

VAR/ co-integration/ ARDL/ ECM

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D step 1: - check stationarity for individual

View \rightarrow unit root test \rightarrow OK.

H₀: It has unit root (non-stationary)

If Prob > 0.05 \Rightarrow accept H₀.

If non-stationary stat level 1. (1st difference)

Stationary I(1)

- ② If all series are stationary at different levels check for cointegration \rightarrow Bivariate test

Sub-step

- 1) for finding out optimal lag, we will make all data open as a group.
- 2) Quick - estimate VAR \rightarrow standard VAR
 \rightarrow endogenous variables (all variables)
 \rightarrow lag 4 periods (1, 4 for quarterly data)
 \rightarrow OK.
- 3) Go down \rightarrow check AIC and SC (which is minimum) \rightarrow View \rightarrow Lag structure \rightarrow Lag length criteria \rightarrow check for '*'
AIC gives or SC (which is minimum)
This will give you the lag length.

Bivariate Test

Before Bivariate Test do ARDL test for that

Quick \rightarrow estimate equation \rightarrow (dependent & independent)

equation \rightarrow choose ARDL model \rightarrow OK.

Another diagnostic dialogue box \rightarrow choose the optimal lag as max lag

Trend specification \rightarrow constant \rightarrow OK
Value \rightarrow coefficient diagonals \rightarrow Long run form
Brennan test \rightarrow OK

go to F statistic
check F statistic value compare with $I(0)$ and
 $I(1)$

If value is great
if F statistic value is $>$ than $I(1)$ or less than

$I(0)$
if F statistic value is $< I(0)$ \rightarrow reject (cannot
reject null hypothesis (there is no co-integration)
so it means no long term relationship b/w
variables, so we are using ARDL model for
estimation.

If F statistic value is $> I(1) \rightarrow$ accept
null hypothesis (co-integration is present)

so we will use ECM model

Do it for all data keeping one by one as dependent
variable. If in all cases co-integration is
present do VECM model.

Estimating ARDL
select the data for ARDL model
Quick \rightarrow estimate correlation \rightarrow VAR \rightarrow ddp \rightarrow c ddp \rightarrow ARDL

Eg:-

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Dependent variable	F-statistic	cointegration	what next?
x	F ..	NO	estimate ARDL (short-run model)
y		Yes	Estimate ECM (Error correction model)
z		NO	Estimate ARDL

For every model we will find optimal lags
for that we will do VAR for each model.
Quick - estimate VAR - standard VAR \rightarrow endogenous
variable (dependent variable) \rightarrow lag \rightarrow exogenous
variable (C and all independent variables) \rightarrow OK.

After that same as substep \Rightarrow ③

do it for all models.

Estimate ARDL

Quick \rightarrow estimate equation \Rightarrow \downarrow .

Since ARDL we will take difference of all variables
 d (dependent variable) (-optimal lags)
 d (independent variable (-optimal lags))

$d(x)$ $d(y(-1))$ $d(g(-1))$

eg: $d(x)$ $d(y(-1))$ $d(g(-1))$
 $d(x(-1))$ $d(z)$ $d(x(-1)(-2))$

for eg 2 $d(x)$ $d(y(-1)(-2))$ $d(z(-1)(-2))$

$\rightarrow \dots$

eg:- for lag 1

$d(x_t) c d(x_{t-1}) d(y_{t-1}) d(z_{t-1})$

for lag 2

$d(x_t) c d(x_{t-1}) d(x_{t-2}) d(y_{t-1}) d(y_{t-2})$
 $d(z_{t-1}) d(z_{t-2})$

check for prob (variable significant)

If $\text{prob} < 0.05 \rightarrow$ significant

check for R² value, Durbin - Watson stat.

proc → make residual series → ordinary \rightarrow ecm

* view → Residual diagnostics → serial correlation test
→ optimal lag → check F statistic
if $\text{prob. F} > 0.05 \rightarrow$ no correlation

view → stability diagnostic → Recursive estimates →

ex sum first \rightarrow 0.1

If the line is inside the significance model is stable.

Estimate ECM

There will be 2 equations

1st will be long run model which will give us errors
correction term 2nd will be error correction model
 $= \text{short term} + \text{error correction terms}$

quick → estimate equation \rightarrow dependent (-Lag)

eg:- dependent variable c_t , independent variable (-Lag)

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eg:- $\text{dc c } \text{occ}(-1) \text{ } \text{y}(-1) \text{ } \text{z}(-1) \rightarrow \text{OK}$.

proc → make residual series → Name for series
(ECM)

$\rightarrow \text{OK}$.

Quick

Spec Estimation

proc →

Quick → estimate equation →

$d(\text{dependent variable}) \text{ c } d(\text{dependent variable } (-\text{lag}))$
 $d(\text{independent variable } (-\text{lag}))$
 $\text{ecm}(-\text{lag})$

eg:-

$d(\text{dc}) \text{ c } d(\text{oc}(-1)) \text{ } d(\text{y}(-1)) \text{ } d(\text{z}(-1))$
 $\text{ecm}(-1) \rightarrow \text{OK}$.

check for significance of ecm

coefficient of ecm and probability of ecm

↙

-vc (error correction will happen) ↘ < 0.05 significant

- ① view → Residual diagnostic → Serial correlation → Optimal lag →
 check f statistic → its prob < 0.05 → no-correction
- ② view → Stability diagnostic → AC Corr VC estimates →

CUSUM test → OK.

