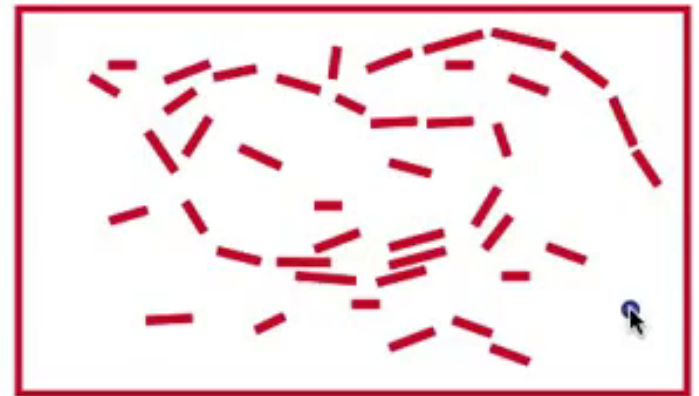


Edge Detection



Edge Detection:

- The process of labeling the locations in the image where the gray level's "rate of change" is high.
 - **OUTPUT:** "edgels" locations, direction, strength



Edge Integration:

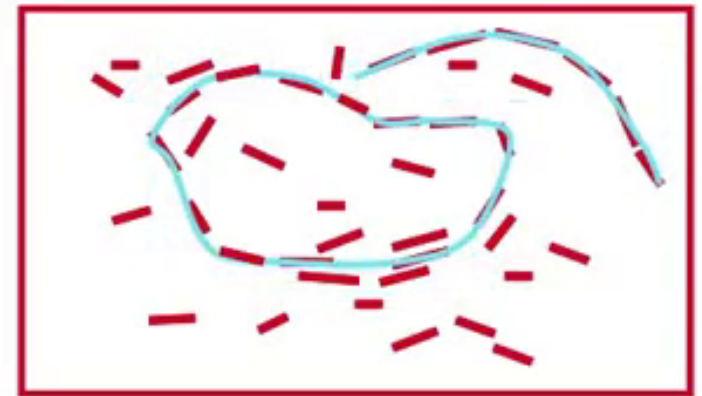
- The process of combining "local" and perhaps sparse and non-contiguous "edgel"-data into meaningful, long edge curves (or closed contours) for segmentation
 - **OUTPUT:** edges/curves consistent with the local data

Edge Detection



Edge Detection:

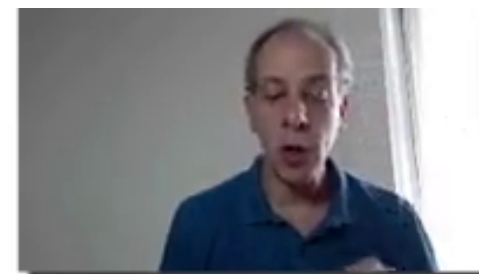
- The process of labeling the locations in the image where the gray level's "rate of change" is high.
 - **OUTPUT:** "edgels" locations, direction, strength



Edge Integration:

- The process of combining "local" and perhaps sparse and non-contiguous "edgel"-data into meaningful, long edge curves (or closed contours) for segmentation
 - **OUTPUT:** edges/curves consistent with the local data

