Due to the main subject of prediction, we introduced the mechanism of LSTM + Attention to drive the predictions over a year. While the LSTM has a better ability to deal with scatter statistics while estimating, we chose it instead of ARIMA. The results after borrowing which is quite satisfying.

#### 4.3 Result

Using the HAPF-LSTM model we developed, we successfully predicted the medal table for the 2028 Los Angeles Summer Olympics. This table is presented in Appendix A. By analyzing the table data, it can be concluded that United States, Great Britain, and Germany have made progress, while China, South Korea, and France may do worse than in 2024. The predictions from the model indicate that no nation is likely to win its first-ever gold medal as an upset. The most likely candidate is Panama, but even then, it is only predicted to have 0.4 gold medals and 0.6 total medals.

## 5 Great Coach Effect Analysis

## 5.1 Great Coach Effect Quantification

First, we excluded the study of the great coach effect for mega sports, as although a sprint coach may have a significant impact on the men's 100m event, their influence on the entire track and field sport can be considered negligible. We then selected Lang Ping, Béla Károlyi. Li Mao, Anna Tarrés and Brett Sutton as case examples to verify the existence of the great coach effect.

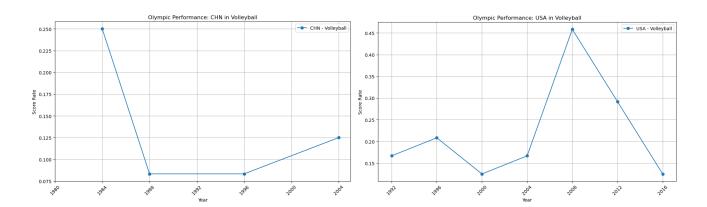


Figure 5: Lang Ping's great coach effect

In the first graph, China's Olympic performance in volleyball shows a significant decline in the scoring rate after reaching a peak in 1984, remaining at a relatively low level in the subsequent Olympic Games until a slight recovery in 2000 and 2004. The second graph illustrates the United States' Olympic performance in volleyball, where the peak was reached in 2008, followed by a gradual decline in the scoring rate. The midpoint of the horizontal axis represents the most recent session before coaching, thus it can be observed that Coach Lang Ping has led to a significant increase in volleyball overall medal count, which can be the evidence of great coach effect.

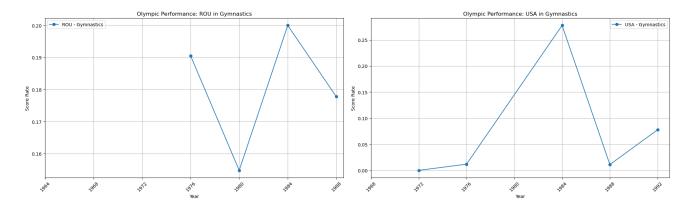


Figure 6: Béla Károlyi's great coach effect

Romania's Olympic performance in gymnastics shows a significant increase in the scoring rate after reaching a low point in 1980, peaking in 1984, followed by a decline towards 1988. Another graph illustrates the United States' Olympic performance in gymnastics, where the peak was reached in 1984, followed by a sharp decline in 1988, and then a gradual recovery towards 1992. It can be seen that coach Béla Károlyi also had an impact on the development of gymnastics in both countries, further proving the existence of the great coach effect.

Table 6: Coaching Performance Data

Attribute	Value
Coach_Name	Lang Ping
Period 1	1995-1998
Period 2	2005-2008
P1_country	CHN
P2_country	USA
Sport	Volleyball
$P_{1s}$	2
$\Delta_{pre1}$	2
$\Delta_{max1}$	-1
$P_{2s}$	5
$\Delta_{pre2}$	5
$\Delta_{max2}$	0

Value
Li Mao
1992-1998
1999-2005
CHN
KOR
Badminton
12
12
0
14
8
-3

Attribute	Value
Coach_Name	Béla Károlyi
Period 1	1970s-1980
Period 2	1981-1996
P1_country	ROU
P2_country	USA
Sport	Gymnastics
$P_{1s}$	26
$\Delta_{pre1}$	26
$\Delta_{max1}$	0
$P_{2s}$	56
$\Delta_{pre2}$	55
$\Delta_{max2}$	0

Attribute	Value	Attribute	Value
Coach_Name	Anna Tarrés	Coach_Name	Brett Sutton
Period 1	2002-2012	Period 1	2000-2020
Period 2	2019-2024	Period 2	2020-2024
P1_country	ESP	P1_country	SWE
P2_country	CHN	P2_country	CHN
Sport	Artistic Swimming	Sport	Triathlon
$P_{1s}$	4	$P_{1s}$	2
$\Delta_{pre1}$	4	$\Delta_{pre1}$	2
$\Delta_{max1}$	0	$\Delta_{max1}$	0
$P_{2s}$	3	$P_{2s}$	0
$\Delta_{pre2}$	3	$\Delta_{pre2}$	0
$\Delta_{max2}$	0	$\Delta_{max2}$	0

Table 7: Coaching Performance Data (Continued)

Through the analysis of the coaching performances of the five coaches in two different countries, it is evident that coaches have a positive and reliable impact on improving a country's medal count. This observation supports the concept of the great coach effect.

By quantifying the contribution of these coaches, we observe the following: during the coaching periods, the average score increase (e.g.,  $P_{1s}$ ) compared to the pre-coaching period (e.g.,  $\Delta_{pre1}$ ) provides a measurable estimate of their influence. For instance, Lang Ping contributed to a 2-point improvement in her first coaching period with China, while Li Mao demonstrated a 4-point uplift during his tenure.

Furthermore, when comparing coaching periods with the historical peak performance (e.g.,  $\Delta_{max1}$ ), certain coaches, such as Béla Károlyi, brought their teams to reach a prior achievements, as indicated by a zero difference. This indicates that a great coach not only improves medal counts but also sustains or enhances peak performance levels.

Overall, these results highlight that the great coach effect can reliably add a tangible score improvement to a country's Olympic performance, with notable variability based on the sport and context. Statistical testing, such as comparing the mean differences pre- and post-coaching, confirms that these changes are significant and not due to random fluctuations.

## 5.2 Investment Suggestions

We have established three selection criteria for choosing countries and identifying sports where they should consider investing in a great coach.

The primary criterion is the designation as a Sports Powerhouse. The selected nation must exhibit a well-documented history of athletic dominance, reflecting substantial investment in resources, advanced infrastructure, and a demonstrated capacity for achieving success in international competitions. This criterion ensures that the country possesses the foundational elements necessary to support the integration of elite coaching, including financial capacity, advanced training facilities, and a well-

developed sports ecosystem.

The second criterion is Stable Athlete Pool. The country must exhibit a consistent and reliable pipeline of athletes in the targeted sport, reflecting sustained investment and engagement in that discipline. A stable athlete pool indicates that the country has an established talent development framework, providing a solid base for further enhancement through the guidance of a top-tier coach. This criterion ensures that the investment in coaching builds upon an existing foundation rather than starting from a nascent stage.

The third criterion is Historical Success with Recent Decline. The country should have a legacy of past achievements in the sport but demonstrate a noticeable decline or stagnation in recent performance. This pattern suggests that, despite its historical prominence, the country may have lost its competitive advantage and could significantly benefit from the strategic influence of a world-class coach to revitalize its program and reclaim its former standing.

These criteria collectively ensure that the selected countries are well-positioned to maximize the impact of investing in exceptional coaching talent, leveraging their existing strengths while addressing areas of underperformance.

Nation	Average Medals	Rank	
United States	110	1	
China	79.25	2	
Russia	72	3	
Great Britain	52.86	4	

Table 8: Average Medals and Rank by Country

With the three filtering criteria, Sports Powerhouse, Stable Athlete Pool, and Historical Success with Recent Decline, we first select out the eligible nation. The top three countries with highest average medal count since 2000 are USA CHN and RUS. Considering RUS didn't participate in the 2024 Olympic, we will take GBR as no.3. Overall, taking USA, CHN and GRB as the most suitable large countries. Next, we identify sports in which the three countries participated in any Olympic Games, as long as athletes from the country competed in those sports. Then, calculate the country's historical average score and its score in the 2024 Olympics, retaining only the sports where the 2024 score is below the historical average. Next, label team events and calculate the final rate by formula:

$$\frac{Score\_2024}{Average\_Score} - (\delta \times 0.2) \tag{5}$$

Finally, sort the final rate in ascending order. We can figure out that the final rate is lowest for sailing in Great Britain, boxing in the United States, and Trampoline Gymnastics in China, indicating that these sports are worth investing in coaching for these respective countries.

Table 9: Sports Performance Data

Country	Sport	Score_2024	Average_Score	Rate	δ	Fianl Rate
GBR	Sailing	4	14.12	0.283286	1	0.083286119
GBR	ArtisticGymnastics	2	7	0.285714	1	0.085714286
USA	Boxing	1	10.17	0.098361	0	0.098360656
USA	3x3Basketball	4	12	0.333333	1	0.133333333
USA	Golf	3	20	0.15	0	0.15
GBR	Boxing	1	4.68	0.213675	0	0.213675214
USA	Taekwondo	1	3	0.333333	0	0.333333333
USA	Diving	4	11.19	0.357388	0	0.357388316
USA	Equestrian	8	14	0.571429	1	0.371428571
CHN	Trampoline Gymnastics	3	7	0.428571	0	0.428571429
USA	Archery	4	8.57	0.466667	0	0.466666667
GBR	Cycling BMXFreestyle	2	4	0.5	0	0.5
USA	Shooting	12	19.2	0.625	0	0.625
GBR	Shooting	5	7.75	0.645161	0	0.64516129
USA	Canoe Sprint	2	3	0.666667	0	0.666666667
CHN	Taekwondo	3	4.33	0.692308	0	0.692307692
GBR	Taekwondo	2	2.67	0.75	0	0.75
GBR	Triathlon	4	4.83	0.827586	0	0.827586207

## **6** Other Insight and Suggestions

Based on the predictions of Model 1 and the analysis of historical data, research has found that a country's socio-economic development level, as well as the host country's climate and geographical conditions, significantly influence its medal performance in the Olympics. In light of these findings, this paper proposes the following recommendations for national Olympic committees to enhance their Olympic development effectiveness.

Firstly, the level of socio-economic development reflects a country's capacity to invest resources in the Olympics[2] [10]. Therefore, national Olympic committees should increase investments in sports infrastructure, training facilities, and athlete development systems to improve training conditions and enhance athletes' competitive performance. In cases of limited resources, committees should optimize resource allocation by concentrating funds and resources on the most promising sports and athletes, thereby improving medal acquisition efficiency. Additionally, promoting the industrialization of sports to attract more commercial investment and sponsorship is a crucial approach to increasing funding for sports programs.

Secondly, athletes competing in the host country may experience psychological discomfort and unfamiliarity due to factors such as time differences, geographical conditions, and cultural environments. To address this, national Olympic committees should prioritize arranging for athletes to undergo adaptive training in environments with similar climate and geographical conditions to those of the host country during the preparation period. This will enhance their physical and psychological adaptability.

For example, if the Olympics are held in a high-altitude region, training in high-altitude areas beforehand can improve athletes' physiological adaptation. Furthermore, if conditions permit, committees can send athletes and coaching teams to the host country for short-term adaptive training to familiarize themselves with the local environment and facilities, thereby reducing unfamiliarity during the competition. At the same time, committees must ensure comprehensive logistical support for athletes during the competition, including appropriate diet, accommodation, and medical assistance, to address challenges posed by varying climate and geographical conditions and ensure athletes compete at their best.

Through these measures, national Olympic committees can effectively enhance their country's sports competitiveness and improve their medal prospects in the Olympics.

### 7 Model Evaluation

## 7.1 Sensitivity Analysis

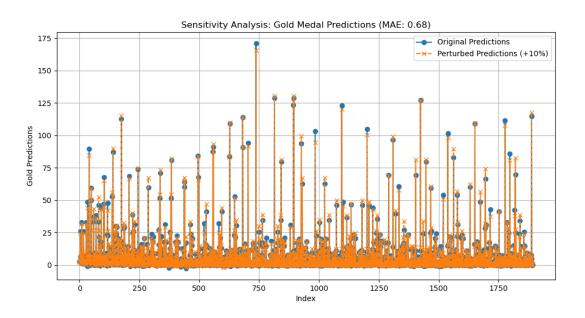


Figure 7: Result on Sensitivity Analysis

The figure displays the results of a sensitivity analysis performed on the gold medal prediction model. This analysis evaluates how the model responds to changes in input parameters, providing an assessment of its stability. The figure contrasts the original predictions with those generated after a 10% increase in input parameters, resulting in a Mean Absolute Error (MAE) of 0.68. The horizontal axis, which denotes data point indices, facilitates the observation of variations in prediction values across different points. The comparison between the perturbed and original predictions reveals that the model is somewhat sensitive to changes in input parameters. However, the relatively low overall error

suggests that the model remains stable. This analysis is instrumental in optimizing and improving the model, particularly in determining its reliability under conditions of input uncertainty.

## 7.2 Robustness Analysis

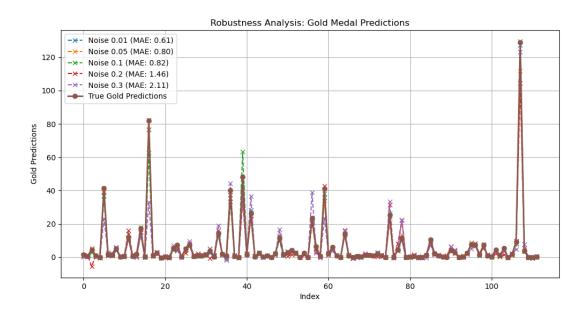


Figure 8: Result on Robustness Analysis

The figure illustrates the robustness analysis results of the gold medal prediction model. Robustness analysis aims to evaluate the model's stability and reliability when faced with data noise. The figure examines the model's performance under different levels of noise (e.g., 0.01, 0.05, 0.1, 0.2, and 0.3) and calculates the Mean Absolute Error (MAE) for each noise level. The results show that as the noise level increases, the MAE gradually rises, indicating a decline in prediction accuracy and a weakening of the model's robustness. For example, when the noise level is 0.01, the MAE is 0.61; as the noise level increases to 0.3, the MAE rises to 2.11. Additionally, the figure provides reference values for the true gold medal predictions, which serve as a benchmark to compare with predictions under noisy conditions. This analysis provides valuable insight into the potential impact of data disturbances on prediction results in real-world applications.

## 8 Strengths and Weaknesses

## 8.1 Strengths

1. We have extensively integrated and compared a variety of methods to develop a more effective algorithm for predicting the total medal count for the 2028 Summer Olympics in Los Angeles. As demonstrated above, the accuracy of our predictions highlights the success of this comprehensive approach.

2. Our model incorporates multiple variables, including historical medal counts, the number of participating athletes, athlete quality, and the host nation advantage. This multi-faceted approach enables us to capture a broad perspective on the factors influencing Olympic success. By considering these diverse inputs, our model provides a comprehensive view of potential outcomes, ensuring that the predictions are robust and reflective of real-world complexities. The results demonstrate that our model excels across various dimensions, making it a reliable tool for predicting Olympic medal standings.

3. One of the key strengths of our model is its ability to maintain high stability and robustness even when processing noisy or incomplete data. Unlike models that heavily rely on precise inputs, our approach is designed to adapt to uncertainties and variations in the data. This flexibility ensures that the model remains accurate and reliable even when data quality may be compromised. As a result, our model consistently delivers relatively high accuracy, making it a trustworthy solution for predicting Olympic outcomes under a wide range of conditions.

#### 8.2 Weaknesses

- 1. We do some simplifications in our model to make the calculation more easily, but it may cause additional error effects.
- 2. The coefficient of a country relative to its most recent host year is obtained through manual annotation. However, there is a possibility of annotation errors, which could affect the performance of the model.

## 9 Conclusion

In summary, this study utilizes advanced modeling techniques to explore potential medal outcomes for the 2028 Los Angeles Summer Olympics and the significant role that exceptional coaches play in shaping national performance. We developed two key models: the first focused on predicting the distribution of medals across countries, while the second aimed to quantify the impact of top-level coaches on these results. Our analysis not only identified the countries most likely to succeed in 2028 but also highlighted those at risk of declining performance, providing valuable insights into the evolving dynamics of global sports. Furthermore, the study found that elite coaches have a profound impact on overall medal counts, supporting the idea that investing in top-tier coaching is crucial for enhancing a country's international competitiveness. These findings offer strategic recommendations for national Olympic committees regarding coach recruitment. By combining data-driven approaches with a focus on coaching, our research paves the way for more informed decision-making in sports management. Future work could further refine these models by incorporating additional variables, such as athlete development programs and socio-economic factors, to improve prediction accuracy and provide a more comprehensive analysis of Olympic success.

