



# Lecture 24

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Interpreting Confidence

# **Announcements**

# Estimation

# Inference: Estimation

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- **Parameter**: Fixed quantity in the population
  - How can we figure out the value of an unknown parameter?
  - If you don't have a census:
    - Take a random sample from the population
    - Use a statistic as an **estimate** of the parameter
  - One sample → One estimate
  - But the random sample could have come out differently
  - And so the estimate could have been different
  - We need to know how different it could have been
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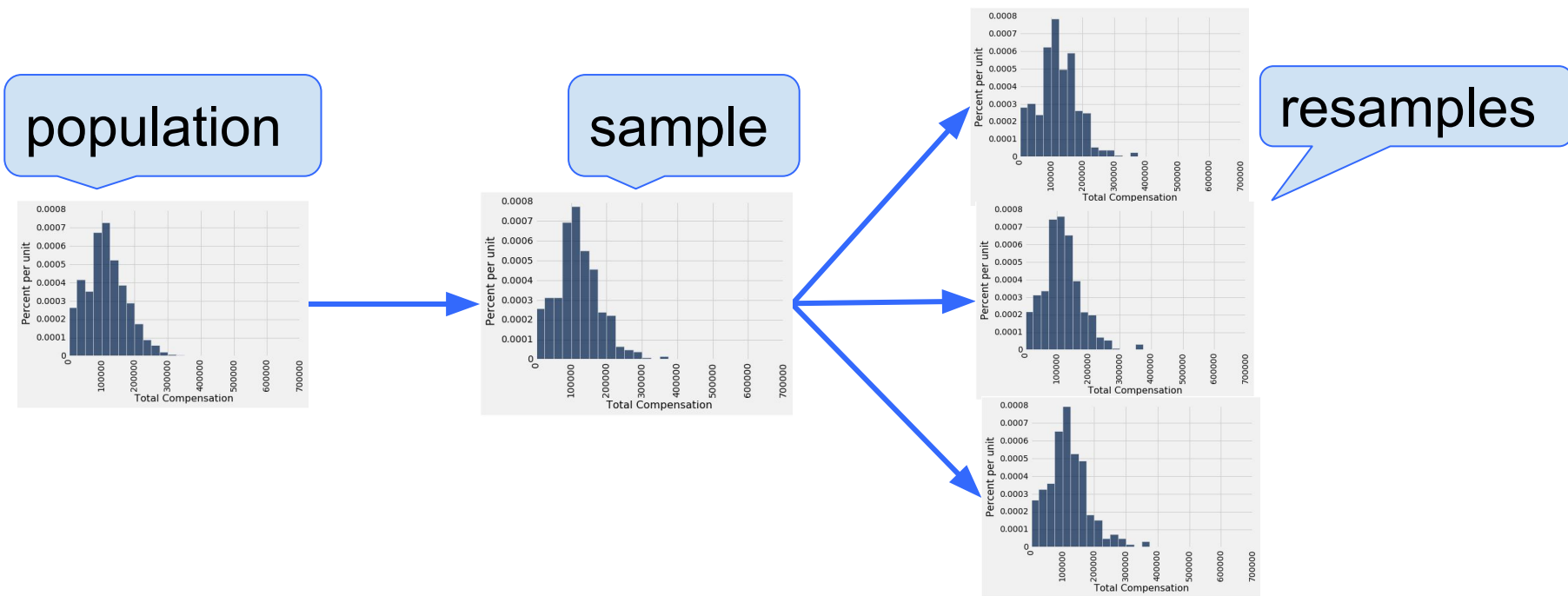
# Where to Get Another Sample?

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- We want to understand variability of our estimate
  - We only have the **sample**
  - To get many values of the estimate, we need many random samples
  - We can't go back and sample again from the population
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# The Bootstrap

# Why the Bootstrap Works



All of these look pretty similar, most likely.

# Key to Resampling

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- From the original sample,
  - draw at random
  - with replacement
  - as many values as the original sample contained
- The size of the new sample has to be the same as the original one, so that the two estimates are comparable

(Demo)

