Error localization

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Error localization

Data validation and error localization answer different questions.

Data validation

Which errors are there?

Error localization

Where do I need to make changes to fix the errors?





Example

Ruleset

```
age >= 0
age <= 120
if (drivers_licence == TRUE) age >= 18
```

Data

```
age drivers_licence
```

Question:





Error localization

Definition

Error localization is a procedure that points out fields in a data set that can be altered or imputed in such a way that all validation rules can be satisfied.





Example

Ruleset

```
if (married == TRUE ) age >= 16
if (attends == "kindergarten") age <= 6</pre>
```

Data

age	married	attends
3	TRUE	kindergarten

Question





Principle of Fellegi and Holt

Find the minimal (weighted) number of fields to adjust such that all rules, including implied rules, can be satisfied.

IP Fellegi and D Holt, JASA **71** 353 17–35 (1976).

Note

This should be used as a last resort, when no further information on the location of errors is available.





Implied rules?

This implies (substituting profit):

```
total.cost >= 0.4 * turnover
```

We need to take into account such *essentially new* rules (edits) —unstated relations between variables that can be derived from the explicitly defined rules.



Error localization is a set covering problem

Given a record $\mathbf{x} = (x_1, \dots, x_n)$, restricted by a set of explicit and implicit validation rules. Minimize the sum

$$\sum_{j\in S} w_j, \ w_j > 0,$$

Where $S \subseteq \{1, ..., n\}$ such that all (explicit and implicit) validation rules can be satisfied by replacing $x_i, j \in S$ with new values.

Algorithms: De Waal et al (2011), John Wiley & Sons.





Solution types

(1) Feasible solution

Any set of variables that can be altered so that all rules, including implied ones can be satisfied. Example: change every variable.

(2) Feasible solution of minimal size

A set of variables that is a feasible solution and as small as possible.

(3) Feasible solution of minimal weight

A set of variables that is a feasible solution and minimizes the total weight.





Choosing weights

All weights equal (usually to one)

Least nr of variables adapted. In case of multiple solutions: choose randomly (e.g. by adding a small random perturbation to the weights).

Weights represent reliability

Heigher weight \rightarrow variable is less likely chosen.

- Can be made to depend on 'outlierness', or expert judgement.
- Possible problem: minimal weights vs minimal nr of variables?





Choosing weights

Question

Is it possible to choose a set of weights, such that

- 1. The smallest number of variables is chosen
- 2. The weights are minimized

Intuition

If the weights do not differ too much, no extra variables will be introduced on top of the variables in a feasible solution of of minimal size.



Proposition

Given a set of weights $\mathbf{w} = (w_1, \dots, w_n)$ and write

$$w_j = 1 + \delta_j$$
 with $0 \le \delta_j \le \delta^{max}$.

If $\delta^{max} < 1/(n-1)$ then a feasible solution of minimal weight is a feasible solution of minimal size.

Proof: van der Loo (2015) Rom. Stat. Rev. 2 141–152; SDCR §7.5





Scaling rule

Given set of n weights $\mathbf{w} = \mathbf{1} + \delta$. Then the following rescaling ensures that a solution of minimal weight also a solution of minimal size.

$$w_j' = 1 + rac{w_j - w^{min}}{w^{max} - w^{min}} imes rac{1}{n}$$

Procedure

- 1. Determine reliability weights (outlierness, expert judgement...)
- 2. Apply scaling rule