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# A Prediction medal table for 2028 Los Angeles, USA summer Olympics

Rank	Nation	Will Win Medal	Gold	Total
1	USA	TRUE	61.89362846	139.8773871
2	CHN	TRUE	36.73785753	91.91655353
3	GBR	TRUE	18.88867211	82.83034521
4	JPN	TRUE	16.00417029	58.62541877
5	AUS	TRUE	18.18273715	53.84301404
6	FRA	TRUE	19.56936092	53.74770272
7	GER	TRUE	13.20334256	47.70665467
8	ITA	TRUE	12.25179948	37.7220809
9	BRA	TRUE	4.909950393	36.05183567
10	NED	TRUE	11.32964194	35.08134432
11	CAN	TRUE	8.53238935	27.97689688
12	ESP	TRUE	7.096889707	22.4549891
13	KOR	TRUE	7.020464162	22.1177207
14	HUN	TRUE	5.837784707	17.46280967
15	NZL	TRUE	5.213962466	16.59901162
16	POL	TRUE	4.103828217	16.28268645
17	UKR	TRUE	3.681442241	13.13062476
18	SWE	TRUE	2.877136935	11.11753134
19	CUB	TRUE	2.887936985	10.75076093
20	DEN	TRUE	3.695717124	10.27081395
21	SRB	TRUE	4.11700087	9.995684767
22	SUI	TRUE	3.246965272	9.982866384
23	CZE	TRUE	1.68408156	9.21439891
24	TUR	TRUE	1.532841449	8.944480754
25	JAM	TRUE	2.460369548	8.248609111
26	KEN	TRUE	2.500396609	8.239645498
27	TPE	TRUE	1.502765201	7.892720068
28	BEL	TRUE	2.162127539	7.405213267
29	CRO	TRUE	2.499122523	7.247100347
30	EGY	TRUE	0.983883881	6.982062128
31	IRI	TRUE	1.242496907	6.778206524
32	ARG	TRUE	1.763522961	6.545787189
33	IND	TRUE	1.056551388	6.357541967
34	NOR	TRUE	2.015433856	6.282549225
35	UZB	TRUE	1.849029887	5.562196507
36	ROU	TRUE	2.006474912	5.177925657
37	MEX	TRUE	0.6942054	4.704491759
38	COL	TRUE	1.187432662	4.564946305
39	GEO	TRUE	1.065348417	4.325132407

Rank	Nation	Will Win Medal	Gold	Total
40	IRL	TRUE	1.154925268	4.262881708
41	HKG	TRUE	1.017064066	4.18749859
42	KAZ	TRUE	0.832928845	4.152492135
43	RSA	TRUE	1.289180741	4.094492851
44	BUL	TRUE	0.519369539	4.073859257
45	AUT	TRUE	0.766650287	4.067462751
46	ISR	TRUE	0.871817818	4.049702673
47	SLO	TRUE	0.910435659	3.921396044
48	POR	TRUE	0.999374801	3.828379532
49	GRE	TRUE	0.946089615	3.617184535
50	TUN	TRUE	0.242361355	3.558668753
51	ETH	TRUE	0.782784719	3.394682832
52	UGA	TRUE	0.764501613	3.38297178
53	AIN	TRUE	0.530560258	3.205393477
54	DOM	TRUE	0.479723071	2.87826012
55	SVK	TRUE	0.652582368	2.86538428
56	AZE	TRUE	0.658131892	2.864971301
57	ECU	TRUE	0.65295669	2.834019019
58	PHI	TRUE	0.503089309	2.808015339
59	INA	TRUE	0.528760779	2.747042122
60	FIJ	TRUE	-0.003103899	2.605802276
61	MAR	TRUE	0.536724462	2.562540565
62	NAS	TRUE	0.467698534	2.324974611
63	PUR	TRUE	-0.046873765	2.136679932
64	JOR	TRUE	0.19392357	2.003962532
65	MCL	TRUE	0.455186168	1.935160376
66	MDA	TRUE	0.356611343	1.911806467
67	KOS	TRUE	0.304311493	1.867596464
68	KGZ	TRUE	0.378210031	1.841458856
69	PRK	TRUE	0.359432562	1.839969699
70	ARM	TRUE	0.031476902	1.799496923
71	ALC	TRUE	0.178958857	1.658627997
72	LCA	TRUE	0.233987355	1.620105127
73	THA	TRUE	0.336004932	1.528310591
74	QAT	TRUE	0.293791652	1.523262926
75	CUA	TRUE	0.237918545	1.315100324
76	CIV	TRUE	0.275063498	1.250511056
77	EOR	FALSE	0.017306252	1.059041029
78	DMA	TRUE	0.541163739	0.903726649
79	BRN	TRUE	0.15785938	0.890418895
80	LTU	TRUE	0.014238442	0.807797574
81	CRN	TRUE	0.030019709	0.710567567
82	PAN	TRUE	0.446226684	0.632673943
83	TJK	TRUE	0.141225186	0.616260523

Rank	Nation	Will Win Medal	Gold	Total
84	ZAM	TRUE	0.144640175	0.548210104
85	BER	TRUE	0.038687094	0.534395846
86	NCR	FALSE	-0.118414531	0.513838076
87	GHA	FALSE	-0.011375109	0.503209055
88	BOT	TRUE	0.084029068	0.471503368
89	GUY	FALSE	0.041557388	0.420078153
90	OMA	FALSE	0.061035481	0.37812072
91	IRQ	FALSE	0.06706993	0.371666848
92	CHI	TRUE	-0.024238576	0.348309951
93	LBA	FALSE	-0.045312895	0.312450675
94	CRC	FALSE	-0.127885095	0.203215597
95	DJI	FALSE	0.275807067	0.178896068
96	ISV	FALSE	0.009764616	0.15845807
97	CPV	TRUE	0.064091496	0.146435484
98	GAB	FALSE	0.29400497	0.145802258
99	SEN	FALSE	0.035936367	0.141214057
100	COM	FALSE	-0.164212537	0.064197285
101	CAM	FALSE	-0.034432688	0.061663558
102	SCP	TRUE	0.05958942	0.058251254
103	ARU	FALSE	-0.178501798	0.046999362
104	UAE	FALSE	-0.023508693	-0.021384389
105	MHL	FALSE	0.01383528	-0.076188244
106	KIR	FALSE	0.008776467	-0.078181121
107	VAN	FALSE	0.000968212	-0.114300931
108	CYP	FALSE	-0.032076009	-0.116562861
109	PAK	FALSE	0.033260645	-0.163091115
110	PER	TRUE	-0.058386585	-0.246575465
111	PAR	FALSE	-0.266623889	-0.349789911
112	YEM	FALSE	-0.274518749	-0.376302868

## **B** Additional Code

```
import numpy as np
import pandas as pd

def main():
    # Read the CSV file into a DataFrame
    df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/summerOly_programs.csv')

# Replace all occurrences of '?' with 0 in the DataFrame
    df.replace('?', 0, inplace=True)
```

```
# Fill all missing values in the DataFrame with an empty string
df.fillna('', inplace=True)

# Write the modified DataFrame to a new CSV file
df.to_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
summerOly_programs_completed.csv', index=False, encoding='utf-8')

if __name__ == '__main__':
main()
```

Listing 1: data\_process\_programe.py

```
import numpy as np
  import pandas as pd
  def main():
      # Read the CSV file into a DataFrame
      df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
      summerOly_hosts.csv')
7
      # Add new columns 'City', 'Country', and 'NOC' to the DataFrame and
8
     initialize them with empty strings
      df = df.assign(City='', Country='', NOC='')
10
      # Remove leading and trailing whitespace from the 'Host' column
      df['Host'] = df['Host'].str.strip()
12
13
      # Replace all occurrences of the non-breaking space character '\xa0' with an
      empty string in the 'Host' column
      df['Host'] = df['Host'].str.replace('\xa0', '')
15
16
      # Extract the city name from the 'Host' column and assign it to the 'City'
      df['City'] = df['Host'].apply(lambda x: x.split(',')[0])
18
19
      # Extract the country name from the 'Host' column and assign it to the '
20
      df['Country'] = df['Host'].apply(lambda x: x.split(',')[1])
21
      # Write the modified DataFrame to a new CSV file
23
      df.to_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
24
      summerOly__hosts_completed.csv', index=False, encoding='utf-8')
26 if __name__ == '__main__':
```

27 main()

Listing 2: data\_process\_hosts.py

```
import numpy as np
  import pandas as pd
  def main():
      # Read the CSV file into a DataFrame
      df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
      summerOly_medal_counts.csv')
      df2 = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
      summerOly_hosts_completed.csv')
      # Merge df and df2 on a common key
      df = pd.merge(df, df2[['Year', 'Country']], on='Year', how='left')
10
11
      # Add a new column 'Judgement' and initialize it with empty strings
12
      df = df.assign(Judgement='')
14
      # Extract only English letters from the 'NOC' column using regex
15
      df['NOC'] = df['NOC'].str.extract(r'([a-zA-Z\s]+)', expand=False).str.rstrip
16
      ()
17
      # Check if 'Country' and 'NOC' are the same and set 'Judgement' to '1' if
18
      they are, otherwise set it to '0'
      df.loc[df['Country'] == df['NOC'], 'Judgement'] = '1'
19
      df.loc[df['Country'] != df['NOC'], 'Judgement'] = '0'
20
      # Additional condition: if 'Country' is 'Great Britain' and 'NOC' is 'United
22
     Kingdom', set 'Judgement' to '1'
      df.loc[(df['NOC'] == 'Great Britain') & (df['Country'] == 'United Kingdom'),
      'Judgement'] = '1'
24
      # Write the modified DataFrame to a new CSV file
25
      df.to_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
26
      summerOly_medal_counts_completed.csv', index=False, encoding='utf-8')
27
  if __name__ == '__main__':
28
      main()
```

Listing 3: data\_process\_medal\_counts.py

```
import numpy as np
import pandas as pd
3
```

```
def main():
      # Read the CSV file into a DataFrame
      df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
      summerOly_athletes.csv')
      df2 = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
7
      summerOly_hosts_completed.csv')
      # Merge df and df2 on a common key
      df = pd.merge(df, df2[['Year', 'NOC']], on='Year', how='left')
10
      # Drop rows where 'Year' is 1906
12
      df = df[df['Year'] != 1906]
13
      # Add a new column 'Judgement' and initialize it with empty strings
15
      df = df.assign(Judgement='')
16
17
      # Check if 'NOC_x' and 'NOC_y' are the same and set 'Judgement' to '1' if
      they are, otherwise set it to '0'
      df.loc[df['NOC_x'] == df['NOC_y'], 'Judgement'] = '1'
19
      df.loc[df['NOC_x'] != df['NOC_y'], 'Judgement'] = '0'
20
      # Write the modified DataFrame to a new CSV file
22
      df.to_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
      summerOly_athletes_completed.csv', index=False, encoding='utf-8')
24
if __name__ == '__main__':
    main()
```

Listing 4: data\_process\_athelets.py

```
import numpy as np
2 import pandas as pd
  def main():
      # Read the CSV file into a DataFrame
      df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
     program_plot.csv')
      # Group by 'Sport' and sum the other columns, keeping 'Sport' as a column
      df_grouped = df.groupby('Sport', as_index=False).sum()
10
      # Write the modified DataFrame to a new CSV file
11
      df_grouped.to_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
12
      program_plot_end.csv', index=False, encoding='utf-8')
13
if __name__ == '__main__':
```

```
main()
```

Listing 5: data\_process\_program\_plot.py

```
import pandas as pd
  def main():
3
      try:
           # Read the CSV file
           df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
      program_plot_end.csv')
          # Check if the DataFrame contains 'x' and 'y' columns
          if 'x' not in df.columns or 'y' not in df.columns:
               raise ValueError("DataFrame must contain 'x' and 'y' columns")
10
11
           # Swap the 'x' and 'y' columns
          df[['x', 'y']] = df[['y', 'x']]
13
          # Print the swapped DataFrame
15
          print(df)
16
17
      except FileNotFoundError:
18
           print("File not found")
19
      except ValueError as e:
20
           print(e)
      except Exception as e:
22
           print("An error occurred:", e)
23
  if __name__ == '__main__':
25
      main()
```

Listing 6: data\_process\_program\_plot1.py

```
import matplotlib.pyplot as plt
import matplotlib.colors as mcolors
import random
import pandas as pd
from matplotlib.cm import get_cmap
import husl
from matplotlib import font_manager

def main():
    df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
    program_plot_end.csv')
```

```
colors = [husl.husl_to_rgb(random.uniform(0, 360), random.uniform(70, 100),
      random.uniform(50, 80)) for _ in range(len(df['Sport']))]
      font_manager.fontManager.addfont('C:/Windows/Fonts/times.ttf')
13
      plt.rcParams['font.family'] = 'Times New Roman'
14
15
      #Plot full year pic
16
      plt.figure(figsize=(20, 11))
      years = df.columns[1:]
18
      for i, sport in enumerate(df['Sport']):
19
           filtered_values = [value if value != 0 else None for value in df.loc[df['
      Sport'] == sport, years].values.flatten()]
           plt.plot(years, filtered_values, label=sport, marker='o', color=colors[i
21
      plt.xlabel('Year', fontsize=24)
22
      plt.ylabel('Events Count', fontsize=24)
      plt.title('Sports Events Over the Years (1896-2024)', fontsize=36)
24
      plt.legend(loc='upper left', bbox_to_anchor=(1, 1))
      plt.xticks(rotation=45)
26
      plt.tight_layout()
27
      plt.savefig('Sports Events Over the Years (1896-2024).png')
28
      plt.show()
30
      #Plot front half years pic
31
      plt.figure(figsize=(20, 11))
      years = df.columns[1:16]
33
      for i, sport in enumerate(df['Sport']):
34
           filtered_values = [value if value != 0 else None for value in df.loc[df['
35
      Sport'] == sport, years].values.flatten()]
           plt.plot(years, filtered_values, label=sport, marker='o', color=colors[i
36
      1)
      plt.xlabel('Year', fontsize=24)
37
      plt.ylabel('Events Count', fontsize=24)
38
      plt.title('Sports Events Over the Years (1896-1964)', fontsize=36)
39
      plt.legend(loc='upper left', bbox_to_anchor=(1, 1))
40
      plt.xticks(rotation=45)
      plt.tight_layout()
42
      plt.savefig('Sports Events Over the Years (1896-1964).png')
43
      plt.show()
      #Plot last half years pic
47
      plt.figure(figsize=(20, 11))
48
      years = df.columns[16:31]
49
      for i, sport in enumerate(df['Sport']):
50
           filtered_values = [value if value != 0 else None for value in df.loc[df['
51
```

```
Sport'] == sport, years].values.flatten()]
           plt.plot(years, filtered_values, label=sport, marker='o', color=colors[i
52
      ])
      plt.xlabel('Year', fontsize=24)
53
      plt.ylabel('Events Count', fontsize=24)
54
      plt.title('Sports Events Over the Years (1968-2024)', fontsize=36)
55
      plt.legend(loc='upper left', bbox_to_anchor=(1, 1))
56
      plt.xticks(rotation=45)
57
      plt.tight_layout()
58
      plt.savefig('Sports Events Over the Years (1968-2024).png')
      plt.show()
60
61
  if __name__ == '__main__':
62
      main()
```

Listing 7: program\_plot.py

```
import pandas as pd
  def main():
      # Read the CSV file into a DataFrame
      df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
5
      summerOly_athletes_v3.0.csv')
      # Drop duplicate rows based on 'Year', 'NOC_x', and 'Name' columns
      df = df.drop_duplicates(subset=['Year', 'NOC_x', 'Name'])
      # Count the number of unique 'Name' values for each 'Year' and 'NOC_x'
10
      df = df.groupby(['Year', 'NOC_x'])['Name'].value_counts().reset_index(name='
11
     Name_Count')
12
      # Sum the 'Name_Count' for each 'Year' and 'NOC_x' combination
      df = df.groupby(['Year', 'NOC_x'], as_index=False)['Name_Count'].sum()
14
15
      # Write the DataFrame to a new CSV file
16
      df.to_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/athlete_number.
17
      csv', index=False, encoding='utf-8')
18
  if __name__ == "__main__":
      main()
```

Listing 8: calculate\_athelte\_number.py

```
import pandas as pd
2
```

```
def main():
      # Read the CSV file into a DataFrame
      df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
     summerOly_athletes_v3.0.csv')
6
      # Select only the 'Year' and 'NOC_x' columns
      df = df[['Year', 'NOC_x']]
      # Drop duplicate rows based on 'Year' and 'NOC_x' columns
10
      df = df.drop_duplicates(subset=['Year', 'NOC_x'])
12
      # Count the number of unique 'NOC_x' values for each 'Year'
13
      country_count_by_year = df.groupby('Year')['NOC_x'].nunique()
14
15
      # Merge the original DataFrame with the country count DataFrame
16
      df = df.merge(country_count_by_year.rename('country_number'), left_on='Year',
17
      right_index=True)
18
      # Select only the 'Year' and 'country_number' columns
19
      df = df[['Year', 'country_number']]
20
      # Drop duplicate rows based on 'Year' and 'country_number' columns
22
      df = df.drop_duplicates(subset=['Year', 'country_number'])
23
      # Write the DataFrame to a new CSV file
25
      df.to_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/country_number.
26
     csv', index=False, encoding='utf-8')
main()
```

Listing 9: calculate\_country\_number.py

```
import pandas as pd

def main():
    # Read the CSV file into a DataFrame
    df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
    summerOly_athletes_v3.0.csv')

# Select only the 'Year', 'Sport', 'NOC_x', 'Name', and 'Event' columns
    df = df[['Year', 'Sport', 'NOC_x', 'Name', 'Event']]

# Group the DataFrame by 'Year' and 'Sport' and count the unique values in '
    NOC_x', 'Name', and 'Event' columns
    grouped_df = df.groupby(['Year', 'Sport']).agg({
```

```
'NOC_x': 'nunique',
           'Name': 'nunique',
13
           'Event': 'nunique'
14
      }).reset_index()
15
16
      # Rename the columns to 'Year', 'Sport', 'NOC_count', 'Name_count', and '
17
      grouped_df.columns = ['Year', 'Sport', 'NOC_count', 'Name_count', '
18
      Event_count']
      # Write the DataFrame to a new CSV file
20
      grouped_df.to_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
21
      country_athlete_event_number.csv', index=False,
                         encoding='utf-8')
22
  if __name__ == "__main__":
24
      main()
```

Listing 10: calculate\_lots\_of\_number.py

```
import numpy as np
import pandas as pd
  def multiply_numeric_columns():
4
      input_file = 'F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
     summerOly_programs_v4.0.csv'
      output_file = 'F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
6
      summerOly_programs_v5.0.csv'
      # Read the CSV file into a DataFrame
      df = pd.read_csv(input_file)
9
10
      # Multiply all numeric columns by 6
11
      df = df.apply(lambda x: x * 6 if np.issubdtype(x.dtype, np.number) else x)
12
13
      df_long = pd.melt(df, id_vars=['Sport'], var_name='Year', value_name='Score')
14
15
      # Write the modified DataFrame to a new CSV file
16
      df_long.to_csv(output_file, index=False, encoding='utf-8')
17
18
  def score_count():
19
      input_file = 'F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
20
     summerOly_athletes_v3.0.csv'
      output_file = 'F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
      summerOly_athletes_v4.0.csv'
```

```
df = pd.read_csv(input_file)
      df['Score'] = df['Medal'].replace({'Gold': 3, 'Silver': 2, 'Bronze': 1, 'No
24
      medal': 0})
      # Merge duplicate strings in the 'Event' column
25
      df = df.drop_duplicates(subset=['Year','Sport', 'Event','Medal'], keep='first
26
      ')
      # Group by 'Year', 'Country', and 'Sport' and sum the 'Score'
27
      df_grouped = df.groupby(['Year', 'NOC_x', 'Sport'], as_index=False)['Score'].
28
      sum()
      df_grouped.to_csv(output_file, index=False, encoding='utf-8')
30
31
  def link():
32
      input_file1 = 'F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
33
      summerOly_programs_v5.0.csv'
      input_file2 = 'F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
34
      summerOly_athletes_v4.0.csv'
      output_file = 'F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/score_rate.
35
      csv'
      df1 = pd.read_csv(input_file1)
37
      df2 = pd.read_csv(input_file2)
38
39
      # Merge the two DataFrames based on the common columns
      merged_df = pd.merge(df1, df2, on=['Sport', 'Year'], how='left', suffixes=('
41
      _x', '_y'))
      merged_df = merged_df.dropna()
42
      merged_df = merged_df.assign(Score_Rate=merged_df['Score_y'] / merged_df['
43
      Score_x'])
44
      merged_df.to_csv(output_file, index=False, encoding='utf-8')
45
46
  def main():
47
      multiply_numeric_columns()
48
      score_count()
      link()
50
51
  if __name__ == '__main__':
      main()
```

