# Homework 2

## SOLUTIONS

### Part A

1.

```
College.HS <- lm(College~HighSchool, data=state.data); College.HS

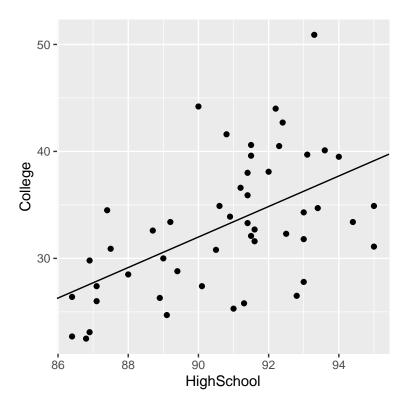
##
## Call:
## lm(formula = College ~ HighSchool, data = state.data)
##
## Coefficients:
## (Intercept) HighSchool
## -96.366 1.426</pre>
2.
```

For each additional percent of a state's population that earns a high school diploma, we expect college graduation percent to increase by 1.4%.

3.

Certainly a line seems appropriate here. There are some outliers (points far from the line) on the right side of the graph.

```
#Here you should have the code to make the scatterplot with line
gf_point(College~HighSchool, data=state.data)+ geom_abline(intercept=College.HS$coefficients[1], slope=
```



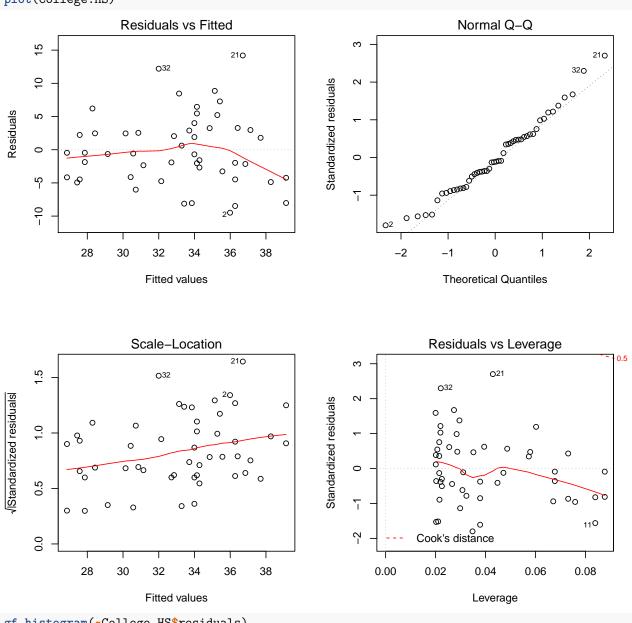
The output below shows an  $R^2$  of 29.2%, which is the percent of the variation in college graduation percentage explained by this model.

# summary(College.HS)

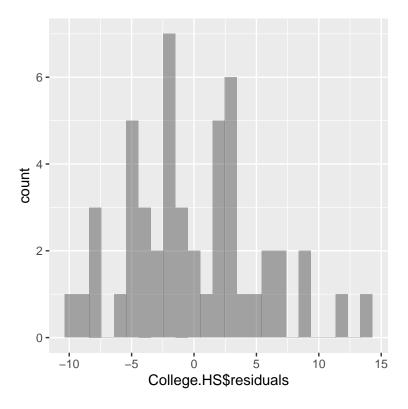
```
##
## Call:
## lm(formula = College ~ HighSchool, data = state.data)
##
## Residuals:
##
      Min
                1Q Median
                               3Q
                                      Max
  -9.4907 -4.1541 -0.6078 2.9490 14.1962
##
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -96.3657
                          29.0740 -3.314 0.00175 **
                                    4.454 5.03e-05 ***
## HighSchool
                 1.4263
                           0.3202
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5.37 on 48 degrees of freedom
## Multiple R-squared: 0.2924, Adjusted R-squared: 0.2777
## F-statistic: 19.84 on 1 and 48 DF, p-value: 5.03e-05
```

Constant variance might be a concern, as shown in the first residual plot – it's hard to say because there isn't much data (only 50 points). Normality is fine - even though the histogram doesn't look good, the normal probability plot shows that the residuals are reasonably normal.

par(mfrow=c(2,2)) plot(College.HS)



gf\_histogram(~College.HS\$residuals)



