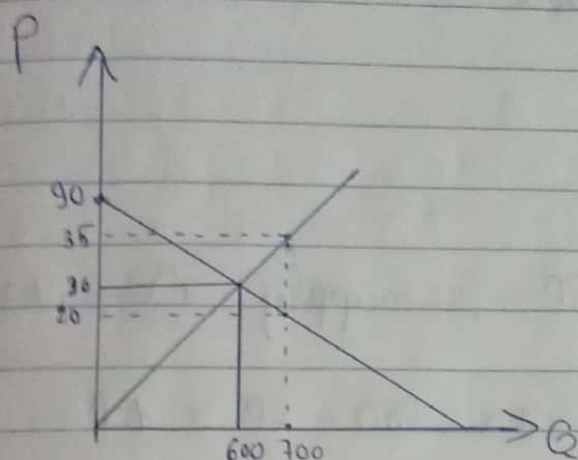


Question 4:

Demand $Q = -10P + 900$; Supply $Q = 20P$ 

$$Q_D = Q_S$$

$$\Rightarrow -10P + 900 = 20P$$

$$\Rightarrow P_E = 30$$

$$\Rightarrow Q_E = 600$$

$$\Rightarrow \text{Consumer surplus} = \frac{1}{2} \times (90 - 30) \times 600 = 18000$$

$$\text{Producer surplus} = \frac{1}{2} \times 30 \times 600 = 9000$$

$$\Rightarrow \text{total} = 27,000$$

* Subsidy \$15

$$\Rightarrow Q_S^* = 20(P + 15) \Leftrightarrow 20P + 300$$

$$Q_S^* = Q_D \Leftrightarrow 20P + 300 = -10P + 900$$

$$\Rightarrow P^* = 20$$

$$\Rightarrow (P^*) = 30 + (\cancel{30} - 20) *$$

$$P^* = 35; \text{ new } Q = 10 \times 35 = 700$$

$$\text{New Consumer surplus} = \frac{1}{2} (90 - 35) \times 700 = 24500$$

$$\text{New Producer surplus} = \frac{1}{2} \times 35 \times 700 = 12250$$

$$\text{Government lost} = 15 \times 700 = 10500$$

$$\Rightarrow \text{DWL} = 27000 - (24500 + 12250 - 10500) = 750$$

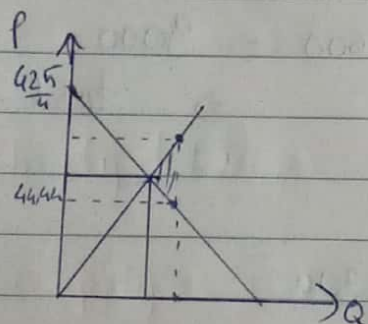
\Rightarrow there is a DWL because Government lost more than the actual amount received.

Question 4.1

Demand $Q = 850 - 8P$; Supply $Q = 10P$

\Rightarrow Equilibrium : $Q_D = Q_S \Leftrightarrow 850 - 8P = 10P$

$\Rightarrow P_E = \frac{425}{9} = 47,22 \Rightarrow Q_E = \frac{4250}{9} = 472,22$



+ Con Surplus : $\frac{1}{2} \times \left(\frac{425}{4} - \frac{425}{9} \right) \times \frac{4250}{9}$
 $= 13937,11$

+ Producer Surplus = $\frac{1}{2} \times \frac{425}{9} \times \frac{4250}{9}$
 $= 11149,69$

* Subsidy \$5

\Rightarrow new supply: $Q = 10(P+5) = 10P + 50$

$10P + 50 = 850 - 8P \Rightarrow P^* = 44,44$

$\Rightarrow (P^*)' = 47,22 + (5 - (47,22 - 44,44))$
 $= 49,44$

$$\Rightarrow Q^* = 10 \times 49,44 = 494,4$$

$$\Rightarrow \text{new Consumer surplus} : \frac{1}{2} \times \left(\frac{425}{4} - 49,44 \right) \times 494,4$$

$$= 15279,4$$

$$\text{new ~~profit~~ producer surplus} : \frac{1}{2} \times 49,44 \times 494,4$$

$$= 12221,57$$

$$\text{Government lost} : 5 \times 494,4 = 2472$$

$$\text{DWL} = \frac{(494,4 - 472,22) \times 5}{2} = \textcircled{55,45}$$

$$|DWL| = (15279 + 12221,57) - 2472 - 13937,11$$

$$- 11149,69 =$$

$$= 58,23$$

The total surplus received by producer and consumer is less than amount paid by the government