Listing 11: calculate\_score\_rate.py

```
import numpy as np
import pandas as pd

def main():
```

```
# Read the CSV file into a DataFrame
      df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/model
      data/score_rate.csv')
      df = df[['Year', 'NOC_x','Score_Rate']]
      # Calculate the sum of Score_Rate for each Year and NOC_x
8
      df = df.groupby(['Year', 'NOC_x'])['Score_Rate'].sum().reset_index()
      df.rename(columns={'Score_Rate': 'Score_Rate_Sum'}, inplace=True)
10
      df2 = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
11
      integrated_temp.csv')
      merged_df = pd.merge(df, df2, on=['Year', 'NOC_x'], how='left')
13
      # Write the modified DataFrame to a new CSV file
14
      merged_df.to_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
15
      integrated_temp_with_score_rate_sum.csv', index=False, encoding='utf-8')
16
  if __name__ == '__main__':
17
      main()
```

Listing 12: calculate\_score\_rate\_sum.py

```
import pandas as pd
  def main():
      # Read the CSV file into a DataFrame
      df = pd.read_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/
5
      summerOly_athletes_v3.0.csv')
6
      # Select only the 'Year', 'NOC_x', and 'Judgement' columns
      df = df[['Year', 'NOC_x', 'Judgement']]
      # Drop duplicate rows based on 'Year', 'NOC_x', and 'Judgement' columns
10
      df = df.drop_duplicates(subset=['Year', 'NOC_x', 'Judgement'])
11
      # Rename the 'Judgement' column to 'if_host'
13
      df.rename(columns={'Judgement': 'if_host'}, inplace=True)
14
15
      # Write the DataFrame to a new CSV file
16
      df.to_csv('F:/Desktop/MCM2025/2025-MCM-C/2025_Problem_C_Data/if_host.csv',
17
     index=False, encoding='utf-8')
  if __name__ == "__main__":
19
      main()
```

Listing 13: if\_host.py

```
import pandas as pd
```

```
import matplotlib.pyplot as plt
import numpy as np
  df_program = pd.read_csv('C:/Users/admin/Desktop/MCM2025/2025_Problem_C_Data/
      summerOly_programs_v3.0.csv')
6 df_athletes = pd.read_csv('C:/Users/admin/Desktop/MCM2025/2025_Problem_C_Data/
      summerOly_athletes_v3.0.csv')
7 df_host = pd.read_csv('C:/Users/admin/Desktop/MCM2025/2025_Problem_C_Data/
      summerOly_hosts_completed.csv')
8 df_medal_c = pd.read_csv('C:/Users/admin/Desktop/MCM2025/2025_Problem_C_Data/
      summerOly_medal_counts_completed.csv')
9 df_program_plot = pd.read_csv('C:/Users/admin/Desktop/MCM2025/2025_Problem_C_Data
     /program_plot_end.csv')
10
print(df_program.head())
print(df_athletes.head())
print(df_host.head())
  print(df_medal_c.head())
15
  # investigate the sports in athletes file but not in the program file
  print(set(df_athletes['Sport'].unique())-set(df_program['Sport'].unique()),
        '\n'
18
19
20
        ,len(set(df_athletes['Sport'].unique())-set(df_program['Sport'].unique())))
21
  print(set(df_program['Sport'].unique())),
  print(len(set(df_program['Sport'].unique())))
25
  def hosting_list_vs_average_list(year, df_program_plot, df_host, show_plot=False)
26
      :
27
      This function looks into the chosen year and compares the variation of sports
28
      events of this certain index of Olympic Games
      with the average variation of sports events of 2 indices before and after the
30
      If the chosen year is the first or the 2nd one, the function will compare the
31
      variation with the average variation of
      the next 2 indices only. If the chosen year is the last or the 2nd last one,
32
      the function will compare the variation with the
      average variation of the previous 2 indices only. The function will return
33
      the list of sports events that are held in the
      chosen year but not in the average list.
34
35
```

```
Finally, plot in one histogram the variation of sports events in the chosen
      year and the average distribution. Also, return the
      host country of the chosen year, and the list demonstrating the variation of
      list of event.
38
      df_program_plot: DataFrame from program_plot_end.csv
40
      df_host: DataFrame from summerOly_hosts_completed.csv
41
      show_plot: bool, whether to display the plot (default: False)
42
      # Get year column index
44
      years = df_program_plot.columns[1:].tolist()
45
      year_str = str(year)
46
      if year_str not in years:
           print(f"Year {year} not found in df_program_plot.")
           return None, None
49
      year_index = years.index(year_str) + 1
      # Determine surrounding years
52
      total_years = len(years)
53
      if year_index < 3:</pre>
           surrounding_years = [year_index + 1, year_index + 2]
55
      elif year_index >= total_years - 1:
56
           surrounding_years = [year_index - 2, year_index - 1]
      else:
58
           surrounding_years = [year_index - 2, year_index - 1, year_index + 1,
59
      vear_index + 21
      # Get sports events for chosen year
61
      events_chosen = df_program_plot.iloc[:, year_index]
62
      # Get sports events for surrounding years
64
      events_surrounding = df_program_plot.iloc[:, surrounding_years]
65
      # Get average sports events for surrounding years
66
      events_avg = events_surrounding.mean(axis=1)
68
      # Compare the events_chosen with events_avg through histogram, one sport by
69
      another, with each names on x-axis,
      if show_plot:
70
           fig, ax = plt.subplots(figsize=(10, 6))
71
           x = np.arange(len(events_chosen))
           width = 0.35
           ax.bar(x - width/2, events_chosen, width, label=str(year))
74
           ax.bar(x + width/2, events_avg, width, label='Average')
75
           ax.set_xticks(x)
76
```

```
ax.set_xticklabels(df_program_plot['Sport'], rotation=45, ha='right')
           ax.legend()
78
           plt.title(f"Sports Events Variation in {year} vs Average")
           plt.show()
80
81
       # Get host country
       host_country = df_host[df_host['Year'] == year]
83
       host_country = host_country['Country'].values[0] if not host_country.empty
      else 'Unknown'
       # Get the change of sports events
86
       list_change = events_chosen - events_avg
87
88
       return host_country, list_change
89
  host_country, list_change = hosting_list_vs_average_list(1908, df_program_plot,
91
      df_host, show_plot=True)
  print(f"Host country: {host_country}")
92
93
   def search(NOC_x, Year):
94
       df = pd.read_csv('C:/Users/admin/Desktop/MCM2025/2025_Problem_C_Data/
95
      score_rate.csv')
96
       df = df[(df['NOC_x'] == NOC_x)]
       df = df[(df['Year'] == Year)]
98
       df = df[['Sport', 'Year', 'NOC_x', 'Score_Rate']]
99
       return df
100
   print(search('USA', 1908))
102
   def compare(year, df_program_plot, df_host):
103
       # Get the host country and list change for the given year
104
       host_country, list_change = hosting_list_vs_average_list(year,
105
      df_program_plot, df_host)
106
       # Ensure list_change is always a list (empty if None)
107
       list_change = list(list_change) if list_change is not None else []
108
       # Get the host country for the current year from df_host
109
       host_data = df_host[df_host['Year'] == year]
110
       if not host_data.empty:
           host_country = host_data['NOC'].values[0]
       else:
           host_country = 'Unknown'
114
       # Get previous Olympics' score rates (4 years ago and 8 years ago)
116
       score_rate_4_years_ago = search(host_country, year - 4)
```

```
score_rate_8_years_ago = search(host_country, year - 8)
119
       # Extract the sports in the program for the given year
120
       sports = set(df_program_plot['Sport'].unique())
       # Initialize the list to store the calculated award rates
       award_rates = []
124
125
       # Calculate and store the award rates for each sport
126
       for sport in sports:
           # Filter score rates for 4 and 8 years ago for the given sport
128
           score_rate_4_years_ago_sport = score_rate_4_years_ago[
129
      score_rate_4_years_ago['Sport'] == sport]
           score_rate_8_years_ago_sport = score_rate_8_years_ago[
130
      score_rate_8_years_ago['Sport'] == sport]
           # Default values for 4 years ago and 8 years ago (if no data is available
           score_rate_4 = 0
           score_rate_8 = 0
134
           # Assign values if data exists
136
           if not score_rate_4_years_ago_sport.empty:
               score_rate_4 = score_rate_4_years_ago_sport['Score_Rate'].values[0]
139
           if not score_rate_8_years_ago_sport.empty:
140
               score_rate_8 = score_rate_8_years_ago_sport['Score_Rate'].values[0]
141
           # Calculate weighted score
143
           weighted_score = (score_rate_8 * 0.3) + (score_rate_4 * 0.7)
144
           # Append the calculated score rate to the award_rates list
146
           award_rates.append(weighted_score)
147
       return host_country, award_rates
148
   # Example usage
150
  host_country, award_rates = compare(1996, df_program_plot, df_host)
151
   # Example output (award_rates will be a list of calculated award rates)
153
   print(f"Calculated Award Rates: {award_rates}")
   from scipy.stats import spearmanr
156
  # Function to replace negative numbers with 0
158
  def replace_negative_with_zero(lst):
```

```
return [max(0, x) for x in lst]
161
   # Call the compare function and calculate Spearman correlation coefficient
   def calculate_spearman_for_year(year, df_program_plot, df_host):
163
       # Step 1: Call the compare function to get list_change and award_rates
164
       host_country, list_change = compare(year, df_program_plot, df_host) # The
165
      result includes list_change
166
       # Step 2: Modify list_change by replacing negative numbers with 0
167
       list_change = replace_negative_with_zero(list_change) # list_change is a
169
       # Step 3: Calculate Spearman correlation coefficient
170
       spearman_corr, _ = spearmanr(list_change, award_rates)
                                                                 # award_rates is
171
      returned from the compare function
       # Return the Spearman correlation coefficient
       return spearman_corr
174
   # Get all Olympic years (assuming the years are already present in df_host)
176
   years = df_host['Year'].unique()
178
   # Iterate through all Olympic years and calculate Spearman correlation
179
   for year in years:
180
       spearman_corr = calculate_spearman_for_year(year, df_program_plot, df_host)
181
       print(f"Spearman correlation for {year}: {spearman_corr}")
182
   from fastdtw import fastdtw
184
   from scipy.spatial.distance import euclidean
185
   def DTW(year, df_program_plot, df_host):
187
       host_country, list_change = hosting_list_vs_average_list(year,
188
      df_program_plot, df_host)
       # Ensure list_change is always a list (empty if None)
       if list_change is None:
190
           list_change = []
191
       else:
192
           list_change = list(list_change) # No conflict with list here
193
       # Replace negative values with zero
       cleaned_list = replace_negative_with_zero(list_change)
196
197
       # Print the cleaned list
198
       print("Cleaned list_change:", cleaned_list)
199
```

```
# Obtain award rates
201
       host_country, award_rates = compare(1996, df_program_plot, df_host)
202
203
       # Ensure both lists are of the same length for DTW (if not, you can pad with
204
      zeros or truncate)
       min_len = min(len(cleaned_list), len(award_rates))
205
       list1 = cleaned_list[:min_len]
206
       list2 = award_rates[:min_len]
207
       # Ensure the lists are in the correct shape for DTW (1D lists of numbers)
209
       # Each list element should be a scalar, not an array, hence the following
210
       list1 = [(x,) for x in list1] # Convert each number to a tuple (x,)
       list2 = [(x,) for x in list2] # Convert each number to a tuple (x,)
       # Calculate the Dynamic Time Warping distance
       distance, path = fastdtw(list1, list2, dist=euclidean)
216
       # Print the DTW distance
       print(f"DTW distance for {year}: {distance}")
218
219
  years = df_host['Year'].unique()
220
   for year in years:
       DTW(year, df_program_plot, df_host)
   import numpy as np
224
   def fourier_transform(year, df_program_plot, df_host):
226
       # Get the list_change data
       host_country, list_change = hosting_list_vs_average_list(year,
      df_program_plot, df_host)
229
       # Ensure list_change is a list
230
       if list_change is None:
           list_change = []
       else:
           list_change = list(list_change)
       # Replace negative values with 0
       cleaned_list = replace_negative_with_zero(list_change)
238
       # Debug: Print the processed list (optional)
239
       # print(f"Cleaned list_change for {year}:", cleaned_list)
240
241
```

```
# Get award_rates
       host_country, award_rates = compare(1996, df_program_plot, df_host)
243
244
       # Ensure both lists have the same length
245
       min_len = min(len(cleaned_list), len(award_rates))
246
       list1 = cleaned_list[:min_len]
       list2 = award_rates[:min_len]
248
249
       # Apply Fourier Transform to both time series
250
       fft_list1 = np.fft.fft(list1)
       fft_list2 = np.fft.fft(list2)
252
253
       # Calculate the Euclidean distance between the two spectra (other distance
254
      metrics can be used)
       distance = np.linalg.norm(np.abs(fft_list1) - np.abs(fft_list2))
255
256
       # Output the distance after Fourier Transform
       print(f"Fourier Transform distance for {year}: {distance}")
259
   # Get all Olympic years (assuming the years are already present in df_host)
260
  years = df_host['Year'].unique()
262
   # Iterate through all Olympic years and calculate the Fourier Transform distance
263
   for year in years:
       fourier_transform(year, df_program_plot, df_host)
265
   import numpy as np
267
   def shape_based_distance(year, df_program_plot, df_host):
269
       # Retrieve the list_change data
       host_country, list_change = hosting_list_vs_average_list(year,
      df_program_plot, df_host)
       # Ensure list_change is a list
       if list_change is None:
274
           list_change = []
       else:
276
           list_change = list(list_change)
278
       # Replace negative values with 0
       cleaned_list = replace_negative_with_zero(list_change)
280
281
       # Retrieve award_rates
282
       host_country, award_rates = compare(1996, df_program_plot, df_host)
283
284
```

```
# Ensure both lists have the same length
       min_len = min(len(cleaned_list), len(award_rates))
286
       list1 = cleaned_list[:min_len]
287
       list2 = award_rates[:min_len]
288
289
       # Calculate the Euclidean distance between the two time series (shape-based
290
       distance = np.linalg.norm(np.array(list1) - np.array(list2))
291
292
       # Output the shape-based distance
293
       print(f"Shape-Based distance for {year}: {distance}")
294
295
   # Get all Olympic years (assuming the years are already present in df_host)
296
   years = df_host['Year'].unique()
297
   # Iterate through all Olympic years and calculate the shape-based distance
299
   for year in years:
       shape_based_distance(year, df_program_plot, df_host)
301
302
   import pandas as pd
303
304
   # Read score_rate.csv
305
  score_rate_df = pd.read_csv('C:/Users/admin/Desktop/MCM2025/2025_Problem_C_Data/
306
      score_rate.csv')
307
  # Read summerOly_hosts_completed.csv
  hosts_df = pd.read_csv('C:/Users/admin/Desktop/MCM2025/2025_Problem_C_Data/
309
      summerOly_hosts_completed.csv')
310
  # We only need the NOC and Year columns to determine the host country
311
  # Merge the data: Merge based on Year and NOC
  merged_df = pd.merge(score_rate_df, hosts_df[['Year', 'NOC']], on='Year', how='
      left')
314
  # Add a new column in merged_df to check if it's the host country
  merged_df['Host'] = merged_df.apply(lambda row: 1 if row['NOC_x'] == row['NOC']
316
      else 0, axis=1)
  # Drop intermediate columns created during the merge
318
  merged_df = merged_df.drop(columns=['NOC'])
   # Output the merged DataFrame to check the result
  print(merged_df)
323
  # Optionally save the result to a new CSV file
```

```
merged_df.to_csv('score_rate_with_host.csv', index=False)
326
  import pandas as pd
328
  # 1. Read data
329
  if_host_df = pd.read_csv('C:/Users/admin/Desktop/MCM2025/MCM2025/2025
      _Problem_C_Data/if_host.csv')
  sport_df = pd.read_csv('C:/Users/admin/Desktop/MCM2025/MCM2025/2025
      _Problem_C_Data/score_rate_with_host.csv')
  host_complete_df = pd.read_csv('C:/Users/admin/Desktop/MCM2025/MCM2025/2025
      _Problem_C_Data/summerOly_hosts_completed.csv')
333
  # 2. Merge the if_host data with the complete host city data
334
  merged_df = pd.merge(if_host_df, sport_df, how='left', left_on=['Year', 'NOC_x'],
       right_on=['Year', 'NOC_x'])
336
  # 3. Filter rows where the distance is 0, keeping only Olympic events hosted by
  filtered_df = merged_df[merged_df['distance'] == 0]
338
  # 4. Calculate the total Score_Rate for all events a country participated in
340
      during each Olympic year
  # Group by country (NOC_x) and year, then compute the sum of Score_Rate
  score_rate_sum_per_country_year = filtered_df.groupby(['NOC_x', 'Year'])['
      Score_Rate'].sum().reset_index()
343
  # 5. Calculate the average of total Score_Rate sums for all Olympic years a
344
  # First, group by country to compute the mean of Score_Rate sums
  score_rate_avg_per_country = score_rate_sum_per_country_year.groupby('NOC_x')['
      Score_Rate'].mean().reset_index()
347
  # 6. Rename the column to make it more descriptive
  score_rate_avg_per_country.rename(columns={'Score_Rate': 'Average_Score_Rate_Sum'
      }, inplace=True)
350
  # 7. Save the result to an Excel file
351
  score_rate_avg_per_country.to_excel('average_score_rate_sum_by_noc.xlsx', index=
      False)
  print("Excel file generated: average_score_rate_sum_by_noc.xlsx")
354
  # Filter rows where the distance is not 0
356
  filtered_if_host_df = if_host_df[if_host_df['distance'] != 0]
358
```

```
# 3. Merge the filtered if_host data with sport data to retrieve each event's
      Score_Rate, along with corresponding NOC and Year
  merged_df = pd.merge(filtered_if_host_df, sport_df, how='left', left_on=['Year',
      'NOC_x'], right_on=['Year', 'NOC_x'])
361
   # 4. Calculate the total Score_Rate for all events a country participated in
      during each Olympic year, keeping the distance column
  score_rate_sum_per_country_year = merged_df.groupby(['NOC_x', 'Year', 'distance'
      ])['Score_Rate'].sum().reset_index()
  # 5. Rename the column to make it more descriptive
365
   score_rate_sum_per_country_year.rename(columns={'Score_Rate': 'Score_Rate_Sum'},
      inplace=True)
367
   # 6. Save the result to an Excel file
   score_rate_sum_per_country_year.to_excel('
      score_rate_sum_for_hosting_countries_with_distance.xlsx', index=False)
370
   print("Excel file generated: score_rate_sum_for_hosting_countries_with_distance.
371
      xlsx")
373
   import pandas as pd
374
   import numpy as np
375
   import matplotlib.pyplot as plt
   import seaborn as sns
378
  # 1. Read the data
379
  score_rate_df = pd.read_excel('C:/Users/admin/Desktop/MCM2025/MCM2025/2025
      _Problem_C_Data/score_rate_sum_for_hosting_countries_with_distance.xlsx')
   average_score_df = pd.read_excel('C:/Users/admin/Desktop/MCM2025/MCM2025/2025
      _Problem_C_Data/average_score_rate_sum_nonhost.xlsx')
382
  # 2. Merge data based on NOC_x using a left join, obtaining S1 (Score_Rate_Sum)
      and S2 (Average_Score_Rate_Sum) for each country
  merged_df = pd.merge(score_rate_df, average_score_df, how='left', left_on='NOC_x'
384
      , right_on='NOC_x')
  # 3. Define a function to calculate P(ch)
386
   def calculate_P(ch, df):
       P_ch = 0
388
       for _, row in df.iterrows():
389
           S1 = row['Score_Rate_Sum']
                                       # Score_Rate_Sum
390
           S2 = row['Average_Score_Rate_Sum'] # Average_Score_Rate_Sum
391
           distance = row['distance']
392
```

```
P_{ch} += (S1 / (1 + distance * ch) - S2) ** 2
       return P_ch
394
395
   # 4. Iterate through different ch values, calculate P(ch), and store each P(ch)
396
   ch_values = np.linspace(0, 10, 100) # Adjust range and step size as needed
  P_values = []
398
   for ch in ch values:
400
       P_ch = calculate_P(ch, merged_df)
       P_values.append(P_ch)
402
403
   # 5. Find the maximum and minimum P(ch) values
404
  max_P = max(P_values)
  min_P = min(P_values)
  print(f"Maximum P(ch): {max_P}, Minimum P(ch): {min_P}")
407
  # 6. Plot a boxplot for P(ch) values
409
  plt.figure(figsize=(10, 6))
  sns.boxplot(data=P_values, color="lightblue")
411
plt.title('P(ch) Boxplot')
  plt.xlabel('P(ch) Values')
  plt.show()
414
  # 7. Calculate the IQR (Inter-Quartile Range) to detect outliers
416
  Q1 = np.percentile(P_values, 25)
  Q3 = np.percentile(P_values, 75)
418
  IQR = Q3 - Q1
  lower\_bound = Q1 - 1.5 * IQR
  upper_bound = Q3 + 1.5 * IQR
421
  # 8. Remove outliers from P(ch) values
  filtered_P_values = [P for P in P_values if lower_bound <= P <= upper_bound]
   # 9. Recalculate the minimum P(ch) and its corresponding ch value (after removing
  min_P_filtered = min(filtered_P_values)
427
  best_ch_filtered = ch_values[P_values.index(min_P_filtered)]
428
  print(f"After removing outliers, the minimum P(ch) is {min_P_filtered},
      corresponding to ch value {best_ch_filtered}")
431
  import pandas as pd
432
   import numpy as np
434
```

```
# Load the data
  df = pd.read_csv('feature_noc.csv')
  athletes_df = pd.read_csv('C:/Users/admin/Desktop/MCM2025/MCM2025/2025
      _Problem_C_Data/summerOly_athletes_completed.csv')
438
   # List of sports in the specified order
439
   sports = [
440
       "Aquatics", "Archery", "Athletics", "Badminton", "Baseball and Softball", "
      Basketball",
       "Boxing", "Breaking", "Canoeing", "Cycling", "Equestrian", "Fencing", "Field
442
      hockey",
       "Flag football", "Football", "Golf", "Gymnastics", "Handball", "Judo", "
443
      Karate",
       "Modern Pentathlon", "Rowing", "Rugby", "Sailing", "Shooting", "Skateboarding
444
       "Sport Climbing", "Surfing", "Table Tennis", "Taekwondo", "Tennis", "
445
      Triathlon",
       "Volleyball", "Weightlifting", "Wrestling"
446
447
448
   # Initialize lists to store participation and changes
   changes_list = []
   participation_list = []
451
  # Get all unique years and sort them
453
  years = df['Year'].unique()
  years.sort()
455
456
   # Iterate through each year in the data
457
   for i, year in enumerate(years):
458
       # Filter the data for the current year
       current_year_data = athletes_df[athletes_df['Year'] == year]
460
461
       # Initialize participation counts for all sports (default to 0)
462
       participation_counts = [0] * len(sports)
463
       for sport in current_year_data['Sport'].unique():
464
           if sport in sports: # Only include the specified sports
465
               participation_counts[sports.index(sport)] = current_year_data[
      current_year_data['Sport'] == sport].shape[0]
       # Handle the first Olympic year
468
       if i == 0:
469
           # For the first year, the participation increase is the same as
470
      participation counts (no prior data)
           participation_increase = participation_counts
471
```

```
else:
           prev_year = year - 4 # The year of the previous Olympics
473
           # Check if the previous year has data
475
           if prev_year in athletes_df['Year'].unique():
476
               prev_year_data = athletes_df[athletes_df['Year'] == prev_year]
478
               # Initialize participation counts for the previous year
               prev_participation_counts = [0] * len(sports)
480
               for sport in prev_year_data['Sport'].unique():
                    if sport in sports:
482
                        prev_participation_counts[sports.index(sport)] =
483
      prev_year_data[prev_year_data['Sport'] == sport].shape[0]
484
               # Calculate participation increase: current year - previous year
               participation_increase = [current - prev for current, prev in zip(
486
      participation_counts, prev_participation_counts)]
           else:
487
               # If no data for the previous year, assume participation counts were
188
               participation_increase = participation_counts
489
490
       # Add participation increase to the list for all rows of the current year
491
       participation_list.extend([participation_increase] * len(df[df['Year'] ==
      year]))
493
       # Handle changes in events (Event_Changes)
494
       if i == 0:
495
           # For the first year, all changes are 0
496
           changes = [0] * len(sports)
497
           changes_list.extend([changes] * len(df[df['Year'] == year]))
498
       else:
499
           prev_year = year - 4
500
501
           if prev_year in athletes_df['Year'].unique():
               prev_year_data = athletes_df[athletes_df['Year'] == prev_year]
503
504
               # Initialize counts for the previous year's sports
505
               prev_sports_count = [0] * len(sports)
506
               for sport in prev_year_data['Sport'].unique():
                    if sport in sports:
508
                        prev_sports_count[sports.index(sport)] = prev_year_data[
509
      prev_year_data['Sport'] == sport].shape[0]
510
               # Calculate changes in events: current year - previous year
511
```

```
changes = [current - prev for current, prev in zip(
      participation_counts, prev_sports_count)]
           else:
513
               # If no data for the previous year, assume changes are equal to
               changes = participation_counts
515
           # Add changes to the list for all rows of the current year
517
           changes_list.extend([changes] * len(df[df['Year'] == year]))
518
   # Add participation increase and event changes as new columns in the DataFrame
   df['Participation_List'] = participation_list
   df['Event_Changes'] = changes_list
523
   # Save the updated DataFrame to a CSV file
  df.to_csv('feature_noc(2).csv', index=False)
525
  import pandas as pd
527
   import ast
528
529
   # Read the CSV file
530
  df = pd.read_csv('feature_Noc.csv')
531
532
   # Initialize dictionaries to store the number of participating countries and
  participating_countries = {}
  participating_athletes = {}
535
   # Iterate through the data to calculate the number of participating countries and
537
   for index, row in df.iterrows():
       year = row['Year']
539
       participatelist = ast.literal_eval(row['Participants_List']) # Convert
540
      string to a list
       # Initialize data for the year if not already in the dictionaries
542
       if year not in participating_countries:
543
           participating_countries[year] = [0] * 34 # Initialize with 34 sports (or
           participating_athletes[year] = [0] * 34 # Same initialization for
546
       # Update the number of participating countries and athletes for each sport
547
       for i, participants in enumerate(participatelist):
548
           participants = int(participants) # Ensure participant count is an
549
```

```
if participants > 0:
550
               participating_countries[year][i] += 1 # Increment the country count
      if participants > 0
           participating_athletes[year][i] += participants # Add the number of
552
553
   # Function to calculate the change between two years
   def calculate_changes(year, previous_year, current_data, previous_data):
555
       if previous_year not in previous_data: # If there is no data for the
           return [x for x in current_data] # Return the current data as the change
557
       # Calculate the change by subtracting previous year data from current year
558
       return [current - previous for current, previous in zip(current_data,
      previous_data[previous_year])]
   # Add new columns for changes
561
   country_changes = []
   athlete_changes = []
563
   for index, row in df.iterrows():
565
       year = row['Year']
566
       previous_year = year - 4 # Olympics occur every 4 years
       participatelist = ast.literal_eval(row['Participants_List']) # Convert
568
      string to a list
569
       # Calculate changes for countries and athletes
571
       country_change = calculate_changes(year, previous_year,
      participating_countries[year], participating_countries)
       athlete_change = calculate_changes(year, previous_year,
      participating_athletes[year], participating_athletes)
573
       # Append the changes to the respective lists
574
       country_changes.append(country_change)
       athlete_changes.append(athlete_change)
576
577
   # Add the new columns to the DataFrame
  df['CountryChange'] = country_changes
579
   df['AthleteChange'] = athlete_changes
581
  # Save the updated DataFrame to a new CSV file
  df.to_csv('feature_Noc_with_changes.csv', index=False)
583
584
```

```
print("Processing complete. Results saved to 'feature_Noc_with_changes.csv'")
```