(1)

Volatility

Large changes in stock returns seem to be followed by further large changes \rightarrow volatility clustering

Homoskedasticity \rightarrow constant variance

ARCH MODEL

- \Rightarrow Variance of the residuals at time t depends on the squared error terms from past periods.
- \Rightarrow It is better to model simultaneously the mean and the variance of a series when it is suspected that the conditional variance is not constant.
- \Rightarrow Variance of the residuals (σ^2) depends on history or to have heteroskedasticity because the variance will change over time.
- \Rightarrow to allow this we have the variance depend on one lagged period of the squared error. \rightarrow ARCH(1)

$$y_t = a + \beta' x_t + u_t \rightarrow \text{Mean equation}$$

$$u_t | \Omega_t \sim \text{iid}(0, h_t)$$

$$h_t = v_0 + v_1 u_{t-1}^2 \rightarrow \text{Variance equation}$$

ARCH Model ^{By} ~~from~~ Eviews \rightarrow Financial data.

① Test for stationarity

view \rightarrow Unit Root test \rightarrow Level \rightarrow OK.

② Test for Heteroscedasticity

\rightarrow Lagrange Multiplier (LM) test for ARCH is used

Eg:- Quick \rightarrow estimate equation (to find ARCH(1) is present)

$$\text{Eq: } \sigma_t = \sigma_{t-1} e_t \quad C \sigma_{t-1}^2 e_t (-1)$$

click OK.

View \rightarrow Residuals Diagnostics \rightarrow Heteroskedasticity

test \rightarrow ARCH \rightarrow No of lags (1) \rightarrow OK.

check the probability value of obs* R squared
if it is less than 0.05 then reject null hypothesis

of homoskedasticity

so conclude ARCH(1) is present.

③ Estimate ARCH Model

Quick Estimate equation \rightarrow ARCH \rightarrow Select

ARCH(1) in ARCH (0) \rightarrow OK.

ARCH M - NONE

Threshold Order - 0

equation

To get equation \rightarrow View \rightarrow representation

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To view conditional variance and conditional standard deviation.

View \rightarrow Grach Graphs \rightarrow conditional SD graph
 " " \rightarrow conditional Variance

To obtain variance scores

Proc \rightarrow Make grach Variance Scores

GARCH Model

AR(1) model looks like moving average than autoregression. So they introduce GARCH model

$$y_t = \alpha + \beta^1 x_t + u_t$$

$$u_t | \Omega_t \sim \text{iid } N(0, h_t)$$

$$h_t = v_0 + \sum_{i=1}^p \delta_i h_{t-i} + \sum_{j=1}^q v_j u_{t-j}^2$$

$h_t \rightarrow$ depends both on past values of the stocks which are captured by the lagged squared individual terms, and on past values itself which were captured by lagged h_t terms.

GARCH(1,1)

$$h_t = r_0 + \delta_1 h_{t-1} + \gamma_1 u_t^2 - 1$$

Estimation

Same as ARCH (1)

only difference GARCH (1) in estimate equation

After finding out this effect again check

ARCH LM-test

View \rightarrow Residual diagnosis \rightarrow ARCH LM-test

check Probability of obs & R² square

< 0.05 Accept null

> 0.05 Accept Alternate hypothesis that test statistics do not support for any additional ARCH effect remaining in the residuals of the models which implies that the variance equation is well specified for the market.

GARCH - M Model

- \Rightarrow y_t allow the conditional mean to depend on its own conditional variance.
- \Rightarrow To get the premium, GARCH - M Model is used
- \Rightarrow To capture garch
- \Rightarrow Same as GARCH put in ARCH - M model either variance or std.dev.

(3)

TGARCH Model

- ARCH and GARCH Model are symmetric. i.e. matter is only the absolute value of innovation and not its sign.
- But in the stock markets there is (-ve and +ve) impact. -ve impact shocks in the market have a larger impact on volatility than do positive shocks of the same magnitude.
- This model help us to capture asymmetries in terms of negative and positive shocks.
- To do this, simply add into the variance equation a multiplicative dummy variable to check whether there is a statistically significant difference when shocks are -ve.

- Model same as GARCH put threshold value 1
~~(Resid < 0) \Rightarrow * ARCH(1) \rightarrow~~
~~(Resid(-1)) \wedge_2 * [Resid(-1) < 0] is +ve and~~
~~is statistically significant then the data there~~
~~are asymmetric in the news.~~

Specifically bad news has larger effects on the volatility of the series than good news.

E-GARCH Model

- ⇒ This model makes the leverage effect exponential rather than quadratic and therefore the estimates of the conditional variance are guaranteed to be non-negative.
- ⇒ This is used for testing asymmetric $\varepsilon_1 = \varepsilon_2 = 0 \rightarrow$ Model is symmetric
 $\varepsilon_j < 0$ +ve shock generate less volatility than -ve shock.

so same as TGARCH instead of GARCH / TGARCH
put EGARCH

If any -ve value is there in coefficients then
the bad news has larger effects on
volatility of the series than good news.