

Exercise 5

$$61 \quad Q_D = 21 - 3.5P = P = 6 - \frac{1}{3.5}Q$$

$$13 \text{ people} \Rightarrow P_{\text{total}_1} = 78 - \frac{26}{7}Q$$

$$62 \quad Q_D = 12 - 2P \Rightarrow P = 6 - \frac{1}{2}Q$$

$$9 \text{ people} \Rightarrow P_{\text{total}_2} = 54 - \frac{9}{2}Q$$

$$MP = 16 = SMC$$

$$SMB = P_{t_1} + P_{t_2} = 132 - \frac{115}{14}Q$$

Optimal at  $SMB = SMC$

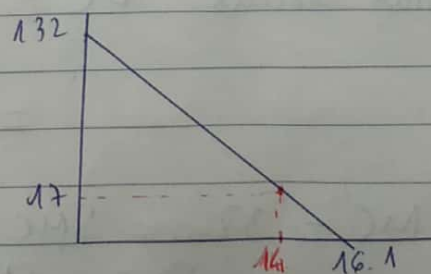
$$\Rightarrow 132 - \frac{115}{14}Q = 16 \Rightarrow Q = 14.12$$

at 14 bus stops

$$\text{Benefit} = \frac{(132 + 17) \times 14}{2} = 1043$$

$$\text{Cost} = 14 \times 16 = 224$$

$$\Rightarrow \text{SSurplus} = 819$$

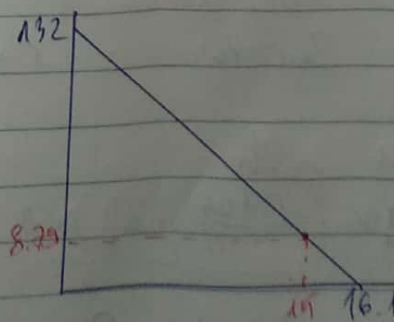


at 15 bus stops

$$\text{Benefit} = \frac{(132 + 8.797) \times 15}{2} = 1055.9$$

$$\text{Cost} = 15 \times 16 = 240$$

$$\Rightarrow \text{SSurplus} = 815.9$$



$\Rightarrow$  optimal Amount = 14

## Exercise 6

$$Q_m = 26 - 6P \Rightarrow P_m = \frac{13}{3} - \frac{1}{6}Q$$

$$Q_n = 18 - 2P \Rightarrow P_n = 9 - \frac{1}{2}Q$$

$$Q_o = 4 - P/4 \Rightarrow P_o = 16 - 4Q$$

$$Q_p = 2 - P/3 \Rightarrow P_p = 6 - 3Q$$

$$MC = 32$$

$$a) m = n = o = p = \frac{32}{4} = 8$$

$$\text{at } P = 8: \quad Q_m = 0, \quad Q_o = 2 \\ Q_n = 2, \quad Q_p = 0$$

$\Rightarrow$  Government will build 2 bus paths

$$b) m + n + o + p = 32$$

$$\text{Total Social DC} = P_m + P_n + P_o + P_p$$

$$= \frac{106}{3} - \frac{23}{3}Q = SMB$$

$$MC = 32 = SMC$$

$$SMC = SMB$$

$$\Rightarrow \frac{106}{3} - \frac{23}{3}Q = 32 \Rightarrow Q = 0.43$$

at 0 bus paths

$$\text{Surplus} = \text{Cost} = \text{benefit} = 0$$

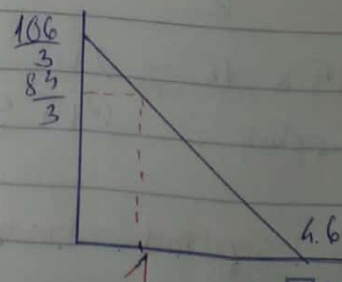
at 1 path

$$\text{benefit} = \frac{\left(\frac{106}{3} + \frac{83}{3}\right) \times 1}{2} = 31.5$$

$$\text{Cost} = 32 \times 1 = 32$$

$$\Rightarrow \text{SSurplus} = -0.5$$

~~bus~~



socially  
 $\Rightarrow$  Optimal Path = 0.

at  $Q=0$

$$P_m = \frac{13}{3}; P_n = 9; P_o = 10; P_p = 6$$

total = 35.3  $\Rightarrow$  able to achieve socially optimal amount.

### Exercise 4

$$Q_D = 24 - 6P; Q_E = 13 - 4P$$

because PRIVATE GOODS  $\Rightarrow$  summed horizontally.

$$SMB = \text{total DC} = 37 - 10P$$

if public, summed vertically.

$$P_D = 4 - \frac{1}{6}Q; P_E = \frac{13}{4} - \frac{1}{4}Q$$

$$\Rightarrow SMB = \frac{29}{4} - \frac{5}{12}Q$$

### Exercise 3

$$Q_H = 18 - 4P \Rightarrow P_H = \frac{9}{2} - \frac{1}{4}Q$$

$$Q_J = 25 - 3P \Rightarrow P_J = \frac{25}{3} - \frac{1}{3}Q$$

$$Q_K = 12 - \frac{1}{2}P \Rightarrow P_K = 24 - 2Q$$

$$MC = 30$$



① taxed evenly  $h-j-k = \frac{30}{3} = 10$

at  $P=10$ ;  $Q_h = 0$ ;  $Q_j = 0$

$Q_k = 7 \Rightarrow$  Government builds 7 (largest asked by any resident)