Active Contours



Image



Edge Indicator
Function

$$g(x, y) = \frac{1}{1 + |\nabla(G_\sigma * I)|^2}$$



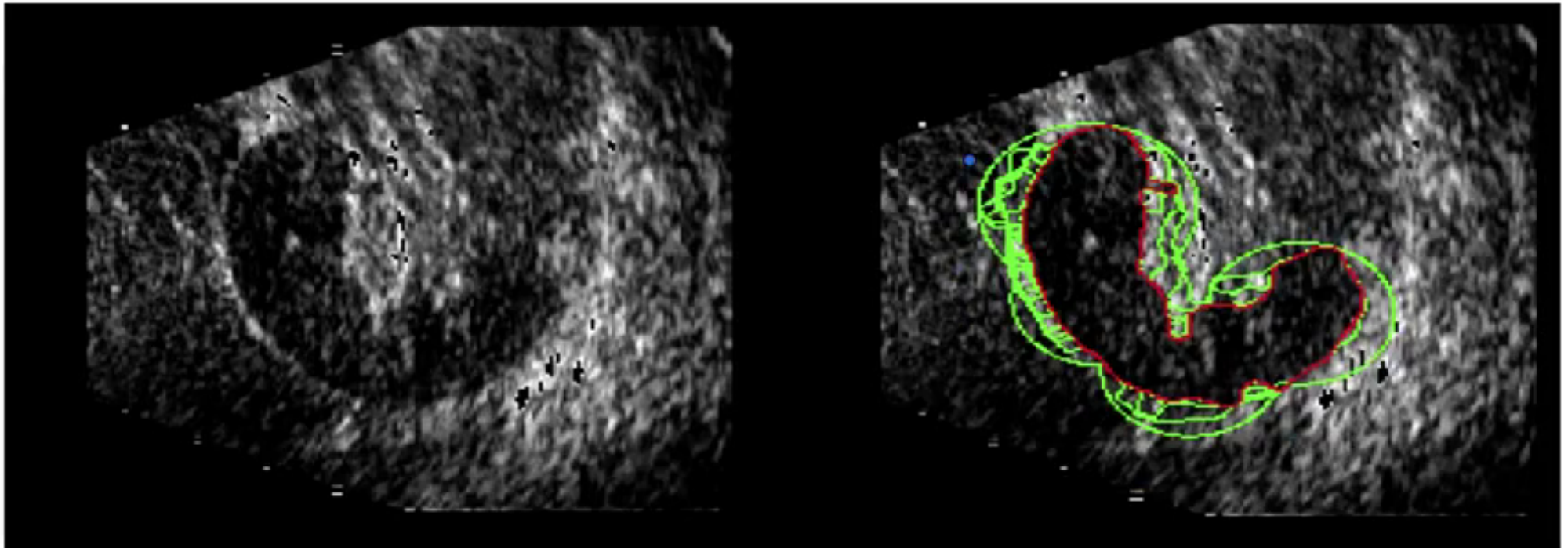
“nice” curves that optimize a functional of $g()$, i.e.

