$\mathop{DATA}_{\mathrm{Fall}\ 2021}\ 8$

Foundations of Data Science

Midterm Solutions

INSTRUCTIONS For questions with circular bubbles, you should fill in exactly one choice.
○ You must choose either this option
Or this one, but not both!
For questions with square checkboxes , you may fill in <i>multiple</i> choices.
☐ You could select this choice.
☐ You could select this one too!
Preliminaries You can complete these questions before the exam starts.
(i) What is your full name?
(ii) What is your Student ID number?
(iii) Who is your Lab GSI?

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1. (18 points) Working with Tables

After the Data 8 midterm, Will, Eddie, and Melissa decide to get dinner at a restaurant in Berkeley, but they're having trouble deciding on a single place. They create a table of all Berkeley restaurants, RESTS_TBL, with four columns:

- "REST NAME": The name of the restaurant
- "CUISTYP": The cuisine (type of food) served at this restaurant
- "Rating": The numerical rating given to the restaurant by the Daily Cal (a float)
- "Distance From Sproul": The distance, in miles, the restaurant is from Sproul Hall (a float)

REST_NAME	CUISTYP	Rating	Distance From Sproul
Imm Thai Berkeley Social Club		9.9 8.7	0.2 0.8
Italian Homemade	Italian	7.9	1.

 $(\dots 76 \text{ more rows})$

(a) (3 pt) Help Will count how many restaurants there are for each cuisine. Write a line of code that outputs a table with two columns: one column with the type of cuisine, and one column containing a count of how many restaurants there are with that cuisine.

Reminder: the columns of RESTS_TBL are "REST_NAME", "CUISTYP", "Rating", and "Distance From Sproul".

```
RESTS_TBL.group("CUISTYP")
```

(b) (3 pt) Will wants to eat at the highest-rated restaurant. Write a line of code that evaluates to the name of the restaurant with the highest rating. (You can assume there is only one restaurant with the highest rating; there are no ties.)

Reminder: the columns of RESTS_TBL are "REST_NAME", "CUISTYP", "Rating", and "Distance From Sproul".

```
RESTS_TBL.sort("Rating", descending=True).column("REST_NAME").item(0)
```

(c) (3 pt) Melissa only wants to eat at a Thai restaurant. Write a line of code that evaluates to a table containing all four columns but only the rows for restaurants whose cuisine is "Thai".

Reminder: the columns of RESTS_TBL are "REST_NAME", "CUISTYP", "Rating", and "Distance From Sproul".

```
RESTS_TBL.where("CUISTYP", "Thai")
```

(d) (3 pt) Eddie didn't want to walk to any restaurants that were further than one mile away from Sproul. Fill in the code below to assign the variable EDDIE_CHOICE to a table containing only restaurants that are less than one mile from Sproul.

```
EDDIE_CHOICE = ...
```

Reminder: the columns of RESTS_TBL are "REST_NAME", "CUISTYP", "Rating", and "Distance From Sproul".

```
EDDIE_CHOICE = RESTS_TBL.where("Distance From Sproul",
are.below_or_equal_to(1)) or EDDIE_CHOICE = RESTS_TBL.where("Distance From Sproul", are.below(1))
```

(e) (3 pt) Will decides to randomly pick a restaurant from the restaurants that are less than one mile from Sproul. Write code to randomly pick a restaurant from the EDDIE_CHOICE table and assigns the variable WILL_CHOICE to the name of that restaurant.

```
WILL_CHOICE = ...
```

Reminder: the columns of RESTS_TBL are "REST_NAME", "CUISTYP", "Rating", and "Distance From Sproul".

```
# Some example solutions - any are OK
WILL_CHOICE = np.random.choice(EDDIE_CHOICE.column("REST_NAME"))
WILL_CHOICE = EDDIE_CHOICE.sample().column("REST_NAME").item(0)
WILL_CHOICE = EDDIE_CHOICE.sample(1).column("REST_NAME").item(0)
```

(f) (3 pt) Write a line of code that evaluates to the number of different cuisines that appear in the "CUISTYP" column of the RESTS_TBL table.

```
RESTS_TBL.group("CUISTYP").num_rows
```

2. (10 points) Arrays and Tables

Several Data 8 staff are reserving rooms for study groups. The **rooms** table has one row per room that can potentially be reserved:

Room	Capacity	Region
110MC Kresge	10	Northside
B4 Gardner	5	Central
Warbler, 435 Moffitt	4	Central

 $(\dots 223 \text{ more rows})$

All room names are different and every room appears only once in the rooms table.

