

# **A BFT protocol**

**Simplified HotStuff**

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# PoW or Certificates

Idea

# BFT protocol

## Certificate vs. PoW

**PoW:** Requiring that blocks contains a proof of work gives the following:

- **Rate limit:** Limit at which rate new blocks are created.
- **Fork probability:** Reduce probability for forks
- **Prevent system split:** Small subsystem will not be able to create blocks at correct rate.

# BFT protocol

## Certificate vs. PoW

**Certificate:** If blocks require a certificate, we get similar properties.

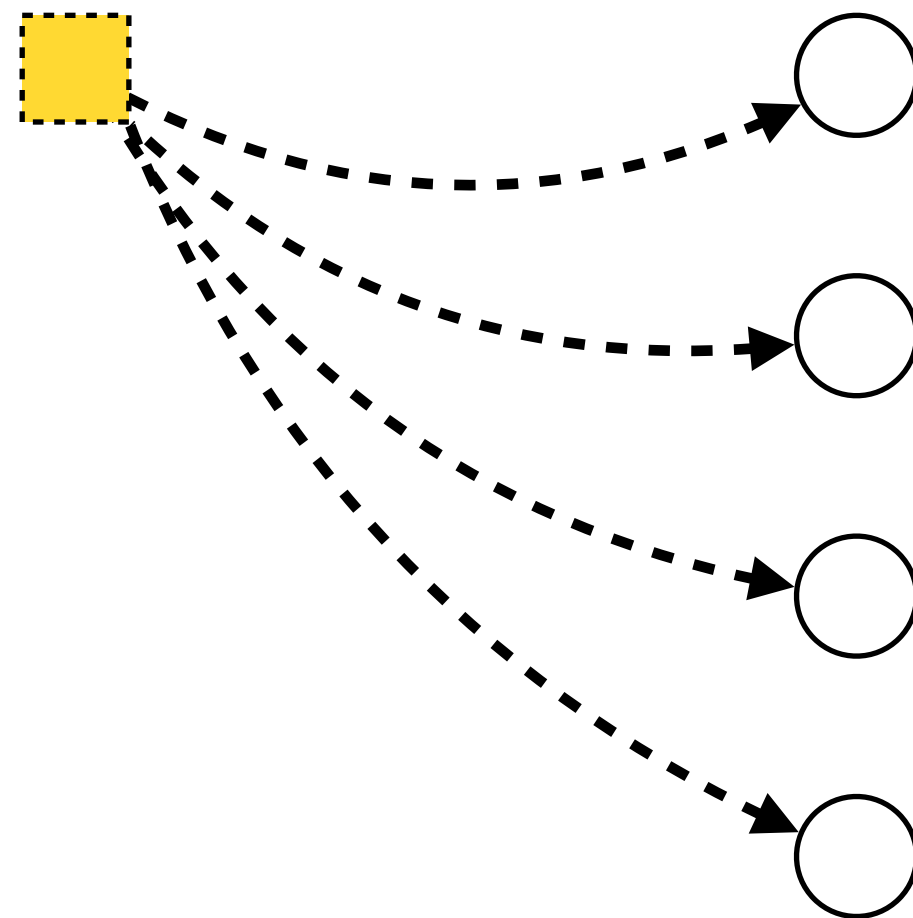
- **Rate limit:**
- **Fork probability:**
- **Prevent system split:**

