### Lecture 4: Predictive Modeling

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In some scenarios we may be interested in building a statistical model to predict an outcome. In this case, for instance, we may want to use different models to predict the location of a firm. The Compustat data entail US and Canadian enterprises. In the next chunks of code I will build five different models (logistic regression, CART, Conditional Inference Tree, Random Forest, Bayesian Additive Regression Trees) to predict the location of the firm.

Moreover, I will provide details on the most widely used performance measures in the case of a classification problem.

```
library(readxl)
library(caret)
## Loading required package: lattice
## Loading required package: ggplot2
library(randomForest)
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
## Attaching package: 'randomForest'
## The following object is masked from 'package:ggplot2':
##
##
       margin
library(bartMachine)
## Loading required package: rJava
## Loading required package: bartMachineJARs
## Loading required package: car
## Loading required package: carData
## Loading required package: missForest
## Loading required package: foreach
## Loading required package: itertools
## Loading required package: iterators
## Welcome to bartMachine v1.2.3! You have 0.48GB memory available.
## If you run out of memory, restart R, and use e.g.
## 'options(java.parameters = "-Xmx5g")' for 5GB of RAM before you call
```

```
## 'library(bartMachine)'.
library(PRROC)
library(rpart)
library(party)
## Loading required package: grid
## Loading required package: mvtnorm
## Loading required package: modeltools
## Loading required package: stats4
##
## Attaching package: 'modeltools'
## The following object is masked from 'package:car':
##
##
       Predict
  The following object is masked from 'package:rJava':
##
##
##
       clone
## Loading required package: strucchange
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
## Loading required package: sandwich
```

First things first, let's upload the Compustat data and perform a naive trimming of the data, excluding all the missing observations.

Before running the analyses, I restict the set of predictors to the following variables and I create a dummy variable that assumes value 1 if the firm is located in the US and 0 if it is located in Canada.

In order to check how good are the five models, I randomly split the data into two disjoint sets: a training set that I will use to build the model and a test set that I will use to validate the quality of the model's

prediction.

Moreover, I am renaming the variables in the dataset and constructing the "formula" that I will use for all the predictive models that I will run.

```
colnames(train) <- c("assets", "short term borrow",</pre>
                      "current_assets", "debt",
                      "debt liabilities", "employees",
                      "EBIT", "liabilities",
                      "net_income", "r_d",
                      "gic", "SICC", "iso_code")
colnames(test) <- c("assets", "short_term_borrow",</pre>
                      "current_assets", "debt",
                      "debt_liabilities", "employees",
                      "EBIT", "liabilities",
                      "net_income", "r_d",
                      "gic", "SICC", "iso_code")
predictors <- c("assets", "short_term_borrow",</pre>
                      "current_assets", "debt",
                      "debt_liabilities", "employees",
                      "EBIT", "liabilities",
                      "net_income", "r_d",
                      "gic", "SICC")
formula <- as.formula(paste("as.factor(iso_code) ~",</pre>
                             paste(predictors, collapse="+")))
formula
## as.factor(iso_code) ~ assets + short_term_borrow + current_assets +
       debt + debt_liabilities + employees + EBIT + liabilities +
##
       net_income + r_d + gic + SICC
```

#### Logistic Regression

The first model that I run is a logistic regression with the inclusion of all the covariates.

```
logit<-glm(formula, data= train, family=binomial(link='logit'))</pre>
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
summary(logit)
##
## Call:
## glm(formula = formula, family = binomial(link = "logit"), data = train)
##
## Deviance Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -1.4832 -0.4930 -0.3027 -0.1754
                                        3.1015
##
```

```
## Coefficients:
##
                     Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                     8.663e-01 1.508e-01 5.743 9.29e-09 ***
                     4.599e-04 3.459e-04
                                           1.330 0.183633
## assets
## short_term_borrow -1.684e-02 9.810e-03 -1.716 0.086105 .
## current assets
                    -2.555e-03 7.378e-04 -3.463 0.000535 ***
## debt
                    -6.835e-03 6.994e-03 -0.977 0.328398
## debt_liabilities 1.073e-02 6.779e-03
                                         1.582 0.113545
## employees
                    -4.996e-02 3.530e-02 -1.415 0.156980
## EBIT
                     2.414e-03 2.280e-03 1.059 0.289682
## liabilities
                    -8.082e-04 6.295e-04 -1.284 0.199163
## net_income
                    -4.237e-04
                               2.352e-03 -0.180 0.857055
## r_d
                    1.391e+02 5.892e+03
                                          0.024 0.981162
## gic
                    -4.632e-02 6.250e-03 -7.411 1.26e-13 ***
## SICC
                    -3.329e-04 3.724e-05 -8.938 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 2140.2 on 2869
                                     degrees of freedom
## Residual deviance: 1669.4 on 2857
                                     degrees of freedom
## AIC: 1695.4
## Number of Fisher Scoring iterations: 25
```