$$\int_{\text{curve}} g() ds$$

nice: “regularized”, smooth,
fit some prior information

Edge Curves

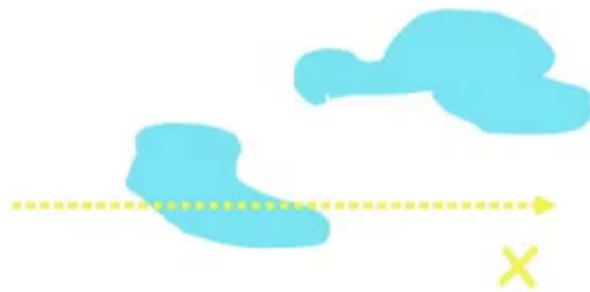
Segmentation



Potential Functions



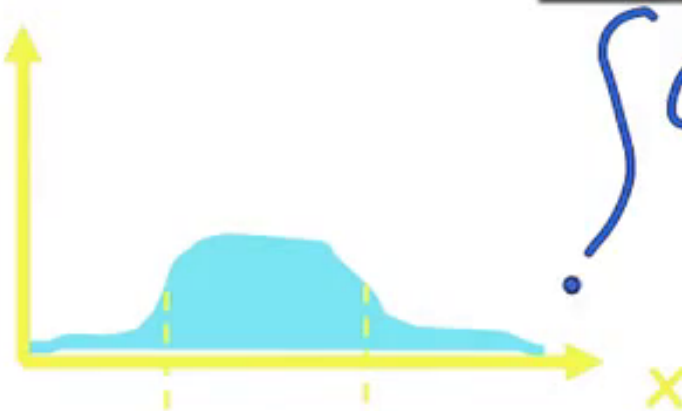
$I(x,y)$
Image



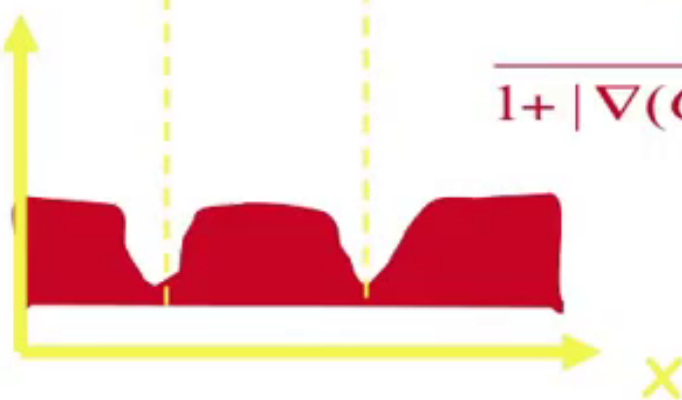
$g(x,y)$
Edges



$I(x)$



$g(x)$



$\int g$

$$\frac{1}{1 + |\nabla(G_\sigma * I)|^2}$$

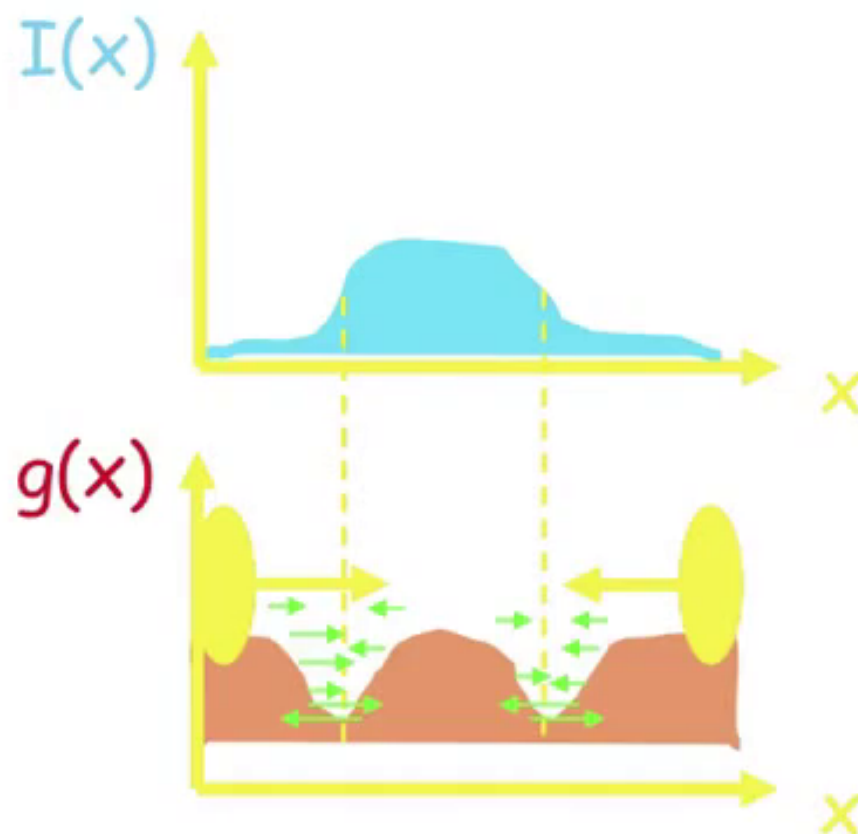


Geodesic Active Contours in 1D

Geodesic active contours are
reparameterization invariant

$$\frac{dC}{dt} = \left(g(C)\kappa - \langle \nabla g(C), \vec{N} \rangle \right) \vec{N}$$