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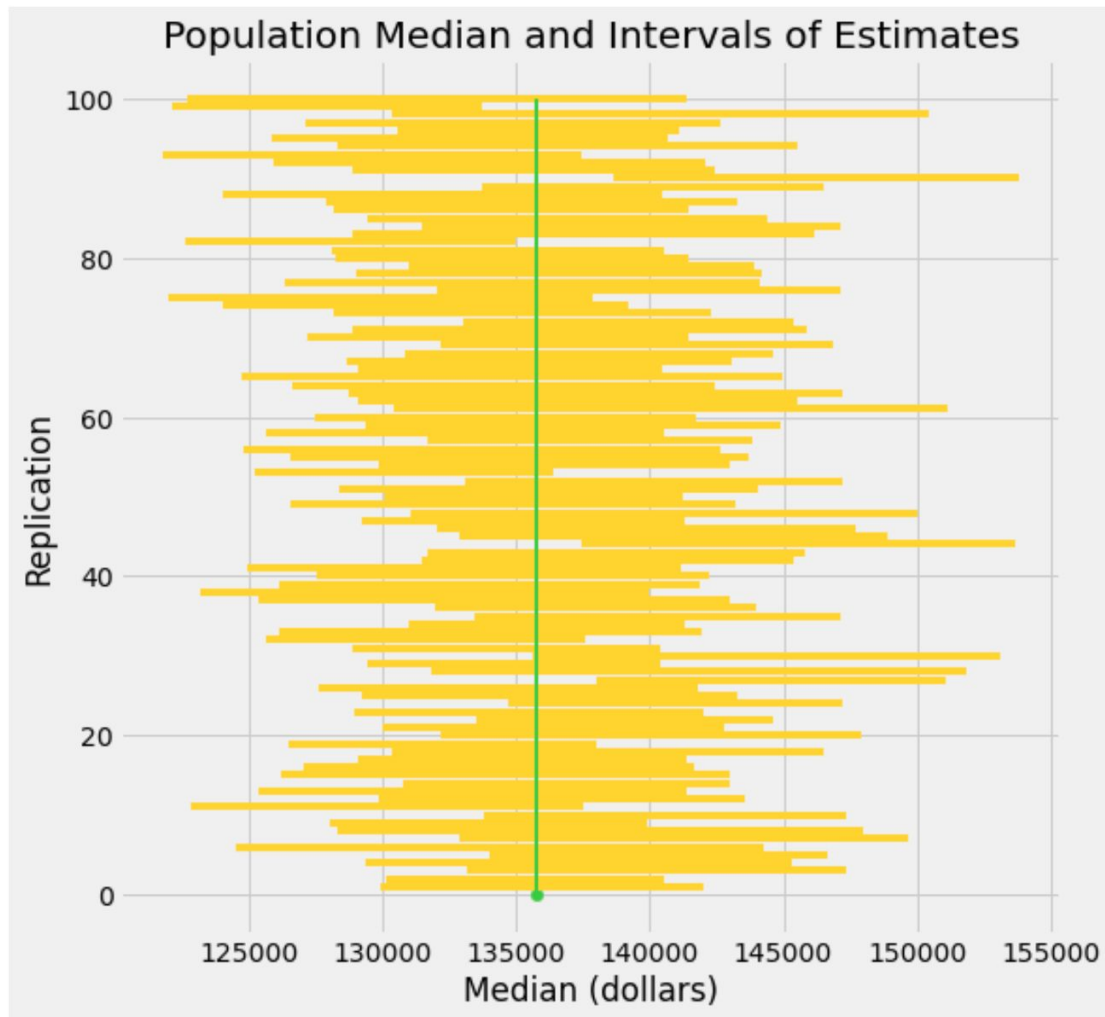


# Confidence Intervals

# 95% Confidence Interval

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- Interval of **estimates of a parameter**
  - Based on random sampling
  - 95% is called the confidence level
    - Could be any percent between 0 and 100
    - Higher level means wider intervals
  - A “good” interval is one that contains the parameter
  - The **confidence is in the process** that creates the interval:
    - It generates a “good” interval about 95% of the time.  
(Demo)
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## The Meaning of 95% confidence

The green dot is the parameter. It is fixed.

Each yellow line is a 95% confidence interval based on a fresh sample from the population

There are 100 intervals. 95 of them contain the parameter.

**Use Methods Appropriately**

# When *Not* to Use Our Bootstrap Method

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- If you're trying to estimate any parameter that's greatly affected by rare elements of the population
  - Very high or very low percentiles, or min and max
- If the probability distribution of your statistic is not roughly bell shaped (the shape of the empirical distribution will be a clue)
- If the original sample is very small

(Demo)

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# Can You Use a CI Like This?

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By our calculation, an approximate 95% confidence interval for the average age of the mothers in the population is (26.9, 27.6) years.

## True or False:

- About 95% of the mothers in the population were between 26.9 years and 27.6 years old.

**Answer: False.** We're estimating that their **average age** is in this interval.

(Demo)

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# Is This What a CI Means?

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An approximate 95% confidence interval for the average age of the mothers in the population is (26.9, 27.6) years.

## True or False:

- There is a 0.95 probability that the average age of mothers in the population is in the range 26.9 to 27.6 years.

**Answer: False.** The parameter is fixed, and the interval (26.9, 27.2) is fixed. The parameter is either in that interval, or not. Once you've picked an interval, there's no probability involved.

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# 95% Confidence

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- Interval of estimates of a parameter
  - Based on random sampling
  - The process results in a random interval
  - A “good” interval is one that contains the parameter
  - The **confidence is in the process** that creates the interval:
    - It generates a “good” interval with chance 95%
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# Confidence Intervals For Testing

# Using a CI for Testing

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- Null hypothesis: **Population average =  $x$**
  - Alternative hypothesis: **Population average  $\neq x$**
  - Cutoff for p-value:  $p\%$
  - Method:
    - Construct a  $(100-p)\%$  confidence interval for the population average
    - If  $x$  is not in the interval, reject the null
    - If  $x$  is in the interval, can't reject the null
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