To get the accuracy of the model I first get the predicted probabilities, then impute the values for the outcome variable.

```
# Accurancy from cv
fitted.results.logit <- predict(logit, newdata = test, type='response')
fitted.logit <- ifelse(fitted.results.logit >= 0.5, 1, 0)
head(fitted.logit)
```

```
## 1 2 3 4 5 6
## 0 0 0 0 0 0
```

Once I get the predicted (or fitted values) for this model, I can evaluate its performance using a number of different performance measures. Below the functions to compute the F-1 Score and the Balanced Accuracy.

```
## F1- Score
# predicted: vector of predicted values
# expected: vector of observed value
# positive.class: class of binary predictions we are mostly interested in (e.g., "1", "0")

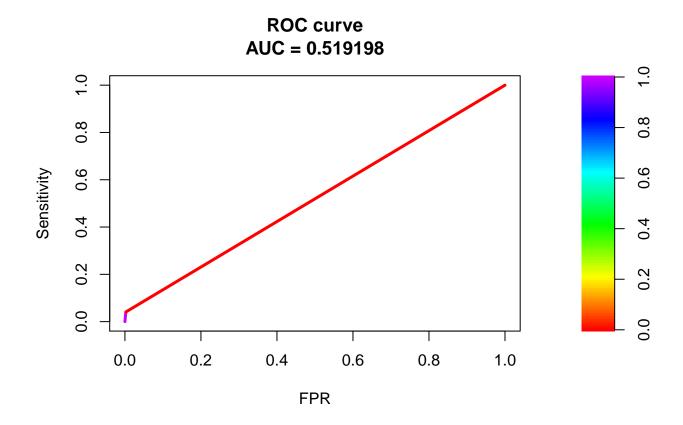
f1_score <- function(predicted, expected, positive.class) {
    # Generate Confusion Matrix
    c.matrix = as.matrix(table(expected, predicted))

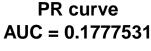
# Compute Precision
precision <- diag(c.matrix) / colSums(c.matrix)

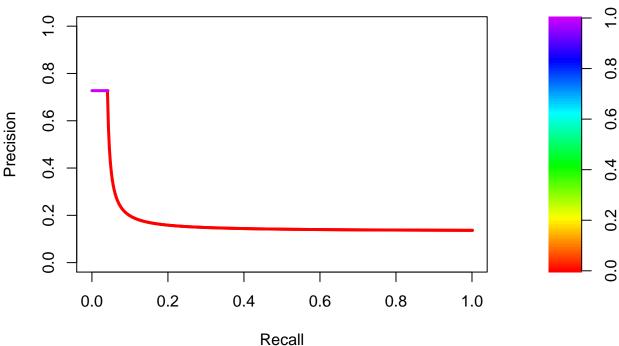
# Compute Recall
recall <- diag(c.matrix) / rowSums(c.matrix)</pre>
```

```
# Compute F-1 Score
  f1 <- ifelse(precision + recall == 0, 0, 2*precision*recall/(precision + recall))
  # Extract F1-score for the pre-defined "positive class"
  f1 <- f1[positive.class]</pre>
  # Assuming that F1 is zero when it's not possible compute it
 f1[is.na(f1)] <- 0
  # Return F1-score
 return(f1)
}
## Balanced Accuracy (BACC)
# predicted: vector of predicted values
# expected: vector of observed value
balanced_accuracy <- function(predicted, expected) {</pre>
  # Generate Confusion Matrix
  c.matrix = as.matrix(table(predicted, expected))
  # First Row Generation
 first.row <- c.matrix[1,1] / (c.matrix[1,1] + c.matrix[1,2])</pre>
  # Second Row Generation
  second.row \leftarrow c.matrix[2,2] / (c.matrix[2,1] + c.matrix[2,2])
  # # "Balanced" proportion correct (you can use different weighting if needed)
 acc <- (first.row + second.row)/2</pre>
  # Return Balanced Accuracy
  return(acc)
}
# RMSE
caret::postResample(fitted.logit, test$iso_code)
         RMSE
##
                Rsquared
                                 MAF
## 0.36476662 0.02285701 0.13305468
# For good predictive model the MAE and RMSE values should be low
# Confusion Matrix
confusionMatrix(data = as.factor(fitted.logit),
                reference = as.factor(test$iso_code))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
               0
            0 2473 376
##
##
            1
                6 16
##
```

```
##
                   Accuracy : 0.8669
                     95% CI: (0.854, 0.8792)
##
       No Information Rate: 0.8635
##
       P-Value [Acc > NIR] : 0.3045
##
##
##
                      Kappa: 0.0637
##
    Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.99758
##
##
               Specificity: 0.04082
            Pos Pred Value: 0.86802
##
            Neg Pred Value: 0.72727
##
##
                Prevalence: 0.86346
##
            Detection Rate: 0.86137
##
      Detection Prevalence: 0.99234
##
         Balanced Accuracy: 0.51920
##
          'Positive' Class : 0
##
##
# Balanced Accuracy
balanced_accuracy_logit<-balanced_accuracy(fitted.logit, test$iso_code)
balanced_accuracy_logit
## [1] 0.7976483
# F1-Score
f1_logit_1 <- f1_score(fitted.logit,</pre>
                      test$iso_code,
                      positive.class="1")
f1_logit_1
## 0.07729469
f1_logit_0 <- f1_score(fitted.logit,</pre>
                      test$iso_code,
                      positive.class="0")
f1_logit_0
##
## 0.9283033
# ROC Curve and PR- Curve
fg.logit <- fitted.logit[test$iso_code==1]</pre>
bg.logit <- fitted.logit[test$iso_code==0]</pre>
roc_logit <- roc.curve(scores.class0 = fg.logit,</pre>
                        scores.class1 = bg.logit,
                        curve = T)
plot(roc_logit)
```