# BFT protocol

## Certificate vs. PoW

**Idea:** Send new block to nodes for validation and signature.  
Then collect certificate.

new block

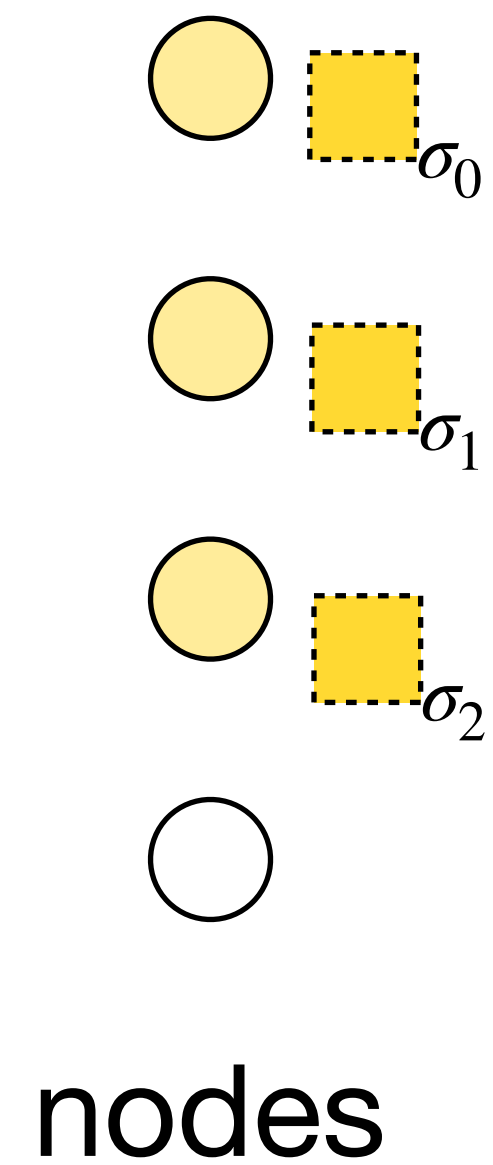


nodes

# BFT protocol

## Certificate vs. PoW

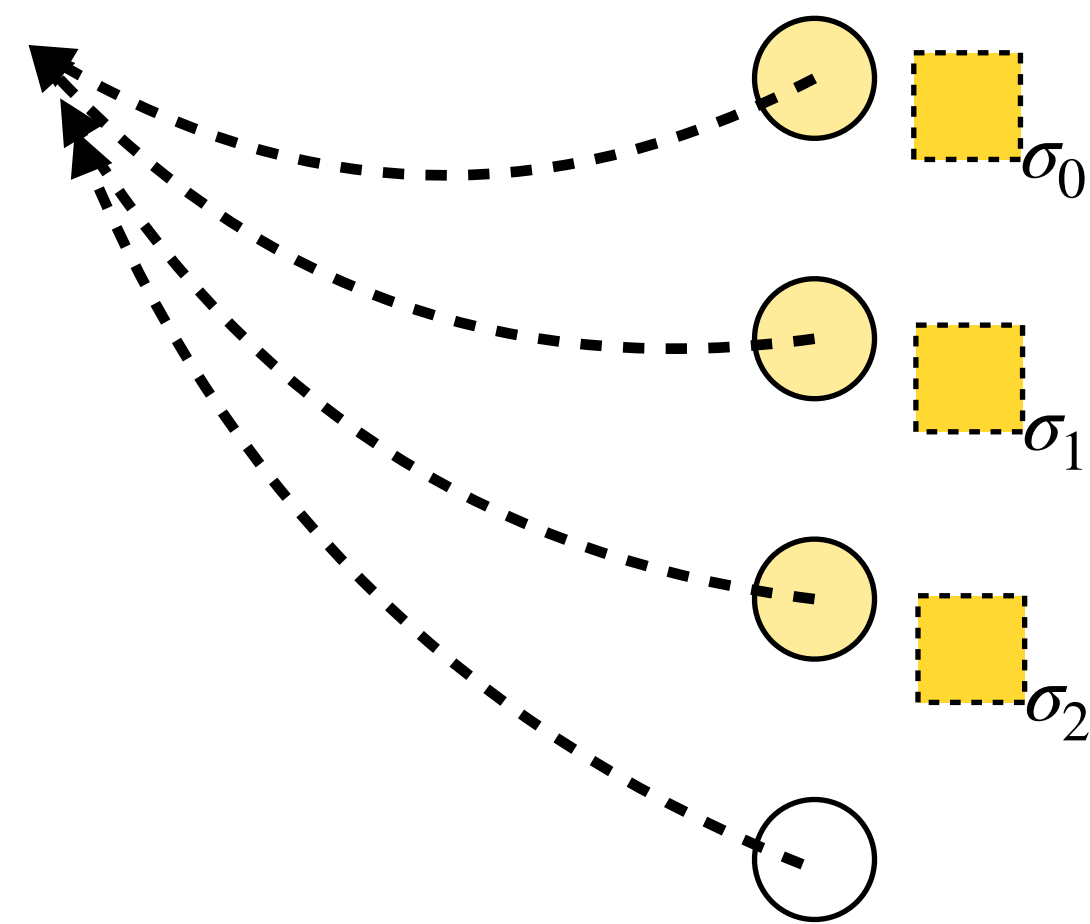
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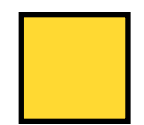


nodes

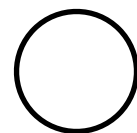
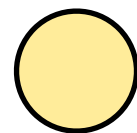
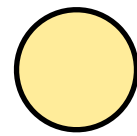
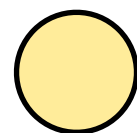
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$\langle \sigma_0, \sigma_1, \sigma_2 \rangle$



nodes



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- **Rate limit:**
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## Certificate vs. PoW

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- **Rate limit:**

# BFT protocol

## Certificate vs. PoW

**Idea:** Send new block to nodes for validation and signature.  
Then collect certificate.

**Certificate:** If blocks require a certificate, we get similar properties.

- **Rate limit:**  
Blocks need to be verified and signed by most of the nodes.  
Cannot create blocks faster than they are verified and signed.
- **Fork probability:**
- **Prevent system split:**

# BFT protocol

## Certificate vs. PoW

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- **Fork probability:**

# BFT protocol

## Model

### Model:

- We assume a permissioned system with  $N = 3f + 1$  nodes.
- Nodes have unique ids and unique, known cryptographic keys.
- At most  $f$  of the nodes are byzantine faulty.