\nearrow
 $\int g$



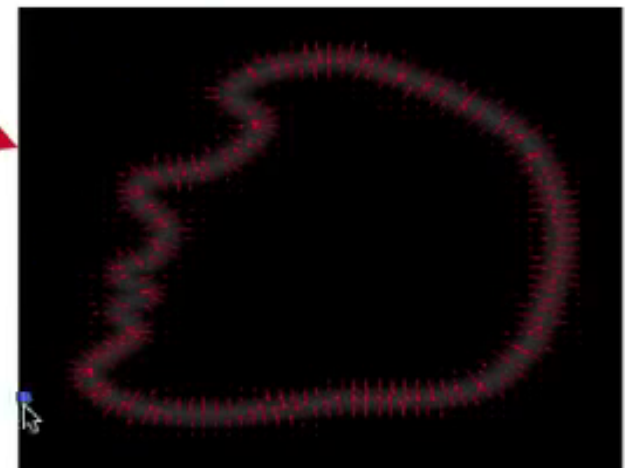
Geodesic Active Contours in 2D



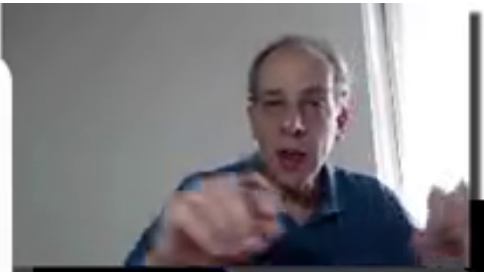
$G_s * I$



$$g(x) = \frac{1}{1 + |\nabla(G_s * I)|^2}$$



$$\frac{dC}{dt} = (g(C)\kappa - \langle \nabla g(C), \vec{N} \rangle) \vec{N}$$