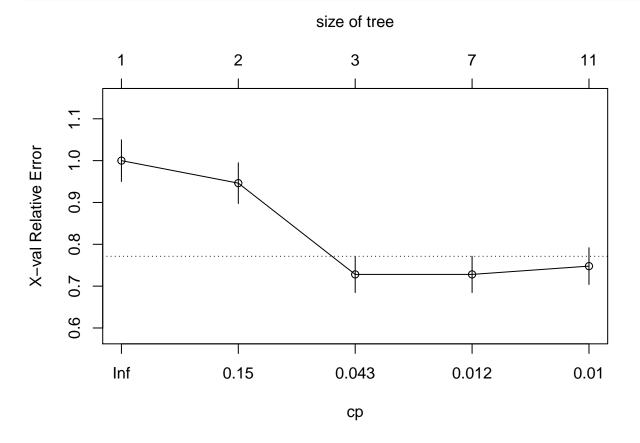


#### Classification and Regression Tree

The second model that I run is a classification and regression tree from the "rpart" package in R.

```
rpart <- rpart(formula, data=train, method="class")</pre>
printcp(rpart) # display the results
## Classification tree:
## rpart(formula = formula, data = train, method = "class")
## Variables actually used in tree construction:
## [1] assets
                        current_assets
                                          debt_liabilities EBIT
## [5] gic
                        liabilities
                                          SICC
##
## Root node error: 353/2870 = 0.123
##
## n= 2870
##
##
           CP nsplit rel error xerror
## 1 0.158640
                       1.00000 1.00000 0.049844
## 2 0.133144
                   1
                       0.84136 0.94618 0.048667
## 3 0.014164
                   2
                       0.70822 0.72805 0.043333
## 4 0.010387
                   6
                       0.65156 0.72805 0.043333
## 5 0.010000
                  10
                       0.60907 0.74788 0.043860
```

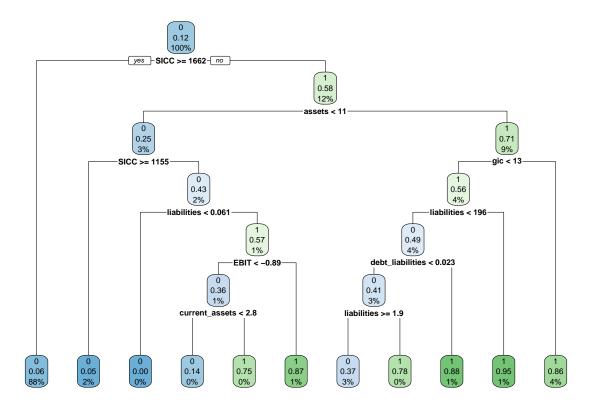
#### plotcp(rpart) # visualize cross-validation results



#### # summary(rpart) # detailed summary of splits

You can depict the classification tree by using the "plot()" function.

#Plot tree
rpart.plot::rpart.plot(rpart)