### Certificate:

- A block has a certificate, if it contains signatures of  $2f + 1$  nodes.

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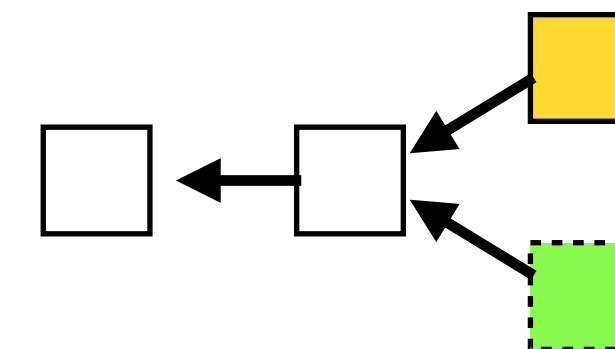
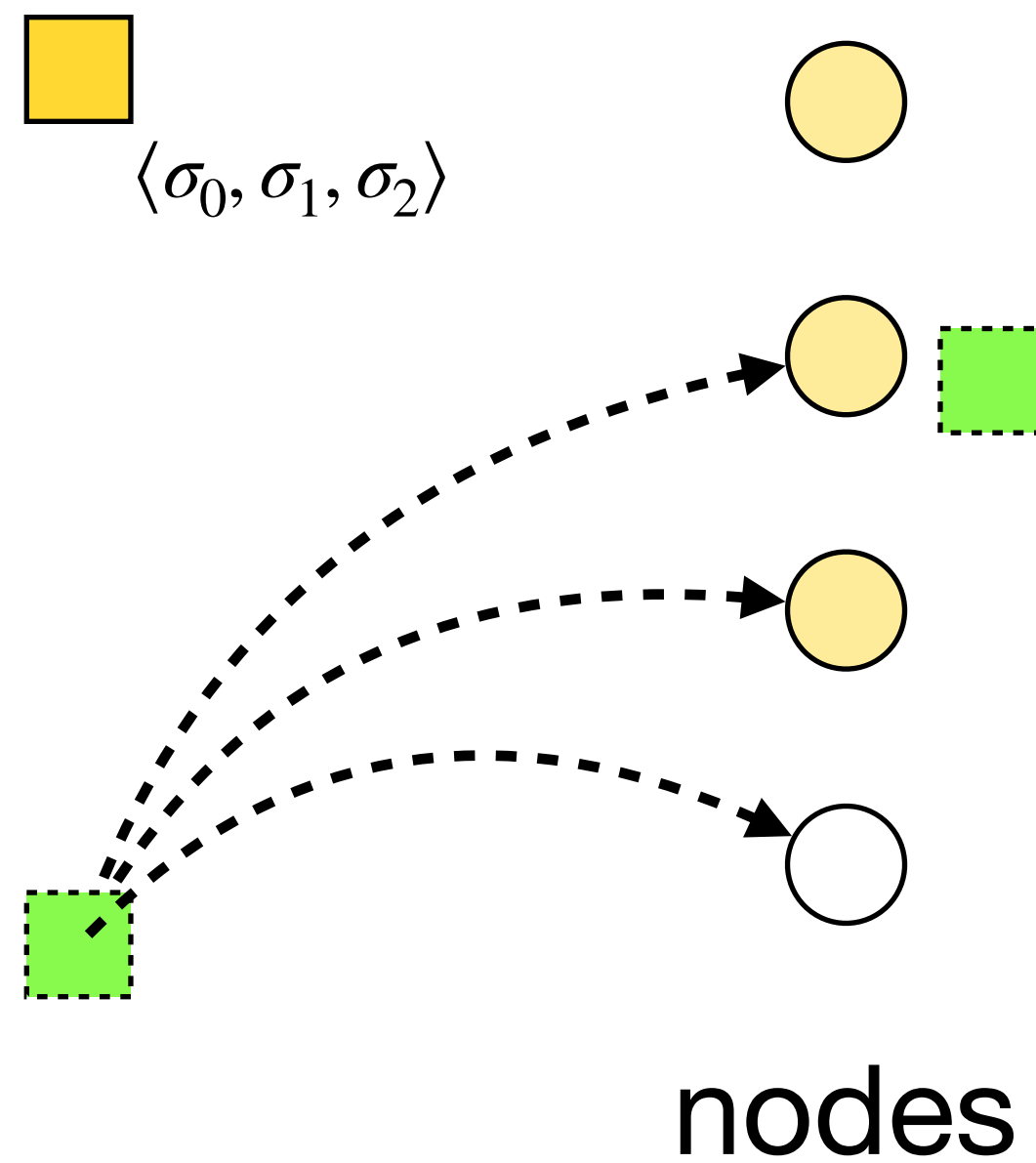
**Certificate:** If blocks require a certificate, we get similar properties.

