Find
$$\int \sqrt{x^2 + 2x} \, dx = \int \sqrt{x^2 + 2x + 1} - 1 \, dx$$

= $\int \sqrt{(x+1)^2 - 1} \, dx$
= $\int \sec^2(1) - 1 \cdot \sec(1) + \cos(1) \, dt$
= $\int \tan(1) \cdot \sec(1) \cdot \tan(1) \, dt$
= $\int \tan^2(1) \cdot \sec(1) \, dt$
= $\int (\sec^2(1) - 1) \cdot \sec(1) \, dt$
= $\int \sec^2(1) - 1 \cdot \sec(1) \, dt$
= $\int \sec^2(1) - 1 \cdot \sec(1) \, dt$

=
$$\int \sec^{2}(t) dt - \int \sec(t) dt$$

direct

we know:

 $M=3$
 $\int \sec^{m}(t) dt = \frac{\tan(1) \sec(t)}{m-1} + \frac{m-2}{m-1} \cdot \int \sec^{m-2}(t) dt$
 $= \frac{\tan(1) \cdot \sec(1)}{2} + \frac{1}{2} \cdot \int \sec(1) dt - \int \sec(1) dt$
 $= \frac{\tan(1) \cdot \sec(1)}{2} - \frac{1}{2} \cdot \ln|\sec(1) + \tan(1)| + C = \oplus$

But, x+1 = sec(+)and we need to find tan (+) ! We Know, 1+ Lan2 (+) = sec2 (+) (=) tan (+) = sec2(+)-1 (=) fan(+) = \sec2(+7-1) (a) $\tan(1) = \sqrt{(x+1)^2 - 1}$ (=) fam(+) = \(x^2 + 2x \) Then,

(2) +211 (2+1) - 1 ln | x+1 + \(x^2 +2x \) + C