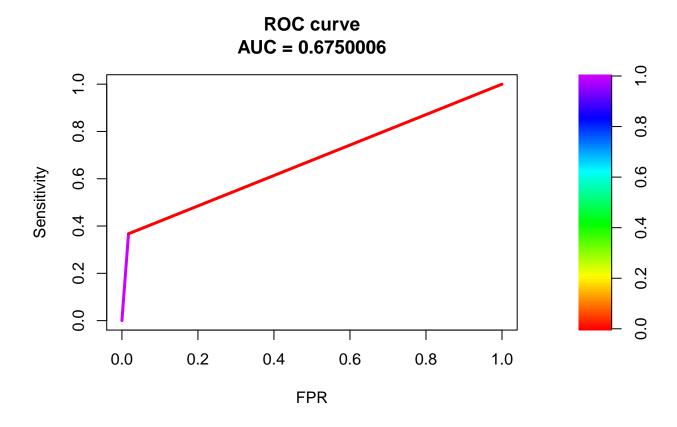


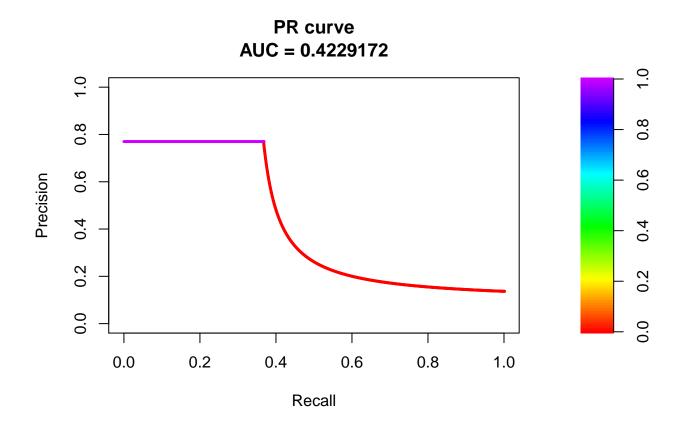
To get the accuracy of the model I first get the predicted probabilities, then impute the values for the outcome variable.

```
fitted.results.rpart <- predict(rpart, newdata=test,type='prob')
fitted.rpart <- ifelse(fitted.results.rpart[,2] >= 0.5, 1, 0)
```

```
Below, I depict the predictive performance of the model.
# RMSE
caret::postResample(fitted.rpart, test$iso_code)
##
        RMSE Rsquared
                              MAE
## 0.3183684 0.2371798 0.1013584
# For good predictive model the MAE and RMSE values should be low
# Confusion Matrix
confusionMatrix(data = as.factor(fitted.rpart),
                 reference = as.factor(test$iso_code))
##
   Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                 0
                       1
##
            0 2436
                    248
                 43
                    144
##
##
                   Accuracy : 0.8986
##
```

```
95% CI: (0.887, 0.9094)
##
       No Information Rate: 0.8635
##
       P-Value [Acc > NIR] : 6.802e-09
##
##
##
                      Kappa: 0.4488
##
##
    Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.9827
               Specificity: 0.3673
##
##
            Pos Pred Value: 0.9076
##
            Neg Pred Value: 0.7701
                Prevalence: 0.8635
##
            Detection Rate: 0.8485
##
##
      Detection Prevalence: 0.9349
##
         Balanced Accuracy: 0.6750
##
          'Positive' Class : 0
##
# Balanced Accuracy
balanced_accuracy_rpart<-balanced_accuracy(fitted.rpart, test$iso_code)
balanced_accuracy_rpart
## [1] 0.838827
# F1-Score
f1_rpart_1 <- f1_score(fitted.rpart,</pre>
                        test$iso_code,
                        positive.class="1")
f1_rpart_1
## 0.4974093
f1_rpart_0 <- f1_score(fitted.rpart,</pre>
                        test$iso_code,
                        positive.class="0")
f1_rpart_0
## 0.9436374
# ROC Curve and PR- Curve
fg.rpart <- fitted.rpart[test$iso_code==1]</pre>
bg.rpart <- fitted.rpart[test$iso_code==0]</pre>
roc_rpart <- roc.curve(scores.class0 = fg.rpart,</pre>
                        scores.class1 = bg.rpart,
                        curve = T)
plot(roc_rpart)
```



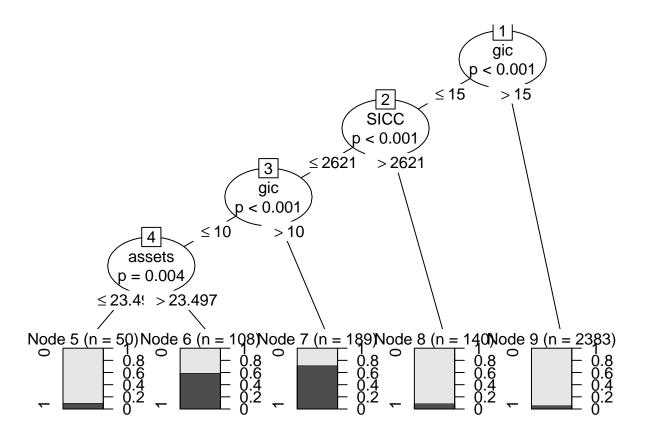


#### Conditional Inference Tree

One potential drawback of the classification and regression trees

You can plot the tree by running the following chunk of code.

```
plot(c.tree, gp = gpar(fontsize = 6))
```



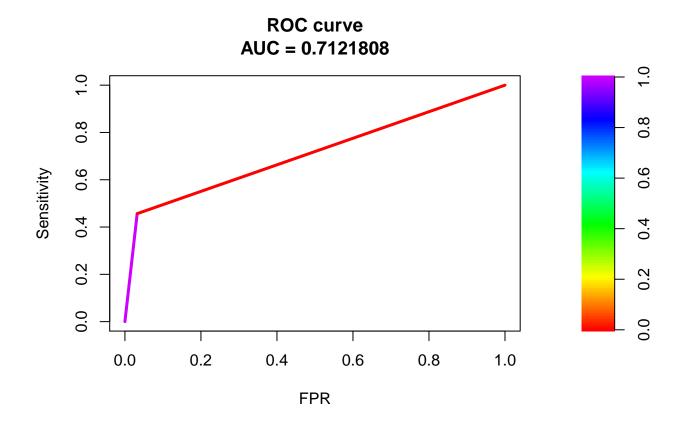
To get the accuracy of the model I first get the predicted probabilities, then impute the values for the outcome variable.