- **Rate limit:**
- **Fork probability:**  
If nodes do not sign multiple blocks, at most one block at a given height can get a certificate.
- **Prevent system split:**

# BFT protocol

## Certificate vs. PoW

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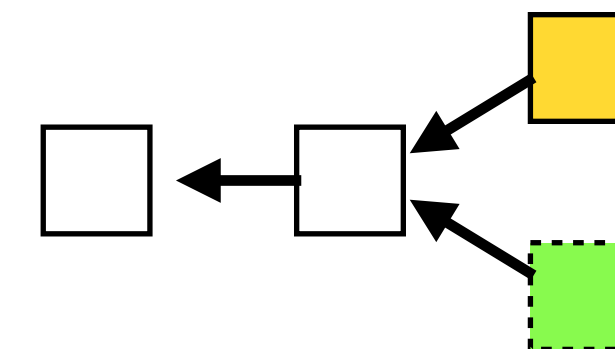
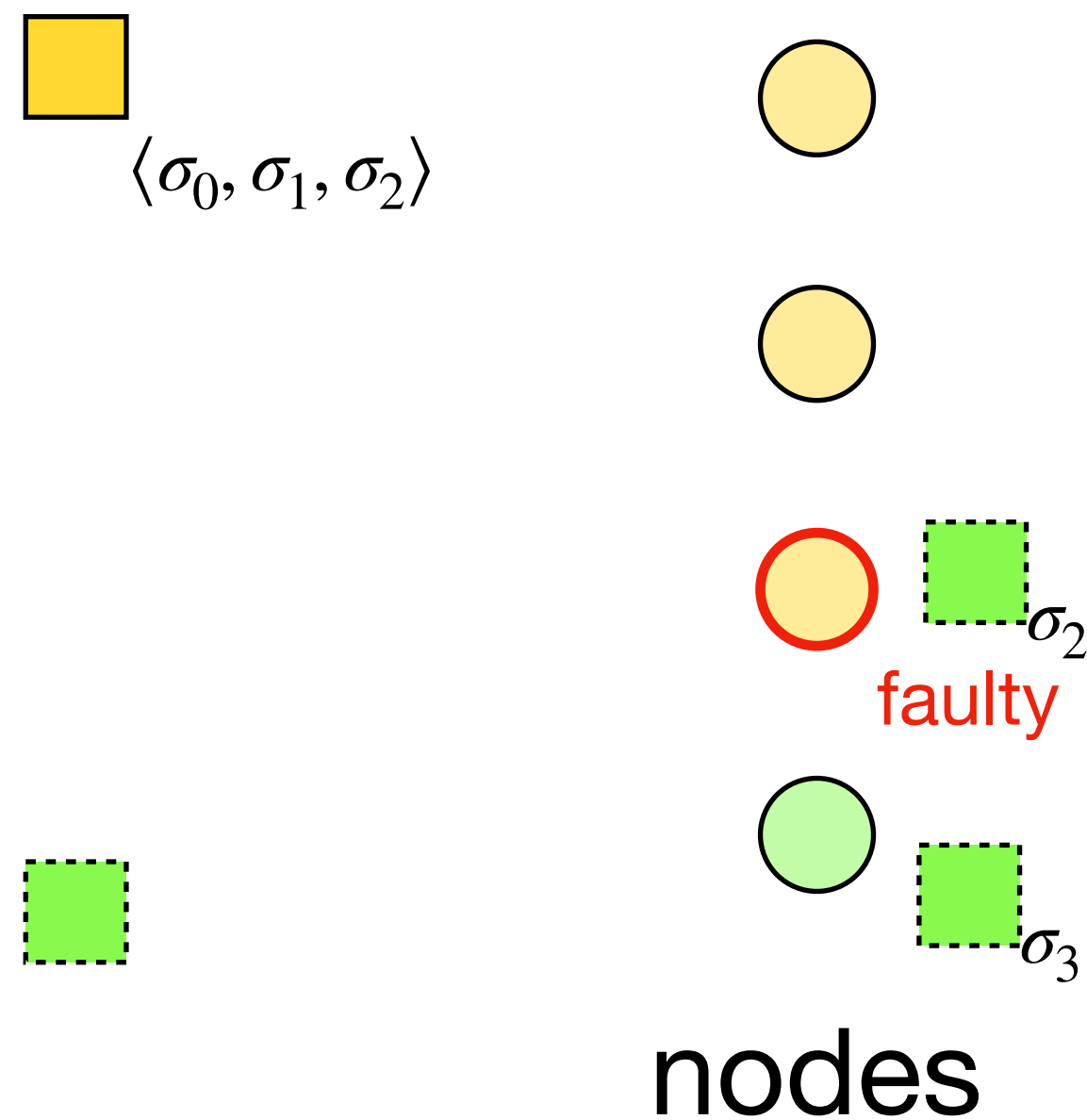