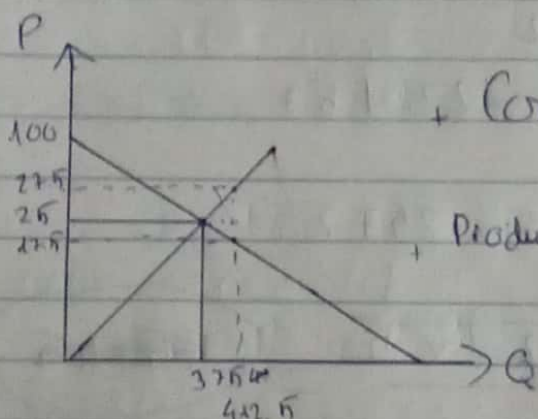
$$\Rightarrow \text{DWL}$$

Question 4.2

Demand: $Q_D = 500 - 5P$; Supply: $Q_S = 15P$

\Rightarrow Equilibrium $Q_D = Q_S \Leftrightarrow 500 - 5P = 15P$

$\Rightarrow P_E = 25$; $Q_E = 375$



+ Consumer surplus: $\frac{1}{2} \times 75 \times 375 = 140625$

+ Producer surplus: $\frac{1}{2} \times 25 \times 375 = 46875$

\Rightarrow total: 18750.

* Subsidy \$10

new supply: $Q'_S = 15(P+10) = 15P + 150$

$Q'_S = Q_D \Leftrightarrow 15P + 150 = 500 - 5P$

$\Rightarrow P^* = 17.5$

$\Rightarrow (P^*)' = 27.5 \Rightarrow Q^* = 27.5 \times 15 = 412.5$

+ New consumer surplus: $\frac{1}{2} (100 - 17.5) \times 412.5 = 17015.625$

+ New producer surplus: $\frac{1}{2} \times 27.5 \times 412.5 = 5671.875$

+ Government lost: $10 \times 412.5 = 4125$

$$\Rightarrow DWL = \frac{1}{2} \times (4125 - 3375) \times 10 = 187.5$$

Amount paid by government is less than amount of surplus added

$$\Rightarrow DWL$$

Question 5

$$Q_s = \frac{100}{8} P ; \quad P_D = 400 - 2.92 Q_D$$

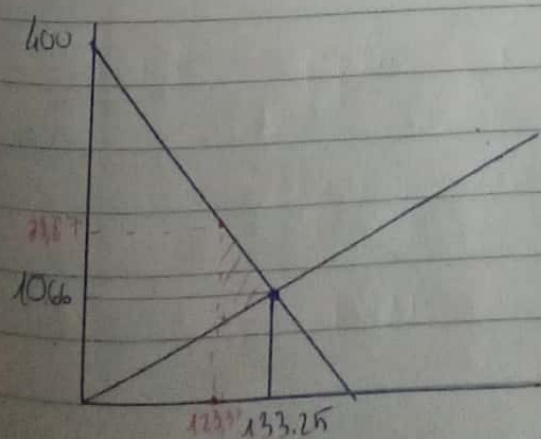
$$\Rightarrow Q_D = \frac{400}{2.92} - \frac{1}{2.92} P_D$$

Equilibrium $Q_s = Q_D$

$$\Rightarrow \frac{100}{8} P = 136.98 - \frac{1}{2.92} P$$

$$\Rightarrow 12.84P = 136.98 \Rightarrow P_E = 10.66$$

$$Q_E = 133.25$$



$$+ C_{\text{surplus}} = \frac{1}{2} \times (400 - 10.66) \times 133.25$$

$$= 25939.78$$

$$+ P_{\text{surplus}} = \frac{1}{2} \times 10.66 \times 133.25$$

$$= 710$$

b) Tax $t = 30$.

Qs New tax supply curve $Q_s^t = \frac{100}{8} (P - 30)$

$$\Rightarrow Q_s^t = \frac{100}{8} P = ~~17.5~~ \cdot 37.5$$

* New equilibrium.