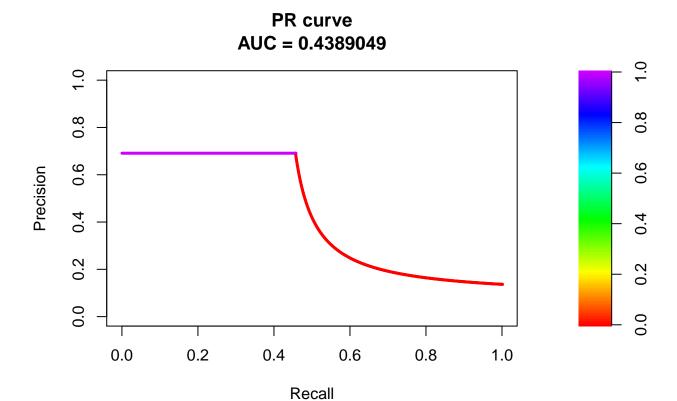
```
fitted.results.tree <- as.matrix(unlist(predict(c.tree,</pre>
                                  newdata = test, type='prob')))
fitted.prob.tree <- fitted.results.tree[seq_along(fitted.results.tree) %%2 == 0]
fitted.tree <- ifelse(fitted.prob.tree >= 0.5, 1, 0)
Below, I depict the predictive performance of the model.
# RMSE
caret::postResample(fitted.tree, test$iso_code)
        RMSE Rsquared
## 0.3194605 0.2586794 0.1020550
# For good predictive model the MAE and RMSE values should be low
# Confusion Matrix
confusionMatrix(data = as.factor(fitted.tree),
                reference = as.factor(test$iso_code))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                 0
                       1
            0 2399
                    213
```

##

80 179

```
##
##
                   Accuracy : 0.8979
##
                     95% CI: (0.8863, 0.9088)
##
       No Information Rate: 0.8635
##
       P-Value [Acc > NIR] : 1.347e-08
##
##
                      Kappa: 0.4951
##
##
    Mcnemar's Test P-Value: 1.243e-14
##
##
               Sensitivity: 0.9677
##
               Specificity: 0.4566
            Pos Pred Value: 0.9185
##
##
            Neg Pred Value: 0.6911
##
                Prevalence: 0.8635
##
            Detection Rate: 0.8356
##
      Detection Prevalence: 0.9098
##
         Balanced Accuracy: 0.7122
##
          'Positive' Class: 0
##
##
# Balanced Accuracy
balanced_accuracy_tree<-balanced_accuracy(fitted.tree, test$iso_code)
balanced_accuracy_tree
## [1] 0.8047865
# F1-Score
f1_tree_1 <- f1_score(fitted.tree,</pre>
                        test$iso_code,
                        positive.class="1")
f1_tree_1
## 0.5499232
f1_tree_0 <- f1_score(fitted.tree,</pre>
                        test$iso_code,
                        positive.class="0")
f1_tree_0
##
## 0.9424475
# ROC Curve and PR- Curve
fg.tree <- fitted.tree[test$iso_code==1]</pre>
bg.tree <- fitted.tree[test$iso_code==0]</pre>
roc_tree <- roc.curve(scores.class0 = fg.tree,</pre>
                        scores.class1 = bg.tree,
                        curve = T)
plot(roc_tree)
```



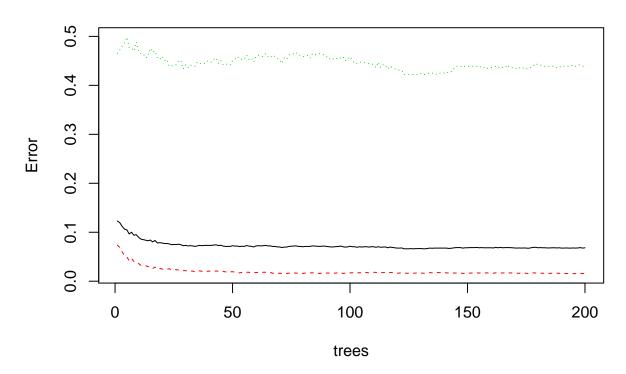


#### **Random Forest**

The last model that I build is a random forest from the "randomForest" package.