②  $h+j+k = 30$ .

total Social DC =  $P_h + P_j + P_k$

$= \frac{221}{6} - \frac{31}{12}Q = \text{SMB}$

$\text{SMB} = \text{SMC} = \text{MD}$

$\Rightarrow \frac{221}{6} - \frac{31}{12}Q = 30 \Rightarrow Q = 2.6$

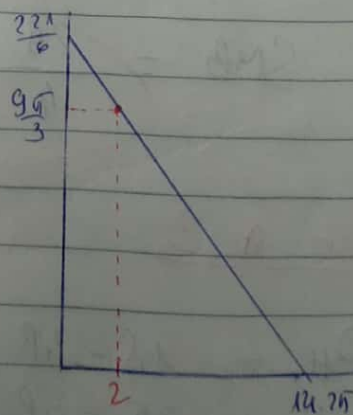
• at 2 traffic signs.

benefit =  $\left(\frac{221}{6} + \frac{95}{3}\right) \times 2 \times \frac{1}{2}$

$= 68.5$

Cost =  $30 \times 2 = 60$

$\Rightarrow \text{SSurplus} = 8.5$



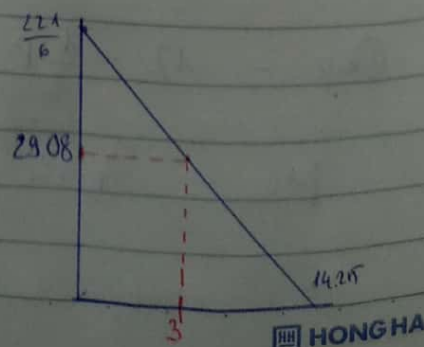
• at 3 traffic signs.

benefit =  $\left(\frac{221}{6} + 29.08\right) \times 3 \times \frac{1}{2}$

$= 98.87$

Cost =  $3 \times 30 = 90$

$\Rightarrow \text{SSurplus} = 8.87$



at 3 Signs

$$P_h = \frac{15}{h} ; P_f = \frac{22}{3} ; P_k = 18$$

$$\text{total} = 29.08 < 30$$

⇒ It's not possible to achieve social optimum.

### Exercise 2

Group 1:  $Q_D = 35 - 5P \Rightarrow P = 7 - \frac{1}{5}Q$

27 people  $\Rightarrow P_{t1} = 189 - \frac{27}{5}Q$

Group 2:  $Q_D = 16 - 3.2P \Rightarrow P = 5 - \frac{1}{3.2}Q$

~~22~~ 12 people  $\Rightarrow P_{t2} = 60 - \frac{15}{4}Q$

Sewer cost = 22 = SMC

$$SMB = P_{t1} + P_{t2} = 249 - \frac{183}{20}Q$$

SMB = SMC is ~~at~~

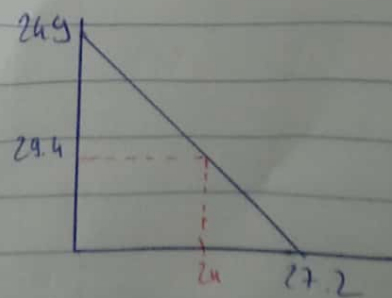
$$\Rightarrow 249 - \frac{183}{20}Q = 22 \Rightarrow Q = 24.8$$

at 24 sewers

$$\text{Benefit} = \frac{(249 + 29.4) \times 24}{2} = 3340.8$$

$$\text{Cost} = 22 \times 24 = 528$$

$$\Rightarrow \text{SSurplus} = 2812.8$$



at 25 sewers.

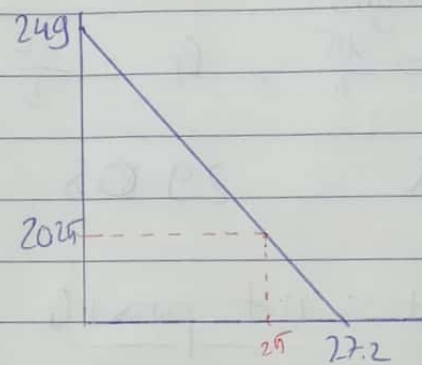
$$\text{Benefit} = \frac{(249 + 20 \cdot 25) \cdot 25}{2}$$

$$= 3365.625$$

$$\text{Cost} = 22 \times 25 = 550$$

$$\Rightarrow \text{SSurplus} = 2815.625$$

$\Rightarrow$  optimum amount at 25 sewers.



Exercise 1

$$Q_M = 35 - 5P ; \quad Q_E = 18 - 2P$$

a) if clothes are private goods.

$$\text{SMB} = Q_M + Q_E = 53 - 7P$$

b) if clothes are public

$$P_M = 7 - \frac{1}{5}Q ; \quad P_E = 9 - \frac{1}{2}Q$$

$$\text{SMB} = P_M + P_E = 16 - \frac{7}{10}Q$$