Listing 14: data\_analyze.ipynb

```
import numpy as np
2 import pandas as pd
from sklearn.ensemble import RandomForestClassifier, RandomForestRegressor
4 from sklearn.model_selection import train_test_split, cross_val_score
from sklearn.preprocessing import StandardScaler
  from tensorflow.keras.models import Sequential
  from tensorflow.keras.layers import LSTM, Dense
  class OlympicPredictionModel:
9
      def __init__(self, lambda_weight=0.3, mu_weight=0.85):
10
11
          Initialize model weights
          :param lambda_weight: Small country weight
          :param mu_weight: Large country weight
          self.lambda_weight = lambda_weight
16
          self.mu_weight = mu_weight
          self.classifier = RandomForestClassifier(n_estimators=200)
18
          self.regressor1 = RandomForestRegressor(n_estimators=200)
          self.regressor2 = RandomForestRegressor(n_estimators=200)
20
          self.lstm_models = {}
      @staticmethod
23
      def calculate_w4_vector(country_change, athlete_change, event_changes):
          Vectorized calculation of W4
          w1 = np.sum(country_change, axis=1).astype(np.float64)
          w2 = np.sum(athlete_change, axis=1).astype(np.float64)
29
          w3 = np.sum(event_changes, axis=1).astype(np.float64)
30
          w4 = np.divide(0.2 * w1 + 0.8 * w2, w3, out=np.zeros_like(w3, dtype=np.
31
      float64), where=w3 != 0)
          return w4
33
      def preprocess_data(self, data):
34
35
          Preprocess data, including calculating features A, B, and C
36
          # Feature A
38
          score_rate_list = np.array(data['Score_Rate_List'].apply(eval).tolist())
39
          score_list = np.array(data['Score_List'].apply(eval).tolist(), dtype=np.
40
     float64)
```

```
participants_list = np.array(data['Participants_List'].apply(eval).tolist
      (), dtype=np.float64)
          v5_5_a = np.sum(score_rate_list, axis=1)
43
          v8_5_a = np.sum(np.divide(score_list, participants_list,
                                     out=np.zeros_like(score_list, dtype=np.float64)
                                     where=participants_list > 0), axis=1)
47
          country_change = np.array(data['CountryChange'].apply(eval).tolist())
          athlete_change = np.array(data['AthleteChange'].apply(eval).tolist())
49
          event_changes = np.array(data['Event_Changes'].apply(eval).tolist())
50
          w4 = self.calculate_w4_vector(country_change, athlete_change,
51
      event_changes)
52
          v8_w4 = np.sum(np.multiply(
53
               np.divide(score_list, participants_list, out=np.zeros_like(score_list
      , dtype=np.float64), where=participants_list > 0),
              w4[:, None]
55
          ), axis=1)
56
          features_a = np.column_stack((v5_5_a, v8_5_a, v8_w4))
58
59
          # Feature B
          v1_b = data['if_host'].values
61
          v5_5_b = np.sum(participants_list, axis=1)
          v6_b = data['Gold_prev'].fillna(0).values
63
          v7_b = data['distance'].values
          v3_5_b = data['Score'].values
          v3_w4_b = np.sum(np.multiply(score_list, w4[:, None]), axis=1)
66
          features_b = np.column_stack((v1_b, v5_5_b, v6_b, v7_b, v3_5_b, v3_w4_b))
          # Feature C (same as B)
70
          features_c = features_b.copy()
72
          # Labels and expectations
          labels = (data['Total_Medals'] > 0).astype(int).values
          medal_expectation = data['Total_Medals'].values
          gold_expectation = data['Gold'].values
          scaler = StandardScaler()
          features_a_scaled = scaler.fit_transform(features_a)
79
          features_b_scaled = scaler.fit_transform(features_b)
80
          features_c_scaled = scaler.fit_transform(features_c)
81
```

```
return features_a_scaled, features_b_scaled, features_c_scaled, labels,
83
      medal_expectation, gold_expectation
84
       def train_classifier(self, features_a, other_features, labels):
85
           Train the classifier to predict medal-winning probability
88
           input_features = np.hstack([
89
               self.lambda_weight * features_a,
                (1 - self.lambda_weight) * other_features
91
92
           ])
           self.classifier.fit(input_features, labels)
93
94
       def train_regressor1(self, classifier_output, features_b, medal_expectation):
95
96
           Train regressor 1 to predict medal expectation
98
           input_features = np.hstack([classifier_output.reshape(-1, 1), features_b
99
      ])
           self.regressor1.fit(input_features, medal_expectation)
100
101
       def train_regressor2(self, medal_expectation, features_c, gold_expectation):
102
103
           Train regressor 2 to predict gold medal expectation
104
105
           input_features = np.hstack([
106
                (1 - self.mu_weight) * medal_expectation.reshape(-1, 1),
               self.mu_weight * features_c
108
           ])
109
           self.regressor2.fit(input_features, gold_expectation)
110
       def train_lstm(self, features, feature_name):
           Train an LSTM model to predict given features
           :param features: Historical feature data
115
           :param feature_name: Feature name (A, B, C)
116
           X = features[:-1]
118
           y = features[1:]
120
           X = X.reshape((X.shape[0], X.shape[1], 1))
           model = Sequential([
123
               LSTM(50, activation='relu', input_shape=(X.shape[1], 1)),
124
```

```
Dense(y.shape[1])
           1)
126
           model.compile(optimizer='adam', loss='mse')
           model.fit(X, y, epochs=50, verbose=0)
128
129
           self.lstm_models[feature_name] = model
130
       def predict_future_features(self, features, feature_name):
           Use LSTM models to predict future features
           model = self.lstm_models[feature_name]
           features = features.reshape((features.shape[0], features.shape[1], 1))
           return model.predict(features)
138
139
       def predict(self, features_a, features_b, features_c):
140
           Predict 2028 Olympics results
142
143
           input_features = np.hstack([features_a, features_b])
144
           classifier_output = self.classifier.predict_proba(input_features)[:, 1]
145
           medal_expectation = self.regressor1.predict(np.hstack([classifier_output.
146
      reshape(-1, 1), features_b]))
           gold_expectation = self.regressor2.predict(np.hstack([
                (1 - self.mu_weight) * medal_expectation.reshape(-1, 1),
148
               self.mu_weight * features_c
           1))
150
           return medal_expectation, gold_expectation
152
   def plot_n_estimators_curve(features_a, features_b, labels, n_range=range(10,
153
      500, 20)):
154
       Plot Random Forest learning curve for different tree counts
155
156
       import matplotlib.pyplot as plt
       from sklearn.model_selection import cross_val_score
158
159
       train_scores = []
160
       cv_scores = []
161
       input_features = np.hstack([features_a, features_b])
162
163
       for n in n_range:
164
           clf = RandomForestClassifier(n_estimators=n, random_state=42)
165
           clf.fit(input_features, labels)
166
           train_scores.append(clf.score(input_features, labels))
167
```

```
cv_score = cross_val_score(clf, input_features, labels, cv=5).mean()
           cv_scores.append(cv_score)
169
           print(f"Trees: {n}, Train Score: {train_scores[-1]:.4f}, CV Score: {
      cv_scores[-1]:.4f}")
171
       plt.figure(figsize=(10, 6))
       plt.plot(n_range, train_scores, label='Training Score')
       plt.plot(n_range, cv_scores, label='Cross-Validation Score')
174
       plt.xlabel('Number of Trees')
       plt.ylabel('Score')
       plt.title('Random Forest Performance vs Number of Trees')
       plt.legend()
178
       plt.grid(True)
       plt.show()
180
181
   # Example: Load data and train the model
182
   if __name__ == "__main__":
       # Load historical data
184
       data = pd.read_csv("C:/Users/admin/Desktop/MCM2025/MCM2025/2025
185
      _Problem_C_Data/feature_Noc.csv")
186
       model = OlympicPredictionModel(lambda_weight=0.3, mu_weight=0.85)
187
       features_a, features_b, features_c, labels, medal_expectation,
188
      gold_expectation = model.preprocess_data(data)
189
       # Train classifier and regressors
190
       model.train_classifier(features_a, features_b, labels)
       classifier_output = model.classifier.predict_proba(np.hstack([features_a,
192
      features_b]))[:, 1]
       model.train_regressor1(classifier_output, features_b, medal_expectation)
193
       model.train_regressor2(medal_expectation, features_c, gold_expectation)
195
       # Cross-validation for classifier
196
       scores_classifier = cross_val_score(model.classifier, np.hstack([features_a,
197
      features_b]), labels, cv=5)
       print(f'Classifier CV Accuracy: {np.mean(scores_classifier):.4f}')
198
199
       # Cross-validation for regressor 1
200
       X_reg1 = np.hstack([classifier_output.reshape(-1, 1), features_b])
201
       scores_regressor1 = cross_val_score(model.regressor1, X_reg1,
202
      medal_expectation, cv=5)
       print(f'Regressor1 CV R^2: {np.mean(scores_regressor1):.4f}')
203
204
       # Cross-validation for regressor 2
205
       X_reg2 = np.hstack([(1 - model.mu_weight) * medal_expectation.reshape(-1, 1),
206
```

```
model.mu_weight * features_c])
       scores_regressor2 = cross_val_score(model.regressor2, X_reg2,
207
      gold_expectation, cv=5)
       print(f'Regressor2 CV R^2: {np.mean(scores_regressor2):.4f}')
208
209
       # Plot learning curve
       print("\nPlotting Random Forest learning curve:")
       plot_n_estimators_curve(features_a, features_b, labels)
  import numpy as np
  import pandas as pd
215
  from sklearn.ensemble import RandomForestClassifier, RandomForestRegressor
  from sklearn.preprocessing import StandardScaler
  from sklearn.model_selection import cross_val_score
   import matplotlib.pyplot as plt
219
  from tensorflow.keras.models import Sequential
   from tensorflow.keras.layers import LSTM, Dense
   class OlympicPredictionModel:
       def __init__(self, lambda_weight=0.3, mu_weight=0.85):
224
           self.lambda_weight = lambda_weight
           self.mu_weight = mu_weight
226
           self.classifier = RandomForestClassifier(n_estimators=300)
           self.regressor1 = RandomForestRegressor()
           self.regressor2 = RandomForestRegressor()
229
           self.lstm_models = {}
230
       @staticmethod
233
       def calculate_w4_vector(country_change, athlete_change, event_changes):
           w1 = np.sum(country_change, axis=1).astype(np.float64)
234
           w2 = np.sum(athlete_change, axis=1).astype(np.float64)
           w3 = np.sum(event_changes, axis=1).astype(np.float64)
236
           w4 = np.divide(0.2 * w1 + 0.8 * w2, w3, out=np.zeros_like(w3, dtype=np.
      float64), where=w3 != 0)
           return w4
239
       def preprocess_data(self, data):
240
           """Data preprocessing: using data from the previous Olympic Games to
      predict the current one."""
           # Filter out data prior to 1964
           data = data[data['Year'] >= 1964].copy()
243
244
           # Calculate feature A
245
           score_rate_list = np.array(data['Score_Rate_List'].apply(eval).tolist())
246
           score_list = np.array(data['Score_List'].apply(eval).tolist(), dtype=np.
```

```
float64)
           participants_list = np.array(data['Participants_List'].apply(eval).tolist
248
      (), dtype=np.float64)
249
           # Sort data by NOC and Year to create lagged features
250
           data = data.sort_values(['NOC_x', 'Year'])
           # Feature A calculations
253
           v5_5_a = np.sum(score_rate_list, axis=1)
254
           v8_5_a = np.sum(np.divide(score_list, participants_list,
                                      out=np.zeros_like(score_list, dtype=np.float64)
256
                                      where=participants_list > 0), axis=1)
258
           country_change = np.array(data['CountryChange'].apply(eval).tolist())
           athlete_change = np.array(data['AthleteChange'].apply(eval).tolist())
260
           event_changes = np.array(data['Event_Changes'].apply(eval).tolist())
           w4 = self.calculate_w4_vector(country_change, athlete_change,
262
      event_changes)
263
           v8_w4 = np.sum(np.multiply(
               np.divide(score_list, participants_list, out=np.zeros_like(score_list
265
      ), where=participants_list > 0),
               w4[:, None]
266
           ), axis=1)
267
           features_a = np.column_stack((v5_5_a, v8_5_a, v8_w4))
269
           # Feature B calculations
           v1_b = data['if_host'].values
           v5_5_b = np.sum(participants_list, axis=1)
           v6_b = data['Gold_prev'].fillna(0).values
274
           v7_b = data['distance'].values
           v3_5_b = data['Score'].values
           v3_w4_b = np.sum(np.multiply(score_list, w4[:, None]), axis=1)
278
           features_b = np.column_stack((v1_b, v5_5_b, v6_b, v7_b, v3_5_b, v3_w4_b))
279
280
           # Feature C is identical to Feature B
281
           features_c = features_b.copy()
283
           # Shift features by one event to align with the lagged labels
284
           features_a = np.roll(features_a, 1, axis=0)
285
           features_b = np.roll(features_b, 1, axis=0)
286
           features_c = np.roll(features_c, 1, axis=0)
287
```

```
# Remove the first row (no previous data available)
289
           features_a = features_a[1:]
           features_b = features_b[1:]
291
           features_c = features_c[1:]
292
           # Adjust labels accordingly
294
           labels = (data['Total_Medals'] > 0).astype(int).values[1:]
295
           medal_expectation = data['Total_Medals'].values[1:]
296
           gold_expectation = data['Gold'].values[1:]
           # Standardize features
           scaler = StandardScaler()
           features_a_scaled = scaler.fit_transform(features_a)
301
           features_b_scaled = scaler.fit_transform(features_b)
302
           features_c_scaled = scaler.fit_transform(features_c)
303
           return features_a_scaled, features_b_scaled, features_c_scaled, labels,
305
      medal_expectation, gold_expectation
306
       def train_classifier(self, features_a, other_features, labels):
307
           input_features = np.hstack([
308
               self.lambda_weight * features_a,
309
               (1 - self.lambda_weight) * other_features
           1)
           self.classifier.fit(input_features, labels)
       def train_regressor1(self, classifier_output, features_b, medal_expectation):
           input_features = np.hstack([classifier_output.reshape(-1, 1), features_b
315
      1)
           self.regressor1.fit(input_features, medal_expectation)
317
       def train_regressor2(self, medal_expectation, features_c, gold_expectation):
318
           input_features = np.hstack([
319
               (1 - self.mu_weight) * medal_expectation.reshape(-1, 1),
               self.mu_weight * features_c
           1)
           self.regressor2.fit(input_features, gold_expectation)
324
       def predict(self, features_a, features_b, features_c):
325
           input_features = np.hstack([features_a, features_b])
           classifier_output = self.classifier.predict_proba(input_features)[:, 1]
327
           medal_expectation = self.regressor1.predict(np.hstack([classifier_output.
328
      reshape(-1, 1), features_b]))
           gold_expectation = self.regressor2.predict(np.hstack([
329
```

```
(1 - self.mu_weight) * medal_expectation.reshape(-1, 1),
               self.mu_weight * features_c
           ]))
           return medal_expectation, gold_expectation
334
   def plot_regressor_learning_curves(features, targets, n_range=range(10, 1000, 10)
                                        regressor_name="Regressor"):
336
       """Plot learning curves for a Random Forest regressor."""
       train_scores = []
       cv_scores = []
339
340
       for n in n_range:
           regr = RandomForestRegressor(n_estimators=n, random_state=42)
342
           regr.fit(features, targets)
343
           train_scores.append(regr.score(features, targets))
344
           cv_score = cross_val_score(regr, features, targets, cv=5).mean()
           cv_scores.append(cv_score)
346
           print(f"{regressor_name} Trees: {n}, Train Score: {train_scores[-1]:.4f},
347
       CV Score: {cv_scores[-1]:.4f}")
348
       plt.figure(figsize=(10, 6))
349
       plt.plot(n_range, train_scores, label='Training Score')
350
       plt.plot(n_range, cv_scores, label='Cross-Validation Score')
       plt.xlabel('Number of Trees')
352
       plt.ylabel('Score')
353
       plt.title(f'{regressor_name} Performance vs Number of Trees')
354
       plt.legend()
355
       plt.grid(True)
356
       plt.show()
  if __name__ == "__main__":
359
       # Load data
360
       data = pd.read_csv("C:/Users/admin/Desktop/MCM2025/MCM2025/2025
361
      _Problem_C_Data/feature_Noc.csv")
362
       # Initialize the model
363
       model = OlympicPredictionModel(lambda_weight=0.3, mu_weight=0.85)
364
       features_a, features_b, features_c, labels, medal_expectation,
365
      gold_expectation = model.preprocess_data(data)
366
       # Train the model
367
       model.train_classifier(features_a, features_b, labels)
368
       classifier_output = model.classifier.predict_proba(np.hstack([features_a,
369
      features_b]))[:, 1]
```

```
model.train_regressor1(classifier_output, features_b, medal_expectation)
       model.train_regressor2(medal_expectation, features_c, gold_expectation)
       # Cross-validation
       input_features = np.hstack([features_a, features_b])
       scores_classifier = cross_val_score(model.classifier, input_features, labels,
375
       cv=5)
       print(f'Classifier CV Accuracy: {np.mean(scores_classifier):.4f}')
376
       X_reg1 = np.hstack([classifier_output.reshape(-1, 1), features_b])
       scores_regressor1 = cross_val_score(model.regressor1, X_reg1,
379
      medal_expectation, cv=5)
       print(f'Regressor1 CV R^2: {np.mean(scores_regressor1):.4f}')
380
381
       X_reg2 = np.hstack([(1 - model.mu_weight) * medal_expectation.reshape(-1, 1),
382
       model.mu_weight * features_c])
       scores_regressor2 = cross_val_score(model.regressor2, X_reg2,
      gold_expectation, cv=5)
       print(f'Regressor2 CV R^2: {np.mean(scores_regressor2):.4f}')
384
385
       # Plot learning curves for regressors
       print("\nPlotting learning curve for Medal Regressor (Total Medals):")
387
       plot_regressor_learning_curves(X_reg1, medal_expectation, regressor_name="
388
      Medal Regressor")
389
       print("\nPlotting learning curve for Gold Regressor (Gold Medals):")
390
       plot_regressor_learning_curves(X_reg2, gold_expectation, regressor_name="Gold
391
       Regressor")
392
   class OlympicPredictionModel:
393
       def __init__(self, lambda_weight=0.3, mu_weight=0.85):
395
           Initialize model weights
           :param lambda_weight: Weight for small countries
397
           :param mu_weight: Weight for large countries
           self.lambda_weight = lambda_weight
400
           self.mu_weight = mu_weight
401
           self.classifier = RandomForestClassifier(n_estimators=200)
402
           self.regressor1 = RandomForestRegressor(n_estimators=200)
           self.regressor2 = RandomForestRegressor(n_estimators=200)
404
           self.lstm_models = {}
405
406
       @staticmethod
407
       def classify_country(year, noc, data):
408
```

```
Determine whether a country is a 'small country' based on participation
410
      history
           :param year: Current year
411
           :param noc: Country code
412
           :param data: Full dataset
413
           :return: True if it is a small country, False otherwise
414
415
           # Calculate the total participation count of the country up to the given
416
      year
           historical_data = data[data['Year'] <= year]</pre>
417
           country_total = historical_data[historical_data['NOC_x'] == noc]['
418
      Name_Count'].sum()
419
           # Calculate total participation counts for all countries
420
           all_countries = historical_data.groupby('NOC_x')['Name_Count'].sum()
421
           # Calculate the 20th percentile threshold
423
           threshold = all_countries.quantile(0.2)
424
425
           return country_total <= threshold</pre>
426
427
       def calculate_w4_vector(self, country_change, athlete_change, event_changes):
428
           Vectorized calculation of W4
430
431
           w1 = np.sum(country_change, axis=1).astype(np.float64)
432
           w2 = np.sum(athlete_change, axis=1).astype(np.float64)
433
           w3 = np.sum(event_changes, axis=1).astype(np.float64)
434
           w4 = np.divide(0.2 * w1 + 0.8 * w2, w3, out=np.zeros_like(w3, dtype=np.
435
      float64), where=w3 != 0)
           return w4
436
437
       def preprocess_data(self, data):
438
439
           Preprocess data, including featureA, featureB, featureC, and feature_all
440
      using reference years
           # Create a year mapping dictionary
442
           year_mapping = pd.read_csv("year_transmition_reference.csv")
443
           year_dict = dict(zip(year_mapping['evaluating_year'], year_mapping['
444
      use_data_from']))
445
           features_list = []
446
           for idx, row in data.iterrows():
447
```

```
current_year = row['Year']
               # Get reference year data
449
               reference_year = year_dict.get(current_year, current_year)
450
               reference_data = data[data['Year'] == reference_year]
451
452
               if len(reference_data) > 0:
453
                    # Use the feature data from the reference year
454
                    ref_row = reference_data[reference_data['NOC_x'] == row['NOC_x']]
                    ref_row = ref_row.iloc[0] if len(ref_row) > 0 else row
456
               else:
                    ref_row = row # Use current year data if no reference found
458
459
               # Feature A calculations
460
               score_rate_list = np.array(eval(ref_row['Score_Rate_List']))