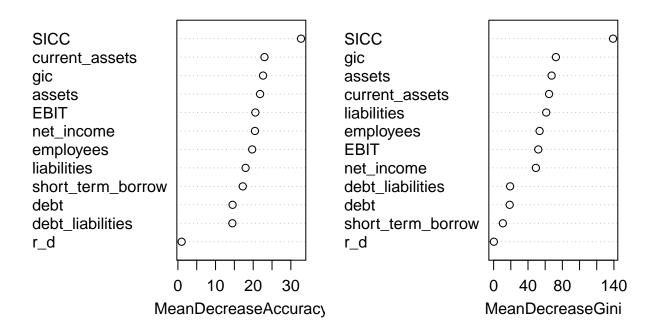
```
set.seed(133234)
rf <- randomForest(formula, data=train, importance=TRUE, ntree=200)</pre>
print(rf)
##
## Call:
##
   randomForest(formula = formula, data = train, importance = TRUE,
                                                                           ntree = 200)
##
                  Type of random forest: classification
##
                        Number of trees: 200
## No. of variables tried at each split: 3
##
##
           OOB estimate of error rate: 6.83%
## Confusion matrix:
##
        0
            1 class.error
## 0 2476 41 0.01628923
## 1 155 198 0.43909348
plot(rf)
```





varImpPlot(rf)

rf



To get the accuracy of the model I first get the predicted probabilities, then impute the values for the outcome variable.

```
fitted.rf <- predict(rf, test)</pre>
fitted.rf <- as.numeric(matrix(fitted.rf))</pre>
Below, I depict the predictive performance of the model.
# RMSE
caret::postResample(fitted.rf, test$iso_code)
                 Rsquared
## 0.28852427 0.36034498 0.08324626
# For good predictive model the MAE and RMSE values should be low
# Confusion Matrix
confusionMatrix(data = as.factor(fitted.rf),
                 reference = as.factor(test$iso_code))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                  0
                    195
##
            0 2435
```

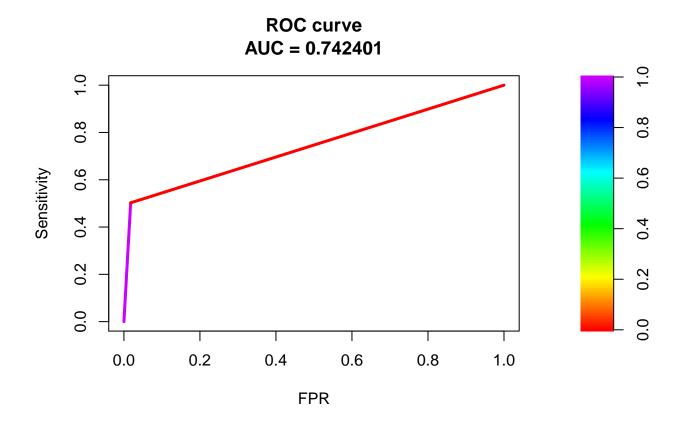
##

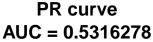
## ## 44

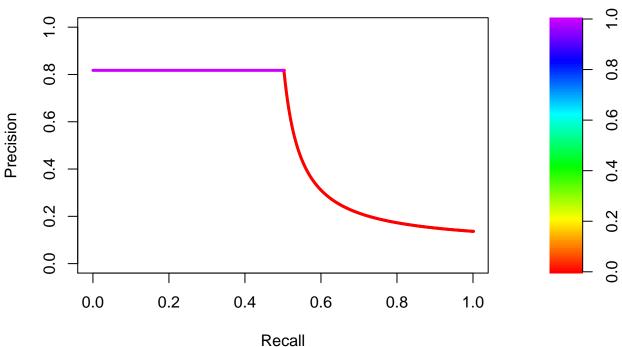
197

Accuracy: 0.9168

```
95% CI: (0.906, 0.9266)
##
       No Information Rate: 0.8635
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                      Kappa: 0.5786
##
##
    Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.9823
##
               Specificity: 0.5026
##
            Pos Pred Value: 0.9259
            Neg Pred Value: 0.8174
##
                 Prevalence: 0.8635
##
##
            Detection Rate: 0.8481
##
      Detection Prevalence: 0.9161
##
         Balanced Accuracy: 0.7424
##
          'Positive' Class : 0
##
# Balanced Accuracy
balanced_accuracy_rf<-balanced_accuracy(fitted.rf, test$iso_code)</pre>
balanced_accuracy_rf
## [1] 0.8716414
# F1-Score
f1_rf_1 <- f1_score(fitted.rf,</pre>
                        test$iso_code,
                        positive.class="1")
f1_rf_1
## 0.6224329
f1_rf_0 <- f1_score(fitted.rf,</pre>
                        test$iso_code,
                        positive.class="0")
f1_rf_0
## 0.9532198
# ROC Curve and PR- Curve
fg.rf <- fitted.rf[test$iso_code==1]</pre>
bg.rf <- fitted.rf[test$iso_code==0]</pre>
roc_rf <- roc.curve(scores.class0 = fg.rf,</pre>
                        scores.class1 = bg.rf,
                        curve = T)
plot(roc_rf)
```