# Part B

## 1.

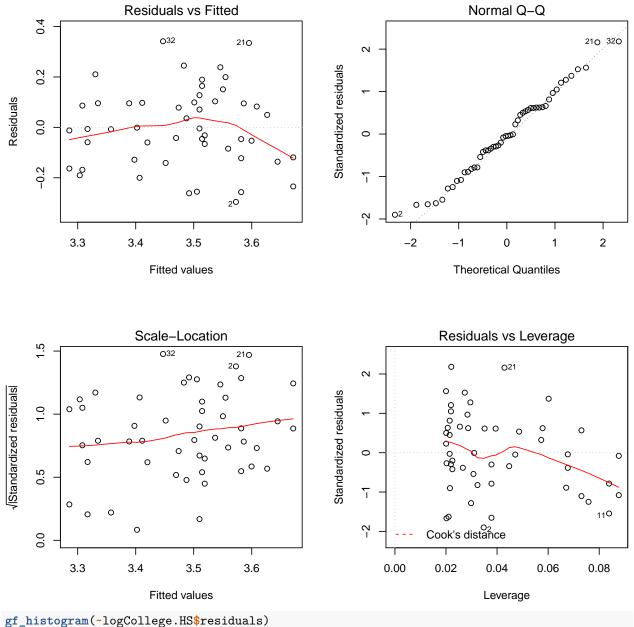
**2**.

```
logCollege.HS <- lm(log(College)~HighSchool, data=state.data); logCollege.HS

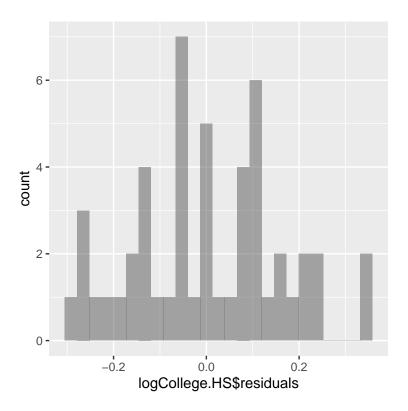
##
## Call:
## lm(formula = log(College) ~ HighSchool, data = state.data)
##
## Coefficients:
## (Intercept) HighSchool
## -0.59195 0.04488</pre>
```

This looks much better! Constant variance and normality both look to be met, and no influential points.

```
par(mfrow=c(2,2))
plot(logCollege.HS)
```



9-----



The test of slope=0 has a p-value of approx. 0, so yes, there is a significant association between log(College graduation %) and High School graduation % for US states.

# summary(logCollege.HS)

```
##
## Call:
## lm(formula = log(College) ~ HighSchool, data = state.data)
##
## Residuals:
##
       Min
                      Median
                 1Q
                                   3Q
                                           Max
## -0.29568 -0.12152 -0.00699 0.09692 0.34156
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.591945
                          0.857195 -0.691
                                              0.493
                                     4.754 1.86e-05 ***
## HighSchool
               0.044879
                          0.009441
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1583 on 48 degrees of freedom
## Multiple R-squared: 0.3201, Adjusted R-squared: 0.3059
## F-statistic: 22.6 on 1 and 48 DF, p-value: 1.856e-05
```

We are 90% confident that high school graduation rate increases by 1%, we expect log(College graduation %) to increase between 0.029 and 0.061.

```
confint(logCollege.HS, level=0.9)

## 5 % 95 %

## (Intercept) -2.02965407 0.84576382
## HighSchool 0.02904399 0.06071403
```

#### **5**.

The F-test (p-value=0.000019) tells us that High School graduation % is useful in predicting log(College graduation %).

```
anova(logCollege.HS)
```

### Part C

#### 1.

Below are the 3 models with the highest  $R^2$  values. Of these, I think the percentage of vaccinated residents is the best predictor. It has the highest  $R^2$  and no major problems with conditions. (If you ignore the outlier of point 31, you'll see that there is no issue with constant variance. And point 31 is not influential.)

```
par(mfrow=c(2,2))
College.8math <- lm(College~EighthGradeMath, data=state.data)
summary(College.8math)</pre>
```