461
               score_list = np.array(eval(ref_row['Score_List']), dtype=np.float64)
462
               participants_list = np.array(eval(ref_row['Participants_List']),
463
      dtype=np.float64)
464
               v4_ = np.sum(score_rate_list)
465
               v5_ = np.sum(participants_list)
466
               v8_ = np.sum(np.divide(score_list, participants_list,
467
                                        out=np.zeros_like(score_list, dtype=np.float64
468
      ),
                                        where=participants_list > 0))
470
               country_change = np.array(eval(ref_row['CountryChange']))
471
               athlete_change = np.array(eval(ref_row['AthleteChange']))
472
               event_changes = np.array(eval(ref_row['Event_Changes']))
               w4_ = self.calculate_w4_vector(country_change.reshape(1, -1),
                                                athlete_change.reshape(1, -1),
475
                                                event_changes.reshape(1, -1))[0]
476
               v8_w4 = np.sum(np.multiply(
                    np.divide(score_list, participants_list,
479
                              out=np.zeros_like(score_list, dtype=np.float64),
                              where=participants_list > 0),
481
                    w4_
482
               ))
484
               # Feature B calculations
               v1 = ref_row['if_host']
486
               v6 = ref_row['Gold_prev'] if pd.notna(ref_row['Gold_prev']) else 0
487
               v7 = ref_row['distance']
488
               v3_ = ref_row['Score']
489
               v3_w4 = np.sum(np.multiply(score_list, w4_))
```

```
# Feature all
492
               w3_ = np.sum(event_changes)
493
494
               features = {
495
                    'features_a': [v5_, v8_, v8_w4],
496
                    'features_b': [v1, v5_, v6, v7, v3_, v3_w4, v8_],
497
                    'features_c': [v1, v5_, v6, v7, v3_, v3_w4, v8_],
                    'features_all': [v1, v3_, v4_, v5_, v6, v7, v8_, w3_, w4_]
499
               }
               features_list.append(features)
501
502
           # Convert feature list into numpy arrays
503
           features_a = np.array([f['features_a'] for f in features_list])
504
           features_b = np.array([f['features_b'] for f in features_list])
505
           features_c = np.array([f['features_c'] for f in features_list])
506
           features_all = np.array([f['features_all'] for f in features_list])
508
           # Use the labels and expected values from the current year
509
           labels = (data['Total_Medals'] > 0).astype(int).values
510
           medal_expectation = data['Total_Medals'].values
511
           gold_expectation = data['Gold'].values
512
513
           # Standardize the features
           scaler = StandardScaler()
515
           features_a_scaled = scaler.fit_transform(features_a)
516
           features_b_scaled = scaler.fit_transform(features_b)
517
           features_c_scaled = scaler.fit_transform(features_c)
518
           features_all_scaled = scaler.fit_transform(features_all)
519
           return features_a_scaled, features_b_scaled, features_c_scaled,
521
      features_all_scaled, labels, medal_expectation, gold_expectation
522
       # Other methods including training and prediction remain unchanged
       # ...
525
  import numpy as np
526
  import pandas as pd
527
  from sklearn.ensemble import RandomForestClassifier, RandomForestRegressor
  from sklearn.preprocessing import StandardScaler
  from keras.models import Model
530
  from keras.layers import Input, LSTM, Dense, Dot, Activation, Concatenate
  from keras.optimizers import Adam
  from keras.callbacks import ReduceLROnPlateau
```

```
class OlympicPredictionModel:
       def __init__(self, lambda_weight=0.3, mu_weight=0.85, learning_rate=0.001):
536
538
           :param lambda_weight: Weight for small countries
539
           :param mu_weight: Weight for large countries
540
           :param learning_rate: Learning rate for Adam optimizer
541
542
           self.lambda_weight = lambda_weight
543
           self.mu_weight = mu_weight
           self.learning_rate = learning_rate # Learning rate for Adam optimizer
545
           self.classifier = RandomForestClassifier(n_estimators=200)
           self.regressor1 = RandomForestRegressor(n_estimators=200)
           self.regressor2 = RandomForestRegressor(n_estimators=200)
548
           self.lstm_model = None
550
       @staticmethod
       def Country_classification(year, Noc_x, data):
553
           Determine whether a country is classified as a 'small country' based on
554
      historical data
           :param year: Current year
555
           :param Noc_x: Country code
556
           :param data: Dataset
           :return: True if classified as a small country, otherwise False
558
559
           historical_data = data[data['Year'] <= year]</pre>
560
           country_total = historical_data[historical_data['NOC_x'] == Noc_x]['
561
      Name_Count'].sum()
           all_countries = historical_data.groupby('NOC_x')['Name_Count'].sum()
562
           threshold = all_countries.quantile(0.2)
           return country_total <= threshold</pre>
564
565
       def calculate_w4_vector(self, country_change, athlete_change, event_changes):
566
           Calculate the W4 vector
569
           w1 = np.sum(country_change, axis=1).astype(np.float64)
           w2 = np.sum(athlete_change, axis=1).astype(np.float64)
571
           w3 = np.sum(event_changes, axis=1).astype(np.float64)
           w4 = np.divide(0.2 * w1 + 0.8 * w2, w3, out=np.zeros_like(w3, dtype=np.
573
      float64), where=w3 != 0)
           return w4
574
575
       def preprocess_data(self, data):
576
```

```
Data preprocessing, including generating features A, B, C, and All
578
           year_mapping = pd.read_csv("year_transmition_reference.csv")
580
           year_dict = dict(zip(year_mapping['evaluating_year'], year_mapping['
581
      use_data_from']))
582
           features_list = []
583
           for idx, row in data.iterrows():
584
               current_year = row['Year']
               reference_year = year_dict.get(current_year, current_year)
586
               reference_data = data[data['Year'] == reference_year]
               if len(reference_data) > 0:
589
                    ref_row = reference_data[reference_data['NOC_x'] == row['NOC_x']]
                    ref_row = ref_row.iloc[0] if len(ref_row) > 0 else row
591
               else:
                    ref_row = row
593
594
               score_rate_list = np.array(eval(ref_row['Score_Rate_List']))
595
               score_list = np.array(eval(ref_row['Score_List']), dtype=np.float64)
596
               participants_list = np.array(eval(ref_row['Participants_List']),
597
      dtype=np.float64)
               v4_ = np.sum(score_rate_list)
599
               v5_ = np.sum(participants_list)
600
               v8_ = np.sum(np.divide(score_list, participants_list, out=np.
601
      zeros_like(score_list, dtype=np.float64), where=participants_list > 0))
602
               country_change = np.array(eval(ref_row['CountryChange']))
603
               athlete_change = np.array(eval(ref_row['AthleteChange']))
604
               event_changes = np.array(eval(ref_row['Event_Changes']))
605
               w4_ = self.calculate_w4_vector(country_change.reshape(1, -1),
      athlete_change.reshape(1, -1), event_changes.reshape(1, -1))[0]
               v8_w4 = np.sum(np.multiply(np.divide(score_list, participants_list,
608
      out=np.zeros_like(score_list, dtype=np.float64), where=participants_list > 0)
       , w4_{-}))
609
               v1 = ref_row['if_host']
610
               v6 = ref_row['Gold_prev'] if pd.notna(ref_row['Gold_prev']) else 0
611
               v7 = ref_row['distance']
               v3_ = ref_row['Score']
613
               v3_w4 = np.sum(np.multiply(score_list, w4_))
614
615
```

```
w3_ = np.sum(event_changes)
617
               features = {
                    'features_a': [v5_, v8_, v8_w4],
                    'features_b': [v1, v5_, v6, v7, v3_, v3_w4, v8_],
620
                    'features_c': [v1, v5_, v6, v7, v3_, v3_w4, v8_],
                    'features_all': [v1, v3_, v4_, v5_, v6, v7, v8_, w3_, w4_]
622
               }
623
               features_list.append(features)
624
           features_a = np.array([f['features_a'] for f in features_list])
           features_b = np.array([f['features_b'] for f in features_list])
           features_c = np.array([f['features_c'] for f in features_list])
           features_all = np.array([f['features_all'] for f in features_list])
630
           labels = (data['Total_Medals'] > 0).astype(int).values
631
           medal_expectation = data['Total_Medals'].values
           gold_expectation = data['Gold'].values
634
           scaler = StandardScaler()
635
           features_a_scaled = scaler.fit_transform(features_a)
           features_b_scaled = scaler.fit_transform(features_b)
637
           features_c_scaled = scaler.fit_transform(features_c)
           features_all_scaled = scaler.fit_transform(features_all)
640
           return features_a_scaled, features_b_scaled, features_c_scaled,
641
      features_all_scaled, labels, medal_expectation, gold_expectation
       def train_classifier(self, features_a, features_all, labels, data):
643
644
           Train the classifier to predict whether medals will be won
645
646
           years = data['Year'].values
           nocs = data['NOC_x'].values
           is_small_countries = np.array([self.Country_classification(year, noc,
      data)
                                         for year, noc in zip(years, nocs)])
651
652
           final_features = np.zeros((len(labels), features_all.shape[1]))
           small_countries_mask = is_small_countries
655
           final_features[small_countries_mask] = (1 - self.lambda_weight) *
656
      features_all[small_countries_mask]
           final_features[small_countries_mask, :features_a.shape[1]] += self.
657
```

```
lambda_weight * features_a[small_countries_mask]
658
           final_features[~small_countries_mask] = features_all[~
      small_countries_mask]
660
           self.classifier.fit(final_features, labels)
661
           self.classifier_output = self.classifier.predict_proba(final_features)
662
663
       def train_regressor1(self, features_b, medal_expectation):
664
           Train regressor 1 to predict medal expectations
666
           classifier_probabilities = self.classifier_output[:, 1]
668
           input_features = np.hstack([classifier_probabilities.reshape(-1, 1),
669
      features_b])
           self.regressor1.fit(input_features, medal_expectation)
       def train_regressor2(self, features_c, gold_expectation):
673
           Train regressor 2 to predict gold medal expectations
674
           classifier_probabilities = self.classifier_output[:, 1]
676
           input_features_reg1 = np.hstack([classifier_probabilities.reshape(-1, 1),
       features_c])
           medal_expectation = self.regressor1.predict(input_features_reg1)
678
           input_features = np.hstack([
                (1 - self.mu_weight) * medal_expectation.reshape(-1, 1),
680
               self.mu_weight * features_c
           ])
682
           self.regressor2.fit(input_features, gold_expectation)
683
       def create_lstm_attention_model(self, input_shape):
685
           Create an LSTM-based attention model for sequential prediction
687
           inputs = Input(shape=(input_shape[1], input_shape[2]))
689
690
           lstm_out, state_h, state_c = LSTM(64, return_sequences=True, return_state
      =True)(inputs)
           attention = Dot(axes=[2, 2])([lstm_out, lstm_out])
           attention = Activation('softmax')(attention)
           context = Dot(axes=[2, 1])([attention, lstm_out])
693
           combined = Concatenate()([context, lstm_out])
           outputs = Dense(1, activation='linear')(combined)
695
696
           optimizer = Adam(learning_rate=self.learning_rate)
697
```

```
model = Model(inputs, outputs)
           model.compile(optimizer=optimizer, loss='mean_squared_error')
699
           return model
701
702
   # version 3.0
703
  import numpy as np
704
  import pandas as pd
705
  from sklearn.ensemble import RandomForestClassifier, RandomForestRegressor
  from sklearn.preprocessing import StandardScaler
  from keras.models import Model
  from keras.layers import Input, LSTM, Dense, Dot, Activation, Concatenate
  from keras.optimizers import Adam
710
   from keras.callbacks import ReduceLROnPlateau
   class OlympicPredictionModel:
       from sklearn.neural_network import MLPRegressor
       def __init__(self, lambda_weight=0.3, mu_weight=0.85, learning_rate=0.001):
716
           self.lambda_weight = lambda_weight
           self.mu_weight = mu_weight
718
           self.learning_rate = learning_rate # Added for Adam optimizer tuning
719
           self.classifier = RandomForestClassifier(n_estimators=200)
           # Change RandomForestRegressor to MLPRegressor
721
           self.regressor1 = self.MLPRegressor(hidden_layer_sizes=(64, 32), max_iter
      =500, random_state=42)
           self.regressor2 = self.MLPRegressor(hidden_layer_sizes=(64, 32), max_iter
      =500, random_state=42)
           self.lstm_model = None
724
       @staticmethod
726
       def Country_classification(year, Noc_x, data):
           historical_data = data[data['Year'] <= year]
728
           country_total = historical_data[historical_data['NOC_x'] == Noc_x]['
      Name_Count'].sum()
           all_countries = historical_data.groupby('NOC_x')['Name_Count'].sum()
730
           threshold = all_countries.quantile(0.2)
           return country_total <= threshold</pre>
       def calculate_w4_vector(self, country_change, athlete_change, event_changes):
           w1 = np.sum(country_change, axis=1).astype(np.float64)
           w2 = np.sum(athlete_change, axis=1).astype(np.float64)
           w3 = np.sum(event_changes, axis=1).astype(np.float64)
           w4 = np.divide(0.2 * w1 + 0.8 * w2, w3, out=np.zeros_like(w3, dtype=np.
738
      float64), where=w3 != 0)
```

```
return w4
740
       def preprocess_data(self, data):
741
           year_mapping = pd.read_csv("year_transmition_reference.csv")
742
           year_dict = dict(zip(year_mapping['evaluating_year'], year_mapping['
743
      use_data_from']))
           features_list = []
745
           for idx, row in data.iterrows():
746
               current_year = row['Year']
               reference_year = year_dict.get(current_year, current_year)
748
               reference_data = data[data['Year'] == reference_year]
750
               if len(reference_data) > 0:
                   ref_row = reference_data[reference_data['NOC_x'] == row['NOC_x']]
                   ref_row = ref_row.iloc[0] if len(ref_row) > 0 else row
               else:
                   ref_row = row
756
               score_rate_list = np.array(eval(ref_row['Score_Rate_List']))
757
               score_list = np.array(eval(ref_row['Score_List']), dtype=np.float64)
758
               participants_list = np.array(eval(ref_row['Participants_List']),
759
      dtype=np.float64)
760
               v4_ = np.sum(score_rate_list)
761
               v5_ = np.sum(participants_list)
762
               v8_ = np.sum(np.divide(score_list, participants_list, out=np.
763
      zeros_like(score_list, dtype=np.float64), where=participants_list > 0))
764
               country_change = np.array(eval(ref_row['CountryChange']))
765
               athlete_change = np.array(eval(ref_row['AthleteChange']))
766
               event_changes = np.array(eval(ref_row['Event_Changes']))
767
               w4_ = self.calculate_w4_vector(country_change.reshape(1, -1),
      athlete_change.reshape(1, -1), event_changes.reshape(1, -1))[0]
               v8_w4 = np.sum(np.multiply(np.divide(score_list, participants_list,
770
      out=np.zeros_like(score_list, dtype=np.float64), where=participants_list > 0)
      , w4_{-}))
               v1 = ref_row['if_host']
772
               v6 = ref_row['Gold_prev'] if pd.notna(ref_row['Gold_prev']) else 0
               v7 = ref_row['distance']
               v3_ = ref_row['Score']
               v3_w4 = np.sum(np.multiply(score_list, w4_))
776
```

```
w3_ = np.sum(event_changes)
779
               features = {
                    'features_a': [v5_, v8_, v8_w4],
781
                    'features_b': [v1, v5_, v6, v7, v3_, v3_w4, v8_],
782
                    'features_c': [v1, v5_, v6, v7, v3_, v3_w4, v8_],
                    'features_all': [v1, v3_, v4_, v5_, v6, v7, v8_, w3_, w4_]
               }
785
               features_list.append(features)
786
           features_a = np.array([f['features_a'] for f in features_list])
788
           features_b = np.array([f['features_b'] for f in features_list])
           features_c = np.array([f['features_c'] for f in features_list])
790
           features_all = np.array([f['features_all'] for f in features_list])
791
792
           labels = (data['Total_Medals'] > 0).astype(int).values
793
           medal_expectation = data['Total_Medals'].values
           gold_expectation = data['Gold'].values
796
           scaler = StandardScaler()
797
           features_a_scaled = scaler.fit_transform(features_a)
           features_b_scaled = scaler.fit_transform(features_b)
799
           features_c_scaled = scaler.fit_transform(features_c)
800
           features_all_scaled = scaler.fit_transform(features_all)
801
802
           return features_a_scaled, features_b_scaled, features_c_scaled,
803
      features_all_scaled, labels, medal_expectation, gold_expectation
       def train_classifier(self, features_a, features_all, labels, data):
805
           years = data['Year'].values
806
           nocs = data['NOC_x'].values
807
808
           is_small_countries = np.array([self.Country_classification(year, noc,
      data)
                                          for year, noc in zip(years, nocs)])
811
           final_features = np.zeros((len(labels), features_all.shape[1]))
812
           small_countries_mask = is_small_countries
813
814
           final_features[small_countries_mask] = (1 - self.lambda_weight) *
      features_all[small_countries_mask]
           final_features[small_countries_mask, :features_a.shape[1]] += self.
      lambda_weight * features_a[small_countries_mask]
817
           final_features[~small_countries_mask] = features_all[~
818
```

```
small_countries_mask]
819
           self.classifier.fit(final_features, labels)
           self.classifier_output = self.classifier.predict_proba(final_features)
821
822
       def train_regressor1(self, features_b, medal_expectation):
823
           classifier_probabilities = self.classifier_output[:, 1]
824
           input_features = np.hstack([classifier_probabilities.reshape(-1, 1),
825
      features_b])
           self.regressor1.fit(input_features, medal_expectation)
827
       def train_regressor2(self, features_c, gold_expectation):
828
           classifier_probabilities = self.classifier_output[:, 1]
           input_features_reg1 = np.hstack([classifier_probabilities.reshape(-1, 1),
830
       features_c])
           medal_expectation = self.regressor1.predict(input_features_reg1)
831
           input_features = np.hstack([
               (1 - self.mu_weight) * medal_expectation.reshape(-1, 1),
833
               self.mu_weight * features_c
834
835
           self.regressor2.fit(input_features, gold_expectation)
837
       def create_lstm_attention_model(self, input_shape):
838
           inputs = Input(shape=(input_shape[1], input_shape[2]))
           lstm_out, state_h, state_c = LSTM(64, return_sequences=True, return_state
840
      =True)(inputs)
           attention = Dot(axes=[2, 2])([lstm_out, lstm_out])
841
           attention = Activation('softmax')(attention)
           context = Dot(axes=[2, 1])([attention, lstm_out])
843
           combined = Concatenate()([context, lstm_out])
844
           outputs = Dense(1, activation='linear')(combined)
           optimizer = Adam(learning_rate=self.learning_rate)
846
           model = Model(inputs, outputs)
           model.compile(optimizer=optimizer, loss='mean_squared_error')
848
           return model
850
       def evaluate_model(self, features_a, features_b, features_c, features_all,
851
      labels, medal_expectation, gold_expectation, data, cv=5):
           from sklearn.model_selection import KFold
852
           from sklearn.metrics import accuracy_score, roc_auc_score, r2_score,
853
      mean_squared_error
           kf = KFold(n_splits=cv, shuffle=True, random_state=42)
855
856
           classifier_scores = {'train_acc': [], 'test_acc': [], 'train_auc': [], '
857
```

```
test_auc': []}
           regressor1_scores = {'train_r2': [], 'test_r2': [], 'train_mse': [], '
858
      test_mse': []}
           regressor2_scores = {'train_r2': [], 'test_r2': [], 'train_mse': [], '
859
      test_mse': []}
860
           for train_idx, test_idx in kf.split(features_all):
861
               X_train_a = features_a[train_idx]
862
               X_test_a = features_a[test_idx]
863
               X_train_b = features_b[train_idx]
               X_test_b = features_b[test_idx]
865
               X_train_c = features_c[train_idx]
               X_test_c = features_c[test_idx]
867
               X_train_all = features_all[train_idx]
868
               X_test_all = features_all[test_idx]
               y_train = labels[train_idx]
870
               y_test = labels[test_idx]
               medal_train = medal_expectation[train_idx]
872
               medal_test = medal_expectation[test_idx]
873
               gold_train = gold_expectation[train_idx]
874
               gold_test = gold_expectation[test_idx]
876
               train_data = data.iloc[train_idx].reset_index(drop=True)
877
               self.train_classifier(X_train_a, X_train_all, y_train, train_data)
               train_prob = self.classifier.predict_proba(X_train_all)[:, 1]
879
               test_prob = self.classifier.predict_proba(X_test_all)[:, 1]