The RESEVS table has one row per reservation they have made:

STNAME	Room	DAYCOL	Time
Meghan Rita	Quail, 431 Moffitt C6 Gardner	Tuesday Monday	10 3
Margaret	110MC Kresge	Friday	12

 $(\dots 47 \text{ more rows})$

(a) (3 pt) Write a line of code that evaluates to the total capacity if we reserved every room in the rooms table.

Reminder: rooms's columns are "Room", "Capacity", and "Region". RESEVS's columns are "STNAME", "Room", "DAYCOL", and "Time".

```
sum(rooms.column("Capacity"))
```

(b) (3 pt) Write a line of code that evaluates to the number of reservations that TARGETPERSON has made.

Reminder: rooms's columns are "Room", "Capacity", and "Region". RESEVS's columns are "STNAME", "Room", "DAYCOL", and "Time".

```
RESEVS.where("STNAME", "TARGETPERSON").num_rows
```

(c) (4 pt) Write code that assigns the variable TOP_REGION to the region of campus that has the most number of reservations. Note that the "Region" column of the rooms table shows the campus region for each room.

```
TOP_REGION = ...
```

Reminder: rooms's columns are "Room", "Capacity", and "Region". RESEVS's columns are "STNAME", "Room", "DAYCOL", and "Time".

```
grouped = RESEVS.join(rooms, "Room").group("Region")
TOP_REGION = grouped.sort("count", descending=True).column("Region").item(0)
```

3. (11 points) Chances

Each morning, Noor grabs a mug from her cabinet for coffee during the day. She has 9 mugs in total: 3 each of the colors green, black, and white.

Each morning, Noor picks one mug at random from all 9 mugs regardless of the mugs she picks on other days. In each question below, pick the correct answer.

- (a) (3 pt) The weekend (Saturday and Sunday) is coming up. What is the chance that Noor picks a green mug on both those days?
 - $\bigcirc \frac{3}{9}$
 - $\bigcirc \ \frac{3}{9} + \frac{3}{9}$
- (b) (4 pt) Noor brings her mug to each Data 8 lecture. Next week, Data 8 lectures will be on Monday, Wednesday, and Friday. What is the chance that Noor brings a black mug to at least one of the three lectures?
 - $\bigcirc \frac{3}{9} + \frac{3}{9} + \frac{3}{9}$
 - $\bigcirc \ \frac{3}{9} \times \frac{3}{9} \times \frac{3}{9}$
 - $1 \left(\frac{6}{9} \times \frac{6}{9} \times \frac{6}{9}\right)$
 - $\bigcirc 1 (\frac{3}{9} \times \frac{3}{9} \times \frac{3}{9})$
- (c) (4 pt) One of Noor's classes has online office hours in the morning. She will attend the office hours on Tuesday and Thursday next week, bringing her mug with her. What is the chance that the mugs she has on those two days are the same color?
 - $\frac{3}{9}$
 - $\bigcirc \ \frac{3}{9} \times \frac{3}{9}$
 - $\bigcirc \ 1 \left(\frac{3}{9} \times \frac{6}{9}\right)$

4. (9 points) Comparing Chances

In the United States, 28% of adults use LinkedIn. Suppose you sample US adults randomly so that each sampled adult has chance 0.28 of being a LinkedIn user independently of all the others.

- (a) (2 pt) For which sample size below is there a higher chance that the percent of LinkedIn users in the sample will be at least 25%?

 200
 400

 (b) (2 pt) For which sample size below is there a higher chance that the percent of LinkedIn users in the sample will be at least 50%?

 200
 400

 (c) (2 pt) For which sample size below is there a higher chance that the percent of LinkedIn users in the sample will be at least 25% but less than 50%?

 200
 400

 (a) 200
 400

 400
- (d) (3 pt) Briefly explain your choices in Parts (a)-(c).

The Law of Averages (Chapter 10.1.4) says that the larger the sample size, the closer the proportion in the sample will be to 28%.