# BFT protocol

## Certificate vs. PoW

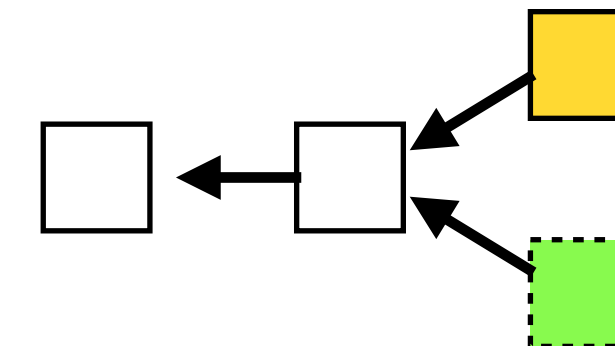
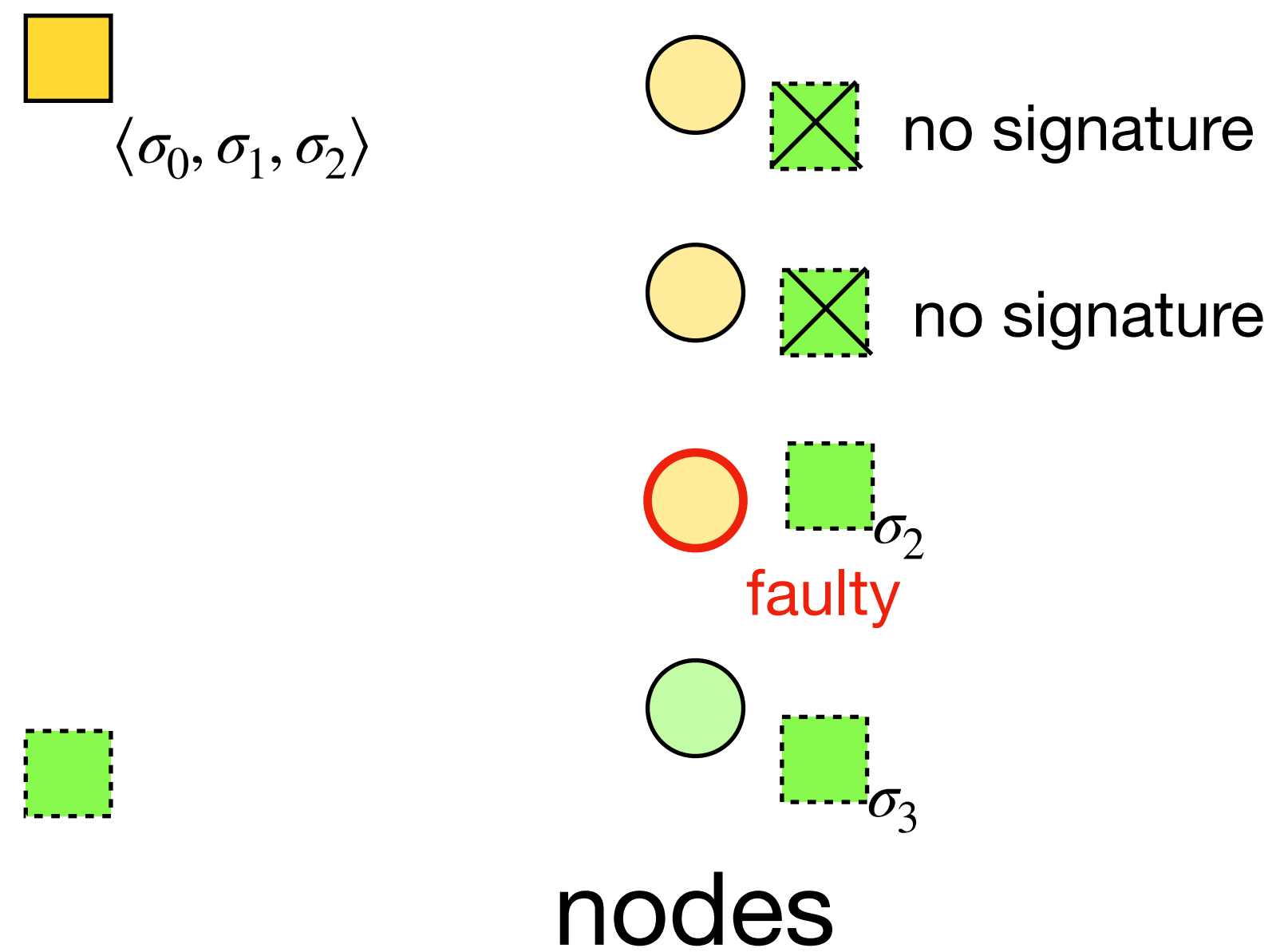
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