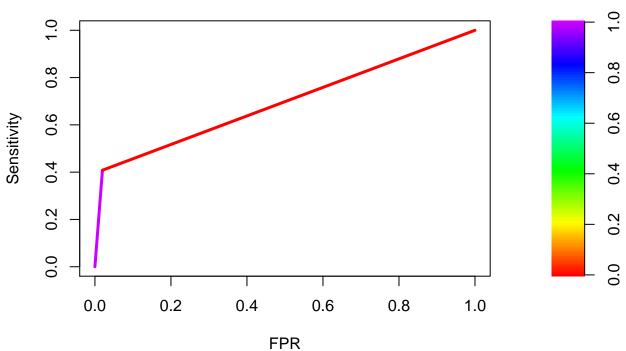


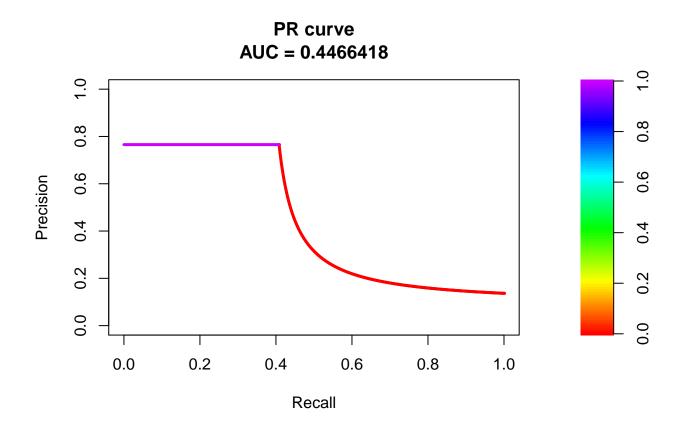
#### Bayesian Forest (Bayesian Additive Regression Trees)

To get the accuracy of the model I first get the predicted probabilities, then impute the values for the outcome variable.

```
# RMSE
caret::postResample(fitted.bart, test$iso_code)
        RMSE Rsquared
                             MAE
## 0.3128503 0.2634878 0.0978753
# For good predictive model the MAE and RMSE values should be low
# Confusion Matrix
confusionMatrix(data = as.factor(fitted.bart),
               reference = as.factor(test$iso_code))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                 0
                      1
            0 2430 232
##
##
            1
                49 160
##
##
                  Accuracy: 0.9021
##
                    95% CI: (0.8907, 0.9128)
##
       No Information Rate: 0.8635
       P-Value [Acc > NIR] : 1.781e-10
##
##
##
                     Kappa: 0.4834
##
##
   Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.9802
               Specificity: 0.4082
##
##
            Pos Pred Value: 0.9128
##
            Neg Pred Value: 0.7656
                Prevalence: 0.8635
##
##
            Detection Rate: 0.8464
##
      Detection Prevalence: 0.9272
##
         Balanced Accuracy: 0.6942
##
##
          'Positive' Class : 0
##
# Balanced Accuracy
balanced_accuracy_bart<-balanced_accuracy(fitted.bart, test$iso_code)
balanced_accuracy_bart
## [1] 0.8391989
# F1-Score
f1_bart_1 <- f1_score(fitted.bart,</pre>
                       test$iso_code,
                       positive.class="1")
f1_bart_1
## 0.5324459
```

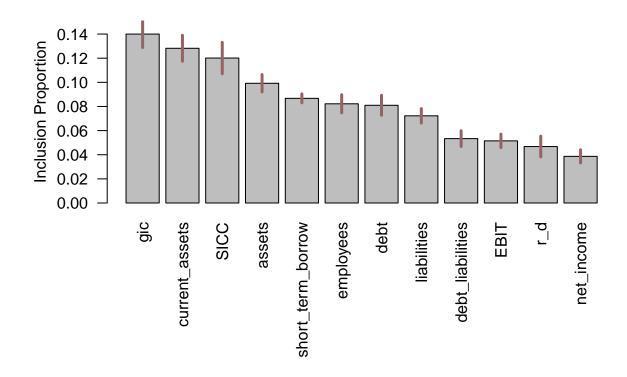
## **ROC curve AUC = 0.6941986**





The package bartMachine provides tools for investigation of variables' importance and variables' selection investigate\_var\_importance(bart\_machine, num\_replicates\_for\_avg = 20)