5. (10 points) A/B Test on Turtles

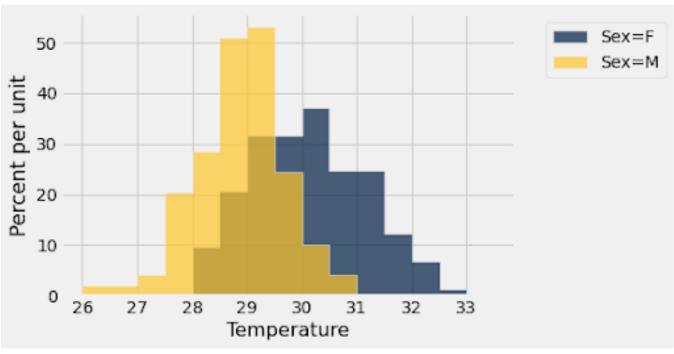
When hatching a baby turtle from an egg, we incubate the egg at some temperature. Ellen read that the temperature an egg is incubated at influences whether or not the turtle that hatches will be male or female.

Ellen loves turtles and is wondering whether this is really right, or whether differences might just be due to chance. She collects data on 100 randomly drawn turtles. She records the incubation temperature (in Celsius) and the sex of the turtle that hatches in the table turtles:

Temperature	Sex
30.8 31.5 32.4	M F
02.1	

 $(\dots 97 \text{ more rows})$

(a) (6 pt) Ellen decides to visualize her data before doing any inference. She creates the following histograms, using the same bins for female and male turtles. All bars of the histograms are clearly visible.

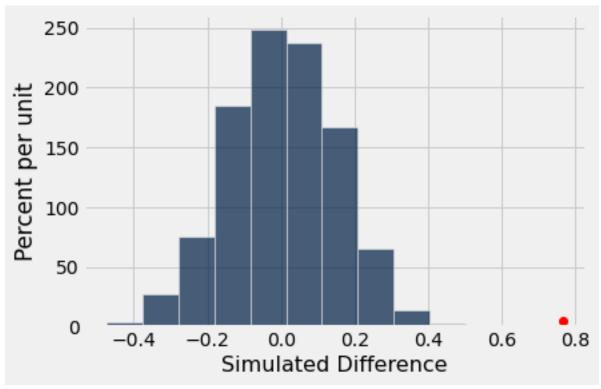


Histogram of incubation temperatures

Which of the following are conclusions that can be drawn from the histogram? Select all that apply.

- ☐ In this sample, the number of male turtles with incubation temperatures between 29.5 and 30 degrees is the same as the number of female turtles incubated between 30.5 and 31 degrees.
- In this sample, the proportion of male turtles with incubation temperatures between 29.5 and 30 degrees is the same as the proportion of female turtles incubated between 30.5 and 31 degrees.
- There was not a single male turtle in this sample incubated at a temperature above 31 degrees.
- For at least half the male turtles in the sample, the incubation temperature was below 29.5 degrees.
- In this sample, males and female turtles have different distributions of incubation temperatures.
- ☐ None of the above

(b) (4 pt) Ellen performs an A/B test to see whether females in the population in general have higher incubation temperatures than the males, or if the observed difference in distributions is due to chance. Ellen's test statistic is the difference between average incubation temperatures, defined as "female average minus male average". She simulates the statistic 1000 times under the null hypothesis. The histogram below shows the 1000 simulated differences. The red dot shows the observed difference.



Results of simulating the test statistic

Which of the following statements is justified based on this visualization?

- O Based on the test, a reasonable conclusion is that the difference observed in the sample is due to chance.
- Based on the test, a reasonable conclusion is that the average incubation temperature of females in the population is higher than the average for males in the population.
- O Based on the test, Ellen cannot reasonably decide between her two hypotheses.

6. (12 points) Testing Hypotheses

In the United States, 31% of adults report being online almost constantly. A team of data scientists took a random sample of 100 adults in San Francisco and found that 37 reported being online almost constantly.

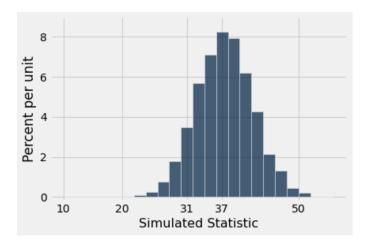
One member of the team says, "The percent of San Francisco adults who are online almost constantly is more than in the nation."

Another member of the team says, "No, it's just chance."

In order to decide between these two positions, the data scientists will conduct a test of hypotheses.