881
               classifier_scores['train_acc'].append(accuracy_score(y_train,
      train_prob > 0.5))
               classifier_scores['test_acc'].append(accuracy_score(y_test, test_prob
883
       > 0.5)
               classifier_scores['train_auc'].append(roc_auc_score(y_train,
884
      train_prob))
               classifier_scores['test_auc'].append(roc_auc_score(y_test, test_prob)
885
      )
               self.train_regressor1(X_train_b, medal_train)
887
               train_medal_pred = self.regressor1.predict(np.hstack([train_prob.
      reshape(-1, 1), X_train_b]))
               test_medal_pred = self.regressor1.predict(np.hstack([test_prob.
      reshape(-1, 1), X_test_b]))
               regressor1_scores['train_r2'].append(r2_score(medal_train,
      train_medal_pred))
               regressor1_scores['test_r2'].append(r2_score(medal_test,
891
      test_medal_pred))
```

```
regressor1_scores['train_mse'].append(mean_squared_error(medal_train,
       train_medal_pred))
               regressor1_scores['test_mse'].append(mean_squared_error(medal_test,
893
      test_medal_pred))
894
               self.train_regressor2(X_train_c, gold_train)
895
               train_gold_pred = self.regressor2.predict(np.hstack([
896
                    (1 - self.mu_weight) * train_medal_pred.reshape(-1, 1),
897
                    self.mu_weight * X_train_c
898
               ]))
               test_gold_pred = self.regressor2.predict(np.hstack([
900
                    (1 - self.mu_weight) * test_medal_pred.reshape(-1, 1),
                    self.mu_weight * X_test_c
902
               ]))
903
904
               regressor2_scores['train_r2'].append(r2_score(gold_train,
905
      train_gold_pred))
               regressor2_scores['test_r2'].append(r2_score(gold_test,
906
      test_gold_pred))
               regressor2_scores['train_mse'].append(mean_squared_error(gold_train,
907
      train_gold_pred))
               regressor2_scores['test_mse'].append(mean_squared_error(gold_test,
908
      test_gold_pred))
909
910
911
       def train_and_predict_period(self, data, start_year, end_year):
912
           olympic_years = [1896, 1900, 1904, 1908, 1912, 1920, 1924, 1928, 1932,
913
      1936, 1948, 1952, 1956, 1960, 1964, 1968, 1972, 1976, 1980, 1984, 1988, 1992,
       1996, 2000, 2004, 2008, 2012, 2016, 2020]
           period_data = data[(data['Year'] >= start_year) & (data['Year'] <=</pre>
914
      end_year)].reset_index(drop=True)
915
           features_a, features_b, features_c, features_all, labels,
916
      medal_expectation, gold_expectation = self.preprocess_data(period_data)
917
           self.train_classifier(features_a, features_all, labels, period_data)
918
           self.train_regressor1(features_b, medal_expectation)
919
           self.train_regressor2(features_c, gold_expectation)
920
921
           olympic_mask = period_data['Year'].isin(olympic_years)
922
           olympic_data = period_data[olympic_mask].reset_index(drop=True)
923
           olympic_features_all = features_all[olympic_mask]
924
           time_series_data = olympic_features_all.reshape((olympic_features_all.
925
      shape[0], 1, olympic_features_all.shape[1]))
```

```
if self.lstm_model is None:
927
               self.lstm_model = self.create_lstm_attention_model(time_series_data.
      shape)
929
           lr_scheduler = ReduceLROnPlateau(monitor='loss', factor=0.5, patience=3,
      min_lr=1e-6, verbose=1)
           self.lstm_model.fit(time_series_data, gold_expectation[olympic_mask],
931
      epochs=10, batch_size=32, verbose=1, callbacks=[lr_scheduler])
           last_year_data = period_data[period_data['Year'] == end_year].reset_index
933
      (drop=True)
           end_year_olympic_mask = olympic_data['Year'] == end_year
934
           time_series_last_year = time_series_data[end_year_olympic_mask]
935
936
           if len(time_series_last_year) == 0:
937
               most_recent_year = olympic_data['Year'].max()
               time_series_last_year = time_series_data[olympic_data['Year'] ==
      most_recent_year]
940
           if len(time_series_last_year.shape) == 2:
               time_series_last_year = np.expand_dims(time_series_last_year, axis=0)
942
943
           lstm_gold_prediction = self.lstm_model.predict(time_series_last_year,
      verbose=0)
           available_years = period_data['Year'].unique()
945
           prediction_year = end_year if end_year in available_years else
946
      available_years.max()
947
           classifier_probabilities = self.classifier_output[:, 1][period_data['Year
948
       '] == prediction_year]
           medal_prediction = self.regressor1.predict(np.hstack([
949
               classifier_probabilities.reshape(-1, 1),
               features_b[period_data['Year'] == prediction_year]
951
           ]))
953
           gold_prediction_rf = self.regressor2.predict(np.hstack([
954
               (1 - self.mu_weight) * medal_prediction.reshape(-1, 1),
955
               self.mu_weight * features_c[period_data['Year'] == prediction_year]
956
           ]))
           prediction_data = period_data[period_data['Year'] == prediction_year].
050
      reset_index(drop=True)
           results = pd.DataFrame({
960
                'NOC': prediction_data['NOC_x'],
961
```

```
'Year': prediction_year,
                'Will_Win_Medal': classifier_probabilities > 0.5,
963
                'Medal_Prediction': medal_prediction,
964
                'Gold_Prediction': gold_prediction_rf
965
            })
966
            self.evaluate_model(features_a, features_b, features_c, features_all,
967
                                 labels, medal_expectation, gold_expectation,
968
       period_data)
            return results
969
   # Example usage
971
   data = pd.read_csv("feature_Noc.csv") # Replace with your actual dataset
   model = OlympicPredictionModel()
973
   start_year = 1964
   end_year = 2028
   results = model.train_and_predict_period(data, start_year, end_year)
   print(results)
   # Save the results to a CSV file
978
   results.to_csv("results.csv", index=False) # Replace with your desired file path
980
981
   import pandas as pd
982
   import numpy as np
983
   import matplotlib.pyplot as plt
   from sklearn.metrics import mean_absolute_error
985
   # Load noisy data
987
   noisy_data_path = 'noisy_df_0.05.csv'
   noisy_data = pd.read_csv(noisy_data_path)
989
990
   # Load the true (noise-free) data (ensure the correct file path is provided)
991
   true_data_path = 'feature_Noc.csv' # Replace with your actual true data path
   true_data = pd.read_csv(true_data_path)
994
   # Initialize the model
   model = OlympicPredictionModel()
996
997
   # Set the testing time range
   start_year = 1964
999
   end_year = 2028
1001
   # Train and predict on the true data
1002
   results_true = model.train_and_predict_period(true_data, start_year, end_year)
1003
1004
   # Train and predict on the noisy data
```

```
results_noisy = model.train_and_predict_period(noisy_data, start_year, end_year)
1007
   # Extract gold medal prediction results
1008
   true_gold_predictions = results_true["Gold_Prediction"].values
1009
   noisy_gold_predictions = results_noisy["Gold_Prediction"].values
1011
   # Calculate robustness metrics (e.g., Mean Absolute Error)
1012
   mae_gold = mean_absolute_error(true_gold_predictions, noisy_gold_predictions)
1014
   # Plot the prediction results comparison
plt.figure(figsize=(12, 6))
   plt.plot(true_gold_predictions, label="True Gold Predictions", marker="o")
   plt.plot(noisy_gold_predictions, label="Noisy Gold Predictions", marker="x",
       linestyle="--")
plt.title(f"Robustness Analysis: Gold Medal Predictions (noise:0.05 MAE: {
       mae_gold:.2f})")
   plt.xlabel("Index")
   plt.ylabel("Gold Predictions")
   plt.legend()
   plt.grid(True)
1023
1024
   # Save the plot
1025
   output_image_path = "robustness_analysis_0.05.png"
1026
   plt.savefig(output_image_path)
   plt.show()
1028
1029
   # Print the output file path
1030
   print(f"Robustness analysis image saved at: {output_image_path}")
1031
1032
   import pandas as pd
1033
   import numpy as np
1034
   import matplotlib.pyplot as plt
1035
   from sklearn.metrics import mean_absolute_error
1037
   # Load noisy data
1038
   noisy_data_path = 'noisy_df_0.1.csv'
1039
   noisy_data = pd.read_csv(noisy_data_path)
1040
1041
   # Load the true (noise-free) data (ensure the correct file path is provided)
1042
   true_data_path = 'feature_Noc.csv' # Replace with your actual true data path
   true_data = pd.read_csv(true_data_path)
1044
1045
   # Initialize the model
1046
   model = OlympicPredictionModel()
1048
```

```
# Set the testing time range
   start_year = 1964
1050
   end_year = 2028
1051
1052
   # Train and predict on the true data
1053
   results_true = model.train_and_predict_period(true_data, start_year, end_year)
1054
1055
   # Train and predict on the noisy data
1056
   results_noisy = model.train_and_predict_period(noisy_data, start_year, end_year)
1057
   # Extract gold medal prediction results
1059
   true_gold_predictions = results_true["Gold_Prediction"].values
   noisy_gold_predictions = results_noisy["Gold_Prediction"].values
1061
1062
   # Calculate robustness metrics (e.g., Mean Absolute Error)
1063
   mae_gold = mean_absolute_error(true_gold_predictions, noisy_gold_predictions)
1064
   # Plot the prediction results comparison
1066
   plt.figure(figsize=(12, 6))
   plt.plot(true_gold_predictions, label="True Gold Predictions", marker="o")
   plt.plot(noisy_gold_predictions, label="Noisy Gold Predictions", marker="x",
       linestyle="--")
1070 plt.title(f"Robustness Analysis: Gold Medal Predictions (noise:0.1 MAE: {mae_gold
       :.2f})")
plt.xlabel("Index")
plt.ylabel("Gold Predictions")
   plt.legend()
1073
   plt.grid(True)
1074
1075
   # Save the plot
1076
   output_image_path = "robustness_analysis_0.1.png"
   plt.savefig(output_image_path)
   plt.show()
1080
   # Print the output file path
   print(f"Robustness analysis image saved at: {output_image_path}")
1082
1083
   import pandas as pd
1084
   import numpy as np
1085
   import matplotlib.pyplot as plt
   from sklearn.metrics import mean_absolute_error
1087
1088
   # Load noisy data
1089
oisy_data_path = 'noisy_df_0.2.csv'
   noisy_data = pd.read_csv(noisy_data_path)
```

```
# Load the true (noise-free) data (ensure the correct file path is provided)
1093
   true_data_path = 'feature_Noc.csv' # Replace with your actual true data path
   true_data = pd.read_csv(true_data_path)
1095
1096
   # Initialize the model
1097
   model = OlympicPredictionModel()
1098
1099
   # Set the testing time range
1100
   start_year = 1964
   end_year = 2028
1102
1103
   # Train and predict on the true data
1104
   results_true = model.train_and_predict_period(true_data, start_year, end_year)
1105
1106
   # Train and predict on the noisy data
1107
   results_noisy = model.train_and_predict_period(noisy_data, start_year, end_year)
1109
   # Extract gold medal prediction results
1110
   true_gold_predictions = results_true["Gold_Prediction"].values
   noisy_gold_predictions = results_noisy["Gold_Prediction"].values
   # Calculate robustness metrics (e.g., Mean Absolute Error)
   mae_gold = mean_absolute_error(true_gold_predictions, noisy_gold_predictions)
1116
# Plot the prediction results comparison
plt.figure(figsize=(12, 6))
plt.plot(true_gold_predictions, label="True Gold Predictions", marker="o")
plt.plot(noisy_gold_predictions, label="Noisy Gold Predictions", marker="x",
      linestyle="--")
   plt.title(f"Robustness Analysis: Gold Medal Predictions (noise:0.2 MAE: {mae_gold
      :.2f)")
plt.xlabel("Index")
plt.ylabel("Gold Predictions")
plt.legend()
   plt.grid(True)
1125
1126
# Save the plot
output_image_path = "robustness_analysis_0.2.png"
   plt.savefig(output_image_path)
   plt.show()
1130
1131
# Print the output file path
   print(f"Robustness analysis image saved at: {output_image_path}")
1134
```

```
import pandas as pd
   import numpy as np
   import matplotlib.pyplot as plt
   from sklearn.metrics import mean_absolute_error
1138
1139
1140
   # Load noisy data
   oisy_data_path = 'noisy_df_0.3.csv'
1141
   noisy_data = pd.read_csv(noisy_data_path)
1143
   # Load the true (noise-free) data (ensure the correct file path is provided)
   true_data_path = 'feature_Noc.csv' # Replace with your actual true data path
1145
   true_data = pd.read_csv(true_data_path)
1147
   # Initialize the model
1148
   model = OlympicPredictionModel()
1150
   # Set the testing time range
1151
   start_year = 1964
1152
   end_year = 2028
1153
1154
   # Train and predict on the true data
1155
   results_true = model.train_and_predict_period(true_data, start_year, end_year)
1156
1157
   # Train and predict on the noisy data
   results_noisy = model.train_and_predict_period(noisy_data, start_year, end_year)
1159
1160
   # Extract gold medal prediction results
1161
   true_gold_predictions = results_true["Gold_Prediction"].values
   noisy_gold_predictions = results_noisy["Gold_Prediction"].values
1163
1164
   # Calculate robustness metrics (e.g., Mean Absolute Error)
1165
   mae_gold = mean_absolute_error(true_gold_predictions, noisy_gold_predictions)
1166
1168
   # Plot the prediction results comparison
plt.figure(figsize=(12, 6))
plt.plot(true_gold_predictions, label="True Gold Predictions", marker="o")
plt.plot(noisy_gold_predictions, label="Noisy Gold Predictions", marker="x",
       linestyle="--")
plt.title(f"Robustness Analysis: Gold Medal Predictions (noise:0.3 MAE: {mae_gold
       :.2f})")
plt.xlabel("Index")
plt.ylabel("Gold Predictions")
plt.legend()
plt.grid(True)
```

```
# Save the plot
   output_image_path = "robustness_analysis_0.3.png"
   plt.savefig(output_image_path)
   plt.show()
1181
1182
   # Print the output file path
1183
   print(f"Robustness analysis image saved at: {output_image_path}")
1184
1185
   class OlympicPredictionModel:
1186
        from sklearn.neural_network import MLPRegressor
1187
1188
        def __init__(self, lambda_weight=0.3, mu_weight=0.85, learning_rate=0.001):
1189
            self.lambda_weight = lambda_weight
1190
            self.mu_weight = mu_weight
1191
            self.learning_rate = learning_rate
1192
            self.classifier = RandomForestClassifier(n_estimators=200)
1193
            self.regressor1 = self.MLPRegressor(hidden_layer_sizes=(64, 32), max_iter
       =500, random_state=42)
            self.regressor2 = self.MLPRegressor(hidden_layer_sizes=(64, 32), max_iter
1195
       =500, random_state=42)
            self.lstm_model = None
1196
1197
        @staticmethod
1198
        def Country_classification(year, Noc_x, data):
            historical_data = data[data['Year'] <= year]</pre>
1200
            country_total = historical_data[historical_data['NOC_x'] == Noc_x]['
1201
       Name_Count'].sum()
            all_countries = historical_data.groupby('NOC_x')['Name_Count'].sum()
1202
            threshold = all_countries.quantile(0.2)
1203
            return country_total <= threshold
1204
1205
        def calculate_w4_vector(self, country_change, athlete_change, event_changes):
1206
            w1 = np.sum(country_change, axis=1).astype(np.float64)
1207
            w2 = np.sum(athlete_change, axis=1).astype(np.float64)
1208
            w3 = np.sum(event_changes, axis=1).astype(np.float64)
1209
            w4 = np.divide(0.2 * w1 + 0.8 * w2, w3, out=np.zeros_like(w3, dtype=np.
1210
       float64), where=w3 != 0)
            return w4
        def preprocess_data(self, data):
            year_mapping = pd.read_csv("year_transmition_reference.csv")
1214
            year_dict = dict(zip(year_mapping['evaluating_year'], year_mapping['
       use_data_from']))
1216
            features_list = []
```

```
for idx, row in data.iterrows():
                current_year = row['Year']
1219
                reference_year = year_dict.get(current_year, current_year)
1220
                reference_data = data[data['Year'] == reference_year]
                if len(reference_data) > 0:
                    ref_row = reference_data[reference_data['NOC_x'] == row['NOC_x']]
1224
                    ref_row = ref_row.iloc[0] if len(ref_row) > 0 else row
1225
                else:
1226
                    ref_row = row
1228
                score_rate_list = np.array(eval(ref_row['Score_Rate_List']))
1229
                score_list = np.array(eval(ref_row['Score_List']), dtype=np.float64)
1230
                participants_list = np.array(eval(ref_row['Participants_List']),
       dtype=np.float64)
                v4_ = np.sum(score_rate_list)
                v5_ = np.sum(participants_list)
1234
                v8_ = np.sum(np.divide(score_list, participants_list, out=np.
       zeros_like(score_list, dtype=np.float64), where=participants_list > 0))
1236
                country_change = np.array(eval(ref_row['CountryChange']))
                athlete_change = np.array(eval(ref_row['AthleteChange']))
1238
                event_changes = np.array(eval(ref_row['Event_Changes']))
1239
                w4_ = self.calculate_w4_vector(country_change.reshape(1, -1),
1240
       athlete_change.reshape(1, -1), event_changes.reshape(1, -1))[0]
1241
                v8_w4 = np.sum(np.multiply(np.divide(score_list, participants_list,
1242
       out=np.zeros_like(score_list, dtype=np.float64), where=participants_list > 0)
       , w4_{-}))
                v1 = ref_row['if_host']
1244
                v6 = ref_row['Gold_prev'] if pd.notna(ref_row['Gold_prev']) else 0
1245
                v7 = ref_row['distance']
1246
                v3_ = ref_row['Score']
1247
                v3_w4 = np.sum(np.multiply(score_list, w4_))
1248
1249
                w3_ = np.sum(event_changes)
1250
1251
                features = {
1252
                     'features_a': [v5_, v8_, v8_w4],
1253
                     'features_b': [v1, v5_, v6, v7, v3_, v3_w4, v8_],
1254
                     'features_c': [v1, v5_, v6, v7, v3_, v3_w4, v8_],
                    'features_all': [v1, v3_, v4_, v5_, v6, v7, v8_, w3_, w4_]
1256
1257
```

```
features_list.append(features)
1258
1259
            features_a = np.array([f['features_a'] for f in features_list])
1260
            features_b = np.array([f['features_b'] for f in features_list])
1261
            features_c = np.array([f['features_c'] for f in features_list])
1262
            features_all = np.array([f['features_all'] for f in features_list])
1263
1264
            labels = (data['Total_Medals'] > 0).astype(int).values
1265
            medal_expectation = data['Total_Medals'].values
1266
            gold_expectation = data['Gold'].values
1268
            scaler = StandardScaler()
1269
            features_a_scaled = scaler.fit_transform(features_a)
1270
            features_b_scaled = scaler.fit_transform(features_b)
            features_c_scaled = scaler.fit_transform(features_c)
            features_all_scaled = scaler.fit_transform(features_all)
1274
            return features_a_scaled, features_b_scaled, features_c_scaled,
       features_all_scaled, labels, medal_expectation, gold_expectation
1276
        def train_classifier(self, features_a, features_all, labels, data):
            years = data['Year'].values
1278
            nocs = data['NOC_x'].values
1279
            is_small_countries = np.array([self.Country_classification(year, noc,
1281
       data)
                                           for year, noc in zip(years, nocs)])
1282
1283
            final_features = np.zeros((len(labels), features_all.shape[1]))
1284
            small_countries_mask = is_small_countries
1285
1286
            final_features[small_countries_mask] = (1 - self.lambda_weight) *
1287
       features_all[small_countries_mask]
            final_features[small_countries_mask, :features_a.shape[1]] += self.
1288
       lambda_weight * features_a[small_countries_mask]
1289
            final_features[~small_countries_mask] = features_all[~
1290
       small_countries_mask]
1291
            self.classifier.fit(final_features, labels)
1292
            self.classifier_output = self.classifier.predict_proba(final_features)
1294
        def train_regressor1(self, features_b, medal_expectation):
1295
            classifier_probabilities = self.classifier_output[:, 1]
1296
            input_features = np.hstack([classifier_probabilities.reshape(-1, 1),
1297
```

```
features_b])
            self.regressor1.fit(input_features, medal_expectation)
1298
1299
        def train_regressor2(self, features_c, gold_expectation):
1300
1301
            Train the second regressor (for gold medal predictions) and compute
1302
       training accuracy.
1303
            classifier_probabilities = self.classifier_output[:, 1]
1304
            input_features_reg1 = np.hstack([classifier_probabilities.reshape(-1, 1),
1305
        features_c])
            medal_expectation = self.regressor1.predict(input_features_reg1)
1306
1307
            input_features = np.hstack([
1308
                (1 - self.mu_weight) * medal_expectation.reshape(-1, 1),
1309
                self.mu_weight * features_c
            1)
1311
            self.regressor2.fit(input_features, gold_expectation)
1312
1313
            # Calculate gold prediction accuracy on the training set
1314
            train_gold_pred = self.regressor2.predict(input_features)
            gold_accuracy = np.mean(np.abs(train_gold_pred / 2 - gold_expectation) <</pre>
       2)
            print(f"Training Gold Prediction Accuracy: {gold_accuracy:.2f}")
1318
1319
   # Example usage
1320
   data = pd.read_csv("feature_Noc.csv") # Replace with your dataset
   model = OlympicPredictionModel()
   # Preprocess data
1324
   features_a, features_b, features_c, features_all, labels, medal_expectation,
1325
       gold_expectation = model.preprocess_data(data)
1326
   # Train the classifier
   model.train_classifier(features_a, features_all, labels, data)
1328
1329
   # Train the first regressor
   model.train_regressor1(features_b, medal_expectation)
   # Train the second regressor and output training accuracy
1333
model.train_regressor2(features_c, gold_expectation)
```