## ......

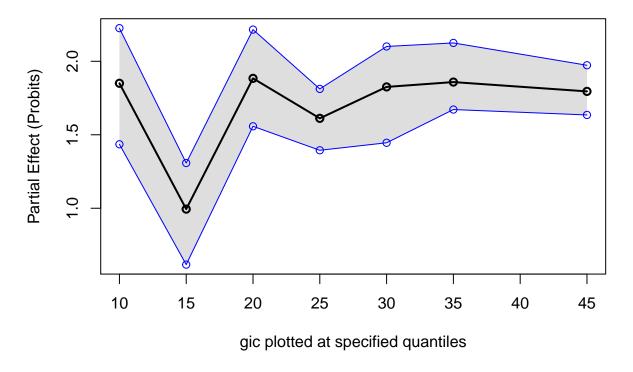


As well as for partial dependency plots.

```
pd_plot(bart_machine, j = "gic")
```

## .....

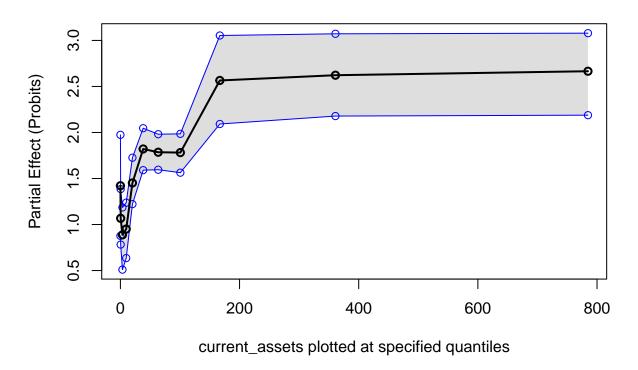
### **Partial Dependence Plot**



```
pd_plot(bart_machine, j = "current_assets")
```

## .....

#### **Partial Dependence Plot**



We can incorporate information on the best predictors in the model by using a different set of priors.

```
predictors
    [1] "assets"
                             "short_term_borrow"
                                                  "current_assets"
##
    [4] "debt"
                             "debt_liabilities"
                                                  "employees"
    [7] "EBIT"
                             "liabilities"
                                                  "net_income"
                                                  "SICC"
## [10] "r_d"
                             "gic"
prior \leftarrow c(rep(1, times = 10), rep(2, times = 2))
set.seed(133234)
bart_prior <- bartMachine(X = as.data.frame(train[predictors]),</pre>
                           cov_prior_vec = prior,
                           y = as.factor(train$iso_code),
                           use_missing_data=FALSE)
## bartMachine initializing with 50 trees...
## bartMachine vars checked...
## bartMachine java init...
## bartMachine factors created...
## bartMachine before preprocess...
## bartMachine after preprocess... 13 total features...
## bartMachine sigsq estimated...
## bartMachine training data finalized...
## Now building bartMachine for classification ...Covariate importance prior ON.
```

## evaluating in sample data...done

```
fitted.prob.bart <- 1- round(predict(bart_prior,</pre>
                              as.data.frame(test[predictors]),
                              type='prob'), 6)
fitted.prior <- ifelse(fitted.prob.bart> 0.5, 1, 0)
Evaluate the performance of this new model.
# RMSE
caret::postResample(fitted.prior, test$iso_code)
##
        RMSE Rsquared
                             MAE
## 0.3072331 0.2839116 0.0943922
# For good predictive model the MAE and RMSE values should be low
# Confusion Matrix
confusionMatrix(data = as.factor(fitted.prior),
                reference = as.factor(test$iso_code))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                0
            0 2435 227
##
##
            1
              44 165
##
##
                  Accuracy: 0.9056
                    95% CI: (0.8943, 0.9161)
##
       No Information Rate: 0.8635
##
       P-Value [Acc > NIR] : 3.168e-12
##
##
##
                     Kappa: 0.5018
##
##
   Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.9823
##
               Specificity: 0.4209
            Pos Pred Value: 0.9147
##
##
            Neg Pred Value: 0.7895
##
                Prevalence: 0.8635
            Detection Rate: 0.8481
##
      Detection Prevalence: 0.9272
##
##
         Balanced Accuracy: 0.7016
##
##
          'Positive' Class : 0
##
# Balanced Accuracy
balanced_accuracy_prior<-balanced_accuracy(fitted.prior, test$iso_code)
balanced_accuracy_prior
## [1] 0.8520997
# F1-Score
f1_prior_1 <- f1_score(fitted.prior,</pre>
                       test$iso_code,
```

```
positive.class="1")
f1_prior_1
##
## 0.5490849
f1_prior_0 <- f1_score(fitted.prior,</pre>
                         test$iso_code,
                         positive.class="0")
f1_prior_0
##
## 0.9472865
# ROC Curve and PR- Curve
fg.prior <- fitted.prior[test$iso_code==1]</pre>
bg.prior <- fitted.prior[test$iso_code==0]</pre>
roc_prior <- roc.curve(scores.class0 = fg.prior,</pre>
                         scores.class1 = bg.prior,
                         curve = T)
plot(roc_prior)
```

# **ROC curve AUC = 0.7015846**