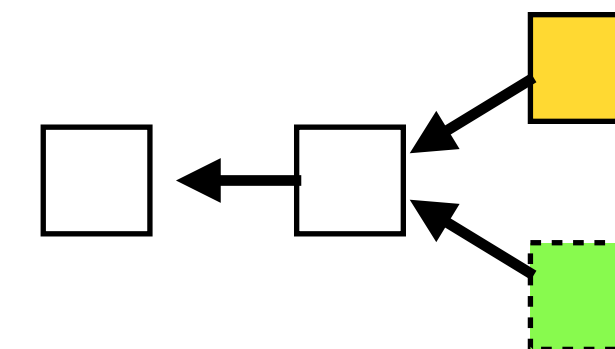
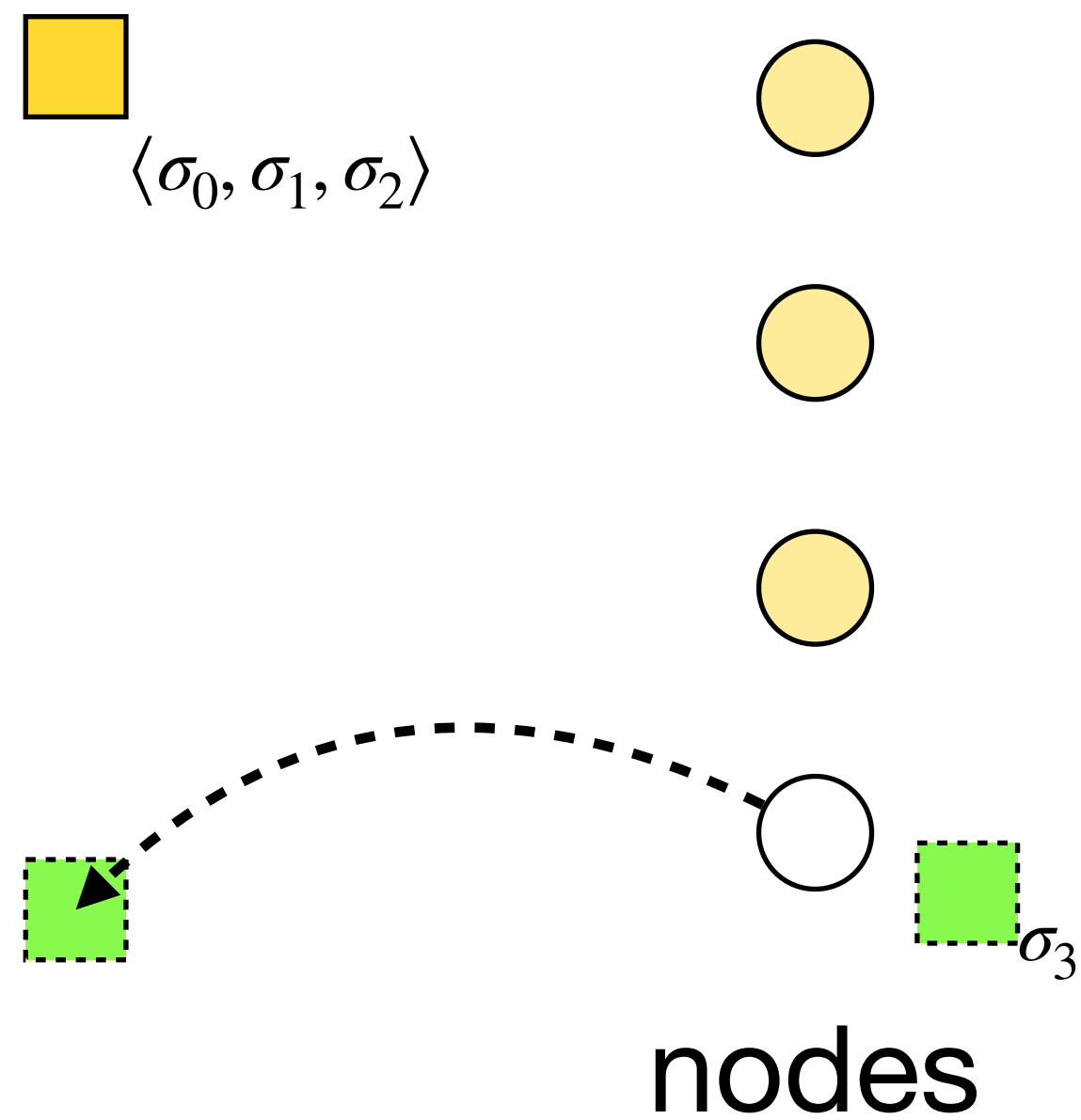
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## Certificate vs. PoW