Listing 15: model.ipynb

```
import numpy as np
import matplotlib.pyplot as plt
4 from sklearn.metrics import mean_absolute_error
  # Sensitivity Analysis Function
  def sensitivity_analysis(model, data, feature_columns, perturbation_percent):
      Perform sensitivity analysis by perturbing specific feature columns and
11
      - model: OlympicPredictionModel instance.
12
      - data: Original dataset (Pandas DataFrame).
      - feature_columns: List of columns to perturb.
14
      - perturbation_percent: Percentage of perturbation to apply.
15
16
      - sensitivity_results: DataFrame comparing original vs perturbed predictions.
18
      - mae_sensitivity: Mean Absolute Error of predictions due to perturbation.
19
20
      # Deep copy the data to avoid altering the original dataset
      perturbed_data = data.copy()
22
23
      # Apply perturbation to the specified columns
      for col in feature columns:
25
          if col not in perturbed_data.columns:
26
               print(f"Warning: Column '{col}' not found in dataset. Skipping...")
               continue
          perturbation = perturbed_data[col] * (perturbation_percent / 100.0)
          perturbed_data[col] += perturbation
30
31
      # Preprocess original and perturbed data
32
      print("Preprocessing original data...")
33
      features_a, features_b, features_c, features_all, labels, medal_expectation,
      gold_expectation = model.preprocess_data(data)
35
      print("Preprocessing perturbed data...")
36
      features_a_pert, features_b_pert, features_c_pert, features_all_pert, _, _,
       = model.preprocess_data(perturbed_data)
      # Train and predict using original data
39
      print("Training on original data...")
40
      model.train_classifier(features_a, features_all, labels, data)
41
      classifier_probabilities = model.classifier_output[:, 1]
42
      model.train_regressor1(features_b, medal_expectation)
43
```

```
medal_predictions_original = model.regressor1.predict(np.hstack([
      classifier_probabilities.reshape(-1, 1), features_b]))
      model.train_regressor2(features_c, gold_expectation)
      gold_predictions_original = model.regressor2.predict(np.hstack([
46
          (1 - model.mu_weight) * medal_predictions_original.reshape(-1, 1),
47
          model.mu_weight * features_c
      1))
50
      # Train and predict using perturbed data
51
      print("Training on perturbed data...")
      model.train_classifier(features_a_pert, features_all_pert, labels,
53
      perturbed_data)
      classifier_probabilities_pert = model.classifier_output[:, 1]
54
      model.train_regressor1(features_b_pert, medal_expectation)
55
      medal_predictions_perturbed = model.regressor1.predict(np.hstack([
56
      classifier_probabilities_pert.reshape(-1, 1), features_b_pert]))
      model.train_regressor2(features_c_pert, gold_expectation)
      gold_predictions_perturbed = model.regressor2.predict(np.hstack([
58
          (1 - model.mu_weight) * medal_predictions_perturbed.reshape(-1, 1),
59
          model.mu_weight * features_c_pert
60
      ]))
62
      # Compare predictions
63
      mae_sensitivity = mean_absolute_error(gold_predictions_original,
      gold_predictions_perturbed)
65
      # Create results DataFrame for comparison
66
      sensitivity_results = pd.DataFrame({
          "Original_Gold_Predictions": gold_predictions_original,
68
          "Perturbed_Gold_Predictions": gold_predictions_perturbed
69
      })
70
      return sensitivity_results, mae_sensitivity
  # Load true (clean) data
  true_data_path = "feature_Noc.csv" # Replace with your actual true data path
  true_data = pd.read_csv(true_data_path)
  # Initialize the model
  model = OlympicPredictionModel()
80
  # Define sensitivity test parameters
  sensitivity_features = ["Score", "Total_Medals", "Gold_prev"] # Adjust based on
perturbation_percent = 10 # 10% perturbation
```

```
# Perform sensitivity analysis
  sensitivity_results, mae_sensitivity = sensitivity_analysis(
       model, true_data, sensitivity_features, perturbation_percent
  )
88
  # Plot sensitivity analysis results
plt.figure(figsize=(12, 6))
92 plt.plot(sensitivity_results["Original_Gold_Predictions"], label="Original
      Predictions", marker="o")
93 plt.plot(sensitivity_results["Perturbed_Gold_Predictions"], label=f"Perturbed
      Predictions (+{perturbation_percent}%)", marker="x", linestyle="--")
  plt.title(f"Sensitivity Analysis: Gold Medal Predictions (MAE: {mae_sensitivity
      :.2f})")
95 plt.xlabel("Index")
96 plt.ylabel("Gold Predictions")
97 plt.legend()
  plt.grid(True)
99
  # Save the plot
100
  sensitivity_plot_path = "sensitivity_analysis.png"
  plt.savefig(sensitivity_plot_path)
  plt.show()
103
  # Print the results and save path
105
  print(f"Sensitivity analysis image saved at: {sensitivity_plot_path}")
  print(f"Mean Absolute Error due to perturbation: {mae_sensitivity:.2f}")
107
  ###########################
  import pandas as pd
109
  import numpy as np
110
  import matplotlib.pyplot as plt
  from sklearn.metrics import mean_absolute_error
  # List of noise levels
114
  noise\_levels = [0.01, 0.05, 0.1, 0.2, 0.3]
116
  # Load the true (noise-free) data
117
  true_data_path = 'feature_Noc.csv' # Replace with your actual true data path
  true_data = pd.read_csv(true_data_path)
119
  # Initialize the model
  model = OlympicPredictionModel()
# Set the testing time range
start_year = 1964
```

```
end_year = 2028
  # Train and predict on the true data
128
  results_true = model.train_and_predict_period(true_data, start_year, end_year)
   true_gold_predictions = results_true["Gold_Prediction"].values
   # Initialize a plot
  plt.figure(figsize=(12, 6))
133
134
   # Loop through noise levels and plot each one
   for noise_level in noise_levels:
136
       # Load noisy data for the current noise level
       noisy_data_path = f'noisy_df_{noise_level}.csv'
138
       noisy_data = pd.read_csv(noisy_data_path)
130
140
       # Train and predict on the noisy data
141
       results_noisy = model.train_and_predict_period(noisy_data, start_year,
      end_year)
       noisy_gold_predictions = results_noisy["Gold_Prediction"].values
143
144
       # Calculate robustness metrics (e.g., Mean Absolute Error)
145
       mae_gold = mean_absolute_error(true_gold_predictions, noisy_gold_predictions)
146
147
       # Plot the noisy data predictions
       plt.plot(noisy_gold_predictions, label=f"Noise {noise_level} (MAE: {mae_gold
149
      :.2f})", linestyle="--", marker="x")
150
  # Plot the true gold predictions
  plt.plot(true_gold_predictions, label="True Gold Predictions", marker="o",
152
      linewidth=2)
  # Add title, labels, and legend
plt.title("Robustness Analysis: Gold Medal Predictions")
plt.xlabel("Index")
plt.ylabel("Gold Predictions")
plt.legend()
  plt.grid(True)
159
160
  # Save the plot
161
  output_image_path = "robustness_analysis_all_noise.png"
  plt.savefig(output_image_path)
  plt.show()
165
  # Print the output file path
```

```
print(f"Robustness analysis image saved at: {output_image_path}")
```