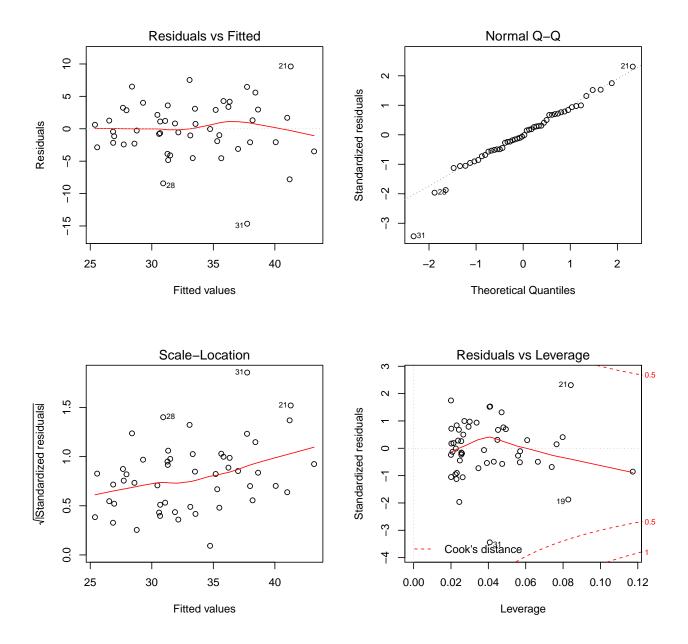
```
##
## Call:
## lm(formula = College ~ EighthGradeMath, data = state.data)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
  -10.7760 -3.2482 -0.5766
                                2.4326
                                       11.7472
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   -177.7598
                                31.5700 -5.631 9.14e-07 ***
## EighthGradeMath
                      0.7497
                                 0.1122
                                          6.680 2.28e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Multiple R-squared: 0.4818, Adjusted R-squared: 0.471
## F-statistic: 44.62 on 1 and 48 DF, p-value: 2.277e-08
plot(College.8math)
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College.Income <- lm(College~HouseholdIncome, data=state.data)</pre>
summary(College.Income)
##
## lm(formula = College ~ HouseholdIncome, data = state.data)
##
## Residuals:
##
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                            Median
                                            ЗQ
                                                      Max
                            0.2105
##
   -15.0295 -2.0356
                                       2.5019
                                                10.2707
##
```

## Residual standard error: 4.596 on 48 degrees of freedom

```
## Coefficients:
##
                                                                           Estimate Std. Error t value Pr(>|t|)
           (Intercept)
                                                                              6.33689
                                                                                                                         4.00559
                                                                                                                                                                 1.582
## HouseholdIncome
                                                                              0.46237
                                                                                                                          0.06834
                                                                                                                                                                 6.766 1.68e-08 ***
##
                                                                                   '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 4.567 on 48 degrees of freedom
## Multiple R-squared: 0.4882, Adjusted R-squared: 0.4775
## F-statistic: 45.78 on 1 and 48 DF, p-value: 1.68e-08
plot(College.Income)
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                                                                               Fitted values
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College.vax <- lm(College~percent_fully_vax, data=state.data)</pre>
summary(College.vax)
```

```
## Call:
## lm(formula = College ~ percent_fully_vax, data = state.data)
## Residuals:
       Min
                 1Q Median
                                   ЗQ
## -14.6497 -2.2589 -0.1564 2.9509
                                       9.6126
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
                                         1.842 0.0716 .
## (Intercept)
                    6.63663
                                3.60211
## percent_fully_vax 0.53818
                                0.07222
                                        7.452 1.5e-09 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
\mbox{\tt \#\#} Residual standard error: 4.347 on 48 degrees of freedom
## Multiple R-squared: 0.5363, Adjusted R-squared: 0.5267
## F-statistic: 55.52 on 1 and 48 DF, p-value: 1.499e-09
plot(College.vax)
```



We are 95% confident that among states with a 48.27% vaccination rate, the mean college graduation percentage will be between 31.37% and 33.86%.

```
median(~percent_fully_vax, data=state.data)

## [1] 48.26808

#Code for confidence interval:
predict.lm(College.vax, data.frame("percent_fully_vax"=48.27), interval="confidence")

## fit lwr upr
## 1 32.61436 31.37187 33.85684
```

We are 95% confident that for a state with a 48.27% vaccination rate, the college graduation percentage will be between 23.79% and 41.44%.

```
#Code for prediction interval:
predict.lm(College.vax, data.frame("percent_fully_vax"=48.27), interval="prediction")

## fit lwr upr
## 1 32.61436 23.78661 41.4421
```