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# BFT protocol

## Certificate vs. PoW

**Idea:** Send new block to nodes for validation and signature.

*Correct nodes sign only one block at given depth.*

Then collect certificate.

**Certificate:** If blocks require a certificate, we get similar properties.

- **Rate limit:**
- **Fork probability:**  
If nodes do not sign multiple blocks, at most one block at a given height can get a certificate.  
*Obs: Faulty nodes may sign multiple blocks!*
- **Prevent system split:**

# BFT protocol

## Certificate vs. PoW

**Idea:** Send new block to nodes for validation and signature.  
*Correct nodes sign only one block at given depth.*  
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**Certificate:** If blocks require a certificate, we get similar properties.

- **Rate limit:**
- **Fork probability:**
- **Prevent system split:**  
A subsystem, with few nodes cannot create certificates.

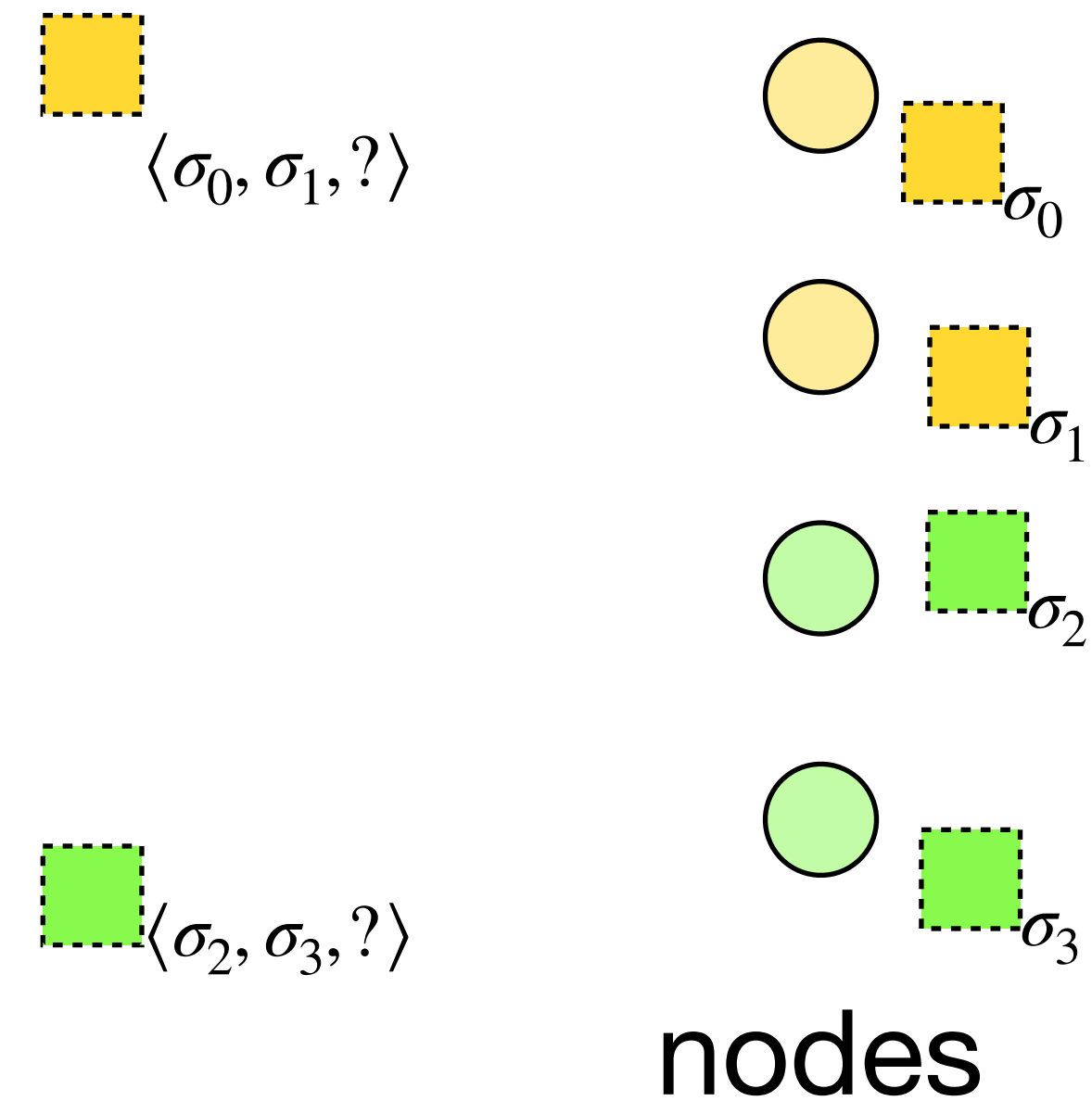
# BFT protocol

## Certificate vs. PoW problem

**Idea:** Send new block to nodes for validation and signature.  
*Correct nodes sign only one block at given depth.*  
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**Problem:** How to ensure that a certificate is created?

- Nodes may sign different blocks
- No block gets a certificate
- **Solution:**



# BFT protocol

## Certificate vs. PoW problem

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- No block gets a certificate
- **Solution:** Leader

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## Certificate vs. PoW problem

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*Correct nodes sign only one block at given depth.*  
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**Problem:** How to know that a certificate was created?

- A certificate may be collected by a single node
- The node with the certificate may fail and come back later
- **Solution:**



# BFT protocol

## Certificate vs. PoW problem

**Idea:** Send new block to nodes for validation and signature.  
*Correct nodes sign only one block at given depth.*  
Then collect certificate.

**Problem:** How to know that a certificate was created?

- A certificate may be collected by a single node
- The node with the certificate may fail and come back later
- **Solution:** Require multiple certificates

# BFT protocol

## Simple HotStuff (2 chain)

### Preliminary:

- Every block includes a parent link (*previous block*).  
=> Blocks form a **tree**.  
Every block includes a **round number**
- Every block must include a **certificate** for its parent
- A blocks **round** must be larger than that of its parent

# BFT protocol

## Simple HotStuff (2 chain)

### Rules

- *Every block must contain certificate for parent*