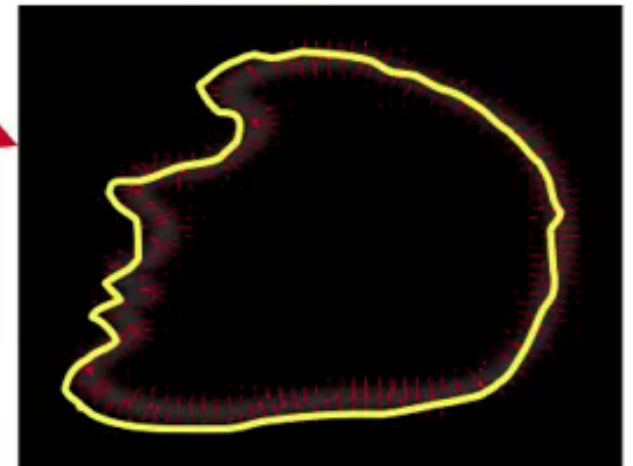
Geodesic Active Contours in 2D



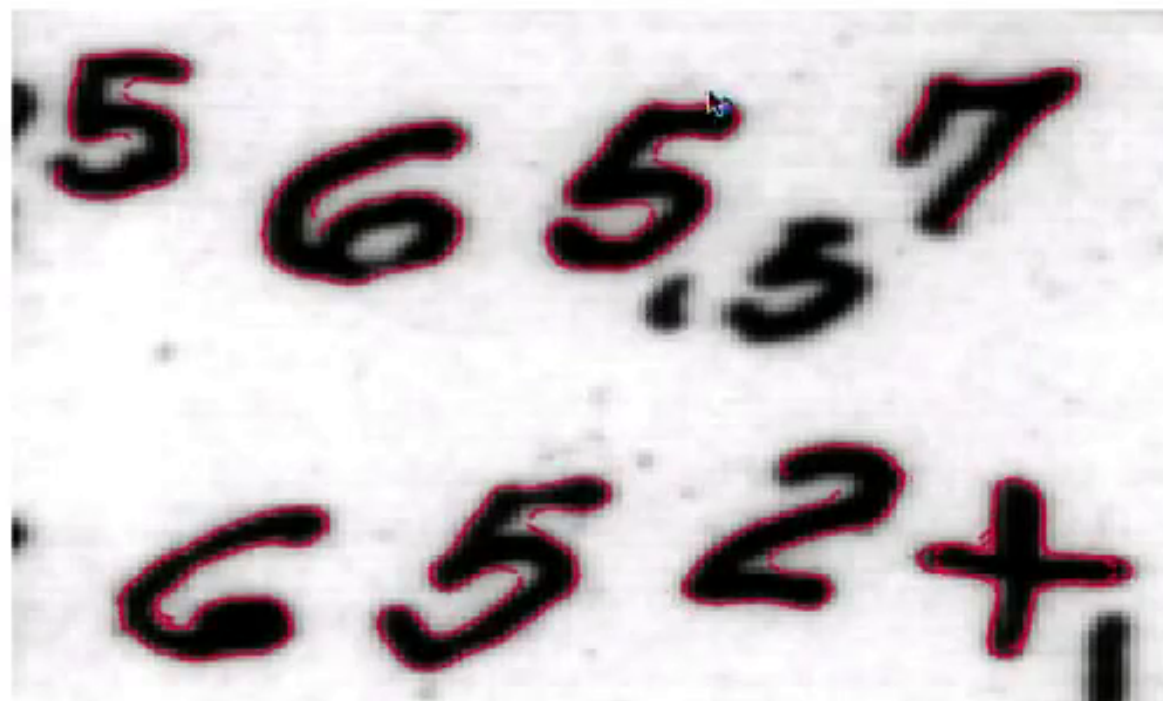
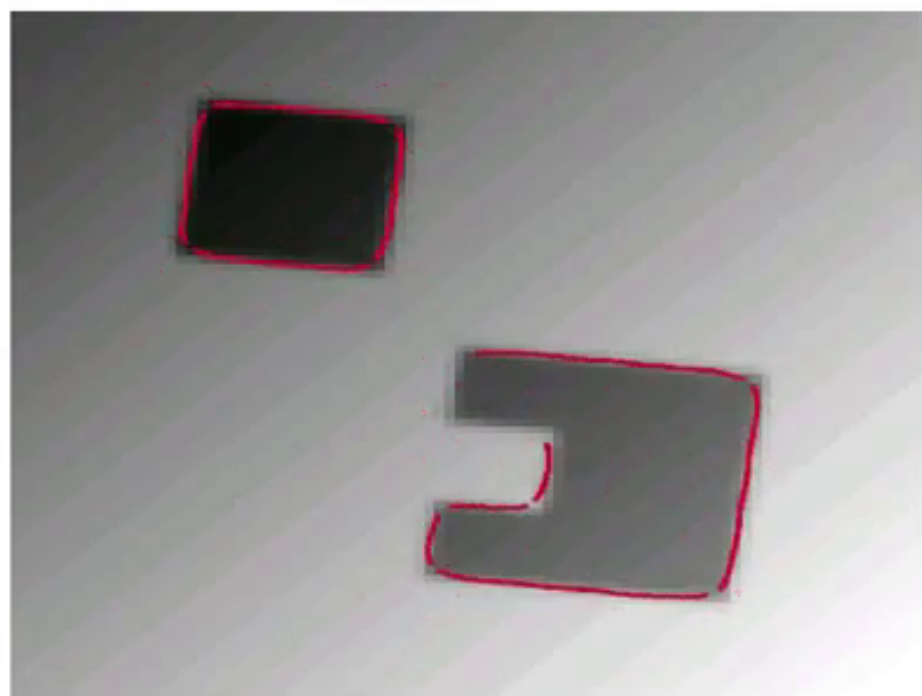
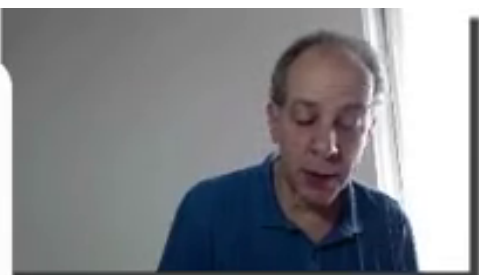
$G_s * I$