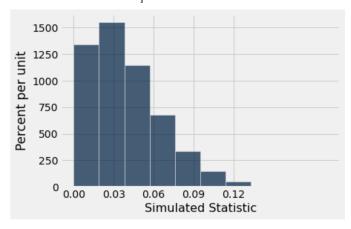
(a) (4 pt) State a clear and complete null hypothesis.

The sample of adults from San Francisco is like draws at random with replacement from individuals of whom 31% are labeled "online almost constantly."

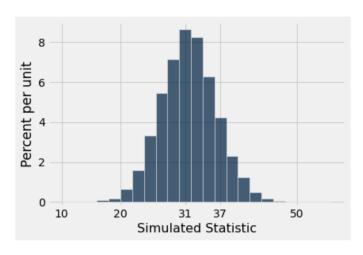


Testing Option C

(b) (3 pt) In order to decide between their two hypotheses, the data scientists have picked an appropriate test statistic and simulated it 10,000 times under appropriate conditions. One of the graphs below is the histogram of their simulated values. Which one is it, and why? [Note that in each graph, some relevant values are labeled on the horizontal axis.]



Testing Option A



Testing Option B

 \bigcirc

 \bigcirc

(c) (2 pt) Explain your choice above. One or two sentences should suffice.

The correct histogram is simulated assuming the null hypothesis is true, so the most likely value must be the value under the null. Additionally, it must contain values both above and below this peak, because the alternative is directional. Option B is the only graph that satisfies both properties. ALTERNATIVELY Option A is wrong because absolute value does not allow us to determine whether the proportion in the sample is greater or less than the proportion in the population. Option C is wrong because it is not simulated under the null - we can tell because it is centered at 37.

(d) (3 pt) The 10,000 simulated values of the data scientists' test statistic are in an array called SIM_STAT_ARR. Write an expression that evaluates to the p-value of the test.

np.count_nonzero(SIM_STAT_ARR >= 37) / 10000

7. (8 points) A/B Testing on News

Each person in a random sample of 1000 U.S. adults was asked if they agreed with the statement, "News organizations are growing in influence." Among the sampled men, 39% agreed. Among the sampled women, 43% agreed.

Data scientists have used an A/B test to see whether or not the observed difference is due to chance.

(a)	(3 pt) The null hypothesis is one of the statements below. Pick the right one.
	O In the sample, the percent of women who agree is the same as the percent of men who agree. The observed difference is due to chance.
	\bigcirc In the U.S., 39% of the men agree and 43% of the women agree, due to chance.
	• In the U.S., the percent of men who agree is the same as the percent of women who agree. The difference in the sample is due to chance.
	O In the U.S., the percent of women who agree is different from the percent of men who agree, due to chance.
(b)	(5 pt) The data scientists are using a 1% cutoff for the p-value of the test. They run the test and the p-value comes out to be 0.5%, that is, 1 in 200.
	Select all of the true statements below. Only one may be true, or more. Make sure you select all that are true.
	\square The data scientists will conclude that the data are consistent with the null hypothesis.
	\square There is only a 1 in 200 chance that the null hypothesis is true.
	☐ There is a 199 in 200 chance that the alternative hypothesis is true.
	The data scientists will reject the null hypothesis.
	The assumptions made in the null hypothesis are used in the calculation of the p-value.
	☐ None of the above statements is true.

8. (14 points) Simulation

The table WELCOME_TBL contains the results of this semester's Data 8 welcome survey. The first two rows are shown below. Each row corresponds to a student. In the column Extraversion, each student scored themselves on a scale of 1 (not extraverted) to 10 (extremely extraverted).

Year	Extraversion	Number of Textees	Hours of Sleep	Handedness	First Pant Leg	Sleep Position
Second	8	5	6	Right- handed	Right	Left
Second	7	8	7.5	Right- handed	Right	Left

 $(\dots 1000 \text{ rows omitted})$

(a) (4 pt) Complete the code below to define a function FUN_NAME that takes a sample size as its argument. The function should sample that many times at random without replacement from all the students and return the maximum extraversion score of the sampled students.

```
def FUN_NAME(...):
    ...
    def FUN_NAME(sample_size):
        samp = WELCOME_TBL.sample(sample_size, with_replacement=False)
        return max(samp.column("Extraversion"))
```

(b) (5 pt) Complete the code below so that the last line evaluates to an array of 10,000 simulated values of the maximum extraversion score in a random sample of size 25 drawn without replacement from all the students. Your code should use the function FUN_NAME that you defined above.

```
repetitions = ...

SIM_VALS = ...

for ... in ...:
...
```