- *Every block must have round  $>$  round of parent*
- **Rule 1:** After signing a block at round  $max = r$ , a node may only sign at round  $r' > max$ .
- **Rule 2:** After signing a block with parent  $p$  and  $p . round = lock$ , only sign blocks with parents in round  $pr \geq lock$

Keep maximum value for  $max$  and  $lock$  in local variables.

# BFT protocol

## Simple HotStuff

### Def.:

- a) A block with  $round = r$  is **confirmed** if it has a child in  $round = r + 1$ , which has a certificate.
- b) A block with  $round = r$  is **confirmed** if it has a grandchild in  $round = r + 2$

**Theorem:** *If a block is confirmed, only descendants of that block, can get a certificate.*

**Proof:** A majority of correct nodes have set their *lock* to the confirmed node.

# BFT protocol

## Simple HotStuff - Leader

**Idea 1:** Every round has a designated leader.

**Idea 2:** Nodes wait for  $\Delta$  time for a proposal in current round, before accepting at next round.

# BFT protocol

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**Idea 1:** Every round has designated leader.

**Idea 2:** Nodes wait for  $\Delta$  time for a proposal in current round, before accepting at next round.

*How can a leader avoid the situation from the example?*

Ask all nodes for most recent certificate.

Wait for  $\Delta$  time to receive proposal from all correct nodes.

# BFT protocol

## Simple HotStuff (3 chain)

### Rules

- *Every block must contain certificate for parent*
- *Every block must have round  $>$  round of parent*
- **Rule 1:** After signing a block at round  $max = r$ , a node may only sign at round  $r' > max$ .
- **Rule 2:** After signing a block with **grandparent**  $p$  and  $p . round = lock$ , only sign blocks with parents in round  $pr \geq lock$

Keep maximum value for  $max$  and  $lock$  in local variables.

# BFT protocol

## Simple HotStuff (3chain)

In this variant we need to wait longer for confirmation!

### Def.:

- a) A block with  $round = r$  is **confirmed** if it has a **grandchild** in  $round = r + 2$ , which has a certificate.
- b) A block with  $round = r$  is **confirmed** if it has a **grand-grandchild** in  $round = r + 3$

**Theorem:** *If a block is confirmed, only descendants of that block, can get a certificate.*

**Proof:** A majority of correct nodes have set their *lock* to the confirmed node.



# BFT protocol

## Simple HotStuff - Leader

**Idea 1:** Every round has designated leader.

**Idea 2:** Nodes wait for  $\Delta$  time for a proposal in current round, before accepting at next round.

*How can a leader avoid the situation from the example?*

Ask all nodes for most recent certificate.  
Wait for  $2f + 1$  replies

A no leader needs not wait for  $\Delta$  time!