$$Q_s^t = Q_D \Rightarrow \frac{100}{8} P - 37.5 = 136.98 - \frac{1}{2.92} P$$

$$\Rightarrow 12.84P = ^{511.98} ~~154.48~~ \Rightarrow P_E = ~~12.03~~$$

$$\Rightarrow P_E' = 39.87 \Rightarrow Q_E' = 123.37$$

$$\Rightarrow \text{Government Tax revenue} = ³⁰ ~~39.87~~ \times 123.37$$

$$= 3701.1$$

$$\Rightarrow DWL = \frac{1}{2} \times 30 \times (133.25 - 123.37)$$

$$= 148.2$$

5.1

$$Q_s = \frac{200}{12} P, \quad P_D = 500 - 5Q_D$$

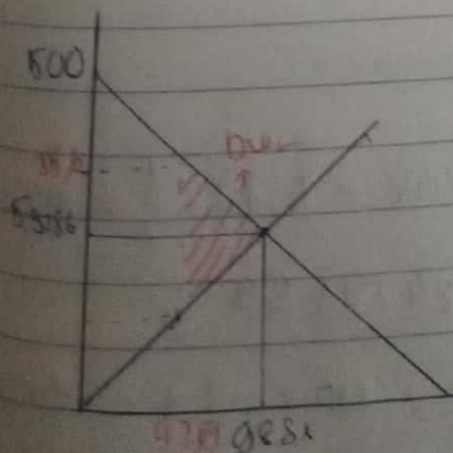
$$\Rightarrow P_s = \frac{Q_s \cdot 200}{12} = \frac{Q_s \cdot 12}{200} = 0.06 Q_s$$

Equilibrium $P_s = P_D$

$$\Rightarrow 0.06 Q_s = 500 - 5Q_D$$

$$\Rightarrow \begin{cases} Q_E = 98.81 \\ P_E = 5.9286 = 5.93 \end{cases}$$

$$\Rightarrow \begin{cases} C_s = \frac{1}{2} \times (500 - 5.93) \times 98.81 = 24409 \\ P_s = \frac{1}{2} \times 5.93 \times 98.81 = 293 \end{cases}$$

* tax $t = 28$

$$\rightarrow \text{new supply curve: } P_s - 30 = 0.06 Q_s$$

$$\Rightarrow P_s = 0.06 Q_s + 30$$

$$0.06 Q_s + 30 = 500 - 5Q_D$$

New equilibrium

$$\begin{cases} P_E' = 35.5734 = 35.6 \\ Q_E' = 92.89 \end{cases}$$

⇒ Government tax revenue

$$= 28 \times 92.89 = 2600.9$$

⇒ DWL

$$= (98.89 - 92.89) \times 28 \times \frac{1}{2}$$

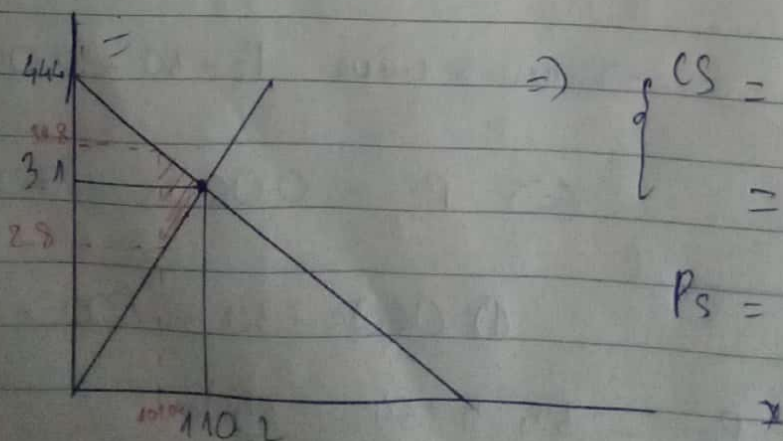
$$= 84$$

(5.2) $Q_s = 30 + 36P \Rightarrow P = \frac{1}{36} Q_s$

$$P = 444 - 4Q_d$$

Equilibrium: $P_s = P_d \Leftrightarrow \frac{1}{36} Q_s = 444 - 4Q_d$

$$\Rightarrow \begin{cases} Q_E = 110.2 \\ P_E = 3.1 \end{cases}$$



$$\Rightarrow \begin{cases} CS = (444 - 3.1) \times \frac{1}{2} \times 110.2 \\ = 24293.59 \end{cases}$$

$$P_s = \frac{1}{2} \times 110.2 \times 3.1 = 170.81$$

$$* \text{ tax } t = 37$$

$$p - 37 = \frac{1}{36} Q_D *$$

$$\Rightarrow P^* = \frac{1}{36} Q_S + 37$$

$$\text{New equilibrium: } \frac{1}{36} Q + 37 = 444 - 4Q$$

$$\Rightarrow \begin{cases} Q'_E = 101.04 \\ P'_E = 39.8 \end{cases}$$

$$\Rightarrow \text{new CS} = \frac{1}{2} \times (444 - 39.8) \times 101.04$$

$$= 20420$$

$$\text{new PS} = \frac{1}{2} \times 2.8 \times 101.04 = 141.456$$

$$\Rightarrow \begin{cases} \text{Government tax revenue} = 101.04 \times 37 = 3738.48 \\ \text{DWL} = \frac{1}{2} \times (110.2 - 101.04) \times 37 \\ = 169.46 \end{cases}$$