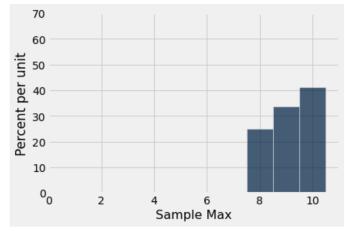
SIM_VALS

```
repetitions = 10000
SIM_VALS = make_array()

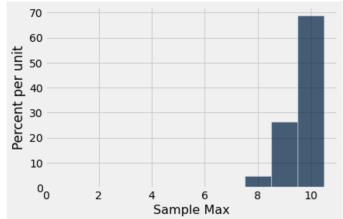
for i in np.arange(repetitions):
    one_sim_max = FUN_NAME(25)
    SIM_VALS = np.append(SIM_VALS, one_sim_max)

SIM_VALS
```

(c) (3 pt) A student mistypes the sample size in the previous question to be 55 instead of 25. One of the histograms below shows the distribution of the maximum values simulated by this student. The other shows the distribution of the maximum values that you simulated using a sample size of 25. Which is which?



A:



- В:
- A is sample of 25, B is sample of 55
- A is sample of 55, B is sample of 25
- (d) (2 pt) Explain your answer above.

The probability of containing 10 (the population maximum) in a given sample is larger for a larger sample size.

9. (8 points) Interpreting Visualizations

A medical institute that specializes in sports medicine has recorded data on athletes with leg injuries. The variables are the distance that the athlete achieved in a test called the triple hop, and how high the athlete could jump vertically. Both distances were measured in centimeters.

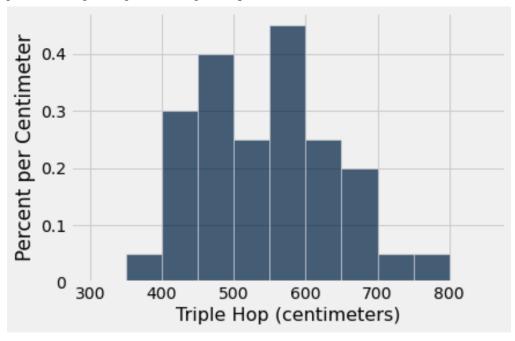
The data are in a table called jump that has columns labeled Triple Hop and Vertical.

Triple Hop	Vertical
443	59
481	62

 $(\dots 86 \text{ more rows})$

(a) (3 pt) The histogram below shows the distribution of the triple hop distances, drawn using the following code.

jump.hist('Triple Hop', bins=np.arange(300, 900, 50))

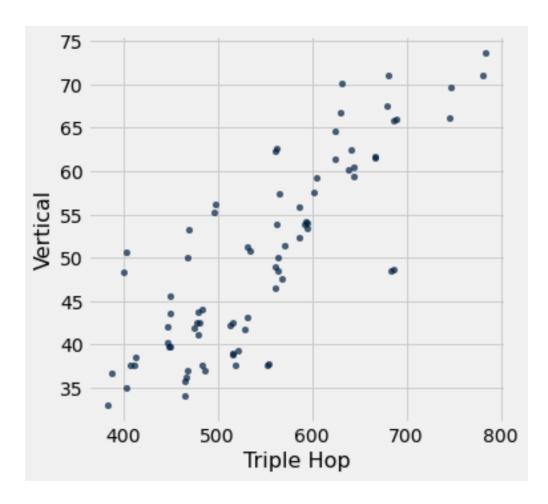


Histogram of triple hop distances

Complete the sentence with the correct option.

The percent of athletes whose triple hop distances were at least 400 centimeters but less than 500 centimeters is equal to

- \bigcirc 0.7%
- O 7%
- 30%
- 35%
- \bigcirc 40%
- some value that is none of the above or cannot be computed based on the information given



Scatter plot of athlete data

(b)	5 pt) The scatter plot below has a point for each of the athletes. Pick all the conclusions that can be cawn from the scatter plot. Make sure you pick all that apply.
	More than half the athletes jumped less than 60 centimeters vertically.
	Most of the athletes whose triple hop distances were longer than average also jumped higher than average.
	If athletes were to increase their triple hop distances then they would be able to jump higher.
	If athletes were to increase the heights of their vertical jumps, they would be able to triple hop longer distances.
	None of the above conclusions can be drawn from the scatter plot.

10. (0 points) Final Words

No more questions.