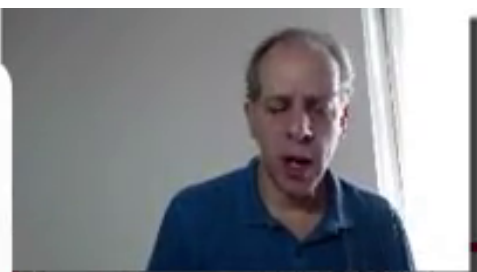


$$g(x) = \frac{1}{1 + |\nabla(G_s * I)|^2}$$



$$\frac{dC}{dt} = (g(C)\kappa - \langle \nabla g(C), \vec{N} \rangle) \vec{N}$$





Gray Matter Segmentation

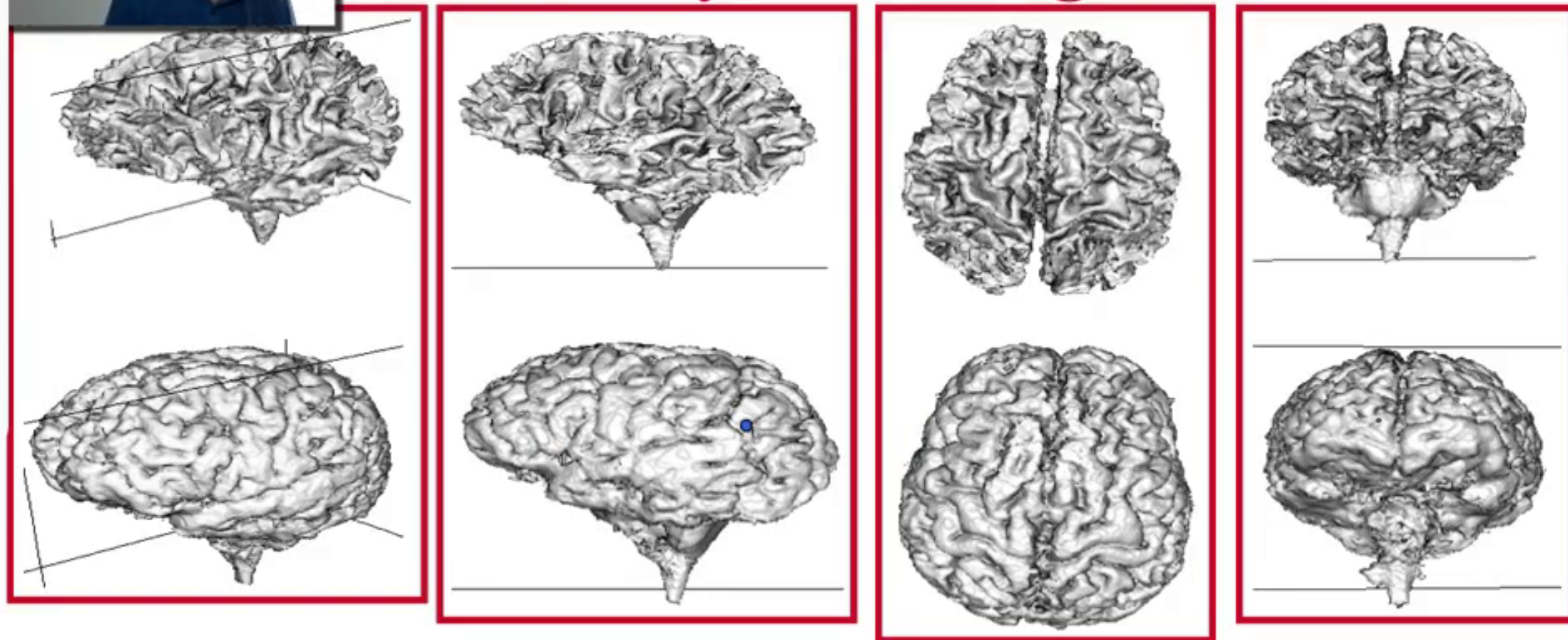
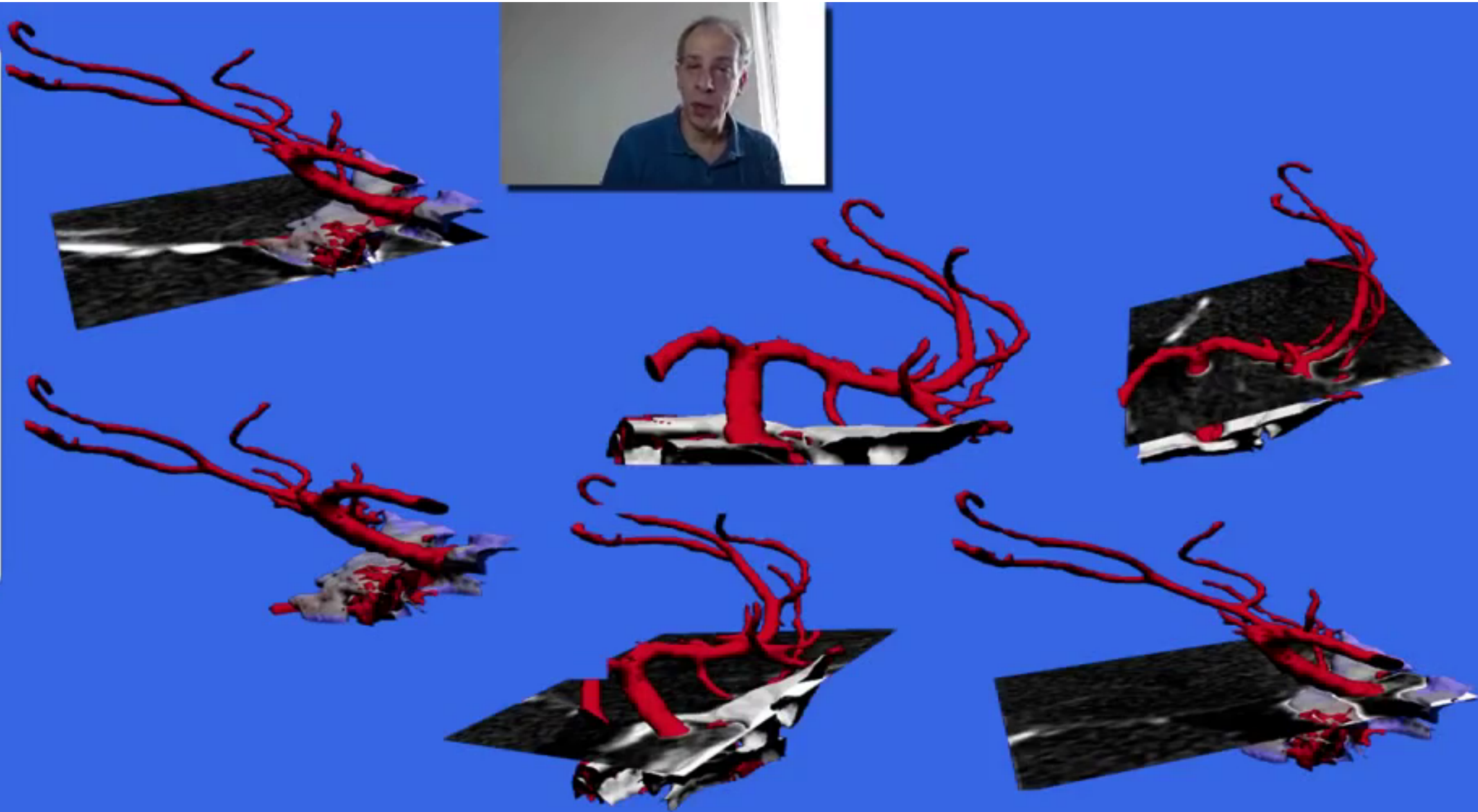


Image courtesy of Goldenberg Kimmel Rivlin Rudzsky,



Images courtesy of Holzman-Gazit, Goldshier, Kimmel