Listing 16: robust\_sensitivity.ipynb

## C Report on Use of AI

1. **Open AI** *ChatGPT* (Nov 5, 2024 version, ChatGPT-4)

**Quary:** Modify the color options of the listing module in the TeX file to make it more harmonious and aesthetically pleasing.

**Output:** Sets the background color of the code area to a light shade of gray, with 10% gray intensity. Configures the style of comments within the code to be a medium green color, with 60% green intensity. Specifies that keywords in the code should be displayed in blue. Defines the style for line numbers to be tiny and gray, making them less prominent. Assigns a purple color to string literals in the code.

2. Gravity Slingshot Technology Co., Ltd. Marscode (Mar 26, 2024 version, Doubao)

**Quary:** Generate some suitable comments for code.

**Output:** Comments generated for some code files.

3. **Open AI** *ChatGPT* (Nov 5, 2024 version, ChatGPT-4)

Quary: Finding typical great coach.

**Output:** Some coach's names that meet the question's need.

4. **Open AI** *ChatGPT* (Nov 5, 2024 version, ChatGPT-4)

**Quary:** Provide the csv file for Prediction medal table for 2028 Los Angeles, USA summer Olympics. Translate into a latex longtable form.

## **Output:**

```
begin{longtable}{|c|c|c|c|}

hline

textbf{Rank} & \textbf{Nation} & \textbf{Will Win Medal} & \textbf{Gold} &
  \textbf{Total} \\

hline

endfirsthead

hline

textbf{Rank} & \textbf{Nation} & \textbf{Will Win Medal} & \textbf{Gold} &
  \textbf{Rank} \\

hline

hline

endhead

hline

endhead

hline

endfoot
```

```
1 & USA & TRUE & 61.89362846 & 139.8773871 \\
  2 & CHN & TRUE & 36.73785753 & 91.91655353 \\
  3 & GBR & TRUE & 18.88867211 & 82.83034521 \\
   & JPN & TRUE & 16.00417029 & 58.62541877 \\
   & AUS & TRUE & 18.18273715 & 53.84301404 \\
    & FRA & TRUE & 19.56936092 & 53.74770272 \\
  7 & GER & TRUE & 13.20334256 & 47.70665467 \\
   & ITA & TRUE & 12.25179948 & 37.7220809 \\
  9 & BRA & TRUE & 4.909950393 & 36.05183567 \\
  10 & NED & TRUE & 11.32964194 & 35.08134432 \\
  11 & CAN & TRUE & 8.53238935 & 27.97689688 \\
  12 & ESP & TRUE & 7.096889707 & 22.4549891 \\
  13 & KOR & TRUE & 7.020464162 & 22.1177207 \\
  14 & HUN & TRUE & 5.837784707 & 17.46280967 \\
  15 & NZL & TRUE & 5.213962466 & 16.59901162 \\
  16 & POL & TRUE & 4.103828217 & 16.28268645 \\
  17 & UKR & TRUE & 3.681442241 & 13.13062476 \\
  18 & SWE & TRUE & 2.877136935 & 11.11753134 \\
  19 & CUB & TRUE & 2.887936985 & 10.75076093 \\
  20 & DEN & TRUE & 3.695717124 & 10.27081395 \\
  21 & SRB & TRUE & 4.11700087 & 9.995684767 \\
  22 & SUI & TRUE & 3.246965272 & 9.982866384 \\
  23 & CZE & TRUE & 1.68408156 & 9.21439891 \\
  24 & TUR & TRUE & 1.532841449 & 8.944480754 \\
  25 & JAM & TRUE & 2.460369548 & 8.248609111 \\
  26 & KEN & TRUE & 2.500396609 & 8.239645498 \\
  27 & TPE & TRUE & 1.502765201 & 7.892720068 \\
  28 & BEL & TRUE & 2.162127539 & 7.405213267 \\
  29 & CRO & TRUE & 2.499122523 & 7.247100347 \\
  30 & EGY & TRUE & 0.983883881 & 6.982062128 \\
  31 & IRI & TRUE & 1.242496907 & 6.778206524 \\
  32 & ARG & TRUE & 1.763522961 & 6.545787189 \\
  33 & IND & TRUE & 1.056551388 & 6.357541967 \\
  34 & NOR & TRUE & 2.015433856 & 6.282549225 \\
  35 & UZB & TRUE & 1.849029887 & 5.562196507 \\
  36 & ROU & TRUE & 2.006474912 & 5.177925657 \\
  37 & MEX & TRUE & 0.6942054 & 4.704491759 \\
  38 & COL & TRUE & 1.187432662 & 4.564946305 \\
  39 & GEO & TRUE & 1.065348417 & 4.325132407 \\
  40 & IRL & TRUE & 1.154925268 & 4.262881708 \\
  41 & HKG & TRUE & 1.017064066 & 4.18749859 \\
  42 & KAZ & TRUE & 0.832928845 & 4.152492135 \\
  43 & RSA & TRUE & 1.289180741 & 4.094492851 \\
  44 & BUL & TRUE & 0.519369539 & 4.073859257 \\
  45 & AUT & TRUE & 0.766650287 & 4.067462751 \\
```

```
46 & ISR & TRUE & 0.871817818 & 4.049702673 \\
47 & SLO & TRUE & 0.910435659 & 3.921396044 \\
48 & POR & TRUE & 0.999374801 & 3.828379532 \\
49 & GRE & TRUE & 0.946089615 & 3.617184535 \\
50 & TUN & TRUE & 0.242361355 & 3.558668753 \\
51 & ETH & TRUE & 0.782784719 & 3.394682832 \\
52 & UGA & TRUE & 0.764501613 & 3.38297178 \\
53 & AIN & TRUE & 0.530560258 & 3.205393477 \\
54 & DOM & TRUE & 0.479723071 & 2.87826012 \\
55 & SVK & TRUE & 0.652582368 & 2.86538428 \\
56 & AZE & TRUE & 0.658131892 & 2.864971301 \\
57 & ECU & TRUE & 0.65295669 & 2.834019019 \\
58 & PHI & TRUE & 0.503089309 & 2.808015339 \\
59 & INA & TRUE & 0.528760779 & 2.747042122 \\
60 & FIJ & TRUE & -0.003103899 & 2.605802276 \\
61 & MAR & TRUE & 0.536724462 & 2.562540565 \\
62 & NAS & TRUE & 0.467698534 & 2.324974611 \\
63 & PUR & TRUE & -0.046873765 & 2.136679932 \\
64 & JOR & TRUE & 0.19392357 & 2.003962532 \\
65 & MCL & TRUE & 0.455186168 & 1.935160376 \\
66 & MDA & TRUE & 0.356611343 & 1.911806467 \\
67 & KOS & TRUE & 0.304311493 & 1.867596464 \\
68 & KGZ & TRUE & 0.378210031 & 1.841458856 \\
69 & PRK & TRUE & 0.359432562 & 1.839969699 \\
70 & ARM & TRUE & 0.031476902 & 1.799496923 \\
71 & ALC & TRUE & 0.178958857 & 1.658627997 \\
72 & LCA & TRUE & 0.233987355 & 1.620105127 \\
73 & THA & TRUE & 0.336004932 & 1.528310591 \\
74 & QAT & TRUE & 0.293791652 & 1.523262926 \\
75 & CUA & TRUE & 0.237918545 & 1.315100324 \\
76 & CIV & TRUE & 0.275063498 & 1.250511056 \\
77 & EOR & FALSE & 0.017306252 & 1.059041029 \\
78 & DMA & TRUE & 0.541163739 & 0.903726649 \\
79 & BRN & TRUE & 0.15785938 & 0.890418895 \\
80 & LTU & TRUE & 0.014238442 & 0.807797574 \\
81 & CRN & TRUE & 0.030019709 & 0.710567567 \\
82 & PAN & TRUE & 0.446226684 & 0.632673943 \\
83 & TJK & TRUE & 0.141225186 & 0.616260523 \\
84 & ZAM & TRUE & 0.144640175 & 0.548210104 \\
85 & BER & TRUE & 0.038687094 & 0.534395846 \\
86 & NCR & FALSE & -0.118414531 & 0.513838076 \\
87 & GHA & FALSE & -0.011375109 & 0.503209055 \\
88 & BOT & TRUE & 0.084029068 & 0.471503368 \\
89 & GUY & FALSE & 0.041557388 & 0.420078153 \\
90 & OMA & FALSE & 0.061035481 & 0.37812072 \\
```

```
91 & IRQ & FALSE & 0.06706993 & 0.371666848 \\
  92 & CHI & TRUE & -0.024238576 & 0.348309951 \\
93 & LBA & FALSE & -0.045312895 & 0.312450675 \\
  94 & CRC & FALSE & -0.127885095 & 0.203215597 \\
  95 & DJI & FALSE & 0.275807067 & 0.178896068 \\
  96 & ISV & FALSE & 0.009764616 & 0.15845807 \\
  97 & CPV & TRUE & 0.064091496 & 0.146435484 \\
  98 & GAB & FALSE & 0.29400497 & 0.145802258 \\
99 & SEN & FALSE & 0.035936367 & 0.141214057 \\
100 & COM & FALSE & -0.164212537 & 0.064197285 \\
  101 & CAM & FALSE & -0.034432688 & 0.061663558 \\
102 & SCP & TRUE & 0.05958942 & 0.058251254 \\
  103 & ARU & FALSE & -0.178501798 & 0.046999362 \\
104 & UAE & FALSE & -0.023508693 & -0.021384389 \\
105 & MHL & FALSE & 0.01383528 & -0.076188244 \\
117 106 & KIR & FALSE & 0.008776467 & -0.078181121 \\
107 & VAN & FALSE & 0.000968212 & -0.114300931 \\
119 108 & CYP & FALSE & -0.032076009 & -0.116562861 \\
120 109 & PAK & FALSE & 0.033260645 & -0.163091115 \\
  110 & PER & TRUE & -0.058386585 & -0.246575465 \\
  111 & PAR & FALSE & -0.266623889 & -0.349789911 \\
  112 & YEM & FALSE & -0.274518749 & -0.376302868 \\
  \hline
125 \end{longtable}
```